Regression for Microbiome Data: Moving From Diversity to Inference

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Updated: 18 June 2020

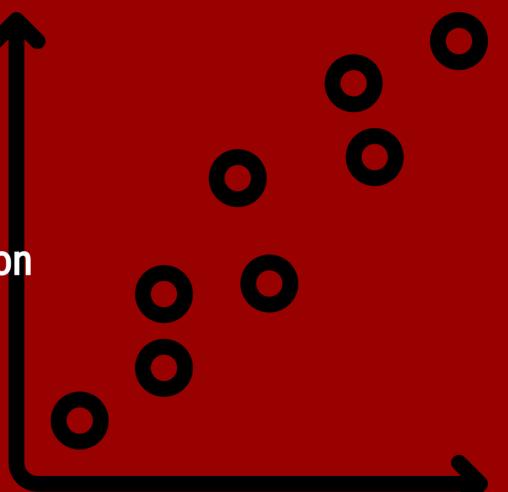
Review α-diversity

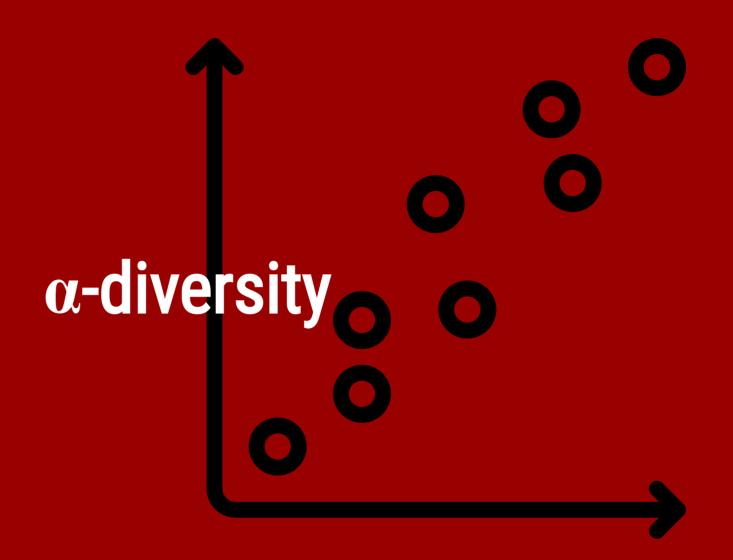
Review β-diversity

 α/β -diversity \rightarrow linear regression

β-diversity → PERMANOVA

Compositional data?





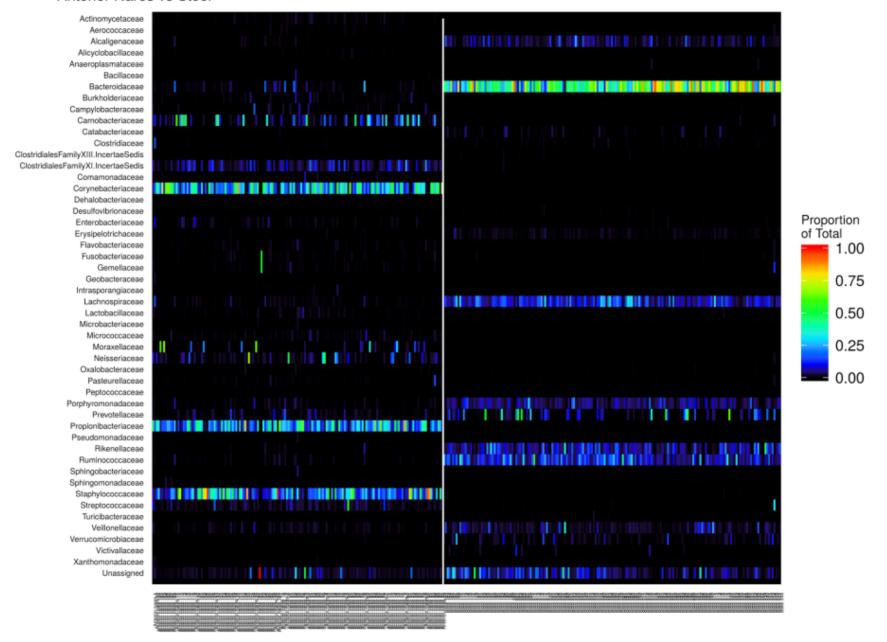
High Dimensional Microbiome Data

##		700013549	700014386	700014403	700014409	700014412	700014415
##	OTU_97.1	0	0	0	0	0	0
##	OTU_97.10	0	0	6	4	1	5
##	OTU_97.100	0	0	133	7	1	4
##	OTU_97.1000	0	0	0	0	0	0
##	OTU_97.10000	0	0	0	0	0	0
##	OTU_97.10001	0	0	0	0	0	1
##	OTU_97.10002	0	0	0	0	0	0
##	OTU_97.10003	0	0	0	0	0	0
##	OTU_97.10004	0	0	0	0	0	0
##	OTU_97.10005	0	0	0	0	0	0
##	OTU_97.10006	0	0	0	0	0	0
##	OTU_97.10007	0	0	0	0	0	0
##	OTU_97.10008	0	1	0	0	0	0
##	OTU_97.10009	0	0	1	0	0	0
##	OTU_97.1001	0	0	0	0	0	0
##	OTU_97.10010	0	0	0	0	0	0

