

DEPARTMENT OF MECHANICAL AND AEROSPACE ENGINEERING

HONOURS THESIS

TRANSIENT SUPERSONIC JETS

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Abstract

This thesis aims to explore the fundamental fluid dynamics for transient supersonic jets by means of varying the exit flow nozzle geometry and introducing an impingement plate set at 90° to the oncoming flow. The study of transient supersonic jets has applications in pressure gain combustion (PGC). PGC is a constant volume combustion process applicable to gas turbines that operates by increasing the stagnation pressure entering the turbine via heat released from combustion. Increasing the turbine inlet pressure allows for considerably more work to be extracted when the turbine expands the flow back to the free stream pressure. The unique design presented in PGC engines predicts possible advances in thermodynamic efficiencies leading to significantly lower fossil fuel consumption. The experiment undertaken compares flow regimes of NUMBER and NUMBER Mach numbers for each nozzle geometry at impingement plate positions of 1 and 4 inner nozzle diameters. Transient jet impingement has previously been studied, although it is absent of extensive, repeated experiments, high quality schlieren, and variable exit geometry. This thesis aims to address absences in the literature and explore in detail the shock-vortex interaction during jet impingement. The fundamental fluid dynamics under investigation are; nozzle geometry effects on the shockvortex interaction and jet impingement, and Mach number variations on all of the latter.

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Nomenclature

- M₁ Ambient Mach number
- P₁ Ambient pressure, Pa
- P_4 Shock tube driver section pressure, Pa
- U_1 Ambient air velocity, m/s
- U_4 Shock tube driver section air velocity, m/s
- γ_1 Ambient specific heat ratio
- γ_4 Driver specific heat ratio

1 Introduction

1.1 Motivation

Understanding transient supersonic jets is integral for the integration of pressure gain combustion in ground and aerospace gas turbine applications. PGC offers a significant gain in thermodynamic efficiencies and subsequent reduction in fossil fuel consumption. The literature adeptly describes transient supersonic jet fluid dynamics for propagation from a no nozzle shock tube, and impingement on plates set to varying angles in respect to the flow. However, there is an absence of extensive, repeated experiments, high quality schlieren, and variable exit geometry. The motivation of this experiment is to address absences in the literature discussed in 2 and to explore in detail, the shock-vortex interaction during jet impingement. To this end the project will seek to answer the following research questions:

1.2 Aims

This thesis aims to explore the fundamental fluid dynamics for transient supersonic jets by means of varying the exit flow nozzle geometry and introducing an impingement plate set at 90° to the oncoming flow. The propagation and time dependent growth of transient and trailing jet Mach disks will be investigated in an attempt to address absences in the literature, and explore in detail the shock-vortex interaction during jet impingement. The pixel relative velocity of the impinging shock wave for plate and no plate experiments will be extracted from the data in order to define each individual flow regime. The fundamental fluid dynamics under investigation are; nozzle geometry effects on the shock-vortex interaction and jet impingement, and Mach number variations on all of the latter.

2 Background Theory

2.1 Pressure Gain Combustion

Gas turbine engines are an integral component for the function of ground based power generation and aircraft engines. They account for a large percentage of power generation world wide. Thermodynamic cycle advances in gas turbine design play an important role in preventing the growth of emissions pollution and prolonged global warming [6]. Pressure gain combustion (PGC) shown in Figure 1 is one possible to method of efficiency improvement. PGC is a constant volume combustion process that operates by increasing the stagnation pressure entering the turbine via heat released from combustion. Increasing the turbine inlet pressure allows for considerably more work to be extracted when the turbine expands the flow back to the free stream pressure. PGC optimises gas turbine thermodynamic cycle efficiency, and has the potential to increase current engine efficiency up to 10% [7].

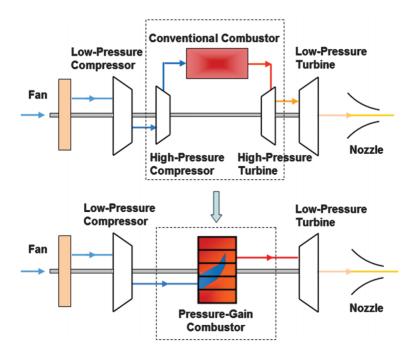


Figure 1: PCG design concept [1].

