

Production of photons (and not only) by high-energy particles (and not only)



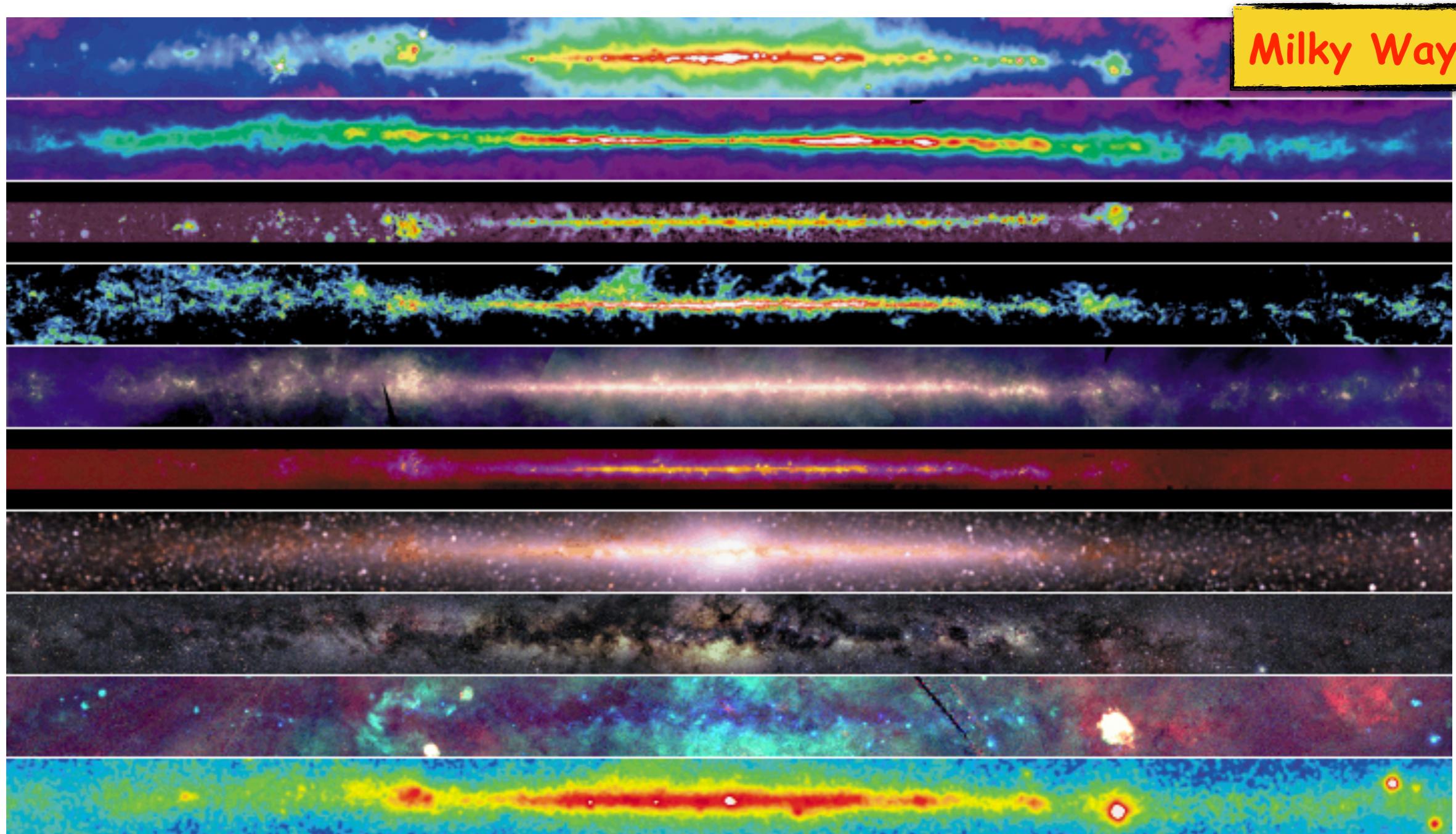
Stefano Gabici
APC, Paris



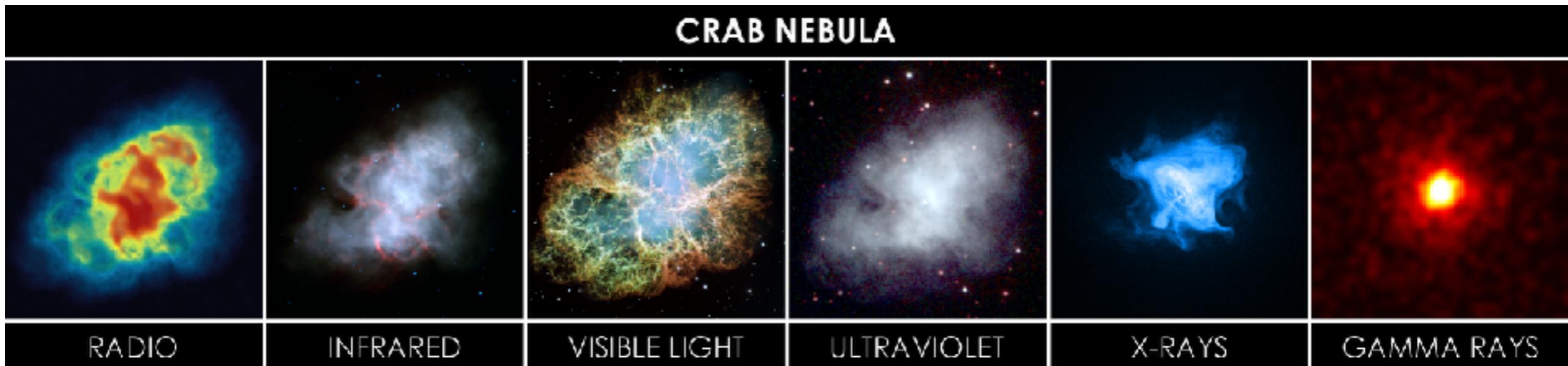
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Milky Way

radio waves — gamma-rays



CRAB NEBULA

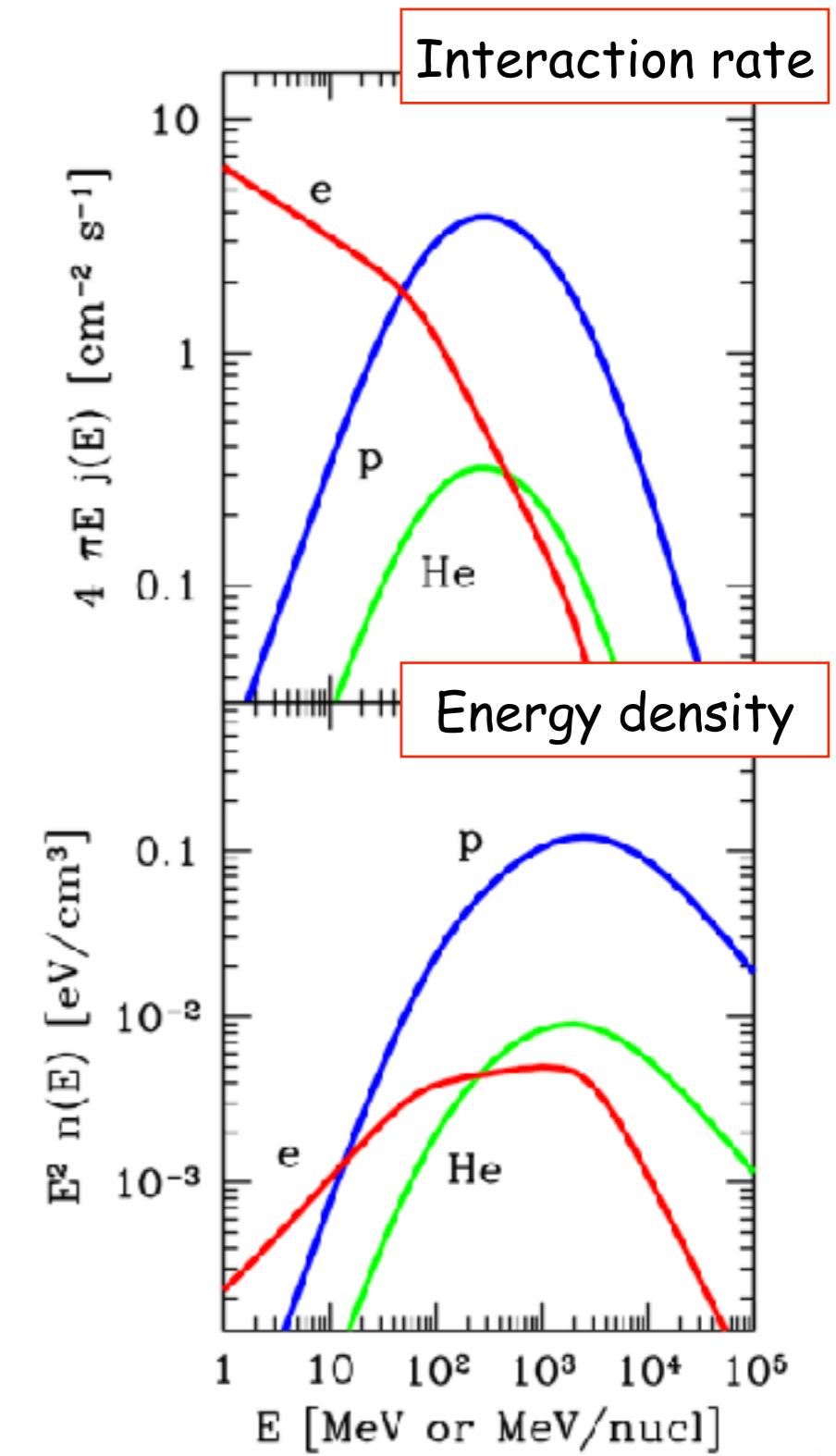
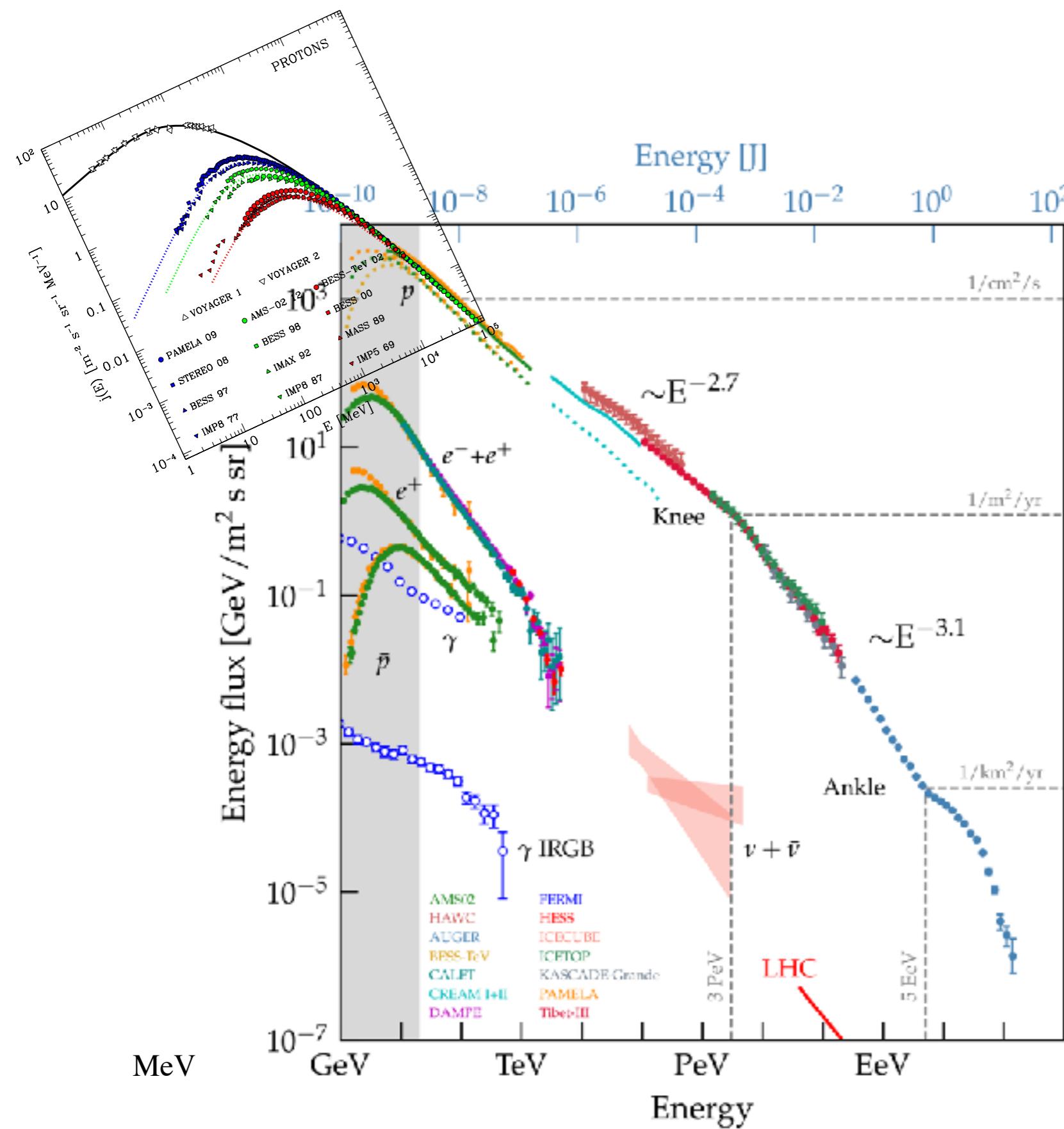