High Dimensional Microbiome Data

- How to deal with high-dimensional microbiome data?
- Descriptive (e.g., heatmaps and stacked barplots)
- Test a priori hypotheses regarding specific OTUs/taxa
- Reduce dimensions:
 - single summary statistic (alpha diversity)
 - pairwise distances (beta diversity) with PCoA or PERMANOVA
 - community types (mixture modeling)

Anterior Nares vs Stool



High Dimensional Microbiome Data

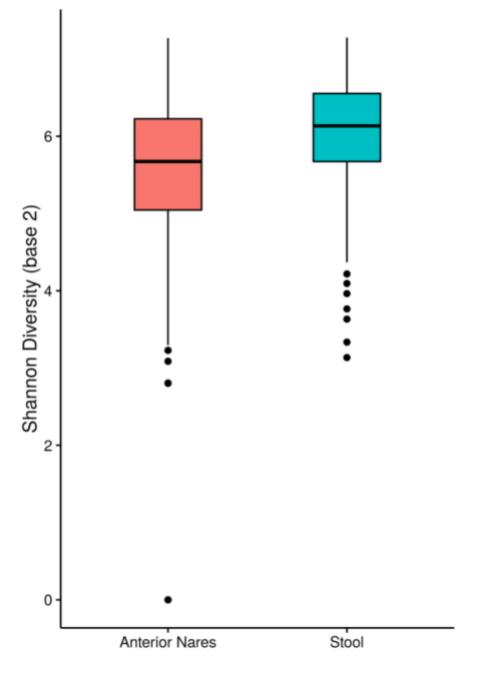
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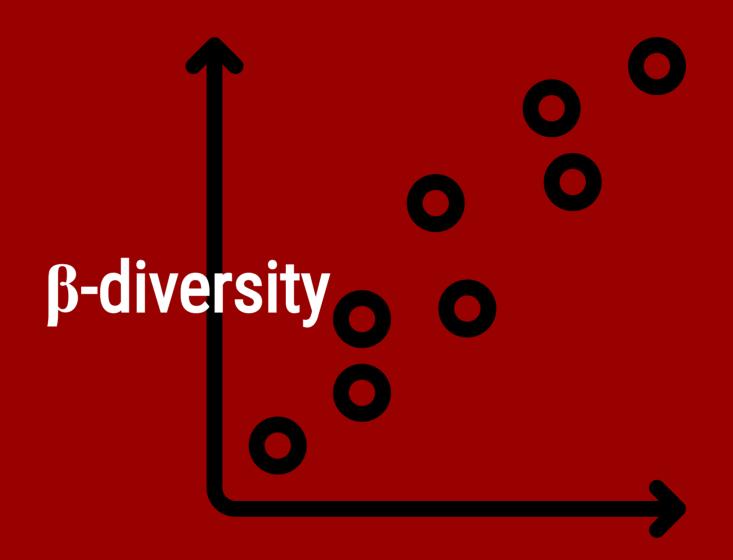
Shannon Diversity

- Richness & evenness
- Shannon diversity:

$$H' = -\sum p_i * \log_b\left(p_i
ight)$$

• "The uncertainty contained in a probability distribution is the average logprobability of an event." (McElreath *Statistical Rethinking, 2nd* 2020)



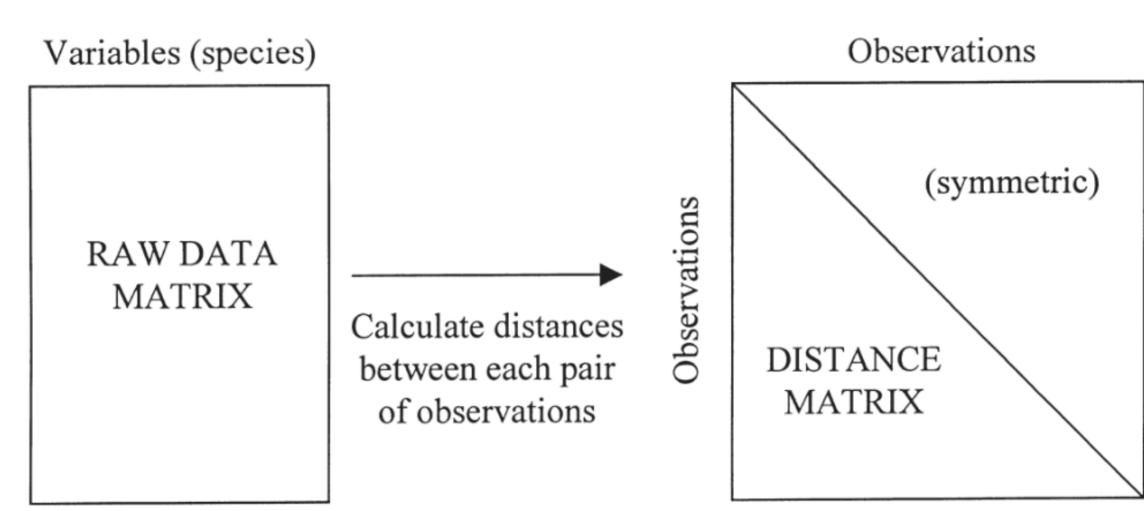


High Dimensional Microbiome Data

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Beta Diversity as Dimension Reduction