PGC is at peak efficiency when accomplished through detonation driven combustion, this involves the implementation of detonation waves within the combuster to cause an increase in the temperature and pressure of the fuel-air mixture [8]. During combustion, detonation waves produce flow at supersonic velocities leading to an approximate constant volume and significant pressure gain across the combustor. For supersonic velocities high pressure turbine inlet flow must be steady. A possible method to achieve steady flow at the turbine inlet is via the implementation of a pulse detonation engine [9] with an equalising plenum chamber. Wear on the first stage of the turbine presents itself as one of the most significant problems of PGC implementation in current engines. Replacing the combustor in a conventional gas turbine with a pulse detonation combustor (PDC) will result in the propergating detonation waves to converge on the first stage of the turbine. This overtime can lead to concentrated wear on the first stage of the turbine high wear stress points [10]. To alleviate turbine wear,

the utilization of a high pressure plenum chamber is placed at the exit of the PDC, and creates steady flow conditions effectively shielding the first stage of the turbine from combustion detonations. It remains unclear on how to integrate a pressure plenum into a PDC design.

2.2 Transient Supersonic Jet

The fluid dynamics characterising the governing flow at the exit of PDC is defined as a shock-driven, transient, supersonic jet process [11]. The governing flow can be classified into several different stages [12]. The first stage of jet evolution is defined by the diffraction of a shock wave around the corners of the tube exit as shown in Figure 2. This region is bounded by the curved part of the incident shock, the nozzle lip, and a reflected sound wave. In the next

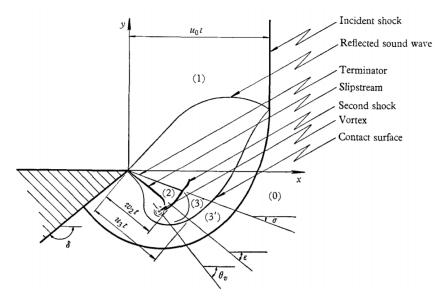


Figure 2: Features of the diffraction pattern [2]

stage of jet evolution, a vortex ring is generated by the roll-up of the shear layer due to Kelvin-Helmholtz type instabilities along the slipstream at the nozzle lip [13, 14]. Kelvin-Helmholtz instabilities exist within the shock as a result of external perturbations (inhomogeneities in the flow) producing oscillations in the vortex sheet separating fluids with different flow characteristics. This structure propagates down the jet axis, and is simultaneously accompanied by the translation of a curved barrel shock formed initially at the nozzle lip. This instigates the formation of a curved Mach disk for a ratio of the nozzle exit to free-stream pressure exceeding 2.06 [15]. MORE ON MACH DISK

A triple point occurs between the leading edge of the barrel shock, the second shock, and the Mach disk. Given a sufficiently strong jet, a slip surface is generated downstream of the triple point. The first shock cell is formed in the third stage of jet evolution which is marked by the pinch-off phenomenon of the vortex ring, and signals the start of the trailing jet phase [16]. Separation of the vortex ring from the flow structure is driven by Kelvin-Helmholtz instabilities within the shear layer of the trailing jet [17]. The final stage of the supersonic jet is defined by the point at which the transient jet and vortex are no longer joined and the trailing jet forms. This is accompanied by the formation of a quasi-steady shock cell in self-sustained oscillation, radiating strong pressure waves. These four stages of jet evolution are illustrated in Figure 3.

