

6.

6.)

P	q	$P \rightarrow q$	$(P \wedge (P \rightarrow q))$	$((P \wedge (P \rightarrow q)) \rightarrow q)$
T	T	T	T	T
T	F	F	F	T
F	T	T	F	T
F	F	T	F	T

Dremið sem vantaði í bókina hjá mér:

$$\begin{aligned}
 (P \wedge (P \rightarrow q)) \rightarrow q &\equiv \neg(P \wedge (\neg P \vee q)) \rightarrow && \text{(Tafla 7 regla 1)} \\
 &\equiv (\neg P \vee (P \wedge \neg q)) \vee q && \text{(de Morgan)} \\
 &\equiv ((\neg P \vee P) \wedge (\neg P \vee \neg q)) \vee q && \text{(Distributive laws)} \\
 &\equiv (T \wedge (\neg P \vee \neg q)) \vee q && \text{(Negation laws)} \\
 &\equiv (\neg P \vee \neg q) \vee q && \text{(Identity laws)} \\
 &\equiv \neg P \vee (\neg q \vee q) && \text{(Associative laws)} \\
 &\equiv \neg P \vee T && \text{(Negation laws)} \\
 &\equiv T && \text{(Domination laws)}
 \end{aligned}$$

24.

P	q	Nand
T	T	F
T	F	T
F	T	T
F	F	T

26.

P	q	Nor
T	T	F
T	F	F
F	T	F
F	F	T

6. $C(x) = x$ has a ~~dog~~ Cat $\wedge = \text{and}$
 $D(x) = x$ has a dog $\vee = \text{or}$
 $F(x) = x$ has a ferret

a.) $\exists x (C(x) \wedge D(x) \wedge F(x))$ b.) $\forall x (C(x) \vee D(x) \vee F(x))$

c.) $\exists x (C(x) \wedge F(x) \neg D(x))$ d.) $\neg \exists x (C(x) \wedge D(x) \wedge F(x))$

e.) $(\neg \exists x C(x)) \vee (\neg \exists x D(x)) \vee (\neg \exists x F(x))$