- Summarize each sample's relationship to other samples:
 - pairwise distances
 - OTU table → square matrix
- Many beta diversity metrics:
 - just counts versus counts + phylogeny
 - weighted versus unweighted



Distance Metrics for Beta Diversity

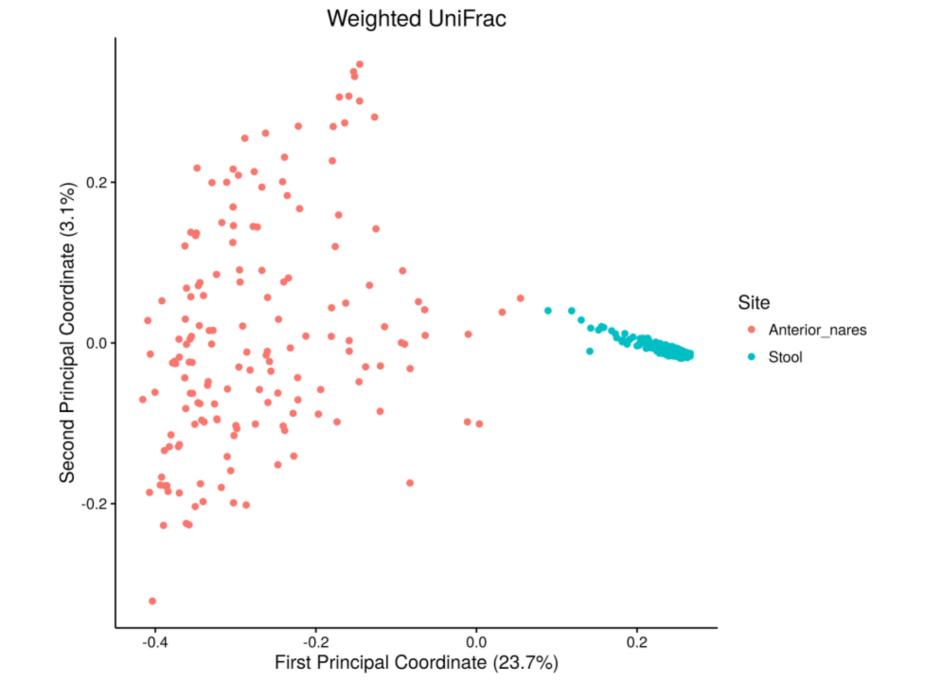
Just counts versus counts + phylogeny:

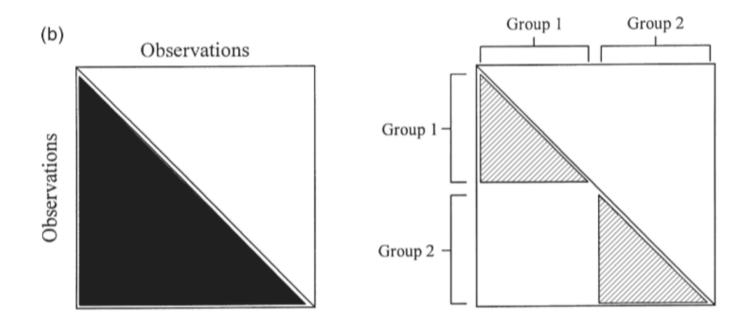
$$\circ$$
 Jaccard: $J(A,B)=rac{A\cap B}{A\cup B}$ & $d_J(A,B)=1-J(A,B)$

- UniFrac: fraction of unique branch length in tree
- Weighted versus unweighted:
 - weighted: counts matter
 - unweighted: binary (presence-absence)

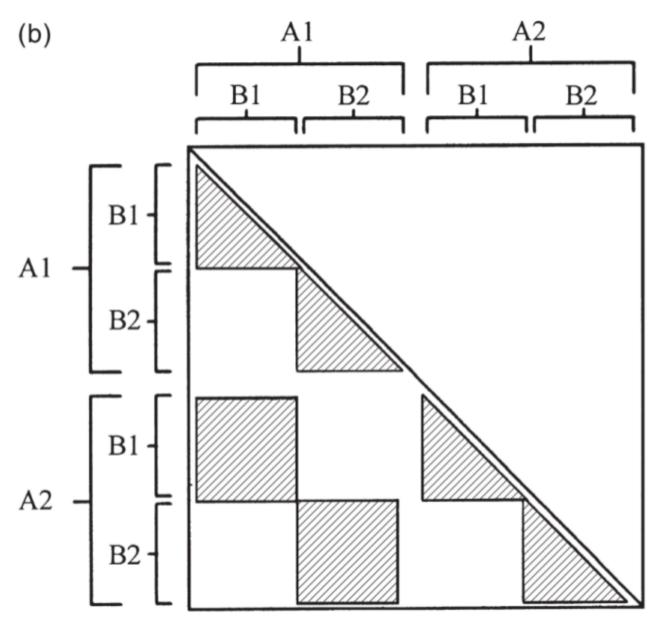
Pairwise Distances → PCoA

- PCoA: principal coordinate analysis
 - any metric distance, even if non-Euclidean
 - like PCA, eigenvalue decomposition (maximum variance) but mediated by distance function (no original descriptors)
 - unlike PCA, does not allow projection of original descriptors in reduceddimension space