it is impossible to review in a decent way “all” radiative processes in 1.5 h*

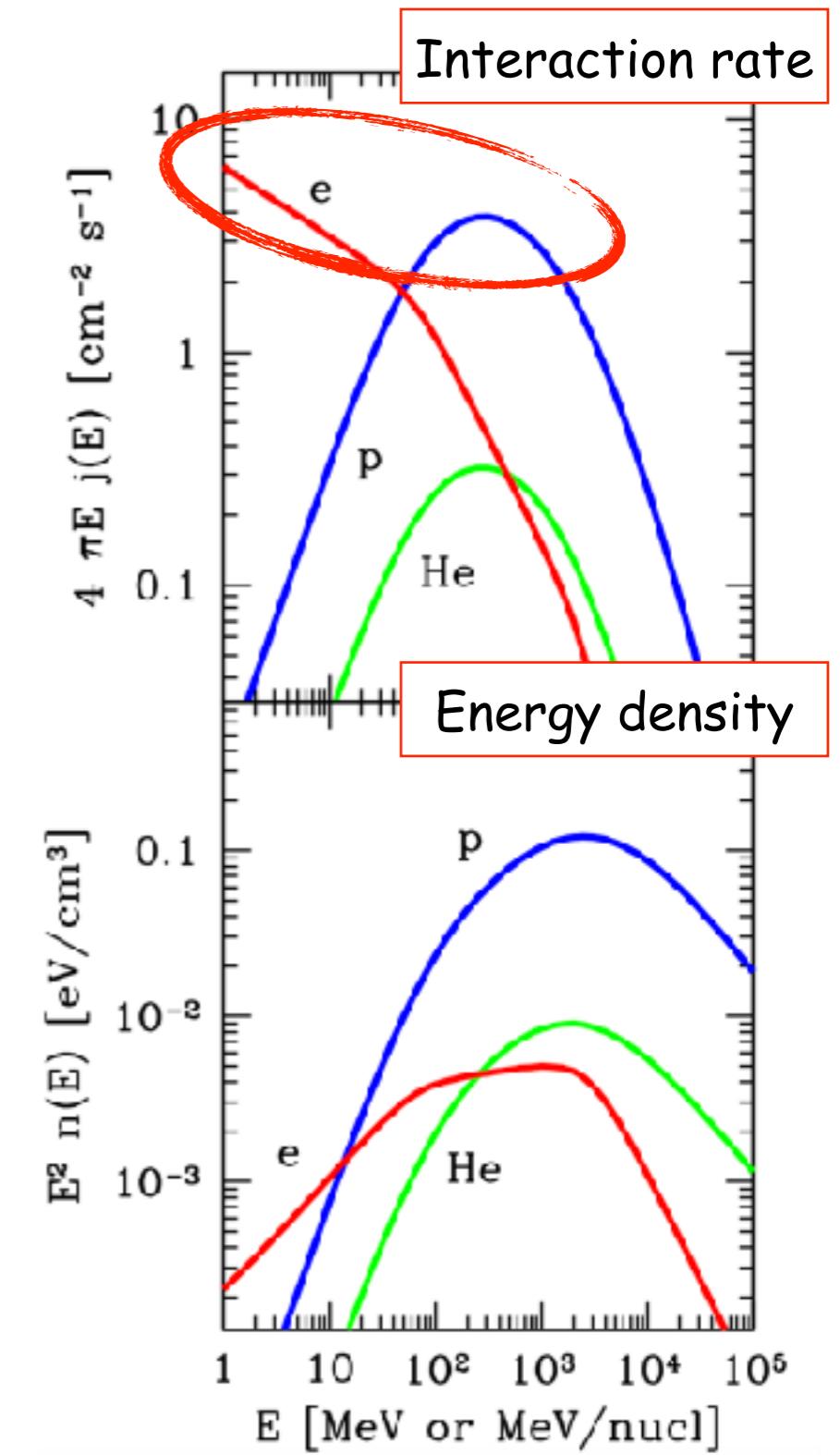
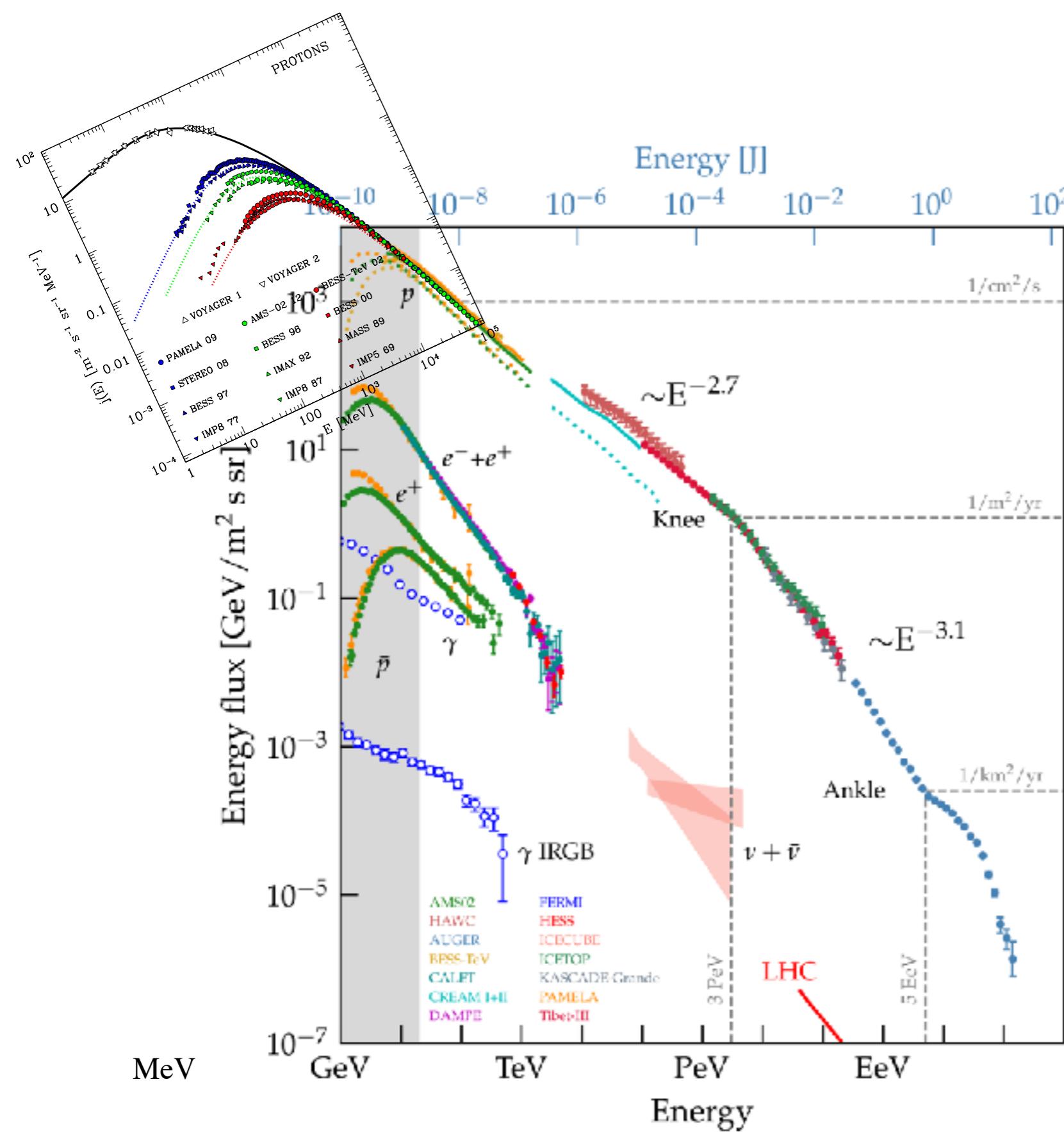


* see also Matteo's classes

One question every 3 (energy) decades...

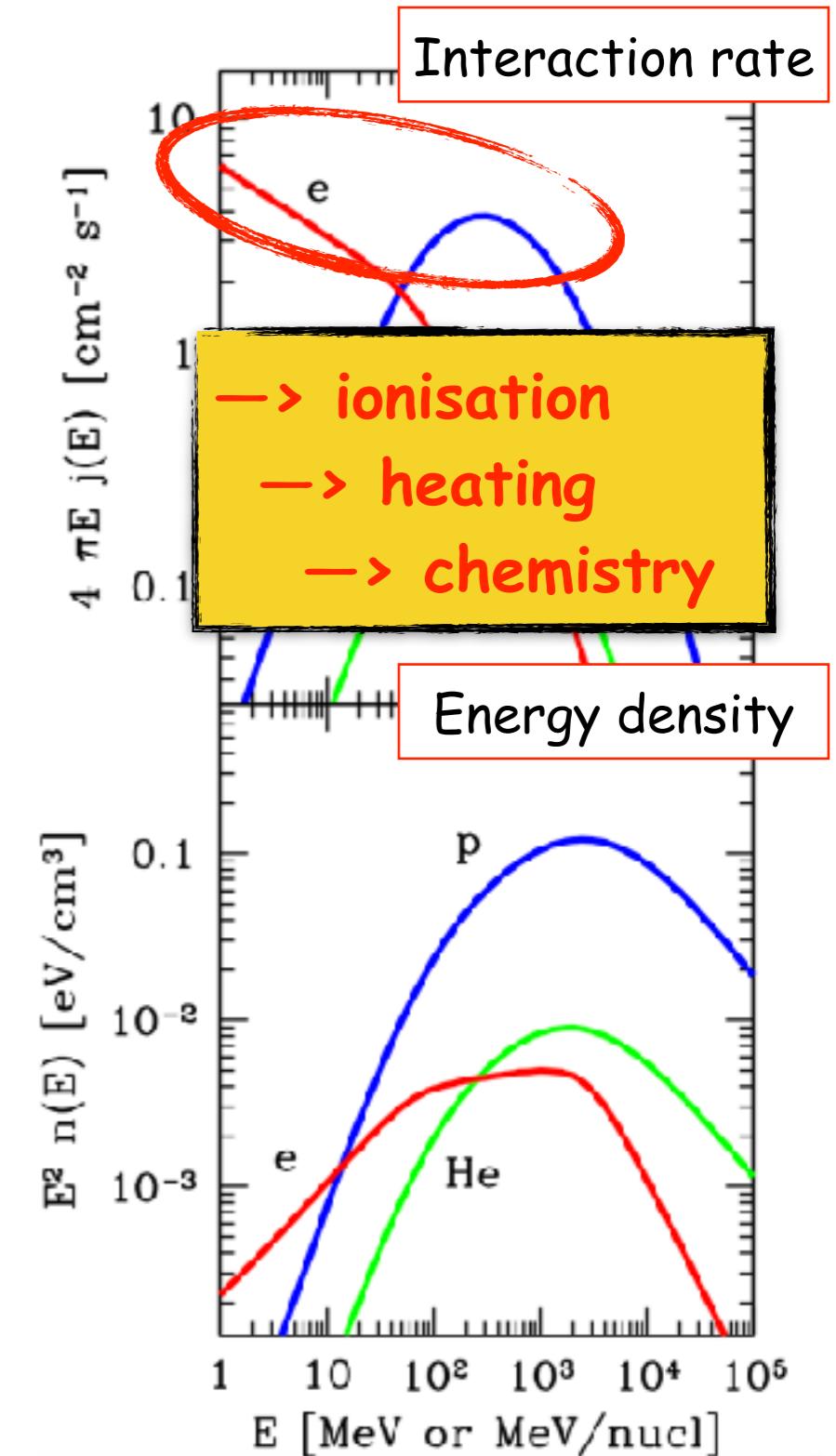
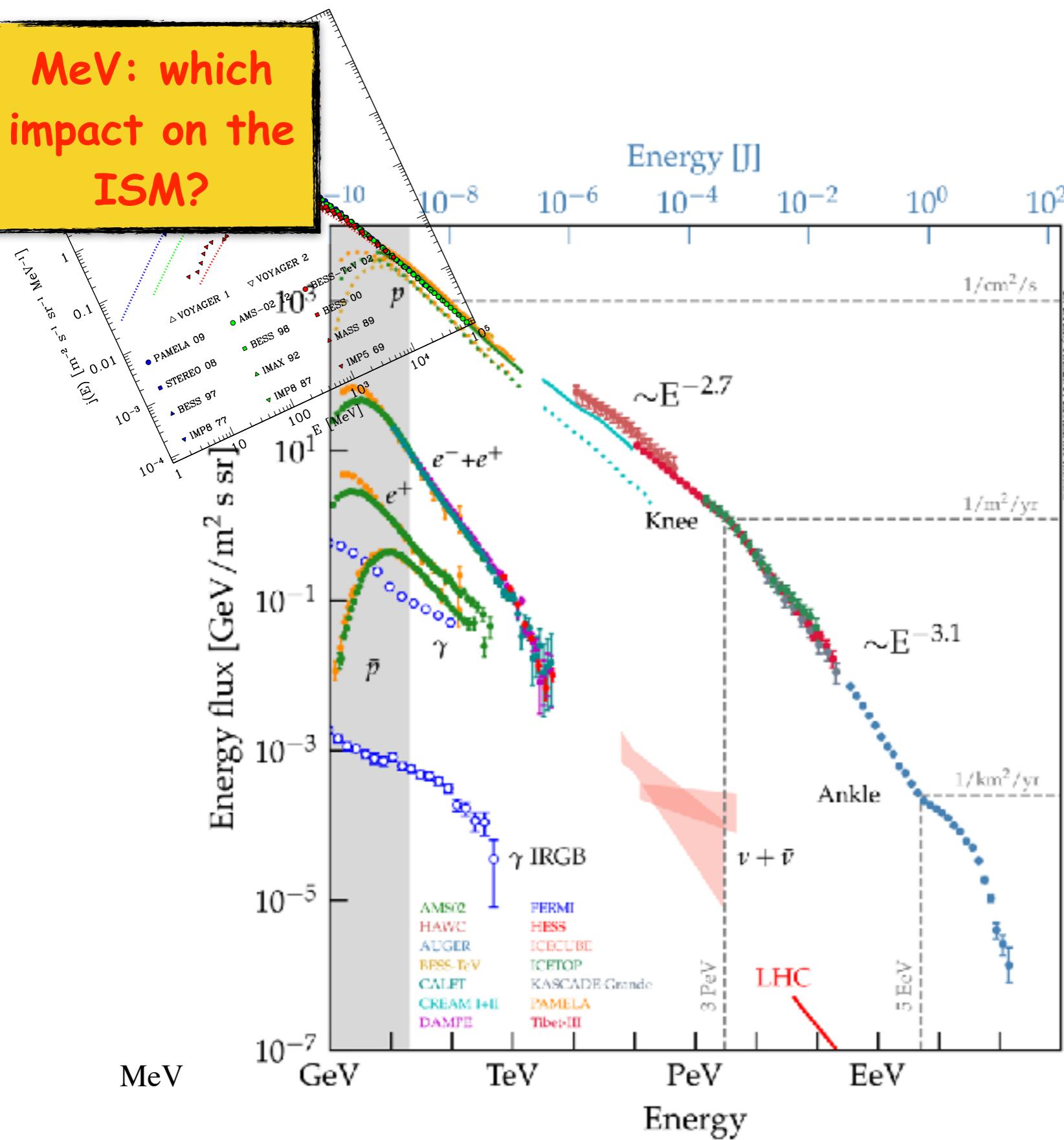


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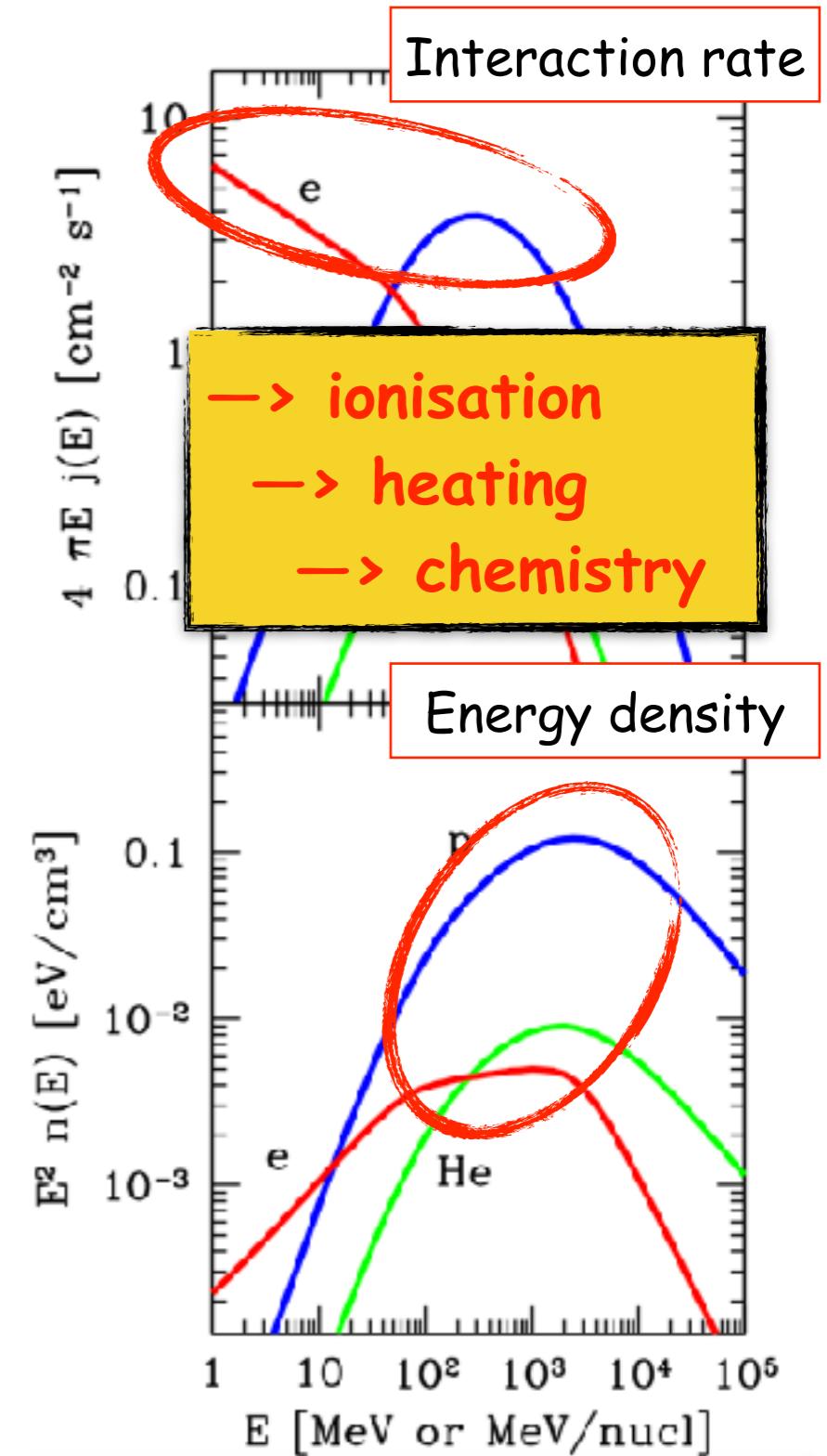
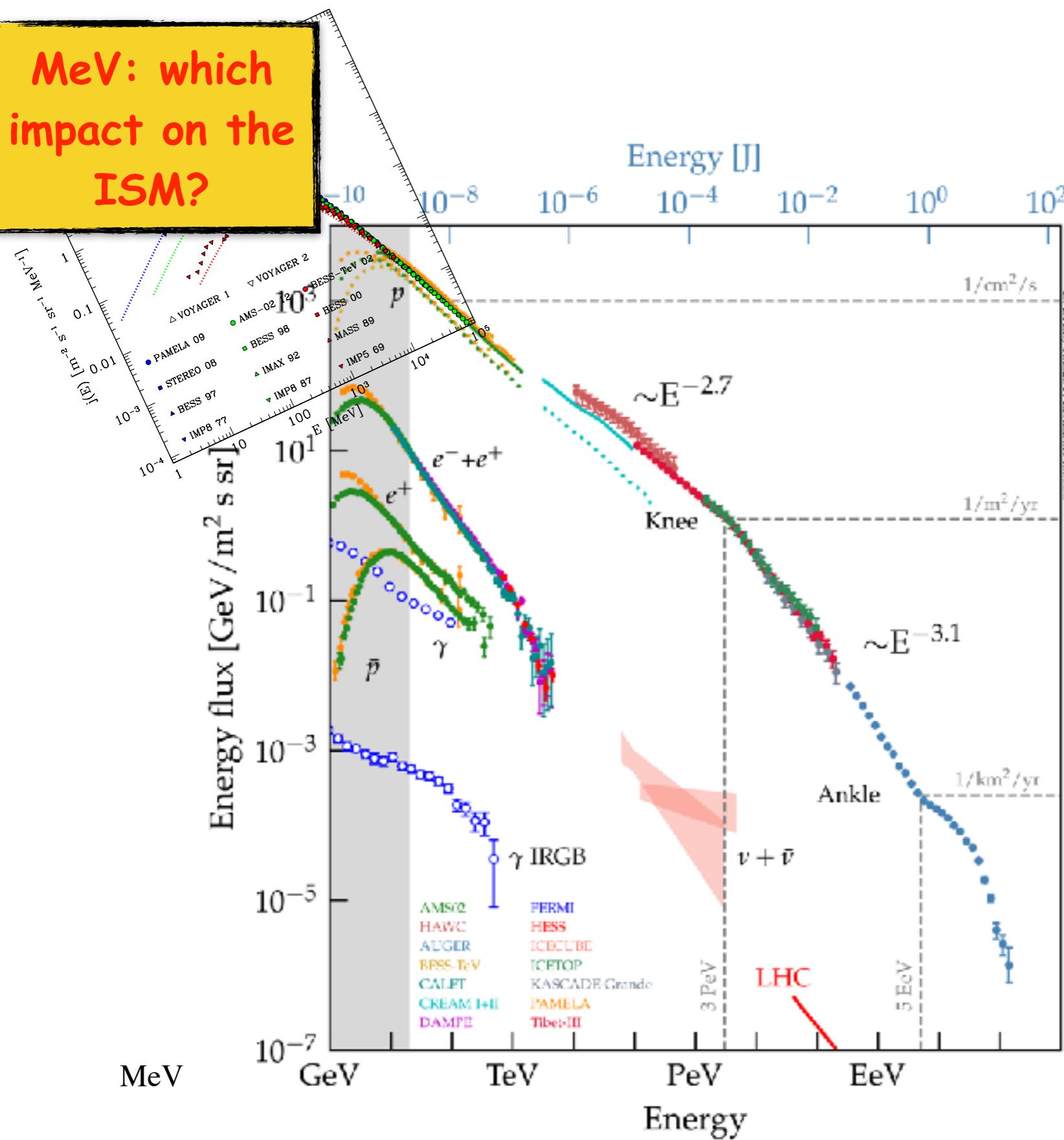
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MeV: which impact on the ISM?



