

```

In[*]:= ourFib[1] = 1; ourFib[2] = 1;
ourFib[n_] := ourFib[n - 1] + ourFib[n - 2]

phi = (1 + Sqrt[5]) / 2;
psi = (1 - Sqrt[5]) / 2;
fastFib[n_] := FullSimplify[(phi^n - psi^n) / (phi - psi)]

table = TableForm[
  Table[
    {
      n,
      ourFib[n],
      Timing[ourFib[n]] [[1]],
      fastFib[n],
      Timing[fastFib[n]] [[1]],
      Fibonacci[n],
      Timing[Fibonacci[n]] [[1]]
    },
    {n, 1, 34}
  ],
  TableHeadings → {None, {
    "n",
    "ourFib[n]",
    "ourFib[] timing",
    "fastFib[n]",
    "fastFib[] timing",
    "Fibonacci[n]",
    "Fibonacci[] timing"}},
  TableAlignments → Center
]

```

Out[ ]//TableForm=

n	ourFib[n]	ourFib[] timing	fastFib[n]	fastFib[] timing	Fibonacci[n]	Fi
1	1	0.	1	0.	1	
2	1	0.	1	0.	1	
3	2	0.	2	0.	2	
4	3	0.	3	0.	3	
5	5	0.	5	0.	5	
6	8	0.	8	0.	8	
7	13	0.	13	0.	13	
8	21	0.	21	0.	21	
9	34	0.	34	0.	34	
10	55	0.	55	0.	55	
11	89	0.	89	0.	89	
12	144	0.	144	0.	144	
13	233	0.	233	0.	233	
14	377	0.	377	0.	377	
15	610	0.	610	0.	610	
16	987	0.	987	0.	987	
17	1597	0.	1597	0.	1597	
18	2584	0.	2584	0.	2584	
19	4181	0.015625	4181	0.	4181	
20	6765	0.015625	6765	0.	6765	
21	10946	0.015625	10946	0.	10946	
22	17711	0.015625	17711	0.	17711	
23	28657	0.015625	28657	0.	28657	
24	46368	0.03125	46368	0.	46368	
25	75025	0.0625	75025	0.	75025	
26	121393	0.078125	121393	0.	121393	
27	196418	0.0625	196418	0.	196418	
28	317811	0.21875	317811	0.	317811	
29	514229	0.265625	514229	0.	514229	
30	832040	0.453125	832040	0.	832040	
31	1346269	0.859375	1346269	0.	1346269	
32	2178309	1.48438	2178309	0.	2178309	
33	3524578	2.32813	3524578	0.	3524578	
34	5702887	3.5625	5702887	0.	5702887	

In[ ]:= Export["C:\\Users\\briek\\OneDrive\\Desktop\\some homework\\table.pdf", table]

Out[ ]=

C:\\Users\\briek\\OneDrive\\Desktop\\some homework\\table.pdf

In[ ]:= F[x\_] := x / (1 - x - x^2)

```
In[ ]:= array = TableForm[
  Table[
    {n,
      TraditionalForm@Simplify[D[F[x], {x, n}]],
      (D[F[x], {x, n}] /. x -> 0) / n!
    },
    {n, 0, 11}
  ]
]
```