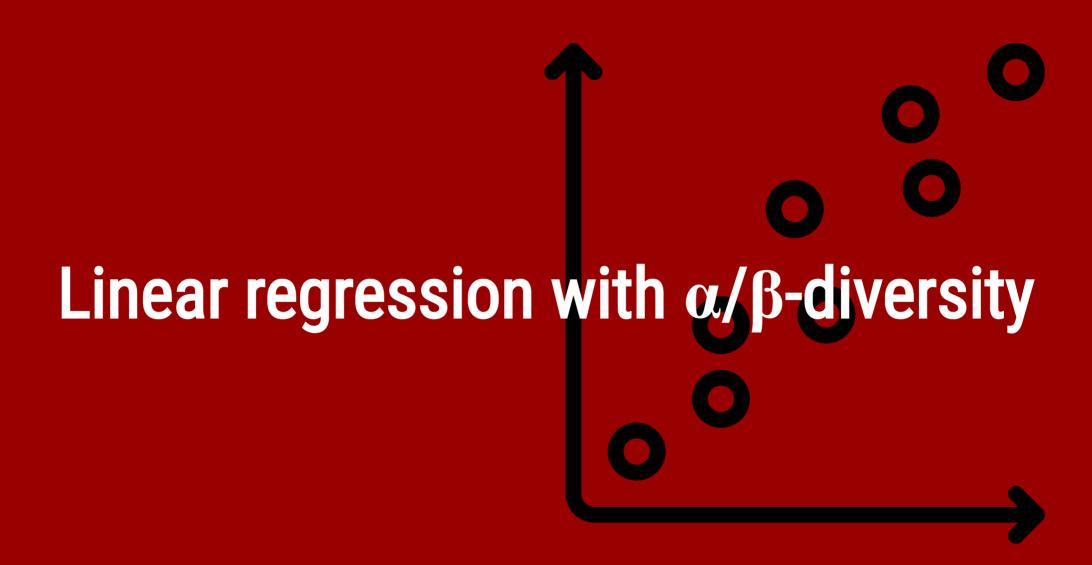
$$F = \frac{SS_A/(a-1)}{SS_W/(N-a)}$$



$$R^2=1-rac{ ext{SS}_{ ext{W}}}{ ext{SS}_{ ext{W}}+ ext{SS}_{ ext{A}}}=rac{ ext{SS}_{ ext{A}}}{ ext{SS}_{ ext{T}}} \qquad \qquad \omega^2=rac{ ext{SS}_{ ext{A}}-(a-1)rac{ ext{SS}_{ ext{W}}}{N-a}}{ ext{SS}_{ ext{T}}+rac{ ext{SS}_{ ext{W}}}{N-a}}$$

Table 1. Effect sizes observed from various exposures/interventions in studies of various microbiome sampling sites are shown as measured by omega-squared (ω^2) statistics, together with the *P*-values from PERMANOVA test

Site	Comparison groups		ω^2/P -value					
	Control	Exposure	Weighted UniFrac	Unweighted UniFrac	Weighted Jaccard	Unweighted Jaccard	Reference	
Nares	Non-smoker (33)	Smoker (29)	0.042/0.001	0.009/0.001	0.023/0.001	0.007/0.001	Charlson et al. (2010)	
Oral	Non-smoker (33)	Smoker (29)	0.032/0.001	0.008/0.001	0.024/0.001	0.007/0.001	Charlson et al. (2010)	
Gut	Before feeding (10)	After feeding (10)	0.056/0.138	0.013/0.986	0/0.989	0.014/0.985	Wu et al. (2011)	
Oral	No azithromycin (42)	Azithromycin (6)	0.063/0.01	0.039/0.001	0.099/0.004	0.032/0.001	Charlson et al. (2012)	
Lung	No azithromycin (34)	Azithromycin (6)	0.065/0.005	0.038/0.001	0.019/0.089	0.033/0.001	Charlson et al. (2012)	
Skin	Left retroauricular (186)	Right retroauricular (187)	0.000/0.828	0.0001/0.327	0.000/0.986	0.000/1.000	HMP Consortium (2012b)	
Human	Anterior nares (161)	Stool (187)	0.567/0.001	0.201/0.001	0.230/0.001	0.117/0.001	HMP Consortium (2012b)	



```
# install.packages("tidyverse")
library(tidyverse)

# install.packages("vegan")
library(vegan)

# install.packages("ape")
library(ape)

set.seed(16)

otu_tab <- read_rds(
"./data/HMP_OTU_table_matrix_stool_nares.rds"
)

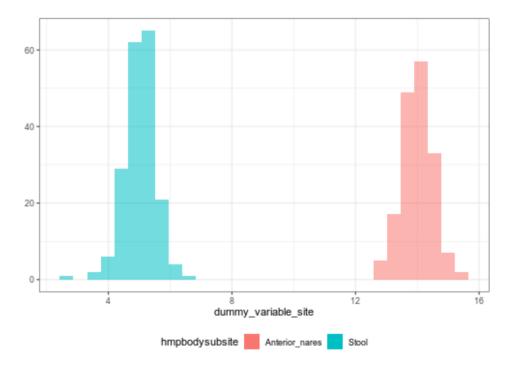
otu_tab %>%
    str(vec.len = 3)
```

```
## num [1:43140, 1:10] 0 0 0 0 0 0 0 0 0 ...
## - attr(*, "dimnames")=List of 2
## ..$ : chr [1:43140] "OTU_97.1" "OTU_97.10" "OTU_97.100" ...
## ..$ : chr [1:10] "700014718" "700014767" "700014923" ...
```