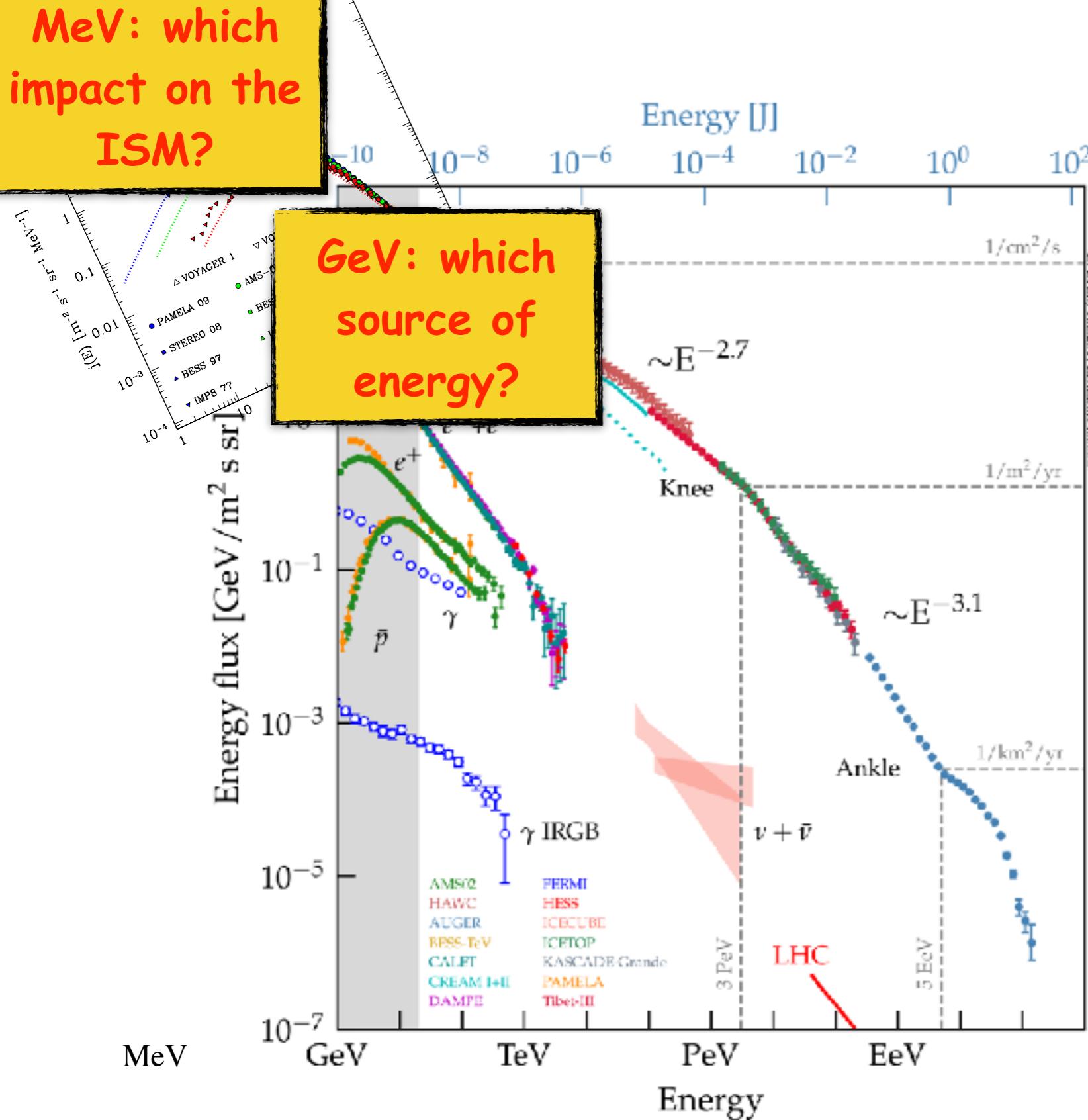
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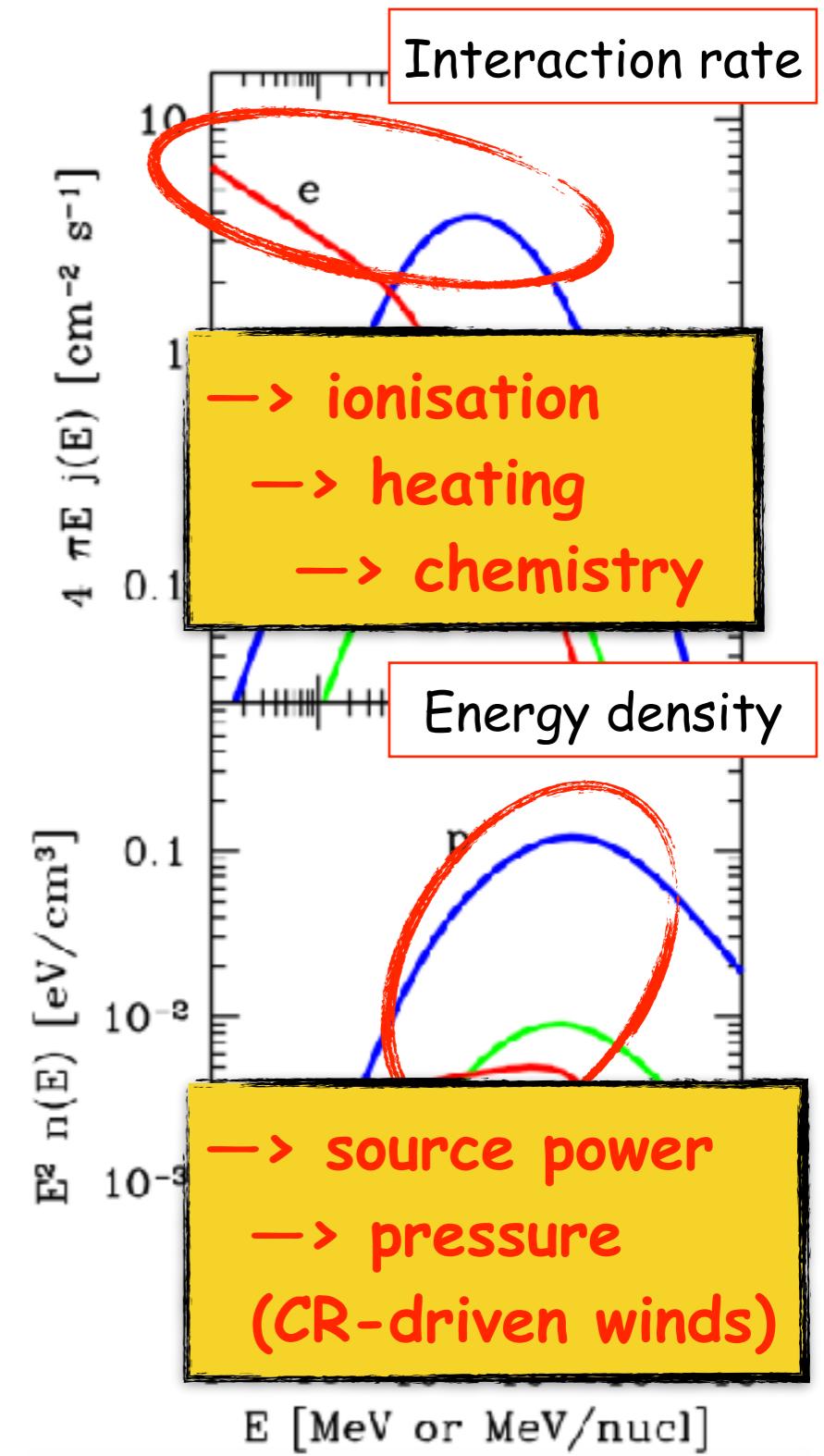


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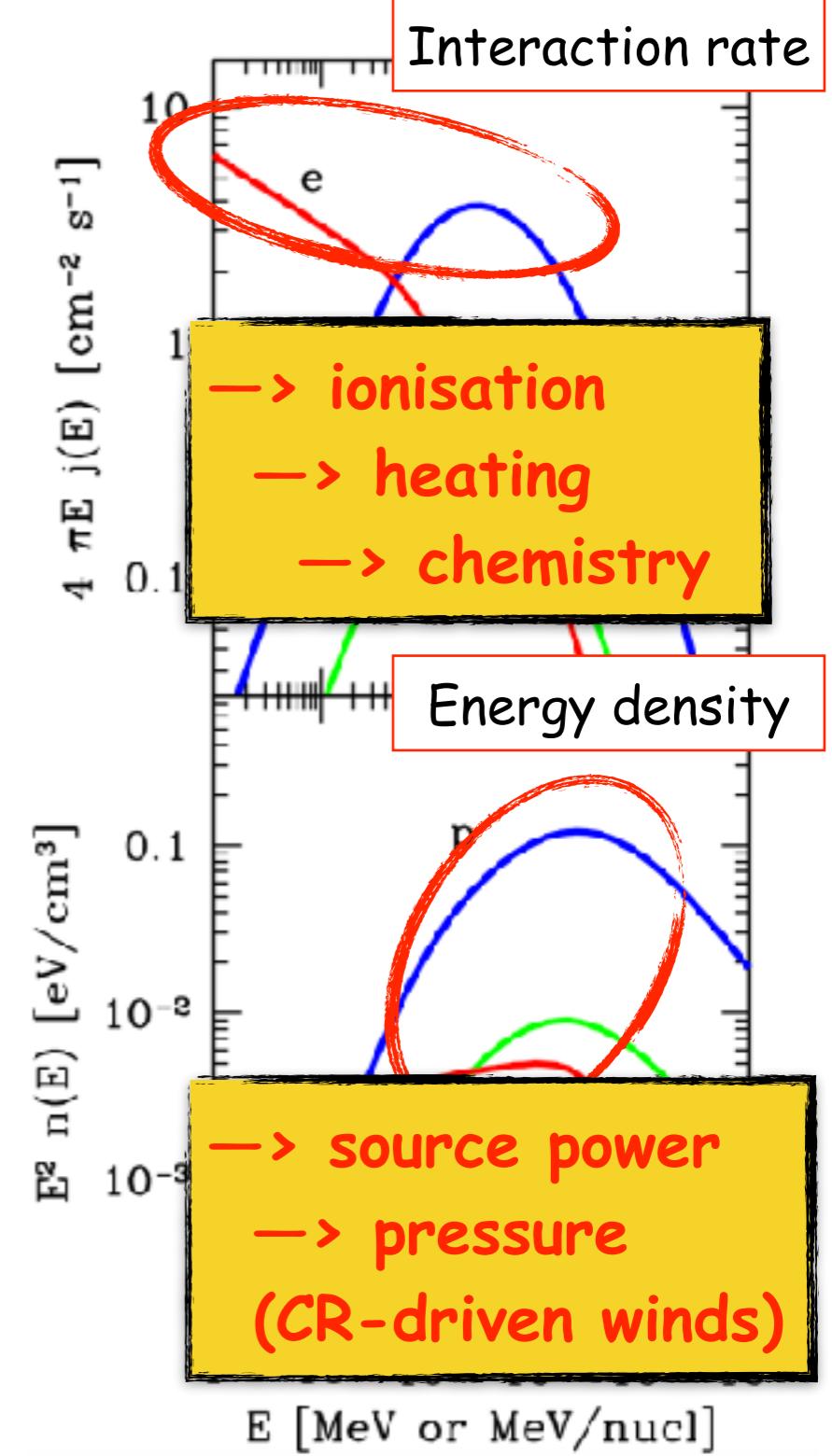
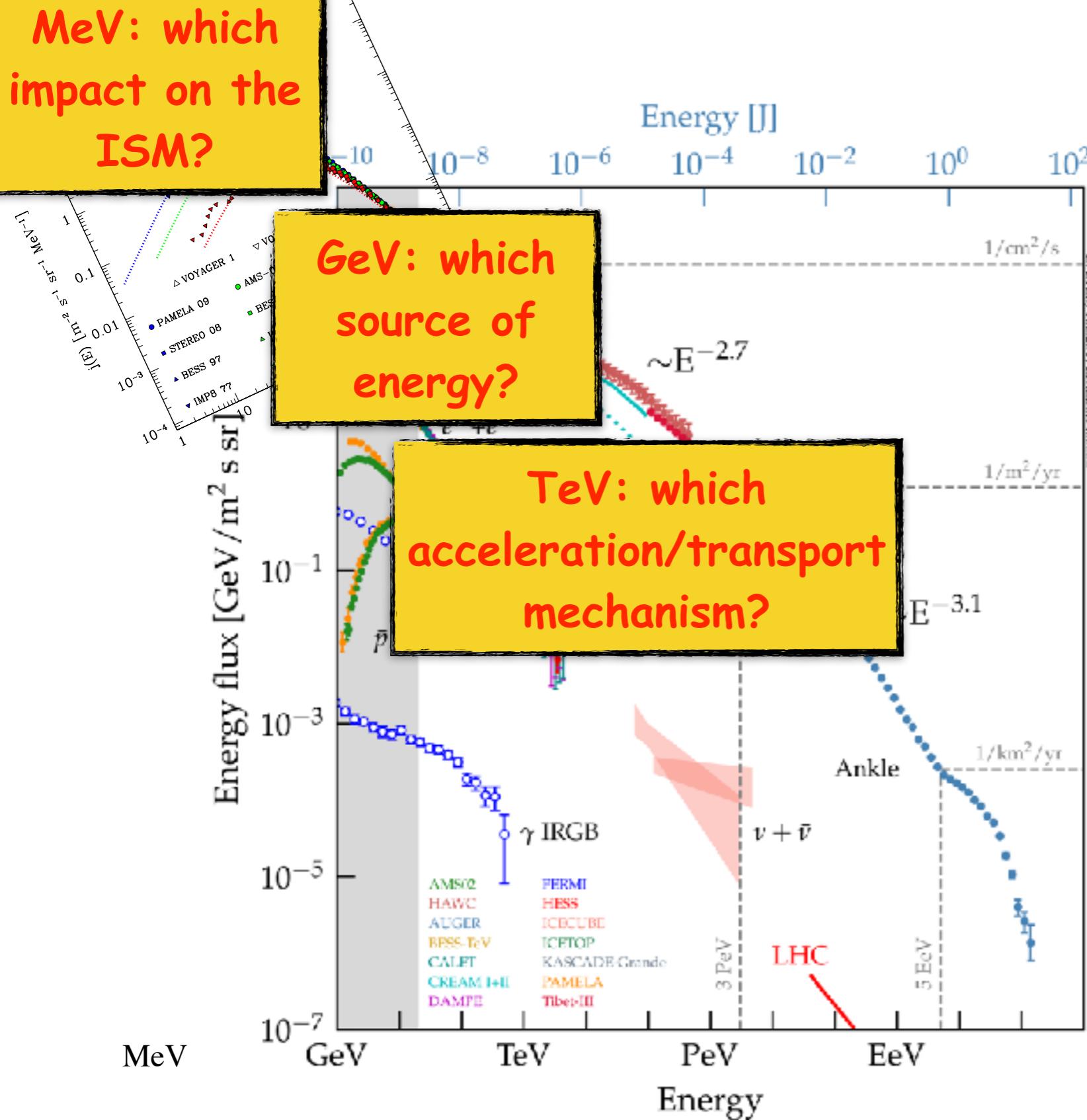


GeV: which source of energy?



