Scanners (Objectives)

 Given a regular expression, the student will be able to construct its corresponding NFA, DFA and scanner

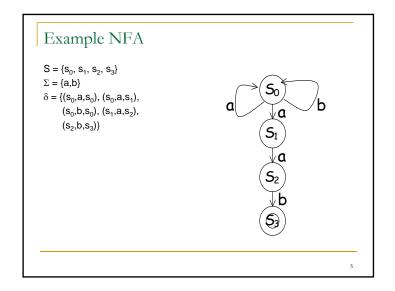
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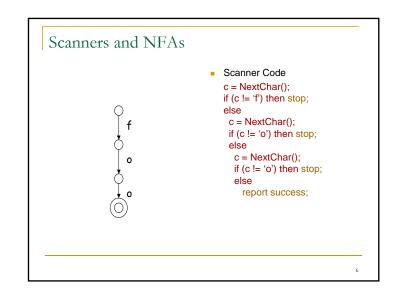
token - name representing a class of character strings token - parser request

Regular Expression Regular Expression NFA DFA Minimized DFA Scanner

NFAs

- NFA nondeterministic finite automaton
 - S a set of states
 - Σ an alphabet
 - \circ δ a transition function
 - s₀ a start state
 - S_F a set of final states $S_F \subseteq S$





Regular Expression (RE) Definitions

• ϵ -the null symbol

• ϵ - the alphabet over which the RE is defined

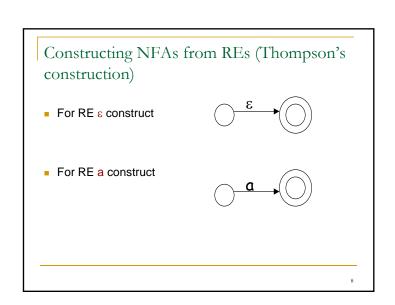
• if $a \in \Sigma$ then a is the RE denoting $\{a\}$ • L(r) is the language denoted by RE r• if r and s are REs then

• r is an RE denoting $L(r) \cup L(s)$ (alternation)

• r is is an RE denoting $L(r) \cap L(s)$ (concatenation)

• r is an RE denoting $L(r) \cap L(s)$ (Kleen closure)

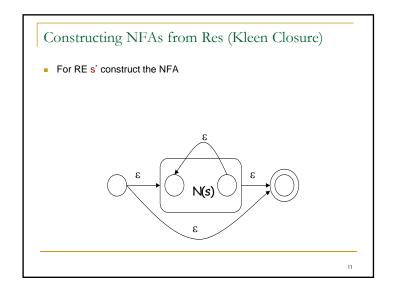
• RE for example (a|b) aab

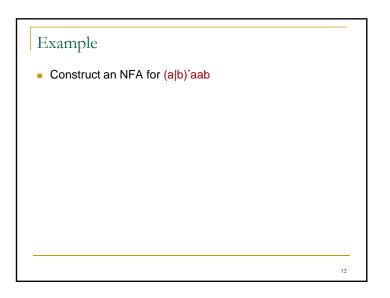


Constructing NFAs from REs (Alternation) Given NFAs N(s) and N(t) for REs s and t The NFA for s|t is

N(s)

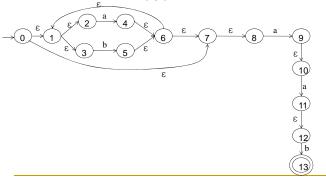
Constructing NFAs from REs (Concatenation) = For RE st construct the following NFA where s_0 of N(s) is the start state and S_F of N(t) are the end states and there is an ϵ -transition from S_F of N(s) to s_0 of N(t)





Example

Construct an NFA for (a|b)*aab



DFAs from NFAs

```
q_0 \leftarrow \epsilon\text{-closure}(\{s_0\})
                                                 ε-closure(T) {
\ddot{Q} \leftarrow \{q_0\}
                                                     push states in T on stack
 while \exists unmarked q_i \in Q {
                                                     C = T
  mark q
                                                     while stack not empty do {
  for each \alpha \in \Sigma {
                                                       t = pop T
   t \leftarrow \varepsilon-closure(move(q_i, \alpha))
                                                        for each t \rightarrow u labeled \epsilon
    if t ∉Q
                                                         if u ∉ C then {
     Q \cup = \{t\}
                                                           C \cup = \{u\}
    T[q_i,\alpha] \leftarrow t
                                                           push u onto stack
```

 $move(q_i, \alpha) = \{s_k \mid \exists s_i \in q_i, s_i \rightarrow s_k | abeled \alpha\}$

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Example

Convert NFA for (a|b)*aab to a DFA

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Example

Convert NFA for (a|b)*aab to a DFA

 $q_0 = \varepsilon - closure(\{s_0\}) = \{s_0, s_1, s_7, s_2, s_3, s_8\} == \{s_0, s_1, s_2, s_3, s_7, s_8\} / / start \quad state$

$$\begin{split} T[q_0,a] &= \mathcal{E} - closure(\{s_4,s_9\}) = \{s_4,s_9,s_6,s_{10},s_1,s_7,s_2,s_3,s_8\} = \{s_1,s_2,s_3,s_4,s_6,s_7,s_8,s_9,s_{10}\} = q_1 \\ T[q_0,b] &= \mathcal{E} - closure(\{s_5\}) = \{s_5,s_6,s_1,s_7,s_2,s_3,s_8\} = \{s_1,s_2,s_3,s_5,s_6,s_7,s_8\} = q_2 \end{split}$$