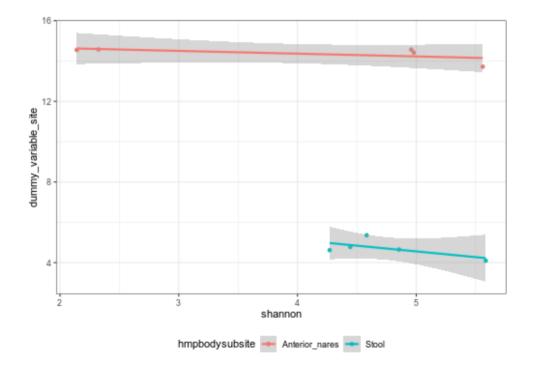
```
## # A tibble: 431,400 x 3
     otu id
                  specimen_id read_count
     <chr>
                  <chr>
                                   <dbl>
   1 OTU 97.1
                 700014718
   2 OTU_97.10
                700014718
   3 OTU_97.100 700014718
   4 OTU_97.1000 700014718
## 5 OTU_97.10000 700014718
## 6 OTU_97.10001 700014718
## 7 OTU_97.10002 700014718
   8 OTU_97.10003 700014718
   9 OTU 97.10004 700014718
## 10 OTU 97.10005 700014718
## # ... with 431,390 more rows
```

```
read_tsv(file = "./data/v13_map_uniquebyPSN.txt.bz2") %>%
  rename_all(.funs = ~ gsub("#","",tolower(.x))) %>%
  rename(specimen_id = sampleid) %>%
  distinct() -> specimen_data
specimen_data %>%
  group_by(hmpbodysubsite) %>%
 mutate(dummy_variable_site =
           rnorm(n = length(hmpbodysubsite).
                 mean = nchar(unique(hmpbodysubsite)),
                 sd = 0.5)) %>%
  ungroup() %>%
  filter(hmpbodysubsite %in%
           c("Anterior_nares", "Stool")) %>%
  select(specimen_id,
         hmpbodysubsite,
         dummy_variable_site) %>%
  mutate(specimen_id = as.character(specimen_id)) %>%
  distinct() -> specimen_data
specimen_data
```

```
## # A tibble: 361 x 3
      specimen_id hmpbodysubsite dummy_variable_site
      <chr>
                  <chr>>
                                                <dbl>
   1 700013549
                  Stool
                                                 5.87
                  Stool
   2 700014386
                                                 4.68
   3 700014445
                  Anterior_nares
                                                14.2
   4 700014488
                  Stool
                                                 4.95
                  Stool
                                                 5.36
   5 700014497
   6 700014527
                                                13.9
                  Anterior nares
                                                 4.39
   7 700014555
                  Stool
                  Stool
                                                 4.10
    8 700014718
    9 700014767
                  Anterior nares
                                                14.5
## 10 700014797
                                                13.3
                  Anterior nares
## # ... with 351 more rows
```

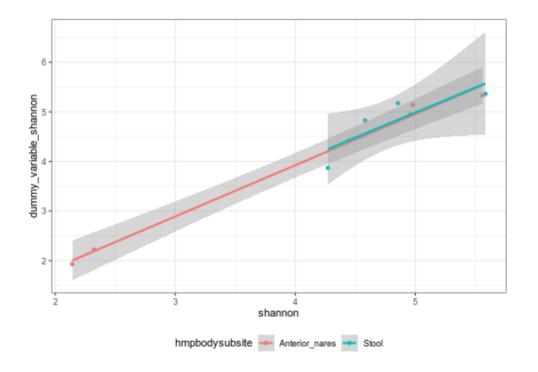


```
## # A tibble: 10 x 5
     specimen_id shannon hmpbodysubsite dummy_variable_site dummy_va
     <chr>
                    <dbl> <chr>
                                                       <dbl>
   1 700014718
                     5.58 Stool
                                                        4.10
   2 700014767
                                                      14.5
                    2.14 Anterior_nares
   3 700014923
                    2.32 Anterior_nares
                                                      14.6
   4 700016920
                                                      14.6
                    4.96 Anterior nares
   5 700023706
                                                      14.4
                    4.98 Anterior_nares
   6 700038343
                                                      13.7
                     5.56 Anterior nares
                                                        4.65
   7 700095956
                    4.86 Stool
   8 700105834
                    4.58 Stool
                                                        5.36
   9 700107189
                    4.27 Stool
                                                        4.62
## 10 700109383
                    4.44 Stool
                                                        4.78
```



```
shannon_summary %>%
    lm(formula = dummy_variable_site ~ shannon,
        data = .) %>%
    summary()
```

```
## Call:
## lm(formula = dummy_variable_site ~ shannon, data = .)
##
## Residuals:
               10 Median
      Min
                                     Max
## -5.0672 -4.0586 -0.9973 4.8409 6.0355
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 16.328
                           6.301
                                   2.591
                                            0.032 *
## shannon
                -1.555
                           1.395 -1.115
                                            0.297
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 5.041 on 8 degrees of freedom
## Multiple R-squared: 0.1345, Adjusted R-squared: 0.02627
## F-statistic: 1.243 on 1 and 8 DF, p-value: 0.2973
```