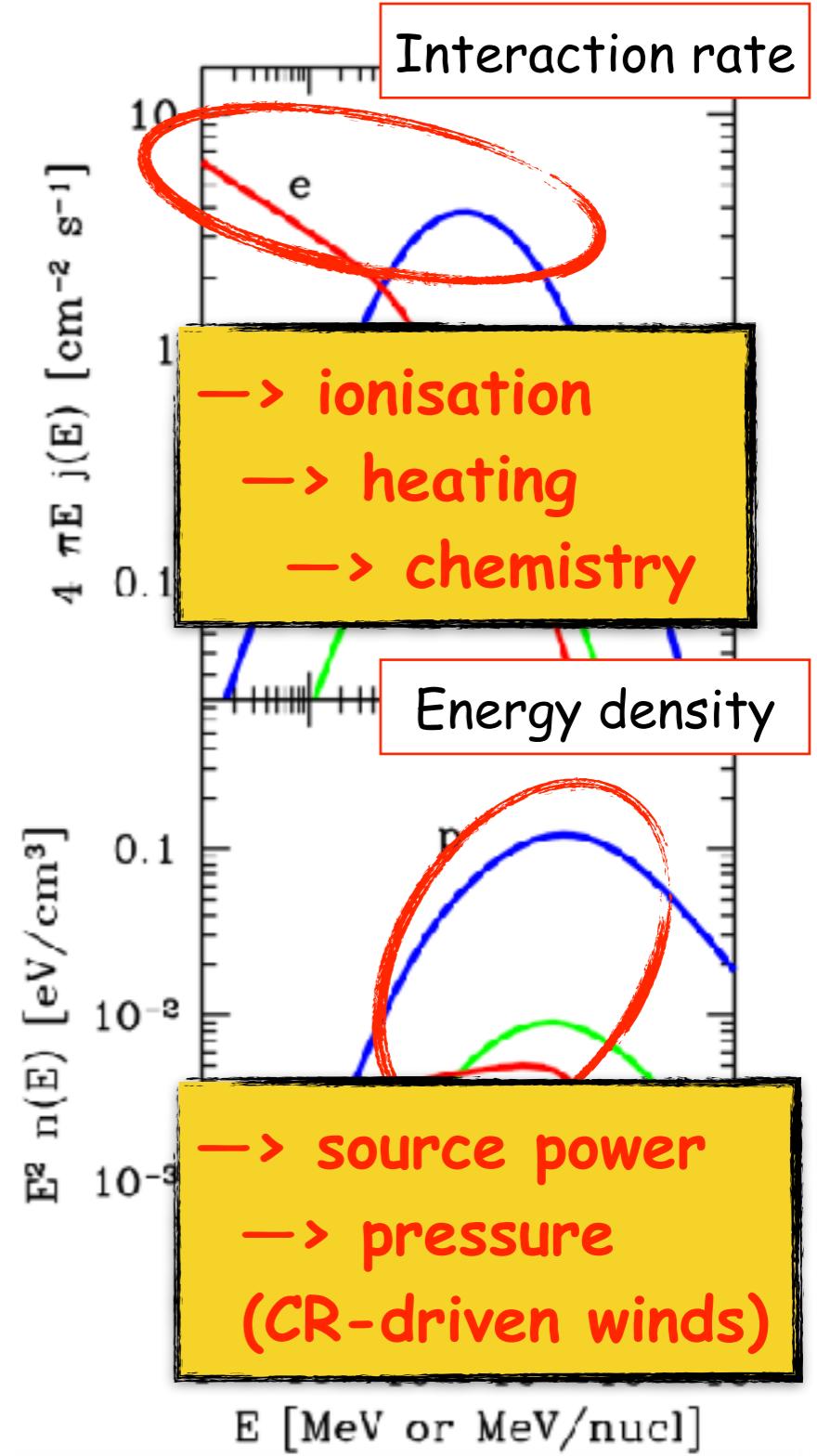
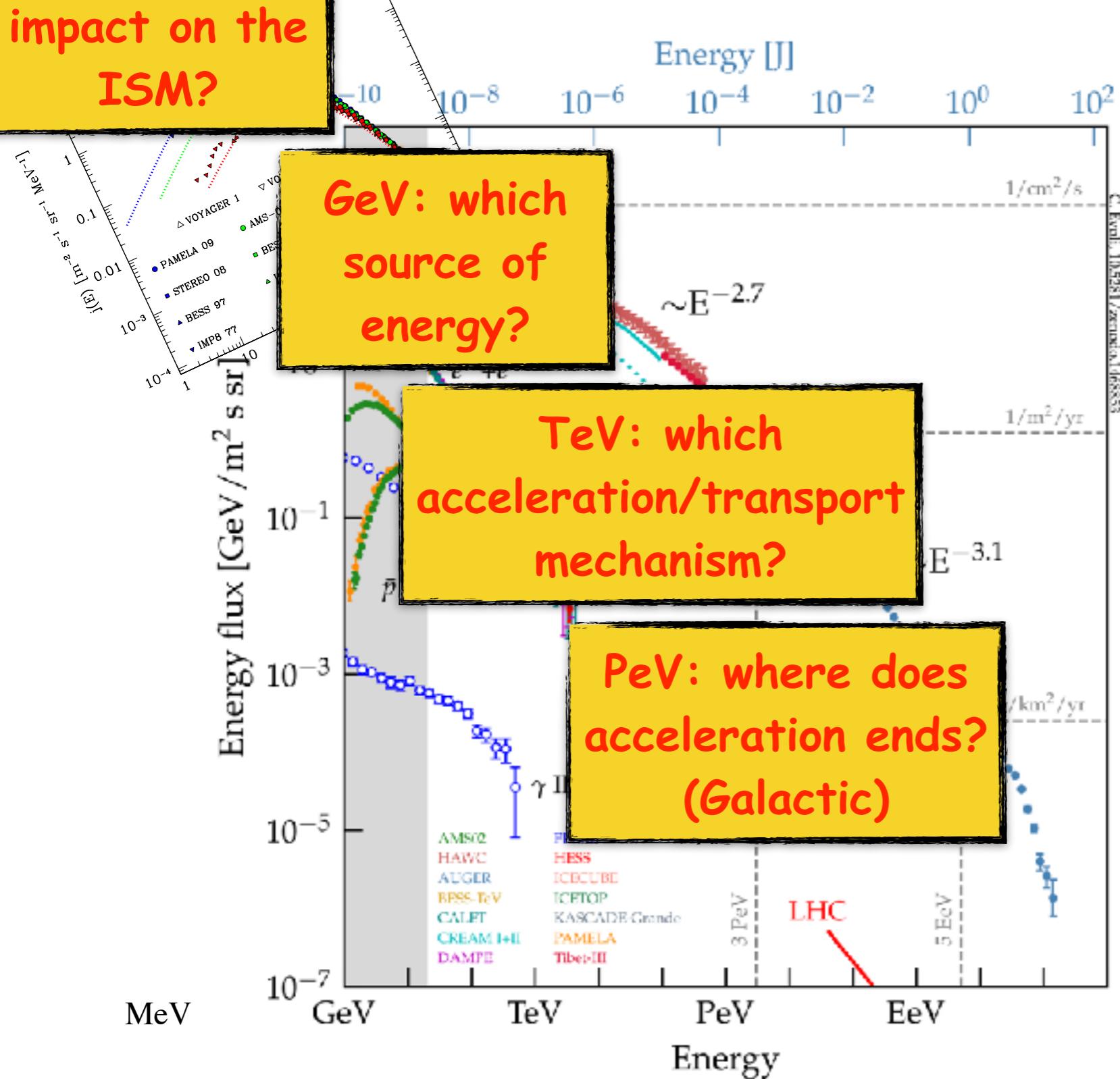
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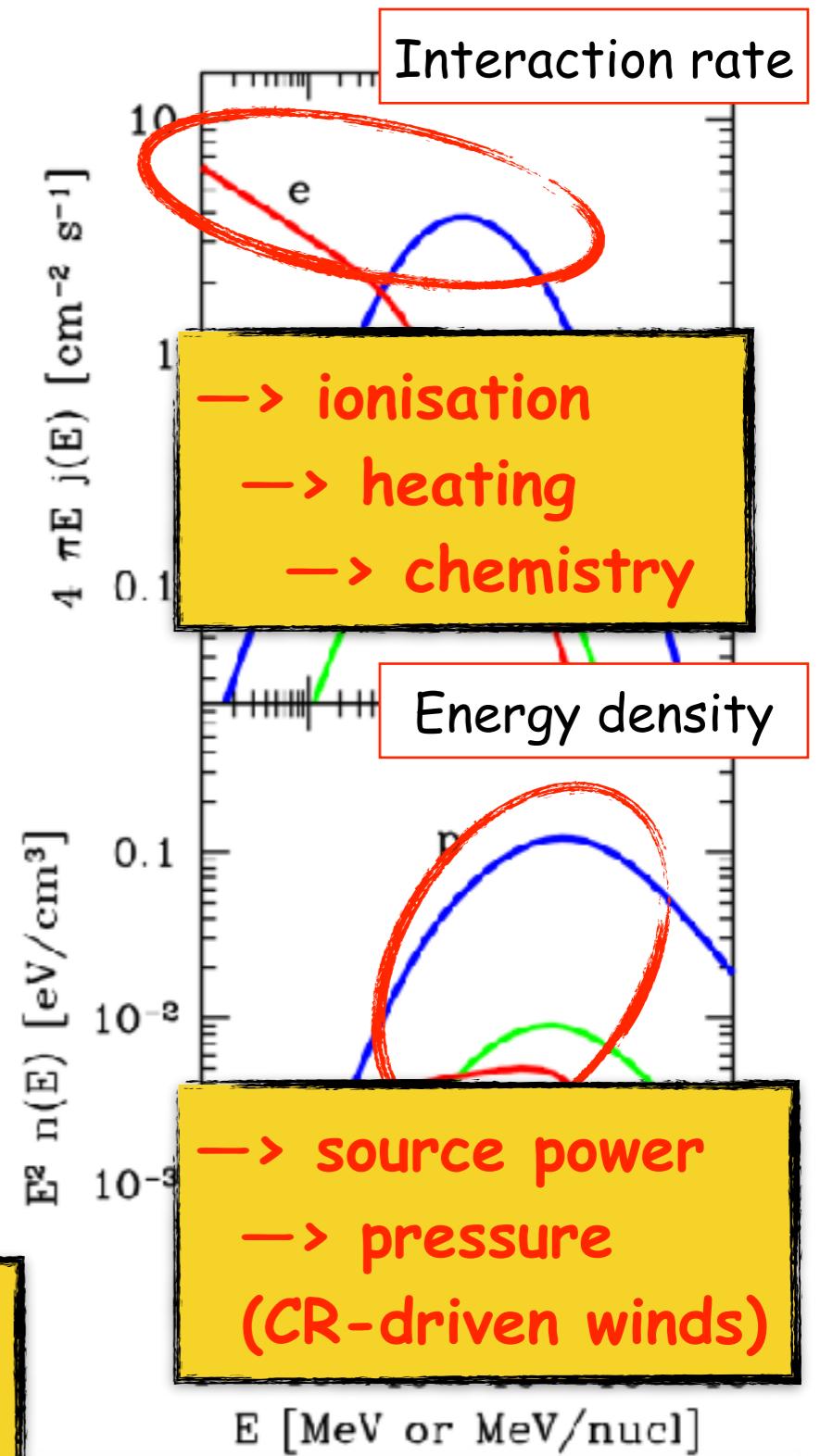
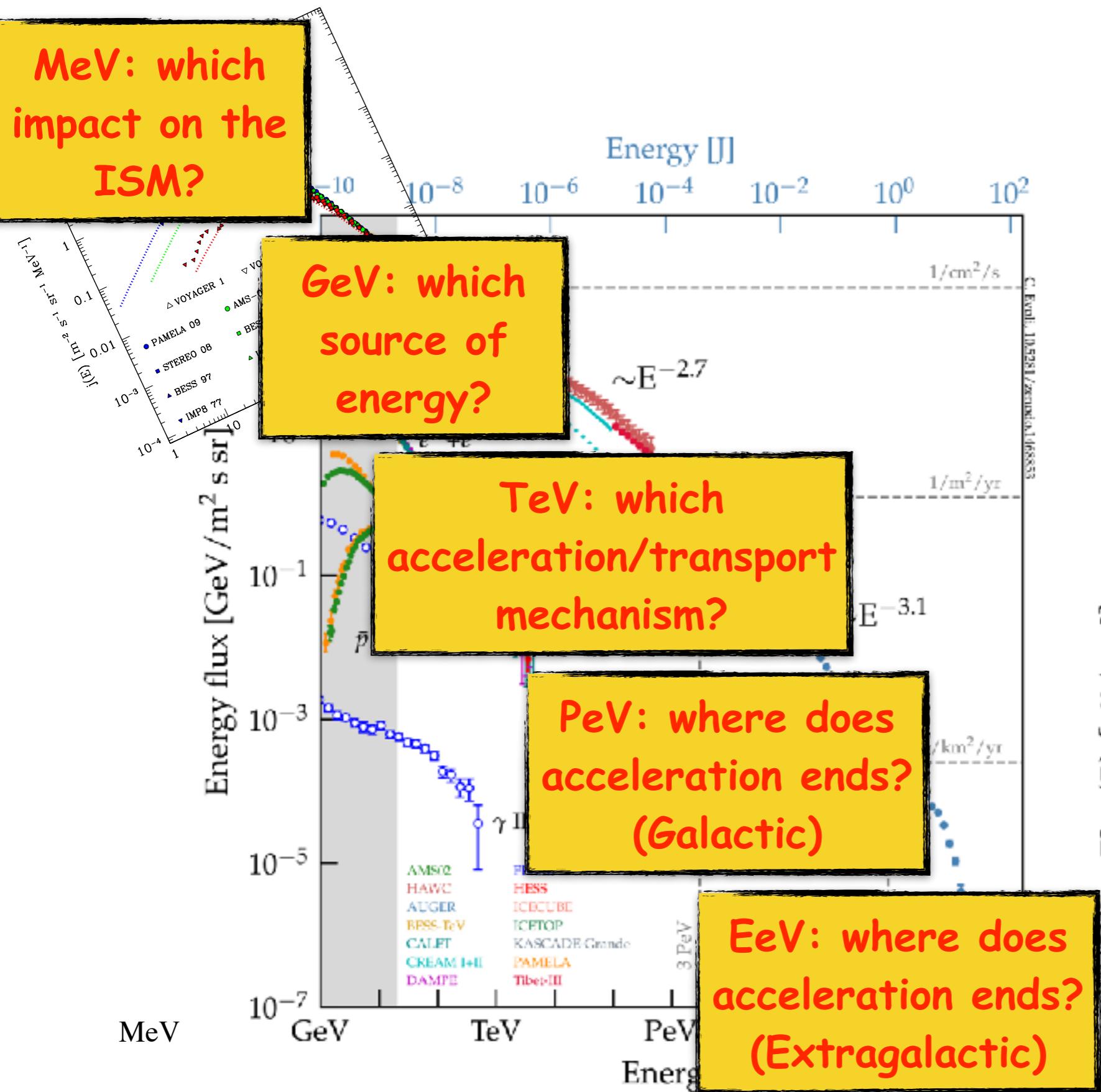


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Astrophysical environments

we will mostly discuss radiation produced
in interactions between energetic particles and matter or radiation/B-fields

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interstellar medium (ISM)

filling factor
↓

Phase	n_{tot} (cm $^{-3}$)	T (K)	M (10 $^9 M_{\odot}$)	f
Molecular	>300	10	2.0	0.01
Cold neutral	50	80	3.0	0.04
Warm Neutral	0.5	8,000	4.0	0.3
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$$B \sim 3 \mu\text{G}$$

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$$\frac{B^2}{8\pi} \sim \omega_{CMB} \sim 0.25 \text{ eV/cm}^3$$

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in int. but not only → high energy radiation without non-thermal particles
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let's begin with estimating the emission of a thermal plasma of temperature T

Simplifying assumptions: fully ionised hydrogen plasma ($n_i = n_e$), protons and electrons in thermal equilibrium (same temperature T)

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ROSAT



→ the hot phase consists of cavities inflated by stellar winds or generated by supernova remnants and emits thermal X-rays

X-ray telescopes onboard of satellites: XMM, Chandra, NuSTAR, eROSITA, ...