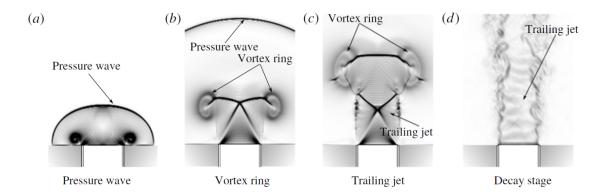


Figure 3: Evolution of the transient supersonic jet. (a) Diffracting shock/Pressure wave. (b) Axial translation of the vortex rings, formation of the curved shock and an unsteady Mach disk. (c) Formation of the trailing supersonic jet. (d) Decay of the trailing jet and the end of the transient jet process. [3]

2.3 Transient Jet Impingement

Investigation into the high pressure plenum chamber required for PDEs currently has not been undertaken within the field. However, the flow dynamics is considered analogous to the impingement of a transient supersonic jet on a flat plate. The governing dynamics of transient jet impingment can be classified into serveral stages. The physical process is initially characterised by the reflection of the incident shock wave on the impinging plate. The reflected shock wave propargates back towards the nozzle and interacts with the approaching vortex ring. The central section of the reflected shock wave is captured by the embedded rearward-facing shock at the centre of the vortex ring, and is intensified by the opposing high-speed flow. Simultaneously, the outer section of the shock wave is diffracted by the vortex core. This process results in the formation of a toroidal shock wave which focuses in the trailing jet along the longitudinal axis of flow. The next stage of the fluid dynamics is defined by the impingement of the propagating vortex ring. Initially, as the vortex ring approaches the wall, its propagation velocity decreases and its diameter increases due to the adverse pressure gradient present [4]. After votex impingement the vortical flow undergoes rapid radial expansion developing a boundary layer on the surface, which slows down the flow and increases the pressure distribution over the plate. After a given duration that is dependent on the initial incident Mach number, the boundary layer separates from the plate and the flow rolls up generating a series of secondary vortices. This also occurs at the thin shear layer present between the jet flow and the exterior fluid as the region rolls up due to Kelvin-Helmholtz instabilities. This produces small interacting secondary vortex rings that propagate towards the plate [18]. Cumulative interactions between the primary and secondary wall vortex rings result in a near standing lift off of the pair. The secondary ring subsequently merges with the primary ring, and the weakened newly formed vortex ring continues to translate down the plate. Stages of impingement are illustrated in Figure 4 below.

For a plate of variable angle, the lower core of the vortex ring impinges initially and generates an asymmetric set of secondary vortices. These new flow structures orbit around the main vortex, creating a temporarily thicker boundary layer at the lower end of the flow field. Again after a period of time, dependent on the incident Mach number, he boundary layer

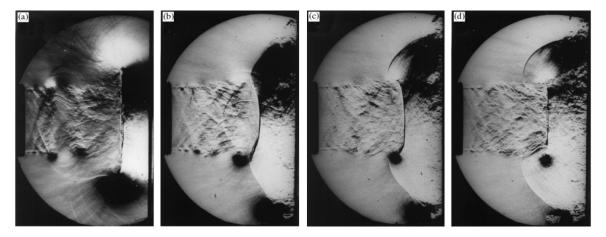


Figure 4: Evolution of jet impingement. (a) Impingement of vortex ring. (b) Vortex ring translates down the plate. (c) Secondary vortex formation. (d) Lift-off of votex rings and dissapation. [4]

separates from the plate. This results in the vortex ring pivoting on the lower core, undergoing negligible deformation, and propergates towards the surface plate. The upper core then impinges on the plate and the upper wall vortex is generated. This new structure begins to expand radially increasing in thickness due to the remaining jet flow. While simultaneously, the lower wall vortex propagates around the outer limits of the main vortex, stops expanding, and dissipates into a thin structure. The impinging jet continues to feed into the upper section of the flow field generating wall vortices with a thicker upper core. For lower angles of plate alignment, the flow field shows an increase in overall velocity and visible curvature of the vortex ring structure during impingement. The toroidal shock wave that forms as a result of impingement propagates perpendicularly with respect to the surface [19].

2.4 Acoustic Noise

The far-field noise developed by the shock wave-vortex interaction can be decomposed into three components, the sound field due to the formation and evolution of the vortex ring, the reflection shock and vortex ring interaction noise production, and the noise due to impingement of the ring on the plate. The plate-votex ring impingement noise is produced by fluctuating pressure due to the deformation and stretching of the vortex ring, formation and growth of a secondary wall vortex ring, and lifting-off of the primary-secondary vortex ring pair [20].