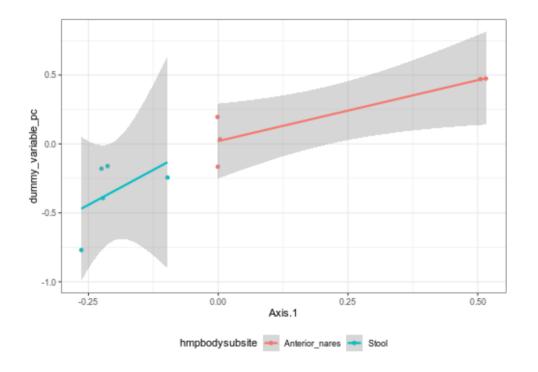


```
shannon_summary %>%
    lm(formula = dummy_variable_shannon ~ shannon,
        data = .) %>%
    summary()
```

```
## Call:
## lm(formula = dummy_variable_shannon ~ shannon, data = .)
##
## Residuals:
       Min
                10 Median
                                         Max
## -0.34993 -0.18375 0.01602 0.14710 0.34814
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.20539
                         0.30165 -0.681
                                           0.515
## shannon
              1.03619
                         0.06678 15.515 2.96e-07 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.2413 on 8 degrees of freedom
## Multiple R-squared: 0.9678, Adjusted R-squared: 0.9638
## F-statistic: 240.7 on 1 and 8 DF, p-value: 2.965e-07
```

```
##
## Call:
## lm(formula = dummy_variable_shannon ~ shannon + hmpbodysubsite.
      data = .)
##
##
## Residuals:
      Min
               10 Median
                                      Max
## -0.3688 -0.1690 0.0134 0.1674 0.3323
## Coefficients:
                      Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                      -0.20055
                                  0.32224 -0.622
                                                    0.553
## shannon
                      1.03088
                                  0.07540 13.672 2.64e-06 ***
## hmpbodysubsiteStool 0.03673
                                  0.17233
                                           0.213
                                                    0.837
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.2572 on 7 degrees of freedom
## Multiple R-squared: 0.968, Adjusted R-squared: 0.9589
## F-statistic: 106 on 2 and 7 DF, p-value: 5.834e-06
```

```
## # A tibble: 10 x 8
                           Axis.2 shannon hmpbodysubsite dummy_varial
     specimen_id
                   Axis.1
     <chr>
                    <dbl>
                            <dbl>
                                    <dbl> <chr>
   1 700014718
                 -2.64e-1
                           0.222
                                     5.58 Stool
   2 700014767
                  5.16e-1
                                    2.14 Anterior_nares
                           0.174
   3 700014923
                  5.05e-1
                           0.183
                                     2.32 Anterior_nares
   4 700016920
                  3.50e-3 -0.434
                                     4.96 Anterior nares
                 -8.28e-4 -0.290
   5 700023706
                                     4.98 Anterior_nares
   6 700038343
                 -1.54e-3 -0.435
                                     5.56 Anterior nares
                 -2.22e-1
   7 700095956
                           0.189
                                     4.86 Stool
                 -2.25e-1
                           0.174
                                     4.58 Stool
   8 700105834
   9 700107189
                 -9.78e-2 0.0363
                                     4.27 Stool
## 10 700109383
                 -2.13e-1 0.180
                                     4.44 Stool
## # ... with 2 more variables: dummy_variable_shannon <dbl>,
      dummy_variable_pc <dbl>
```