Emission from hot plasmas: thermal Bremsstrahlung

Radiation from a thermal electron-proton plasma

Emission from hot plasmas: thermal Bremsstrahlung

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$$v = \sqrt{\frac{3kT}{m}} \rightarrow v_e = \left(\frac{m_p}{m_e}\right)^{1/2} v_p \gg v_p$$

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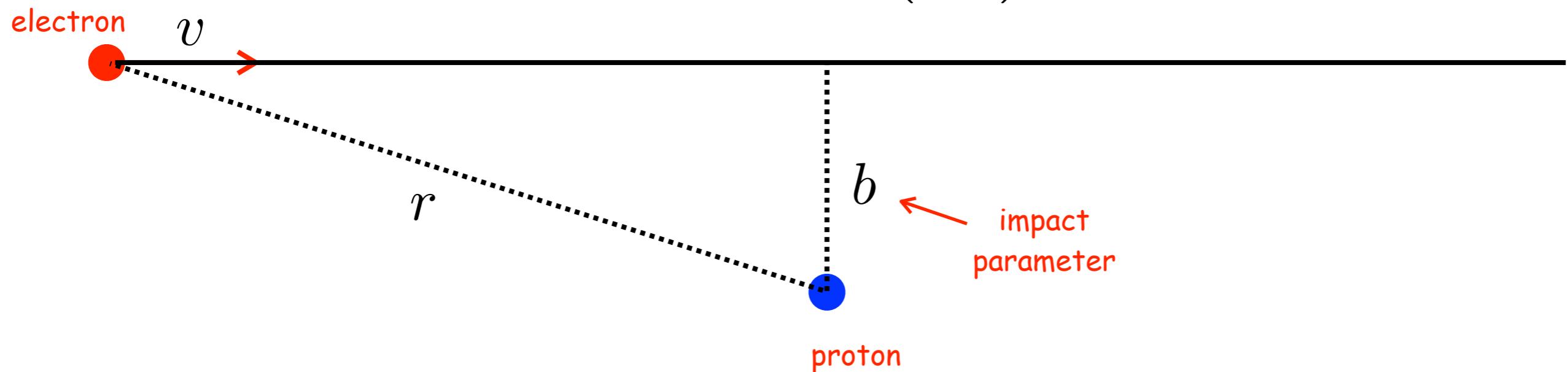
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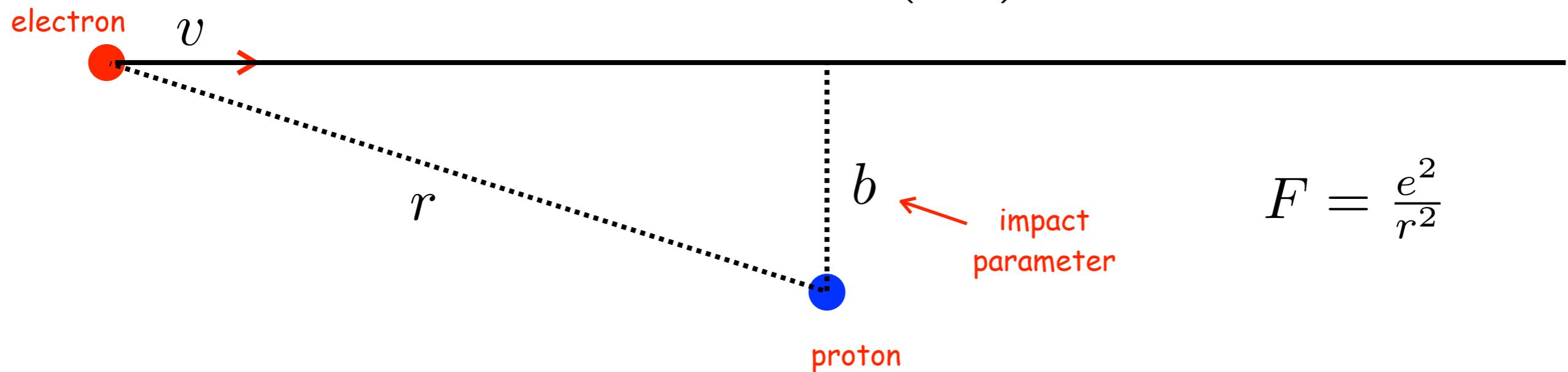
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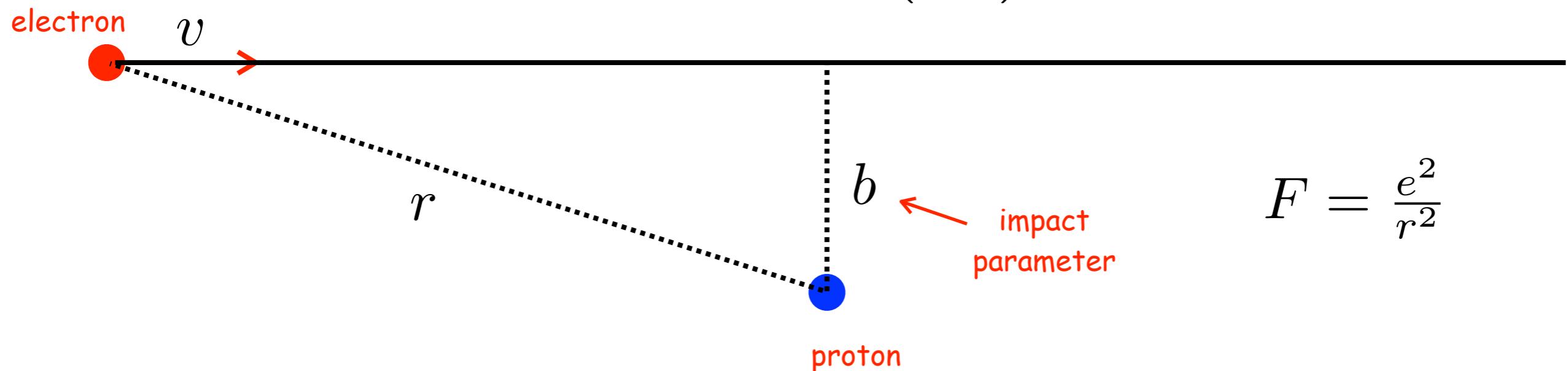
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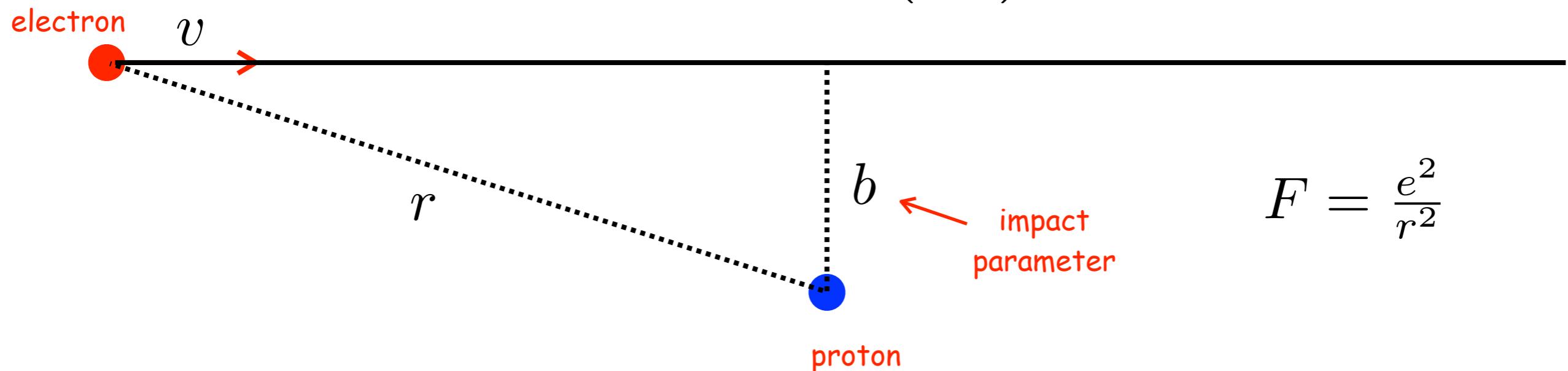
power emitted by an
accelerated charge

$$P = \frac{2e^2}{3c^3} a^2$$

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$$\begin{cases} r \approx b \rightarrow a \approx \frac{e^2}{m_e b^2} \\ r \gg b \rightarrow a \approx 0 \end{cases}$$

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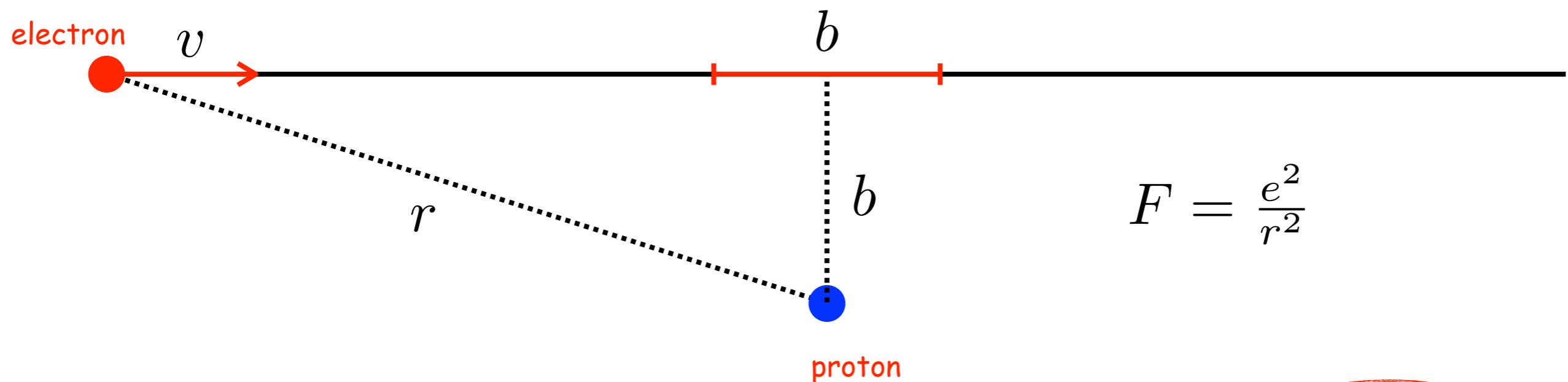
Thermal Bremsstrahlung

very brutal approximations...

characteristic time
for the interaction

$$\tau \approx \frac{b}{v} \longrightarrow \omega \approx \frac{1}{\tau} = \frac{v}{b}$$

characteristic
frequency of the
emitted radiation



power emitted by an
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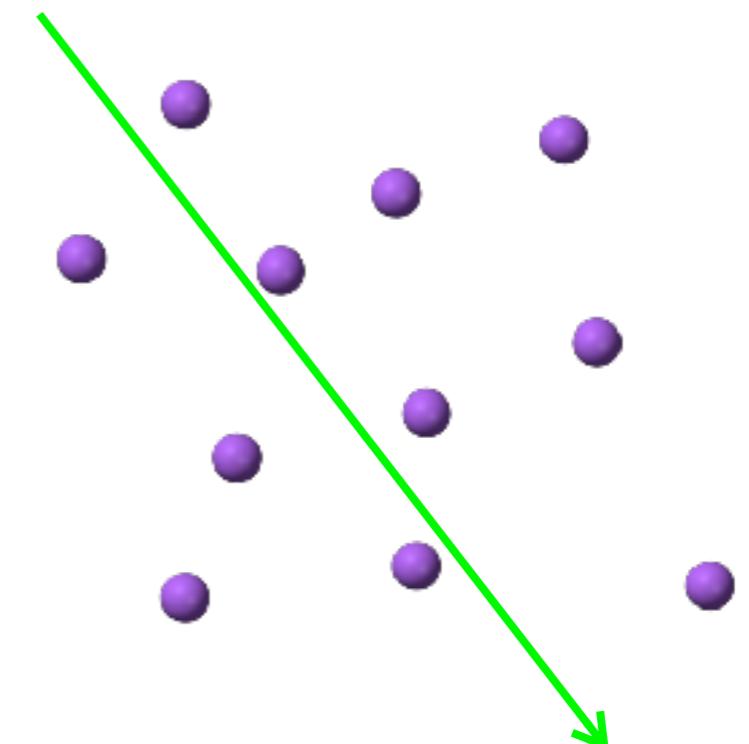
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Thermal Bremsstrahlung

rough estimate of the
impact parameter b

plasma proton density -> n_p

mean distance between protons -> $l_p \sim n_p^{-1/3} \approx b$

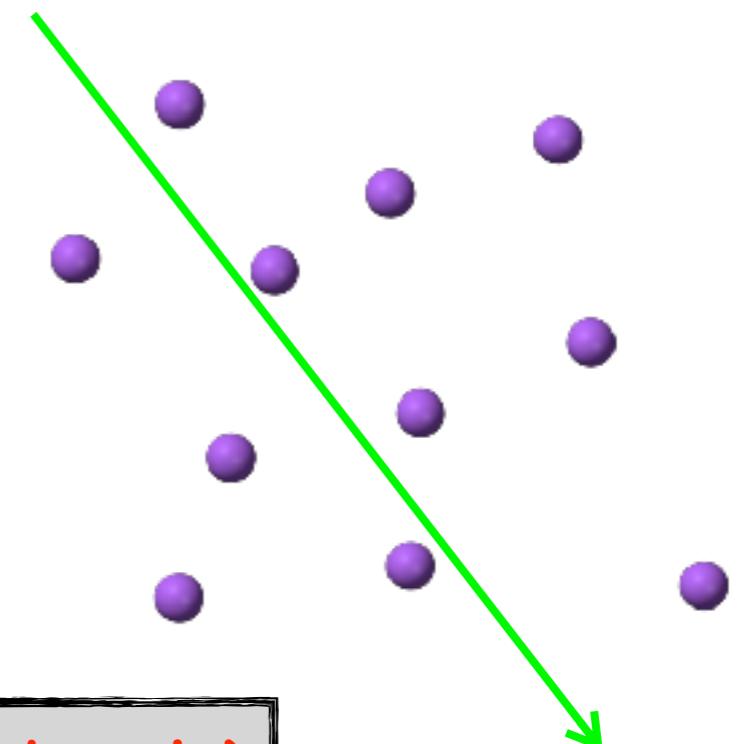


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emissivity (power per unit frequency, volume, and solid angle)

