

X	0	1	1	1	1	1	1	0	0	0
Y	0	0	0	1	1	0	0	1	1	1

$$H(X) = -0.4 * \log_2(0.4) - 0.6 * \log_2(0.6)$$

$$H(Y) = -0.5 * \log_2(0.5) - 0.5 * \log_2(0.5)$$

$$H(X, Y) = -0.1 * \log_2(0.1) - 0.3 * \log_2(0.3) - 0.4 * \log_2(0.4) - 0.2 * \log_2(0.2)$$

$$I(X, Y) = H(X) + H(Y) - H(X, Y) = 0.9710 + 1 - 1.8464 = 0.1246$$

(A)

X	0	1	1	1	1	1	1	0	0	0
Y	0	0	0	1	1	0	0	1	1	1
Z	1	1	0	0	0	1	1	0	0	0

$$H(Z) = -0.4 * \log_2(0.4) - 0.6 * \log_2(0.6)$$

$$H(X, Z) = -0.3 * \log_2(0.3) - 0.1 * \log_2(0.1) - 0.3 * \log_2(0.3) - 0.3 * \log_2(0.3)$$

$$H(Y, Z) = -0.1 * \log_2(0.1) - 0.4 * \log_2(0.4) - 0.5 * \log_2(0.5) - 0.0 * \log_2(0.0)$$

$$H(X, Y, Z) = -0.0 * \log_2(0.0) - 0.1 * \log_2(0.1) - 0.3 * \log_2(0.3) \\ - 0.0 * \log_2(0.0) - 0.1 * \log_2(0.1) - 0.3 * \log_2(0.3) - 0.2 * \log_2(0.2) \\ - 0.0 * \log_2(0.0)$$

$$I(X; Y|Z) = H(X, Z) + H(Y, Z) - H(Z) - H(X, Y, Z) = 0.5999$$

(B)