3 Experimental Methods & Analysis Techniques

3.1 Technical University of Berlin Pulse Detonation Combustion Facility

The initial imaging processing work conducted in this thesis was tested on experimental data supplied by the Technical University of Berlin's pulse detonation combustion (PDC) facility. The PDC consists of a 685 mm deflagration-to-detonation transition (DDT) section and 825 mm exhaust tube. The DDT section has a diameter of 40 mm whilst the exhaust tube has a diameter of 30 mm. Hydrogen and air are fed to the DDT section. A number of orifice plates are used to initiate DDT. The detonation wave front is tracked through the exhaust tube using a number of ionisation and pressure sensors. Schlieren measurements were undertaken using a Toepler Z-Type schlieren system(20). Two 8in parabolic mirrors were combined with a high speed LED(21) to produce images of the exhaust flow. Images were recorded on a Photron SA-Z camera for converging and diverging nozzles.

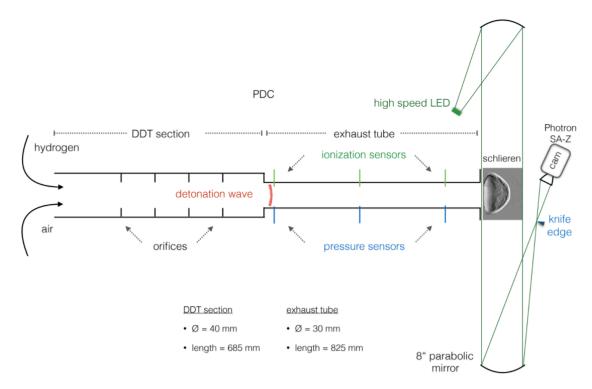


Figure 5: Shock tube facility schematic. Major parts of the system have been labelled.

3.2 Shock Tube Facility

The experiments presented were conducted in the LTRAC Supersonic Jet Facility. A schematic of the facility is shown in Figure 6.

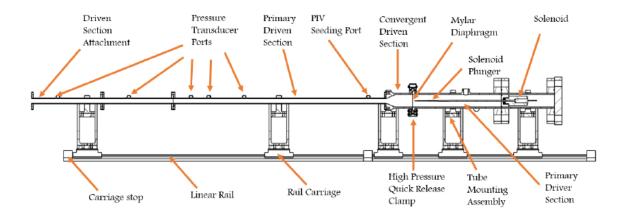


Figure 6: Shock tube facility schematic. Major parts of the system have been labelled.

The facility utilises compressed air delivered by the Monash University compressed air supply system. To produce a canonical transient supersonic jet a shock tube model is adopted [21]. A typical shock tube consists of a high pressure section (driver section) and a low pressure section (driven section) separated by a diaphragm. Air enters the driver section until a desired pressure is reached, the diaphragm is then ruptured via a puncture from an actuated pin. Following the rupture, compression waves are fired down the driven section by the high pressure gas in the driver. As these compression waves travel down the tube they coalesce and form a shock wave that propagates into the test section, diffracts, and produces a transient supersonic jet.

For the aims of this thesis, the supersonic transient jet will be studied with varied nozzle designs including a convergent, divergent and convergent-divergent configuration. Transient flow impingement will be tested via a flat plate set at 90° to the flow. This impinging plate is set exactly at an angle of 90° to the flow by a sequence of precisely 90° connecting supports to the shock tube. The three nozzle designs and impingement plate will be integrated into the existing LTRAC Supersonic Jet Facility.