Out[ ]//TableForm=

0	$-\frac{x}{x^2+x-1}$	0
1	$\frac{x^2+1}{(x^2+x-1)^2}$	1
2	$-\frac{2(x^3+3x+1)}{(x^2+x-1)^3}$	1
3	$\frac{6(x^4+6x^2+4x+2)}{(x^2+x-1)^4}$	2
4	$-\frac{24(x^5+10x^3+10x^2+10x+3)}{(x^2+x-1)^5}$	3
5	$\frac{120(x^6+15x^4+20x^3+30x^2+18x+5)}{(x^2+x-1)^6}$	5
6	$-\frac{720(x^7+21x^5+35x^4+70x^3+63x^2+35x+8)}{(x^2+x-1)^7}$	8
7	$\frac{5040(x^8+28x^6+56x^5+140x^4+168x^3+140x^2+64x+13)}{(x^2+x-1)^8}$	13
8	$-\frac{40320(x^9+36x^7+84x^6+252x^5+378x^4+420x^3+288x^2+117x+21)}{(x^2+x-1)^9}$	21
9	$\frac{362880(x^{10}+45x^8+120x^7+420x^6+756x^5+1050x^4+960x^3+585x^2+210x+34)}{(x^2+x-1)^{10}}$	34
10	$-\frac{3628800(x^{11}+55x^9+165x^8+660x^7+1386x^6+2310x^5+2640x^4+2145x^3+1155x^2+374x+55)}{(x^2+x-1)^{11}}$	55
11	$\frac{39916800(x^{12}+66x^{10}+220x^9+990x^8+2376x^7+4620x^6+6336x^5+6435x^4+4620x^3+2244x^2+660x+89)}{(x^2+x-1)^{12}}$	89

```
In[*]:= TeXForm[array]
```

```
Out[*]//TeXForm=
```

```
\begin{array}{ccc}
0 & & -\frac{x}{x^2+x-1} & & 0 \\
1 & & \frac{x^2+1}{\left(x^2+x-1\right)^2} & & 1 \\
2 & & -\frac{2}{\left(x^3+3 x+1\right)} & & \frac{2}{\left(x^2+x-1\right)^3} & & 1 \\
3 & & \frac{6}{\left(x^4+6 x^2+4 x+2\right)} & & \frac{6}{\left(x^2+x-1\right)^4} & & 2 \\
4 & & -\frac{24}{\left(x^5+10 x^3+10 x^2+10 x+3\right)} & & \frac{24}{\left(x^2+x-1\right)^5} & & 3 \\
5 & & \frac{120}{\left(x^6+15 x^4+20 x^3+30 x^2+18 x+5\right)} & & \frac{120}{\left(x^2+x-1\right)^6} & & 5 \\
6 & & -\frac{720}{\left(x^7+21 x^5+35 x^4+70 x^3+63 x^2+35 x+8\right)} & & \frac{720}{\left(x^2+x-1\right)^7} & & 8 \\
7 & & \frac{5040}{\left(x^8+28 x^6+56 x^5+140 x^4+168 x^3+140 x^2+64 x+13\right)} & & \frac{5040}{\left(x^2+x-1\right)^8} & & 13 \\
8 & & -\frac{40320}{\left(x^9+36 x^7+84 x^6+252 x^5+378 x^4+420 x^3+288 x^2+117 x+21\right)} & & \frac{40320}{\left(x^2+x-1\right)^9} & & 21 \\
9 & & \frac{362880}{\left(x^{10}+45 x^8+120 x^7+420 x^6+756 x^5+1050 x^4+960 x^3+585 x^2+210 x+34\right)} & & \frac{362880}{\left(x^2+x-1\right)^{10}} & & 34 \\
10 & & -\frac{3628800}{\left(x^{11}+55 x^9+165 x^8+660 x^7+1386 x^6+2310 x^5+2640 x^4+2145 x^3+1155 x^2+374 x+55\right)} & & \frac{3628800}{\left(x^2+x-1\right)^{11}} & & 55 \\
11 & & \frac{39916800}{\left(x^{12}+66 x^{10}+220 x^9+990 x^8+2376 x^7+4620 x^6+6336 x^5+6435 x^4+4620 x^3+2244 x^2+660 x+89\right)} & & \frac{39916800}{\left(x^2+x-1\right)^{12}} & & 89 \\
\end{array}
```

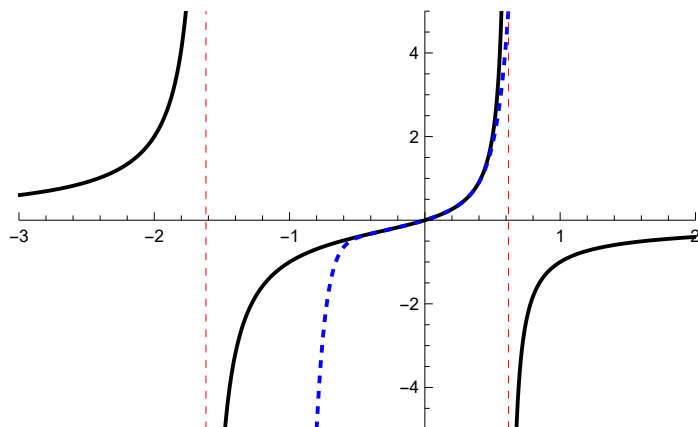
```
In[*]:= VA = Solve[Denominator@F[x] == 0];
```

```

In[ ]:= graph = Plot[
  {F[x],
   Evaluate@Normal@Series[F[x], {x, 0, 11}]},
  {x, -3, 2},
  PlotRange -> {{-3, 2}, {-5, 5}},
  PlotStyle -> {{Black, Automatic}, {Blue, Dashed}},
  Epilog -> {Dashed, Red,
    InfiniteLine[{x, 0}, {0, 1}] /. VA
  }
]

```

Out[ ]=



```

In[ ]:= Export["C:\\Users\\briek\\OneDrive\\Desktop\\some homework\\graph.pdf", graph]

```

Out[ ]=

C:\\Users\\briek\\OneDrive\\Desktop\\some homework\\graph.pdf