 $T[q_1,a] = \varepsilon - closure(\{s_1,s_9,s_{11}\}) = \{s_4,s_9,s_{11},s_6,s_{10},s_{12},s_1,s_7,s_2,s_3,s_8\} = \{s_1,s_2,s_3,s_4,s_6,s_7,s_8,s_9,s_{10},s_{11},s_{12}\} = q_3$ $T[q_1,b] = \varepsilon - closure(\{s_8\}) = q_2$

 $T[q_2, a] = \varepsilon - closure(\{s_4, s_9\}) = q_1$ $T[q_2, b] = \varepsilon - closure(\{s_5\}) = q_2$

 $T[q_3, a] = \varepsilon - closure(\{s_4, s_9, s_{11}\}) = q_3$

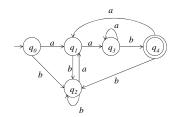
 $T[q_3,b] = \varepsilon - closure(\{s_5,s_{13}\}) = \{s_5,s_{13},s_6,s_1,s_7,s_2,s_3,s_8\} = = \{s_1,s_2,s_3,s_5,s_6,s_7,s_8,s_{13}\} = q_4 \ / \ final \quad state$

 $T[q_4, a] = \varepsilon - closure(\{s_4, s_9\}) = q_1$ $T[q_4, b] = \varepsilon - closure(\{s_5\}) = q_2$

Example

Convert NFA for (a|b)*aab to a DFA

	а	b
q_0	q_1	q_2
q_1	q_3	q_2
q_2	q_1	q_2
q_3	q_3	q_4
q_4	q_1	q_2



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DFA Minimization

- After conversion from an NFA to a DFA, there may be unnecessary states.
- We can minimize the number of states to reduce the space requirement of the DFA.
- Two states are said to be equivalent if they produce the same behavior on any input string.
- The algorithm will partition the set of states $S = \{s_1, s_2, ..., s_n\}$ into partitions $P = \{p_1, p_2, ..., p_m\}$ such that all states $s_i \in p_i$ are equivalent.

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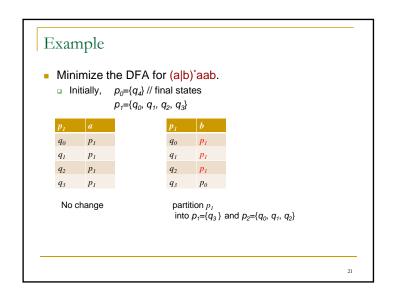
DFA Minimization

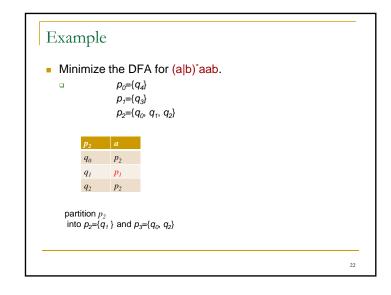
```
\begin{split} T &\leftarrow \{S_F, S - S_F\} \\ \text{repeat} \\ P &\leftarrow T \\ T &\leftarrow \varnothing \\ \text{for each set } p \in P \ \{ \\ \text{for each } \alpha \in \Sigma \\ \text{partition } p \text{ by } \alpha \text{ into } p_1, ..., p_k \\ T &\leftarrow T \cup p_1 \cup ... \cup p_k \\ \} \\ \text{until } T &== P \end{split}
```

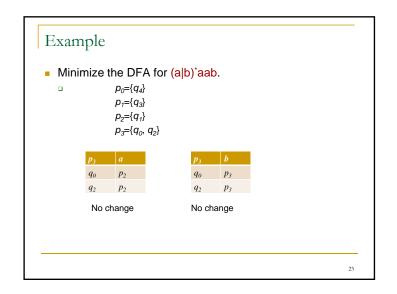
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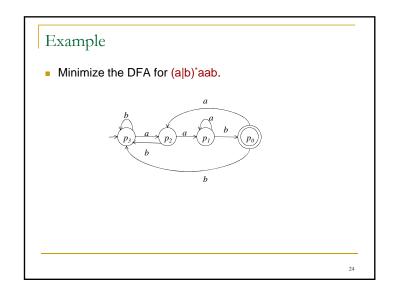
Example

Minimize the DFA for (a|b)*aab.









DFA to Scanner

■ Emit table driven or direct code

char	а	b	other
class	class-a	class-b	other

state	p_0	p ₁	p ₂	p ₃
class-a				
class-b				
other				

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Code for Scanner

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Real Issues

- Note that there is a rule to scan the longest-possible tokens, meaning you return only when the next character can't be used to continue the current token
 - the next character will generally need to be saved for the next token
- In some cases, you may need to peek at more than one character of look-ahead in order to know whether to proceed
 - □ In Pascal, for example, when you have a 3 and you a see a dot
 - do you proceed (in hopes of getting 3.14)? or
 - do you stop (in fear of getting 3..5)?

What else is hard?

PL/I has no reserved words

if then then then = else; else else = then;

Fortran ignores blanks

```
d o10 i=1 ,2 5
do 10 i = 1 . 25
```

Is Fortran really that hard to scan?

```
INTEGERFUNCTIONA
     PARAMETER(A=6,B=2)
     IMPLICIT CHARACTER*(A-B)(C-D)
     INTEGER FORMAT(10), IF(10), DO9E1
     FORMAT(4H)=(3)
     FORMAT(4 )=(3)
     DO9E1=1
     DO9E1=1,2
     1F(X)=1
     IF(X)H=1
     1F(X)300,200
     END
     THIS IS A "COMMENT CARD"
     $FILE(1)
200
     END
```

Example due to Dr. F.K. Zadeck, from Eng. A Compiler, Cooper and Torczon

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Practice Problem

 For the regular expression (aa)* | (ab)*, construct an NFA using the method discussed in class, convert that NFA and then minimize the resulting DFA.