

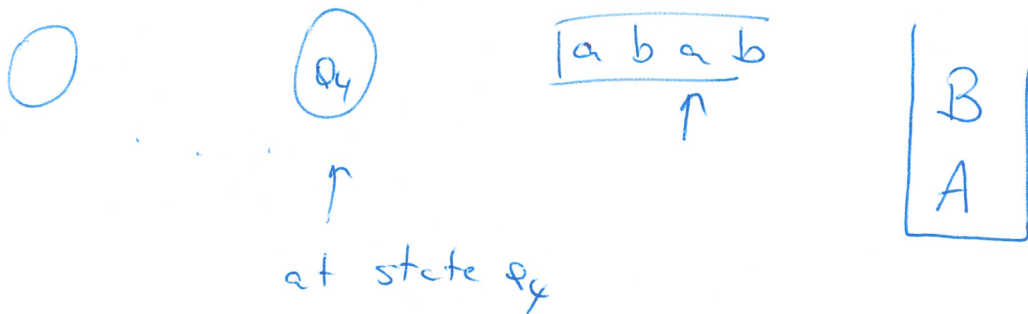
Averages:

exam 1: 80.54 2: 83.84 3: 86.45

Last time: PDA

Configuration of a PDA is represented by a triple $[q_i, w, \alpha]$

↓ snapshot ↓ stack contents
↓ unprocessed input
machine state.



$[q_4, ab, BA]$
↑
top on the left

Definition 7.1.2 Let $M = (Q, \Sigma, \Gamma, \delta, q_0, F)$ be a PDA
A string $w \in \Sigma^*$ is accepted by M if there
is a computation

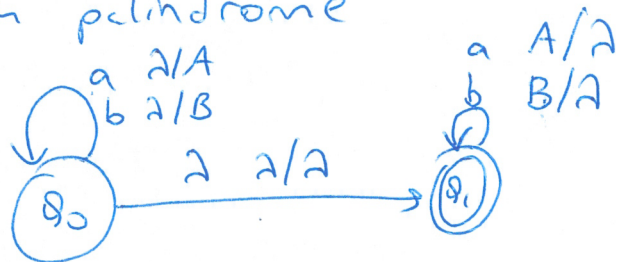
$[q_0, w, \lambda] \xrightarrow{*} [q_i, \lambda, \lambda]$

$q_i \in F$ ↓ the stack has to be empty for acceptance
the entire input must be processed for acceptance

This means there has to be a series of transitions from the starting configuration to an accepting configuration.

(2)

even length palindrome



abba

$[q_0, abba, \lambda]$

$[q_0, bba, A]$ $[q_1, abba, \lambda]$

$[q_d \dots]$

goes to dead state

$[q_0, ba, BA]$ $[q_1, bba, A]$

$[q_d \dots]$

$[q_0, a, BBA]$ $[q_1, ba, BA]$

accepts

PDA \leftrightarrow CFG

~~3331~~ 3311

4811

5811

5311

grad theory course

DFA's are models of regular languages.

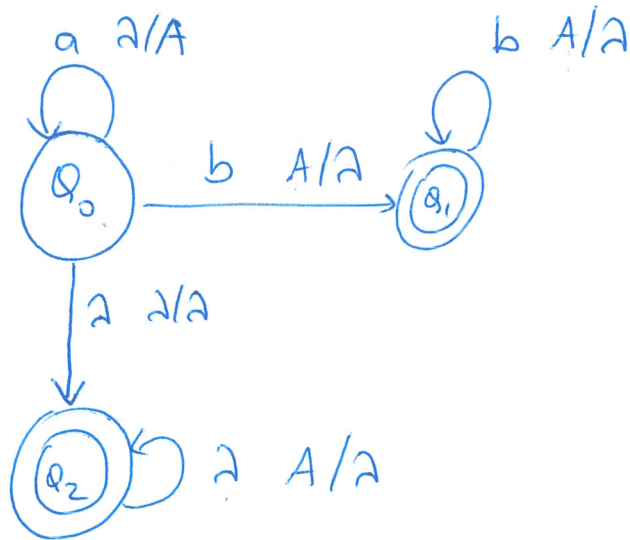
PDA's are models of context free languages.

Not every nondeterministic PDA has an equivalent deterministic PDA.

$a^n b^n$

3

$$L = \{ a^i \mid i \geq 0 \} \cup \{ a^i b^i \mid i \geq 0 \}$$



$\{ i \text{ b's are needed} \}$

$\{ \text{no b's are needed} \}$

aaa

A
A
A

 $[q_2, 2, 2]$

aabb

A
A

 bb will fail at the lower path

A
1

 bb

A

 b

2

 a

q_1 q_1

Chapter 8 Turing machines

4

0

0

0

finite state machine



↑
read/write tape

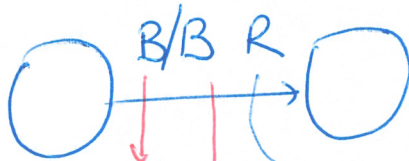
can move left or right

the remainder of the tape is padded with blanks

blank tape character

$B \notin \Sigma$

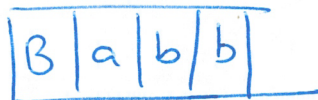
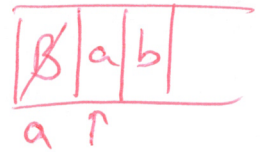
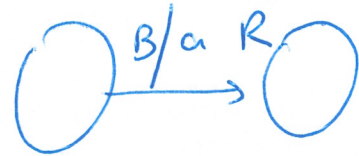
the input is always finite



read

write

direction of movement (by one cell only)



↑

B/B R

a/A L