The relationship between the driver (4) pressure ratio and the ambient (1) pressure of the system is shown in Equation 1, and was utilised to calculate the design incident Mach number propagating from the shock tube [22]. Figure 7 illustrates the effect of specific heat capacity ratio on the relation between incident Mach number and pressure ratio. Helium gas has increasingly lower pressure ratios for higher Mach numbers in comparison to air, and as a result was chosen as the driver section supply gas.

$$\frac{P_4}{P_1} = \frac{2\gamma_1 M_1^2 - (\gamma_1 - 1)}{\gamma_1 + 1} \left(1 - \frac{\gamma_{4-1}}{\gamma_{1+1}} \frac{U_1}{U_4} \left(M_1 - \frac{1}{M_1} \right) \right)^{-2\gamma_4/\gamma_{4-1}} \tag{1}$$

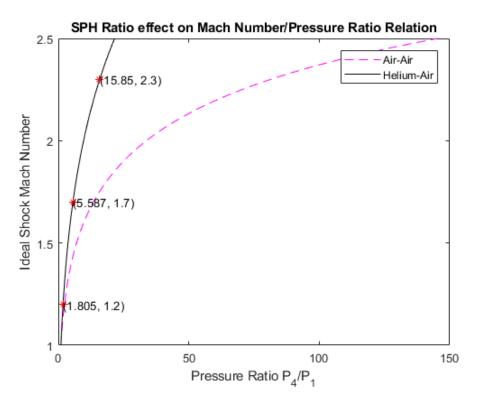


Figure 7: Specific Heat Capacity Ratio effect on Mach Number/Pressure Ratio Relation.

3.3 Facility Development and Calibration

3.4 Nozzle Design

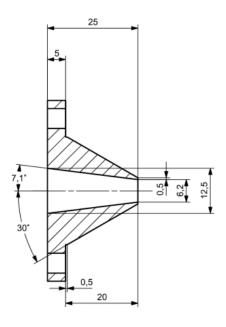
A convergent, divergent, and convergent-divergent nozzle was designed using CAD and manufactured by the Engineering department Mechanical Workshop. All three nozzle designs adopt geometry ratios implemented in the nozzles designed by Technical University of Berlin (TUB). To prevent reflecting flow and acoustic feedback loop interference, each nozzle geometry was designed with a 60° exterior angle and a 0.5mm lip [23]. Each nozzle design and subsequently manufactured component is shown in Figures 8, 9, and 10 below.

3.5 Impingement Plate Design and Development

The impingement plate as shown in Figure ?? is constructed such that it is 90° to the direction of the flow, and in the reference frame of the oncoming flow appears infinite. The plate is mounted on rails which fix to the shock tube rig, this construction can be adjusted to 1 and 4 inner diameters. This construction allows the plate to be removed and replaced with another plate of alternate geometry for future research. During the evolution of a transient supersonic jet, the vortex is fully formed at approximately 3 inner diameters from the exit for a conventional, no nozzle, shock tube [?]. As a result, an impingement plate distance is chosen below and above this limit at 1 and 4 inner diameters, respectively.

INCLUDE PLATE CAD AND PHOTO

The first iterative design of the plate resulted in a slight unexpected wobble during jet impingement, shown in Figure ??. This design error was resolved by the addition of two support frames between the plate and the mounting arms. The position of the support frames

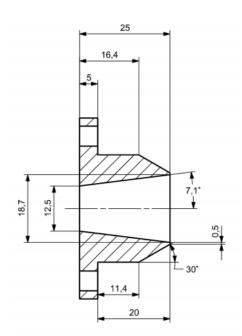


(a) CAD design (all measurements are in mm).



(b) Manufactured nozzle.

Figure 8: Convergent nozzle.

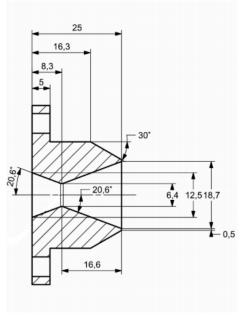


(a) CAD design (all measurements are in mm). $\,$



(b) Manufactured nozzle.

Figure 9: Divergent nozzle.



(a) CAD design (all measurements are in mm).



(b) Manufactured nozzle.

Figure 10: Convergent-divergent nozzle.

was chosen such that interference with the transient supersonic jet and impingement byproducts was not possible. This design iteration is shown in Figure ??