$$\omega \rightarrow v = \omega/2\pi$$

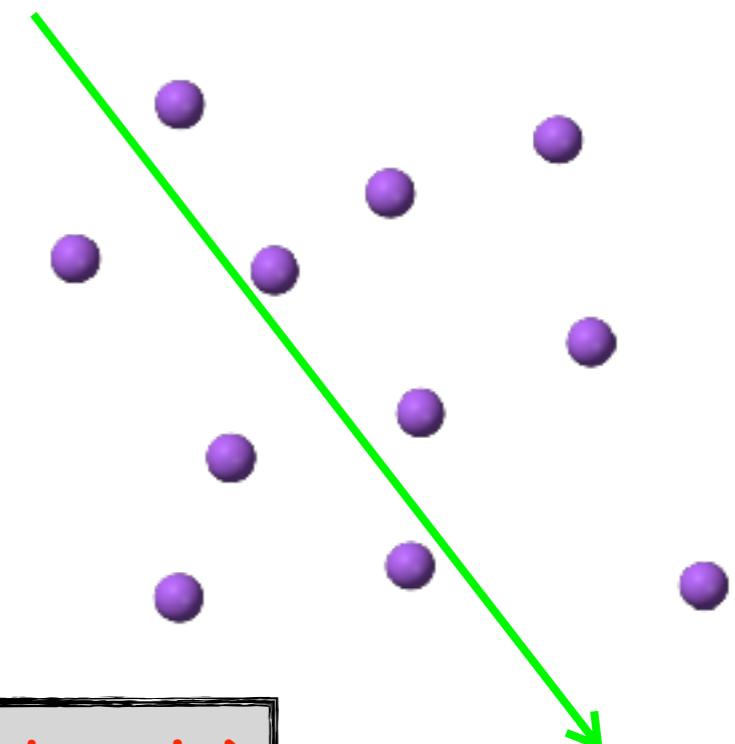
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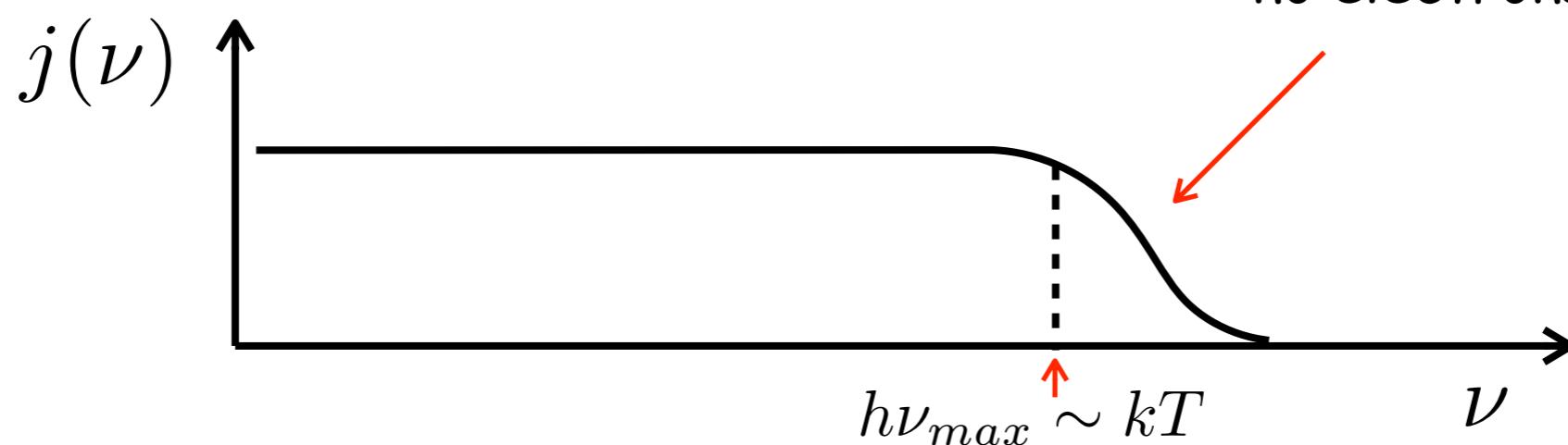


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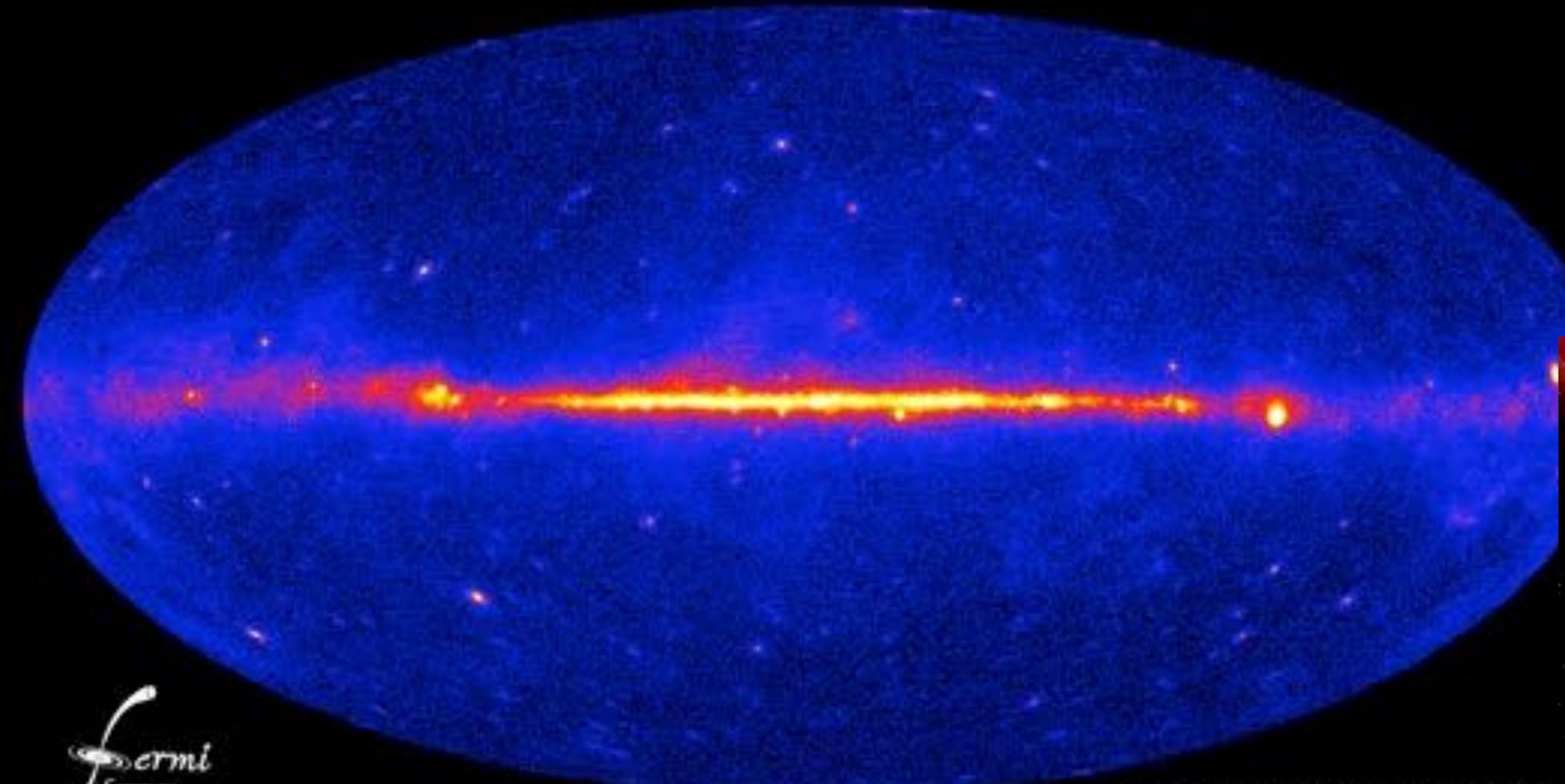
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exponential suppression
 \rightarrow no electrons with energy $\gg kT$



Cosmic ray interactions in the sky

NASA's Fermi telescope reveals best-ever view of the gamma-ray sky

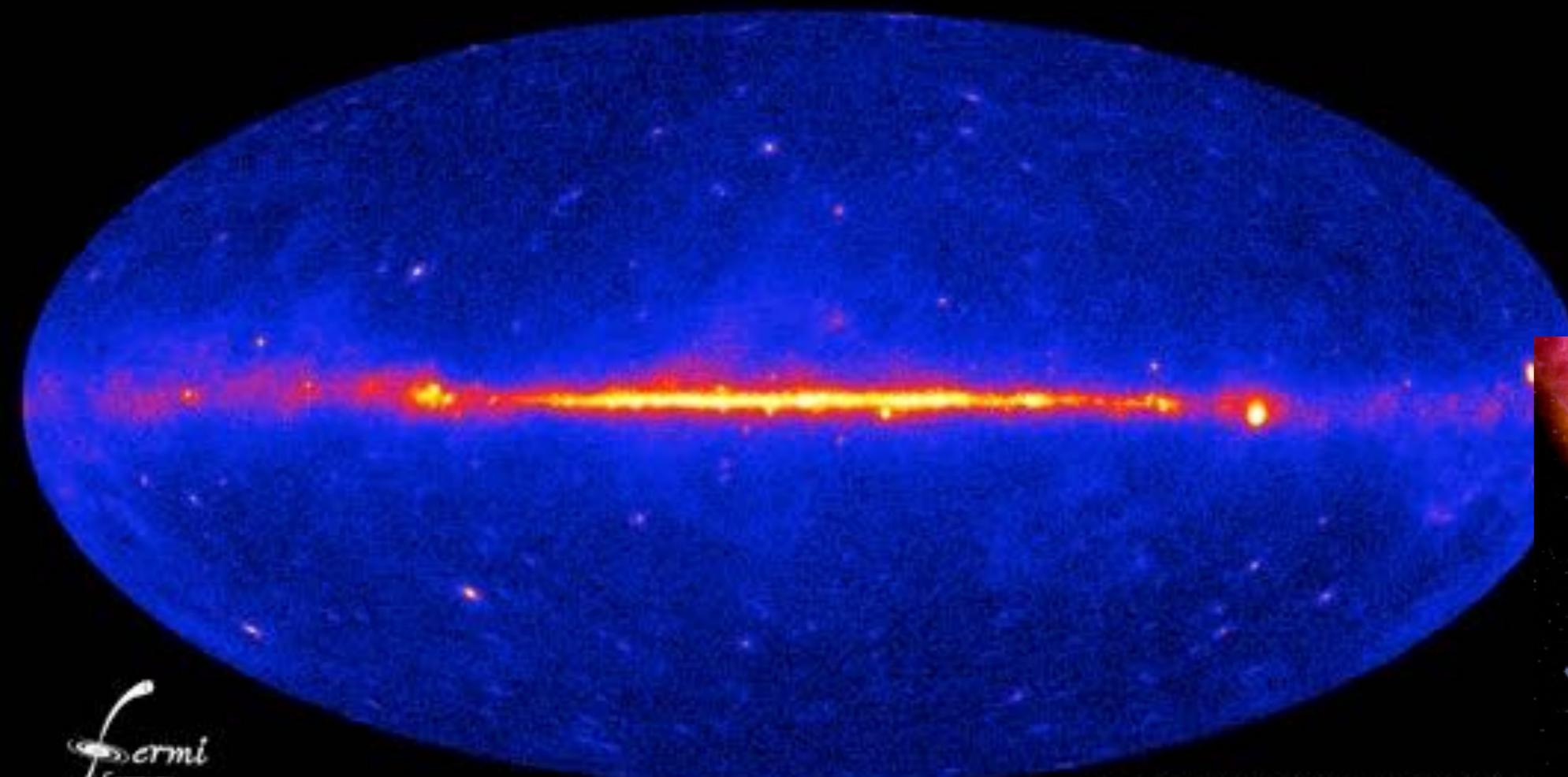


Credit: NASA/DOE/Fermi LAT Collabor

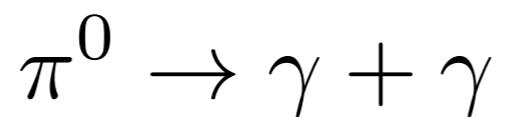
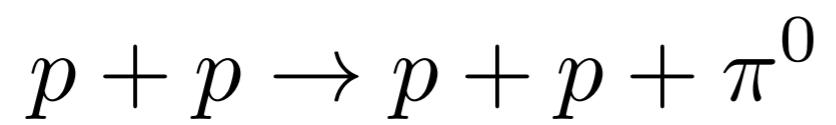


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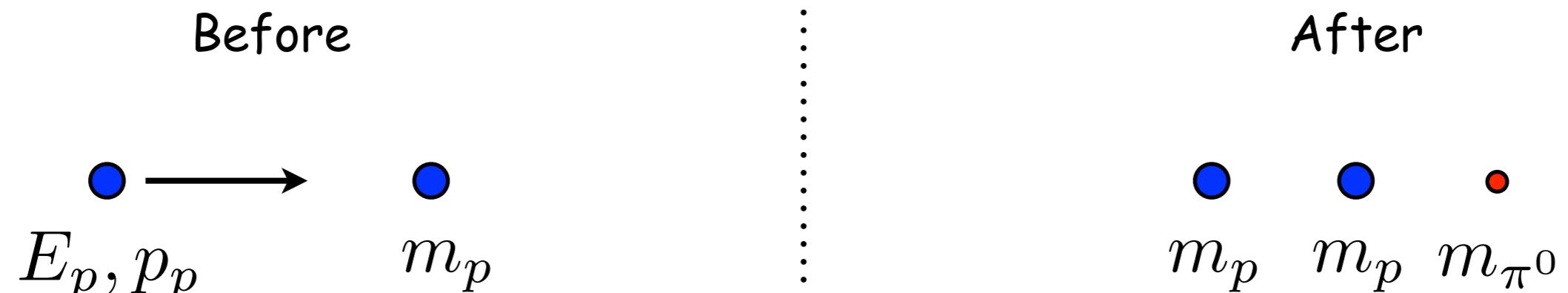
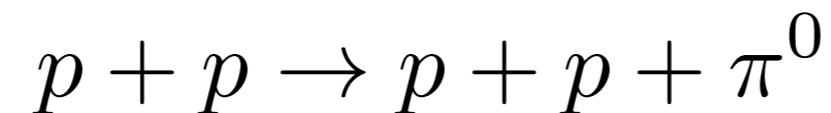


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Gamma-Ray Astronomy: p-p interactions

