Bestern konvergens radien til

$$a) \sum_{n=0}^{\infty} \frac{1}{3^n} x^n$$

Forholdstestem:

$$\lim_{N\to\infty} \left| \frac{N + 1}{3^{N+1}} \frac{X^{N+1}}{X^{N}} \right| = \lim_{N\to\infty} \left| \frac{(N+1) \cdot 3^{N} \cdot X^{N+1}}{N \cdot 3^{N+1} \cdot 3^{N+1}} \right|$$

$$=\lim_{N\to\infty}\left|\frac{N+1}{N},\frac{\infty}{3}\right|=\lim_{N\to\infty}\frac{(N+1)!n}{(N)!n}\frac{1\infty!}{3}$$

$$= \lim_{N\to\infty} \frac{|-1|}{|-3|} \frac{|x|}{3} = \frac{|x|}{3} < 1 \qquad |-3| < 3$$

Konvergensvadien er 3.

For holds fester
$$2(n+1)$$
 $\lim_{n\to\infty} \frac{q^n}{n+1} \times 2n$
 \lim

Rot-testan: lim Man = lim M/1 x" = lim M/1x" = lim m/1x" = lim MixIn = lim [IXI] = 0 < 1 Altid sont. Konvergensvadien er «. 8.5.4 Bestern konvergensomvådet til $9) \sum_{n=0}^{\infty} \frac{(3\pi - 2)^n}{n+1}$ Forholdstesten: $lim \left| \frac{3x-2}{n+1} \right| = lim \left| \frac{3x-2}{n+2} \right| = lim \left| \frac{3x-2}{n+2} \right| = n-\infty$ $lim \left| \frac{3x-2}{n+1} \right| = n-\infty$ Forholdstesten: = lim |3x-2| (n+1):n - lim |3x-2| 1+1/2 = |3x-2| < | n->00 1 < 3x < 3 \frac{1}{3} < x < 1 Vet at relka konvag an var >C & (3,1) Hora med X= = 09 X=1 Hva med ende punktere?

$$\frac{2}{2} \frac{(3x-2)^n}{(3x-2)^n}$$

$$x=\frac{1}{2} : \sum_{n=0}^{\infty} \frac{(3\frac{1}{2}-2)^n}{n+1} = \sum_{n=0}^{\infty} \frac{(-1)^n}{n+1} = \sum_{n=0}^{\infty} \frac{(-1$$

Må sjekke X=4 og X=-4.

$$X=4$$

$$\sum_{n=0}^{\infty} \frac{1}{(n+1)^{n}} = \sum_{n=0}^{\infty} \frac{1}{n}$$

$$\sum_{n=0}^{\infty} \frac{1}{(n+1)^{n}} = \sum_{n=0}^{\infty} \frac{1}{(n+1)^{n}} = \sum_{n=0$$

$$= \sum_{n=0}^{\infty} \frac{x^{n-1}}{(n-1)!} \cdot \frac{x^{n-1}}{(n-$$

(a)
$$v_{i}! \ln x^{i} \cdot \frac{1}{k!} \times x^{i}! = \sum_{n=0}^{\infty} \frac{1}{n!} \cdot \frac{1}{n!} \times x^{i}$$

$$\sum_{n=0}^{\infty} \frac{2^{n+1}}{n!} \cdot \frac{1}{n!} \times x^{i}$$

$$\sum_{n=0}^{\infty} \frac{2^{n+1}}{n!} \cdot \frac{1}{n!} \times x^{i}$$

$$\left(\frac{3}{100} + \frac{3}{100} +$$

8.5.7. Finn vekkentviklingen til hvert integral. a) $\sum_{n=0}^{\infty} \frac{2n}{n!} dt = \sum_{n=0}^{\infty} \frac{2n}{n!} dt$ SE de Le utl $= \sum_{N=0}^{\infty} \frac{1}{N!} \int_{0}^{\infty} \frac{2n}{N!} \int_{0}^{\infty} \frac{2n+1}{2n+1} \times \frac{2n+1}{N!} \int_{0}^{\infty} \frac{2n+1}{2n+1} \times \frac{2n+1}{N!} = \sum_{N=0}^{\infty} \frac{1}{N!} \int_{0}^{\infty} \frac{2n+1}{2n+1} \times \frac{2n+1}{N!} \times \frac{2n+1}{N!} = \sum_{N=0}^{\infty} \frac{1}{N!} \int_{0}^{\infty} \frac{2n+1}{N!} \times \frac{2n$ $= \sum_{N=0}^{\infty} \frac{1}{N!} \cdot \frac{1}{2^{n+1}} \cdot \frac{2^{n+1}}{N!} = \sum_{N=0}^{\infty} \frac{2^{n+1}}{(2^{n+1})^{n}!}$ b) S e -1 de

$$\frac{2x}{5} \underbrace{e^{t}}_{t} dt = \int_{n=1}^{2x} \underbrace{e^{n-t}}_{n!} dt = \int_{n=1}^{2x} \underbrace{e^{n-t}}_{n!} dt \\
= \int_{n=1}^{2x} \underbrace{\frac{2x}{n!}}_{n!} dt = \int_{n=1}^{2x} \underbrace{\frac{2x}{n!}}_{n!} dt \\
= \int_{n=1}^{2x} \underbrace{\frac{2x}{n!}}_{n!} dt = \int_{n=1}^{2x} \underbrace{\frac{2x}{n!}}_{n!} dt \\
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= \int_{n=0}^{2x} \underbrace{\frac{2x}{n!}}_{n!} dt = \int_{n=0}^{2x} \underbrace{\frac{2x}{n!}}_{n!} dt \\
= \int_{n=0}^{2x} \underbrace{\frac{2x}{n!}}_{n!} dt = \int_{n=0}^{2x} \underbrace{\frac{2x}{n$$