- 3.5.1 Hydrostatic Test
- 3.5.2 Sensor Calibration
- 3.5.3 Diaphragm Study
- 3.5.4 LED Calibration

3.6 Schlieren Imaging

Schlieren imaging is a visualization technique that utilises the refraction of light to produce focused optical images of transparent media. Point source light is collimated and passed through a test region containing a transparent media with inhomogeneities. Light entering the test region will refract at varied degrees according to an inhomogeneous density distribution present. When refraction occurs the curvature ϵ of light, for a given test section length L, and refractive index n_0 can be calculated using Equations 2 and 3 for x and y orthogonal coordinates. The light is then refocused and a knife-edge is used to partially block a fraction of incident light from the screen or camera.

$$\epsilon_x = \frac{L}{n_0} \frac{\delta n}{\delta x} \tag{2}$$

$$\epsilon_{y} = \frac{L}{n_0} \frac{\delta n}{\delta y} \tag{3}$$

The shock-driven, transient, supersonic jet is measured using a Toepler Z-type schlieren apparatus [24] (illustrated in Figure 11). This Z-type apparatus incorporates parabolic mirrors to collimate the light. Parabolic mirrors eliminates problems associated with chromatic aberration and provides a unique advantage for imaging in comparison to systems using lenses. However, the use of mirrors introduces common imaging problems including coma and astigmatism. Coma is the result of off-axis, incorrect parabolic mirror tilting and disrupts the collimated light beam. It also causes the focal point of the parabolic mirrors to spread into a line. This issue is resolved by careful calibration of each parabolic mirror titling to achieve an overall cancelling effect. Astigmatism is similarly caused by tilting the parabolic mirror off-axis. It occurs due alternating path lengths of light dependent on their respective optical plane. Astigmatism results in different focal points for each plane of propagating light and requires the knife-edge to be positioned for different density gradients. For Z-type schlieren configurations, coma and astigmatism is minimised by restricting the offset angle (tilt) of the parabolic mirrors to minimum achievable values. Careful calibration prior to experimentation is required to avoid problems associated with coma and astigmatism. This involves correcting mirror allingments, adjusting the knife edge, and positioning the camera distance until the desired image is displayed. The parabolic mirrors used in the facility have an an effective focal length of 1200mm and the light source was supplied by a pulsed LED [25].

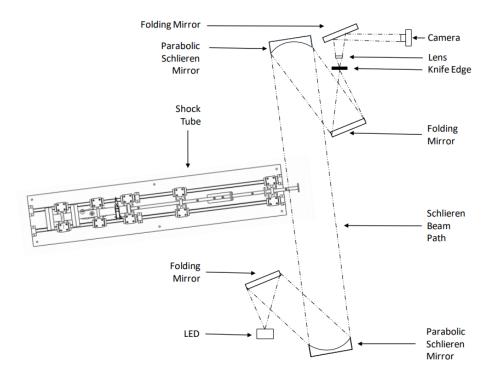


Figure 11: Detail schlieren system diagram

3.6.1 High Resolution Imaging

3.6.2 High Speed Imaging

became in focus. This method was utilised to calibrate both the high resolution and high to with the Shimadzu HPV-1 camera. The Shimadzu has a resolution of 312 x 260 pixels and a

frame rate of up to 1 million fps.

3.6.3 Limitations

Schlieren imaging has a number of limitations. Firstly, schlieren images are constructed using density gradients within the test region. The gradients are integrated over the optical path and as a result, images are developed as two-dimensional projections of an original three-dimensional fluid flow. This introduces possible incorrect projects of three-dimensional features. Additionally, the technique is line-of-sight dependent as the light must be collimated and refocused in order to produce an image. This restricts the layout of test section and sets requirements on the amount of space required for the apparatus.

3.7 Post Processing

Schlieren imaging produces a path integrated density gradient image that is excellent for flow visualisation but, is difficult to quantitatively extract physical parameters directly from image data.