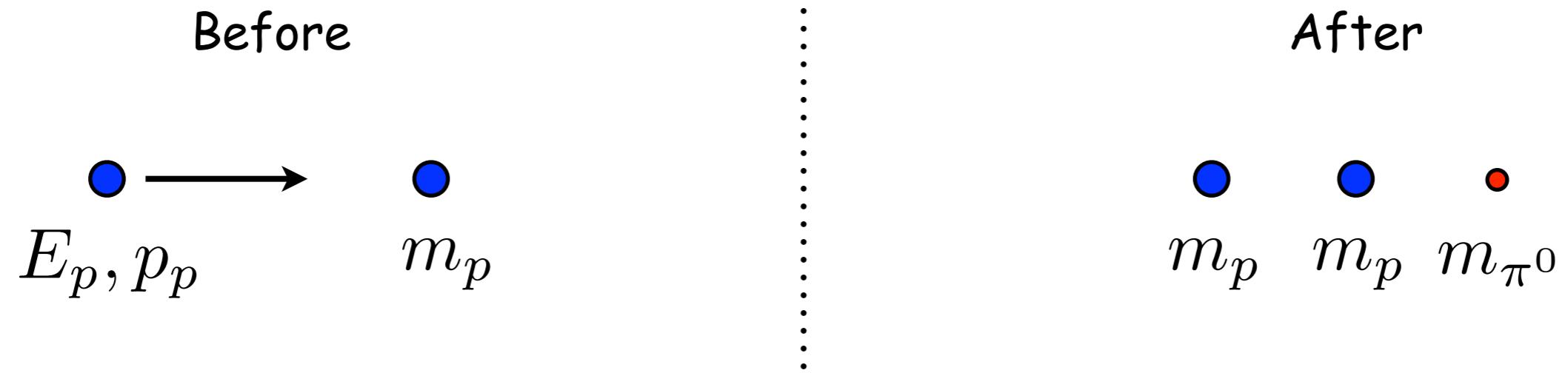
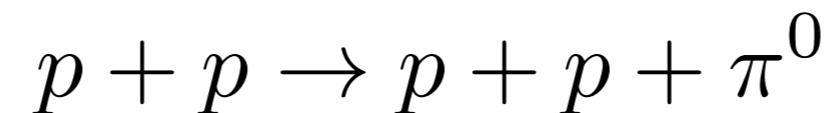
Energy threshold for neutral pion production:



$$E^2 - p^2 c^2$$

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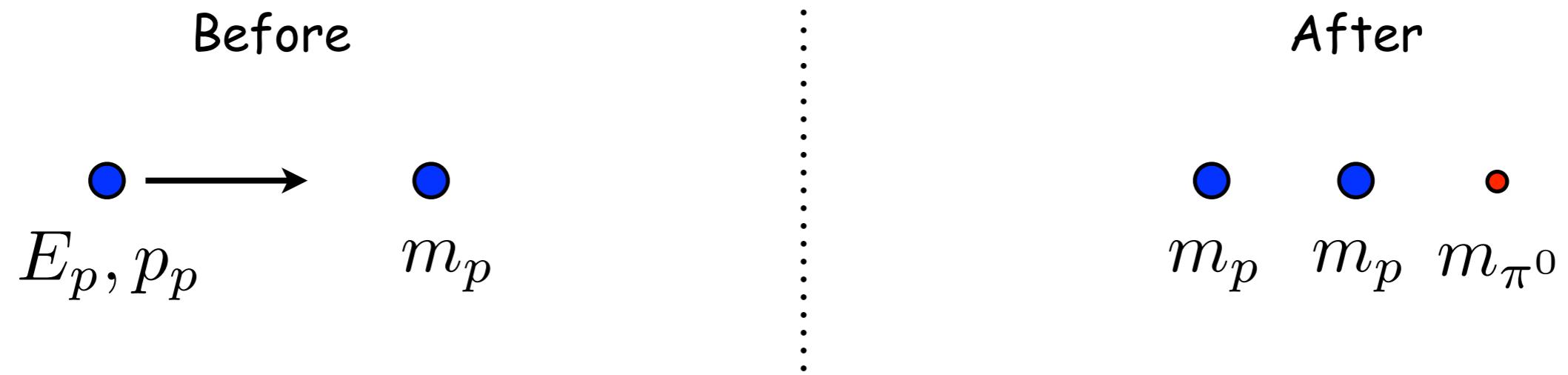
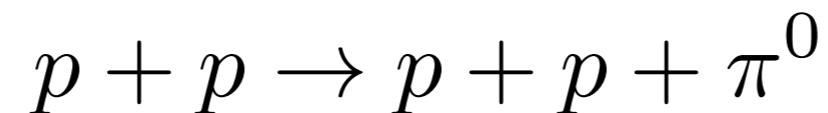
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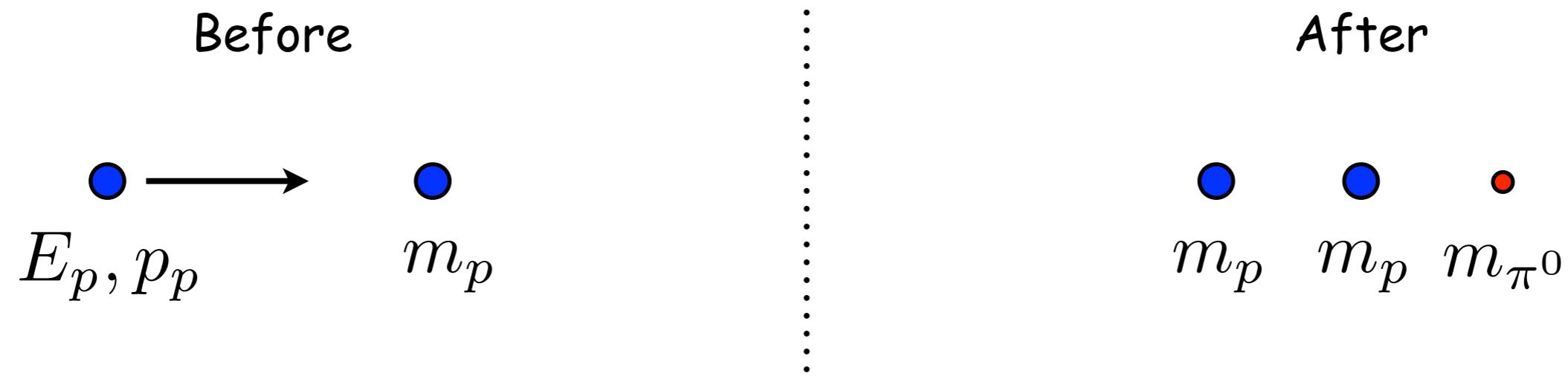
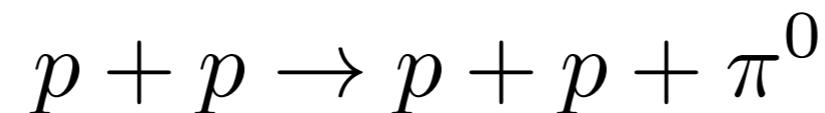
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$$E_p - m_p c^2 > 2m_{\pi^0} c^2 + \left(\frac{m_{\pi^0}}{2m_p} \right) m_{\pi^0} c^2 \approx 280 \text{ MeV}$$

energy threshold

Gamma-Ray Astronomy: p-p interactions

Let's calculate the spectrum of neutral pions:

We assume a power law spectrum for CRs: $N_p(E_p) \propto E_p^{-\delta}$

Fraction of proton kinetic energy transferred to pion (from data): $f_{\pi^0} \approx 0.17$

.....
**production
rate**

**total cross
section**

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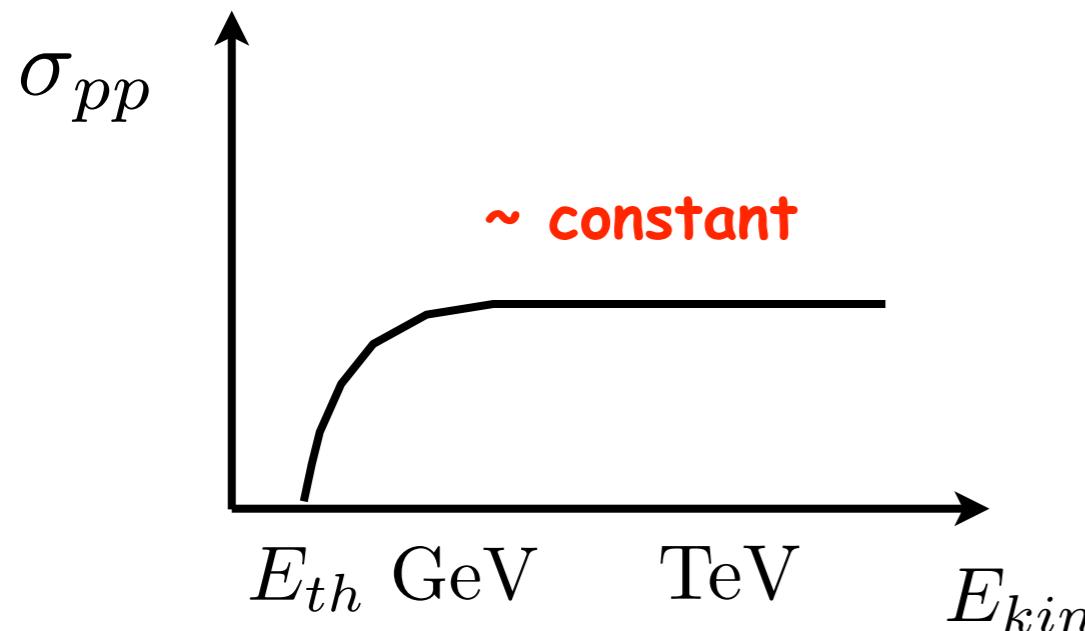
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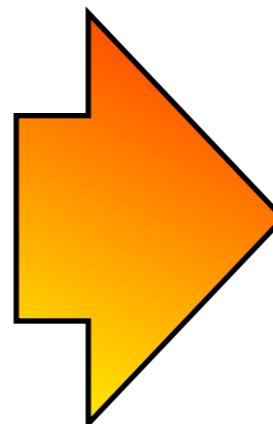
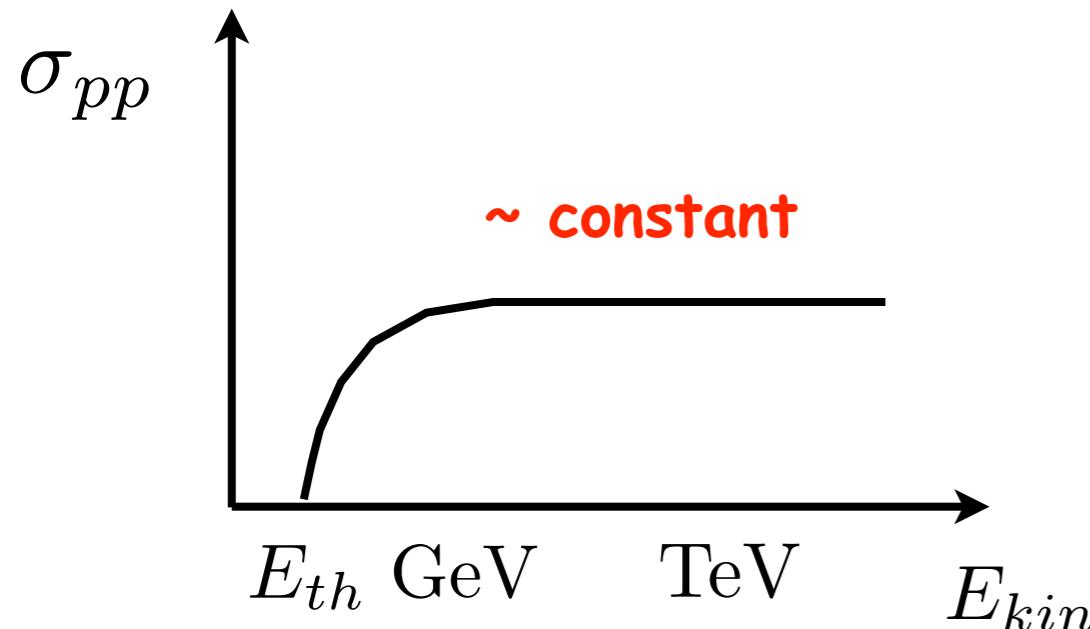
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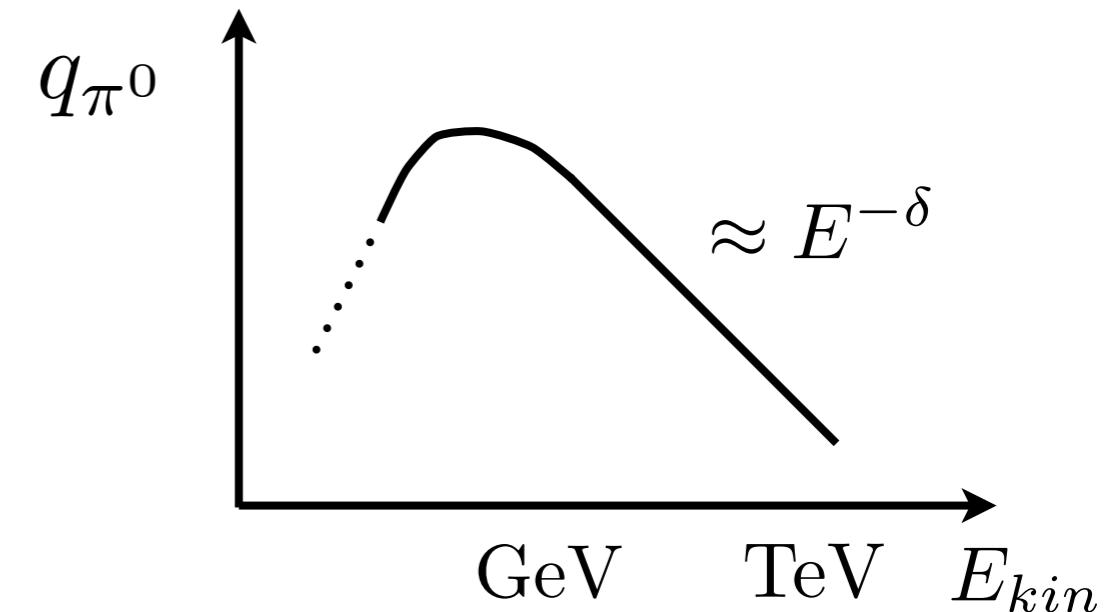
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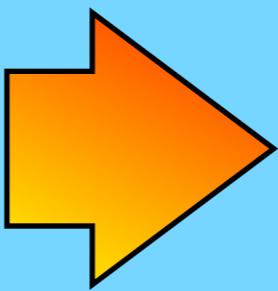
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Gamma-Ray Astronomy: p-p interactions

Let's now calculate the spectrum of photons from pion decay - I

The photon spectrum is
the result of a "one-body-
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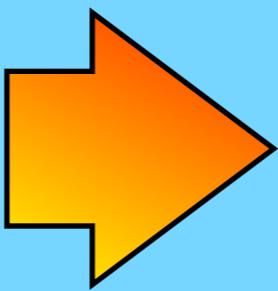


The photon spectrum MUST
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Gamma-Ray Astronomy: p-p interactions

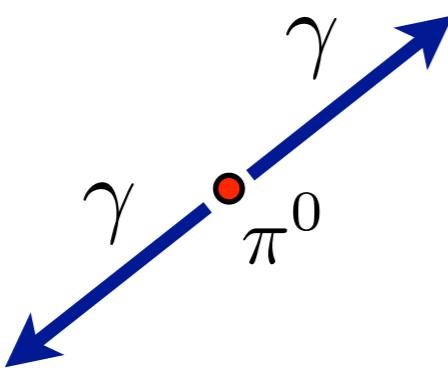
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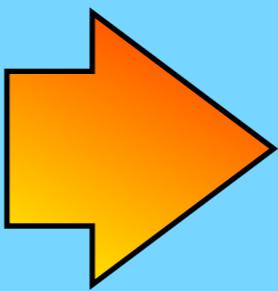


$$E_{\gamma}^{*} = \frac{m_{\pi^0}}{2}$$

Gamma-Ray Astronomy: p-p interactions

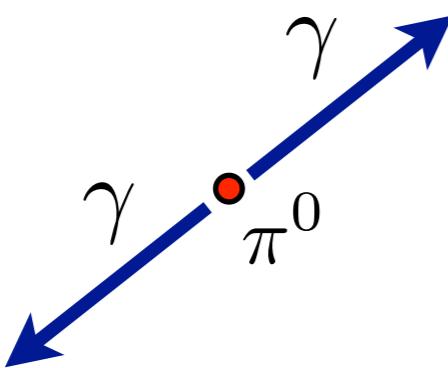
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Lab frame:

$$E_{\gamma} = \gamma (E_{\gamma}^{*} + vp_{\gamma}^{*} \cos \theta^{*})$$

max and min energies $\rightarrow \cos \theta^{*} = \pm 1$

$$\frac{m_{\pi^0}}{2} \sqrt{\frac{1-\beta}{1+\beta}} \leq E_{\gamma} \leq \frac{m_{\pi^0}}{2} \sqrt{\frac{1+\beta}{1-\beta}}$$

Gamma-Ray Astronomy: p-p interactions

Let's now calculate the spectrum of photons from pion decay - II

$$E_{\gamma}^{min} = \frac{m_{\pi^0}}{2} \sqrt{\frac{1-\beta}{1+\beta}} \leq E_{\gamma} \leq \frac{m_{\pi^0}}{2} \sqrt{\frac{1+\beta}{1-\beta}} = E_{\gamma}^{max}$$

(1)
$$\frac{\log E_{\gamma}^{max} + \log E_{\gamma}^{min}}{2} = \log \left(\frac{m_{\pi^0}}{2} \right)$$

in log-scale, the centre
of the interval is half
the pion mass

Gamma-Ray Astronomy: p-p interactions

Let's now calculate the spectrum of photons from pion decay - II

$$E_{\gamma}^{min} = \frac{m_{\pi^0}}{2} \sqrt{\frac{1-\beta}{1+\beta}} \leq E_{\gamma} \leq \frac{m_{\pi^0}}{2} \sqrt{\frac{1+\beta}{1-\beta}} = E_{\gamma}^{max}$$