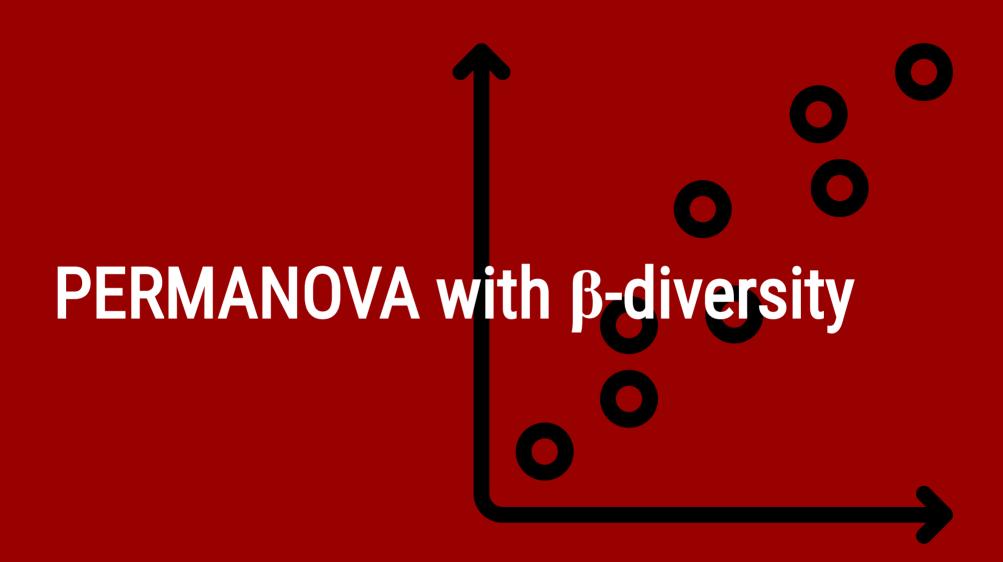


```
pc_summary %>%
    Im(formula = dummy_variable_pc ~ Axis.1,
        data = .) %>%
    summary()
```

```
## Call:
## lm(formula = dummy_variable_pc ~ Axis.1, data = .)
##
## Residuals:
       Min
                 10 Median
                                          Max
## -0.38811 -0.05846 -0.04998 0.14369 0.27116
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.07387
                         0.06180 -1.195 0.266241
## Axis.1
               1.16777
                         0.22633
                                   5.160 0.000864 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1954 on 8 degrees of freedom
## Multiple R-squared: 0.7689, Adjusted R-squared: 0.74
## F-statistic: 26.62 on 1 and 8 DF, p-value: 0.0008641
```

```
pc_summary %>%
    lm(formula = dummy_variable_pc ~ Axis.2,
        data = .) %>%
    summary()
```

```
## Call:
## lm(formula = dummy_variable_pc ~ Axis.2, data = .)
##
## Residuals:
       Min
                 10 Median
                                          Max
## -0.63113 -0.17200 -0.04452 0.10175 0.59896
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.07387
                          0.12574 -0.587
                                            0.573
## Axis.2
              -0.29223
                          0.48408 -0.604
                                            0.563
## Residual standard error: 0.3976 on 8 degrees of freedom
## Multiple R-squared: 0.04357, Adjusted R-squared: -0.07598
## F-statistic: 0.3644 on 1 and 8 DF, p-value: 0.5628
```



```
otu_tab %>%
   t() %>% # TRANSPOSE
   vegdist(x = ., method = "jaccard") -> otu_dist

otu_dist %>%
   str(vec.len = 2)
```

```
## 'dist' num [1:45] 1 0.996 ...
## - attr(*, "Size")= int 10
## - attr(*, "Labels")= chr [1:10] "700014718" "700014767" ...
## - attr(*, "Diag")= logi FALSE
## - attr(*, "Upper")= logi FALSE
## - attr(*, "method")= chr "jaccard"
## - attr(*, "call")= language vegdist(x = ., method = "jaccard")
```

```
labels(otu_dist) %>% #match order from dist
  enframe(value = "specimen_id") %>%
  select(specimen_id) %>%
  left_join(pc_summary, by = "specimen_id") %>%
  mutate(dummy_category = Axis.1 > mean(Axis.1)) %>%
  distinct() -> sorted_summary
sorted_summary
```

```
## # A tibble: 10 x 9
                           Axis.2 shannon hmpbodysubsite dummy_varial
     specimen_id
                   Axis.1
     <chr>
                    <dbl>
                            <dbl>
                                    <dbl> <chr>
   1 700014718
                 -2.64e-1
                           0.222
                                     5.58 Stool
                  5.16e-1
   2 700014767
                           0.174
                                     2.14 Anterior_nares
   3 700014923
                  5.05e-1
                           0.183
                                     2.32 Anterior_nares
                  3.50e-3 -0.434
   4 700016920
                                     4.96 Anterior nares
                 -8.28e-4 -0.290
   5 700023706
                                     4.98 Anterior_nares
   6 700038343
                 -1.54e-3 -0.435
                                     5.56 Anterior nares
                 -2.22e-1
   7 700095956
                           0.189
                                     4.86 Stool
                 -2.25e-1
                                     4.58 Stool
   8 700105834
                           0.174
   9 700107189
                 -9.78e-2 0.0363
                                     4.27 Stool
## 10 700109383
                 -2.13e-1 0.180
                                     4.44 Stool
## # ... with 3 more variables: dummy_variable_shannon <dbl>,
      dummy_variable_pc <dbl>, dummy_category <lql>
```

```
##
## Call:
## adonis(formula = otu_dist ~ hmpbodysubsite, data = sorted_summary)
##
## Permutation: free
## Number of permutations: 999
##
## Terms added sequentially (first to last)
##
                Df SumsOfSqs MeanSqs F.Model R2 Pr(>F)
## hmpbodysubsite 1 0.7036 0.70364 1.5719 0.16422 0.014 *
## Residuals
                 8 3.5811 0.44764
                                          0.83578
## Total
                 9 4.2847
                               1.00000
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

multivariable possible...

