

POLI706: Advanced Methods of Political Analysis

Problem set 5

Exercise 1

For this exercise we will use the `cats` dataset from the `MASS` package. You should use `?cats` to learn about the background of this dataset.

```
library(MASS)
data(cats)
```

- Fit the following simple linear regression model in R. Use heart weight as the response and body weight as the predictor.

$$Y_i = \beta_0 + \beta_1 x_i + \epsilon_i$$

Store the results in a variable called `cat_model`. Use a t test to test the significance of the regression. Report the following:

- The null and alternative hypotheses
- The value of the test statistic
- The p-value of the test
- A statistical decision at $\alpha = 0.05$
- A conclusion in the context of the problem

```
cat_model = lm(Hwt ~ Bwt, data = cats);
summary(cat_model)
```

Exercise 2

What are $\beta_0, \beta_1, \hat{\beta}_0, \hat{\beta}_1, x, x_i, u, \hat{u}_i$ in output of simple linear regression from the Exercise 1?

Exercise 3

Explain under which circumstances you will get a large slope coefficient estimates when you run a regression model.