 $\left(\sum_{N=0}^{\infty} x^{n}\right)^{2} = \sum_{N=0}^{\infty} n \cdot 2x^{n-1} = \sum_{N=1}^{\infty} (n \cdot x^{n-1}) = \sum_{N=0}^{\infty} (m+1) \times m$ $\left(\sum_{N=0}^{\infty} x^{n}\right)^{2} = \sum_{N=0}^{\infty} n \cdot 2x^{n-1} = \sum_{N=0}^{\infty} (m+1) \times m$ $\left(\sum_{N=0}^{\infty} x^{n}\right)^{2} = \sum_{N=0}^{\infty} n \cdot 2x^{n-1} = \sum_{N=0}^{\infty} (m+1) \times m$ $\left(\sum_{N=0}^{\infty} x^{n}\right)^{2} = \sum_{N=0}^{\infty} n \cdot 2x^{n-1} = \sum_{N=0}^{\infty} (m+1) \times m$ $\left(\sum_{N=0}^{\infty} x^{n}\right)^{2} = \sum_{N=0}^{\infty} n \cdot 2x^{n-1} = \sum_{N=0}^{\infty} (m+1) \times m$ $\left(\sum_{N=0}^{\infty} x^{n}\right)^{2} = \sum_{N=0}^{\infty} (m+1) \times m$

$$\frac{1}{(1-x)^{2}} = ((1-x)^{-1})^{1} = -1 \cdot (1-x)^{-2} \cdot (-1)$$

$$= \frac{1}{(1-x)^{2}}$$

$$\sum_{n=0}^{\infty} 2^{n} (n+1) \times^{n} = \sum_{n=0}^{\infty} (n+1)^{(2x)^{n}} = \frac{1}{(1-2x)^{2}}$$

$$\sum_{n=0}^{\infty} (-3)^{n+1} \times^{2n}$$

$$\sum_{n=0}^{\infty} (-3)^{n+1} \times^{2n}$$

$$\sum_{n=0}^{\infty} (-3)^{n+1} \times^{2n}$$

$$\sum_{n=0}^{\infty} (-3)^{n+1} \times^{2n}$$

$$= (-3)^{n$$

$$\left(\frac{1}{1-x}\right)' = \left(\frac{1}{1-x}\right)' = -1 \cdot (1-x)^{-2} \cdot (-1)$$

$$= \frac{1}{(1-x)^{2}}$$

$$=$$

$$\frac{C}{\sum_{n=1}^{\infty}} \frac{2n}{(2n)!}$$

$$\cos x = \sum_{n=0}^{\infty} \frac{(-1)^n}{(a_n)!} x^{a_n}$$

$$\begin{array}{lll}
N=6 \\
Ma & priore & a & give & (-3)^{n+1} \times 2^n = k \cdot (-1)^n y^2 \\
Ma & priore & a & give & (-3)^n \times 2^n = -3 \cdot (-1)^n 3^n \times 2^n \\
(-3)^{n+1} \times 2^n = -3 \cdot (-3)^n \times 2^n = -3 \cdot (-1)^n (\sqrt{3})^{2n} \times 2^n \\
&= -3 \cdot (-1)^n \cdot (\sqrt{3} \times 2)^n \times 2^n = -3 \cdot (-1)^n (\sqrt{3})^{2n} \times 2^n \\
&= -3 \cdot (-1)^n \cdot (\sqrt{3} \times 2)^n \times 2^n
\end{array}$$

$$\frac{5^{a}}{\sum_{n=0}^{\infty} (-3)^{n+1} \frac{x^{n}}{(an)!}} = -3 \underbrace{\sum_{n=0}^{\infty} (-1)^{n}}_{(n=0)} (\sqrt{5} \times x)^{n} = -3 \cdot \cos(\sqrt{3} \cdot 2x).$$



85,111 a) Med utgangs punkt i potansvelden for sinus, forklar $\frac{x}{sin + dt} = \frac{x}{(2n+1)\cdot(2n+1)!} x^{2n+1}$ x = 0 $Sin > C = \sum_{n=0}^{\infty} \frac{(-1)^n x^{2n+1}}{(2n+1)!} = x - \frac{x^3}{6} + \frac{x^5}{120} - \dots$ $\frac{\sin t}{t} = \frac{\sum_{i=0}^{\infty} (-1)^n t^{2n+1}}{(2n+1)! t^n} = \frac{\sum_{i=0}^{\infty} (-1)^n t^{2n}}{(2n+1)! t^n}$ Sint dt= Standt 20 (-1) Standt 2 (2nx1)! o tandt = \(\frac{1}{2n+1!} \cdot \frac{1}{2n+1} \) $= \frac{(-1)^n \times 2^{n-\epsilon}}{(2n+1)(2n+1)!}$

Brak potensvelka til å Sinne en Tilnearming til

Sint dt med Seil mindre enn 10⁻⁴