```
adonis(otu_dist ~ hmpbodysubsite + dummy_category,
       data = sorted_summary)
##
## Call:
## adonis(formula = otu_dist ~ hmpbodysubsite + dummy_category, data = sorted_summary)
##
## Permutation: free
## Number of permutations: 999
##
## Terms added sequentially (first to last)
##
                Df SumsOfSqs MeanSqs F.Model
                                               R2 Pr(>F)
## hmpbodysubsite 1
                     0.7036 0.70364 1.6100 0.16422 0.002 **
## dummy_category 1 0.5218 0.52180 1.1939 0.12178 0.125
## Residuals
                7 3.0593 0.43704
                                           0.71400
## Total
           9 4.2847
                               1.00000
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

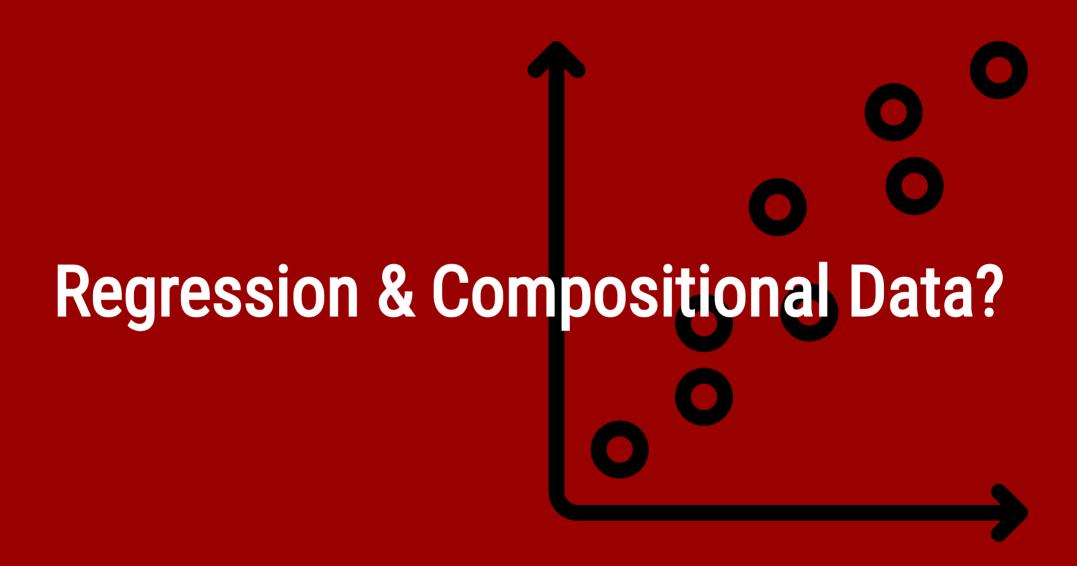
... but order matters!!!

```
adonis(otu_dist ~ dummy_category + hmpbodysubsite,
       data = sorted_summary)
##
## Call:
## adonis(formula = otu_dist ~ dummy_category + hmpbodysubsite, data = sorted_summary)
##
## Permutation: free
## Number of permutations: 999
##
## Terms added sequentially (first to last)
##
                Df SumsOfSqs MeanSqs F.Model
                                               R2 Pr(>F)
                      0.6329 0.63293 1.4482 0.14772 0.018 *
## dummy_category 1
## hmpbodysubsite 1 0.5925 0.59251 1.3557 0.13828 0.036 *
                7 3.0593 0.43704
## Residuals
                                           0.71400
## Total
           9 4.2847
                                    1.00000
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
##
## Call:
## adonis(formula = otu_dist ~ dummy_category, data = sorted_summary,
                                                                       strata = sorted_summary$hmpbodysubsite)
##
## Blocks: strata
## Permutation: free
## Number of permutations: 999
## Terms added sequentially (first to last)
##
                 Df SumsOfSqs MeanSqs F.Model
                                                 R2 Pr(>F)
## dummy_category 1
                      0.6329 0.63293 1.3865 0.14772 0.291
## Residuals
                  8 3.6518 0.45648
                                            0.85228
## Total
                  9 4.2847
                                     1.00000
```

```
adonis(otu_dist ~ dummy_category / hmpbodysubsite,
       data = sorted_summary)
##
## Call:
## adonis(formula = otu_dist ~ dummy_category/hmpbodysubsite, data = sorted_summary)
##
## Permutation: free
## Number of permutations: 999
##
## Terms added sequentially (first to last)
##
                               Df SumsOfSqs MeanSqs F.Model
                                                               R2 Pr(>F)
                                    0.6329 0.63293 1.4482 0.14772 0.009 **
## dummy_category
## dummy_category:hmpbodysubsite 1 0.5925 0.59251 1.3557 0.13828 0.023 *
## Residuals
                                  3.0593 0.43704
                                                           0.71400
## Total
                                9 4.2847
                                                    1.00000
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

... or do you mean nestedness?



Regression & Compositional Data?

• Compositional data approaches correct OTU dependency:

```
o e.g., compositions::clr() or philr::philr()
```

- p >> n challenges persist
- Must pair compositional transform with regularization:
 - o glmnet::glmnet for LASSO/ridge/elastic net
 - Bayesian methods



Thank you!

Slides available: github.com/bjklab

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