3.7.1 Second Order Convolution

the required second order image derivatives are computed by convolution with the second order derivatives of the Gaussian kernel (reference). Mathematically this means that if f denotes the image and G the normalised Gaussian, we compute EQUATIONS where * denotes spatial convolution, x=(x,y) denotes the pixel position, and the derivative directions i and j can be x or y. The eigenvectors and eigenvalues are computed in the algorithm from a standard second derivative Hessian matrix

HESSIAN MATRIX

3.7.2 Ranking Methods

Use a normalised ranking to threshold intensity lower then the 90th percentile

4 Results & Analysis

5 Discussion

6 Conclusions and Recommendations

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A Shock Facility

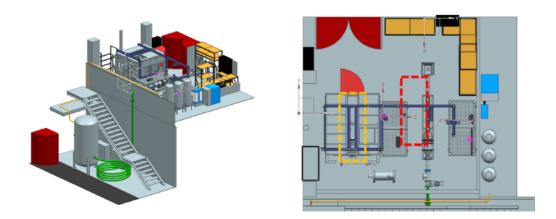


Figure 12: (Left): Isometric view of the LTRAC Shock Lab, with the shock tube facility stored under the shelving. (Right): Top view of the LTRAC Shock Lab, with the PIV (orange) and schlieren (red) sites highlighted.



Figure 13: Isometric view of the design of the shock tube facility. (Right): Progress of the commission of the shock tube facility.

B Literature Comparison

Initially, it is necessary to explore the literature and develop an understanding of the current comprehension of the flow characteristics governing supersonic transient jet impingement, and previous experimental test configurations. Section 2 undertakes an extensive review of previous literature, exploring the fluid dynamics and practical applications of supersonic impinging jets. Table 1 details a summary for the research undertaken in previous literature,

it's important to note all previous literature sources implement a plate diameter such that it can be considered infinite to the flow. Additionally, imaging results from the literature summarised in Table 1 is subsequently shown in appendix ??.

Table 1: Literature Summary

Reference	Main Research Focus	Imaging Technique	Inner Shock Tube Diameter	Incident Mach Number	Impingement Plate Distance (inner diameter				
[18]	Shock-vortex interaction in the flow field	Shadowgraph	40mm	1.35	0.4di				
[4]	Sound generation upon impingement	Schlieren	65mm	1.14	2di				
[20]	Noise due to shock- vortex interaction and impingement	High-speed smoke flow visualisations.	64mm	1.31 - 1.55	4.7di				
[26]	Vortex ring impingement	High-speed smoke flow visualisations.	64mm	1.31 - 1.85	4.7di				
[19] Vortex ring impingement		Schlieren	30mm	1.61	1.66di, 3.33di, 5.00di				

C Shock Relations

In this section, the relationship between the pressure of the flow behind the leading shock and the ambient pressure will be derived. Figure 14 details pressure, temperature, and velocity relations for the shock tube.

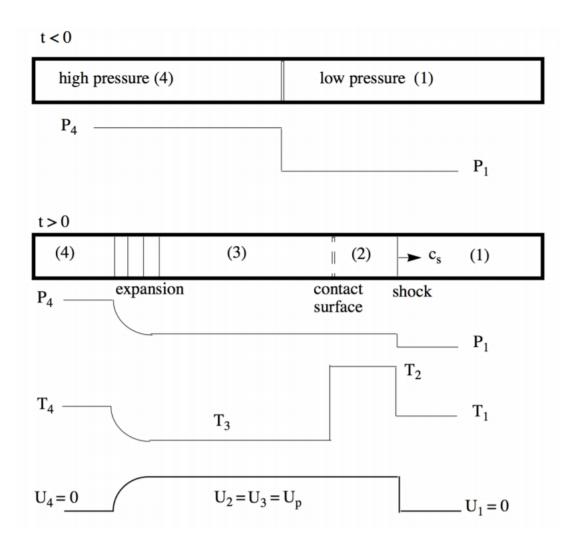


Figure 14: Shock tube flow regions: Region 1 is the flow ahead of the primary shock, region 2 is between contact surface and primary shock, region 3 is between tail of the expansion fan and contact surface, region 4 is ahead of the leading expansion wave [5].

In the following we will combine the results for expansion waves with normal shock relations to derive the so-called shock tube equation. The conditions at the contact surface are:

$$P_2 = P_3 \tag{4}$$

$$U_2 = U_3 = U_p. (5)$$

where U_2 is the speed of the slug of gas set into motion by the opening of the diaphragm.

This is the effective piston speed of the fluid released by the diaphragm.

In a frame of reference moving with the shock wave the gas velocities are

$$U_1' = -c_s \tag{6}$$

$$U_2' = -c_s + U_p \tag{7}$$

and the shock jump conditions are

$$\frac{U_2'}{U_1'} = \frac{1 + \frac{\gamma_1 - 1}{2} M_1^2}{\frac{\gamma_1 + 1}{2} M_1^2} \tag{8}$$

$$\frac{P_2}{P_1} = \frac{\gamma_1 M_1^2 - \frac{\gamma_1 - 1}{2}}{\frac{\gamma_1 + 1}{2}} \tag{9}$$

where $M_1 = c_s/a_1 = -U_1'/a_1$. Using the first relation, Equation 5 above, we can write

$$\frac{U_2' - U_1'}{U_1'} = \frac{1 + \frac{\gamma_1 - 1}{2} M_1^2}{\frac{\gamma_1 + 1}{2} M_1^2} - 1 = \frac{1 - M_1^2}{\frac{\gamma_1 + 1}{2} M_1^2}$$
(10)

The piston velocity is

$$U_p = U_2' - U_1' = U_1' \left(\frac{1 - M_1^2}{\frac{\gamma_1 + 1}{2} M_1 - \frac{U_1'}{\alpha_2}} \right) = \alpha_1 \left(\frac{M_1^2 - 1}{\frac{\gamma_1 + 1}{2} M_1} \right)$$
 (11)

Note that U_p is positive. Using the second relation, Equation 5, Equation 8 can be expressed in terms of the shock pressure ratio as

$$U_p = a_1 \left(\frac{P_2}{P_1} - 1\right) \left(\frac{2}{\gamma_1(\gamma_1 + 1)(P_2/P_1) + \gamma_1(\gamma_1 - 1)}\right)^{1/2}$$
(12)

Equation 9 is the expression for the piston velocity derived using normal shock theory. Now lets work out an expression for the piston velocity using isentropic expansion theory. The velocity behind the expansion is

$$U_3 = U_p = \frac{2a_4}{\gamma_4 - 1} \left(1 - \frac{P_3}{P_4}^{\frac{\gamma_4 - 1}{2\gamma_4}} \right) \tag{13}$$

Equate 9 and 10.

$$a_1 \left(\frac{P_2}{P_1} - 1\right) \left(\frac{2}{\gamma_1(\gamma_1 + 1)(P_2/P_1) + \gamma_1(\gamma_1 - 1)}\right)^{1/2} = \frac{2a_4}{\gamma_4 - 1} \left(1 - \left(\frac{P_3}{P_2} \frac{P_2}{P_1} \frac{P_1}{P_4}\right)^{\frac{\gamma_4 - 1}{2\gamma_4}}\right)$$
(14)

Using the following identity

$$\frac{P_3}{P_4} = \frac{P_3}{P_2} \frac{P_2}{P_1} \frac{P_1}{P_4} \tag{15}$$

and noting that $P_3/P_2 = 1$ solve Equation 10 for $P_4/P_3 = 1$, substituting in P_2/P_1 from Equation 6. Simplifying, the result is the basic shock tube equation

$$\frac{P_4}{P_1} = \frac{2\gamma_1 M_1^2 - (\gamma_1 - 1)}{\gamma_1 + 1} \left(1 - \frac{\gamma_{4-1}}{\gamma_{1+1}} \frac{U_1}{U_4} \left(M_1 - \frac{1}{M_1} \right) \right)^{-2\gamma_4/\gamma_{4-1}}$$
(16)

And given the specific gas information, for the driver helium, $\gamma_4 = 1.667$, and the driven air, $\gamma_1 = 1.4$. Taking the ambient air temperature $T_1 = 273.15K$, the relation in equation 13 can be shown in the Figure ??. This figure highlights the relationship between the driver pressure ratio at 4, and the ambient pressure at 1, for a design incident Mach number. The figure also illustrates the reduced pressure ratio benefit of using a helium to air experiment in comparison to a air to air experiment.