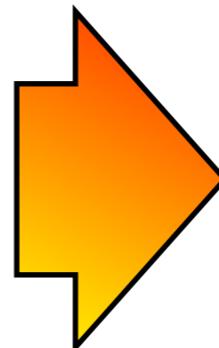
(1) $\frac{\log E_{\gamma}^{max} + \log E_{\gamma}^{min}}{2} = \log \left(\frac{m_{\pi^0}}{2} \right)$

in log-scale, the centre
of the interval is half
the pion mass

(2) in the pion rest frame the photon distribution is isotropic $\frac{dn_{\gamma}}{d\Omega^*} = \frac{1}{4\pi}$

$$d\Omega^* \propto d(\cos \theta^*)$$

$$E_{\gamma} = \gamma (E_{\gamma}^* + vp_{\gamma}^* \cos \theta^*) \rightarrow dE_{\gamma} \propto d(\cos \theta^*)$$

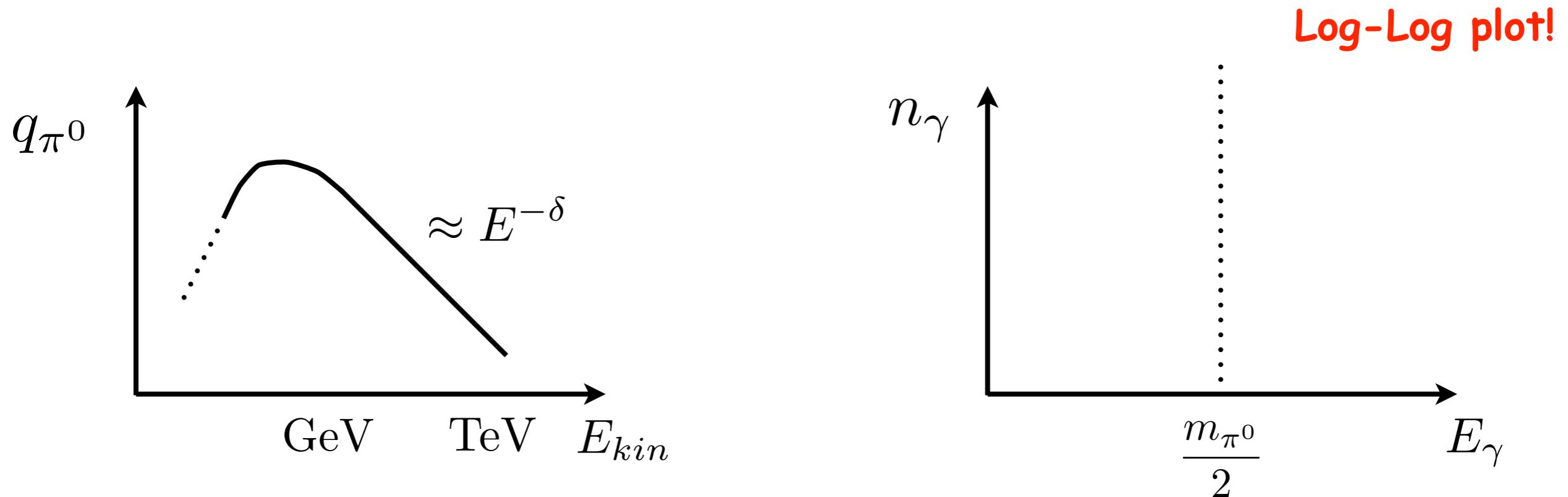


$$\frac{dn_{\gamma}}{dE_{\gamma}} = const$$

The spectrum is flat!

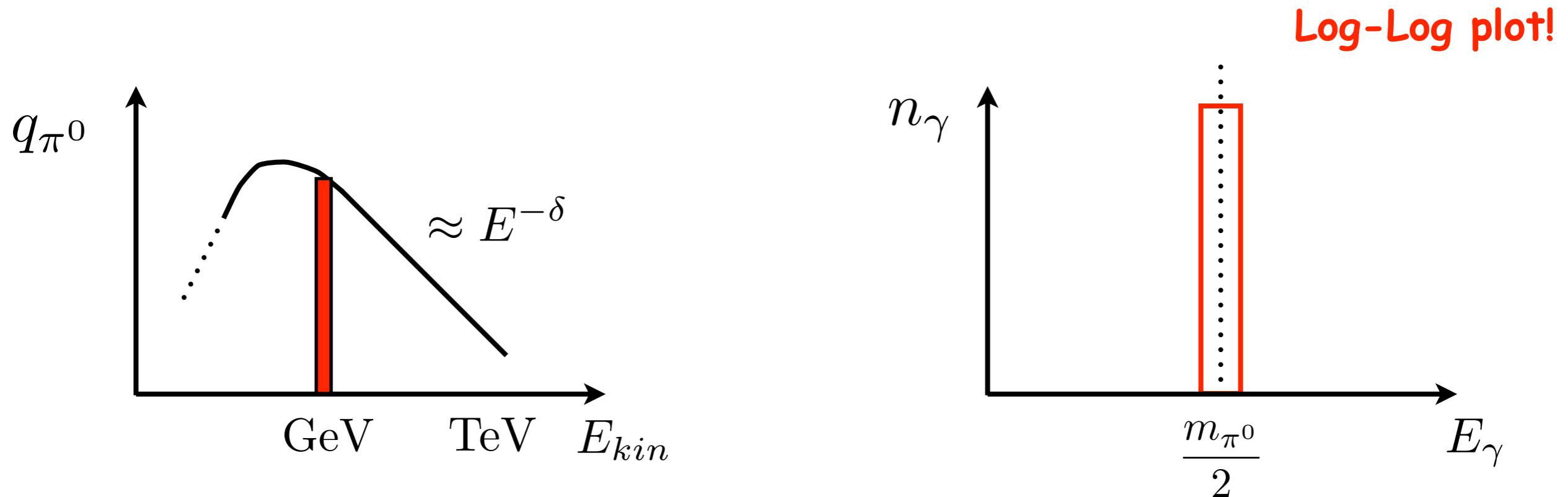
Gamma-Ray Astronomy: p-p interactions

Let's now calculate the spectrum of photons from pion decay - III



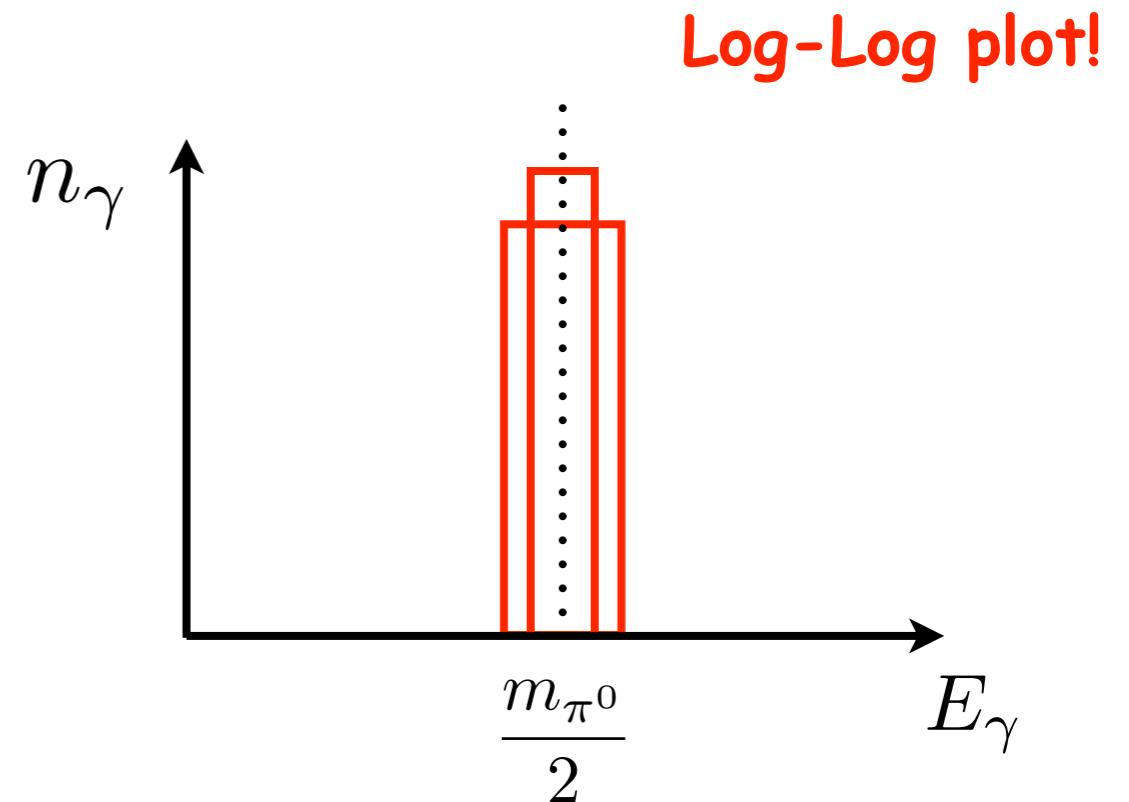
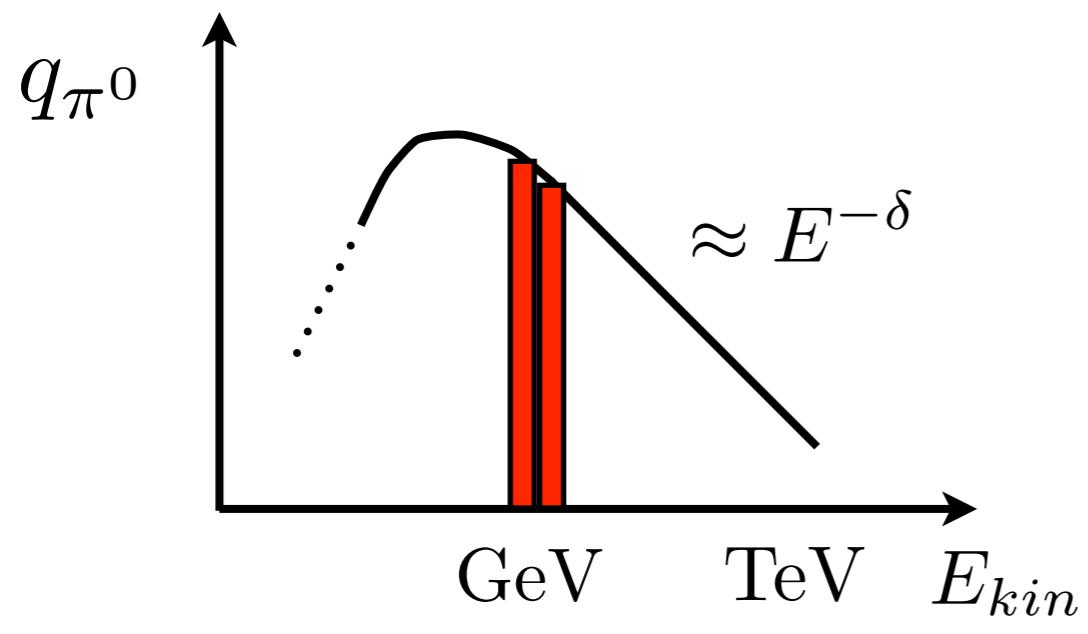
Gamma-Ray Astronomy: p-p interactions

Let's now calculate the spectrum of photons from pion decay - III



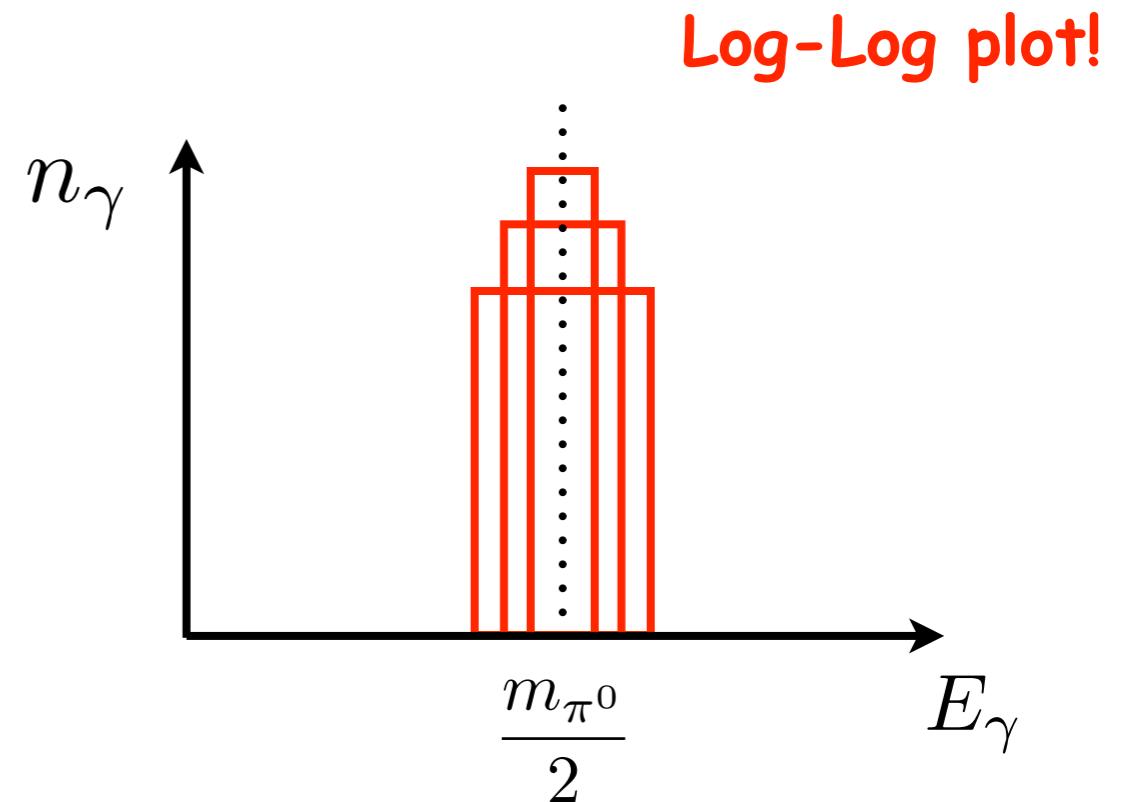
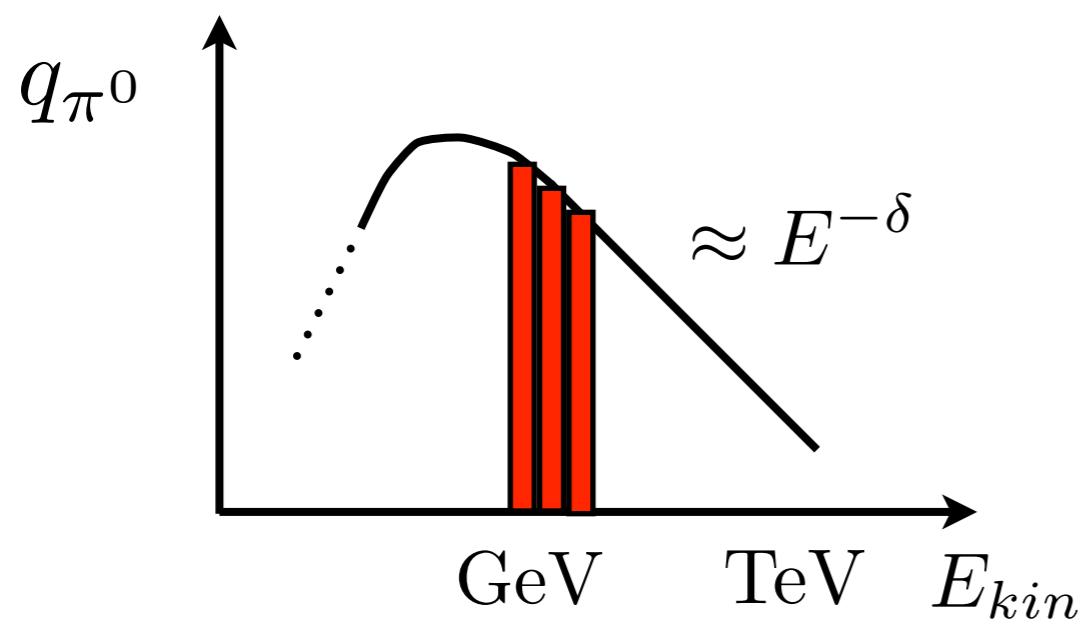
Gamma-Ray Astronomy: p-p interactions

Let's now calculate the spectrum of photons from pion decay - III



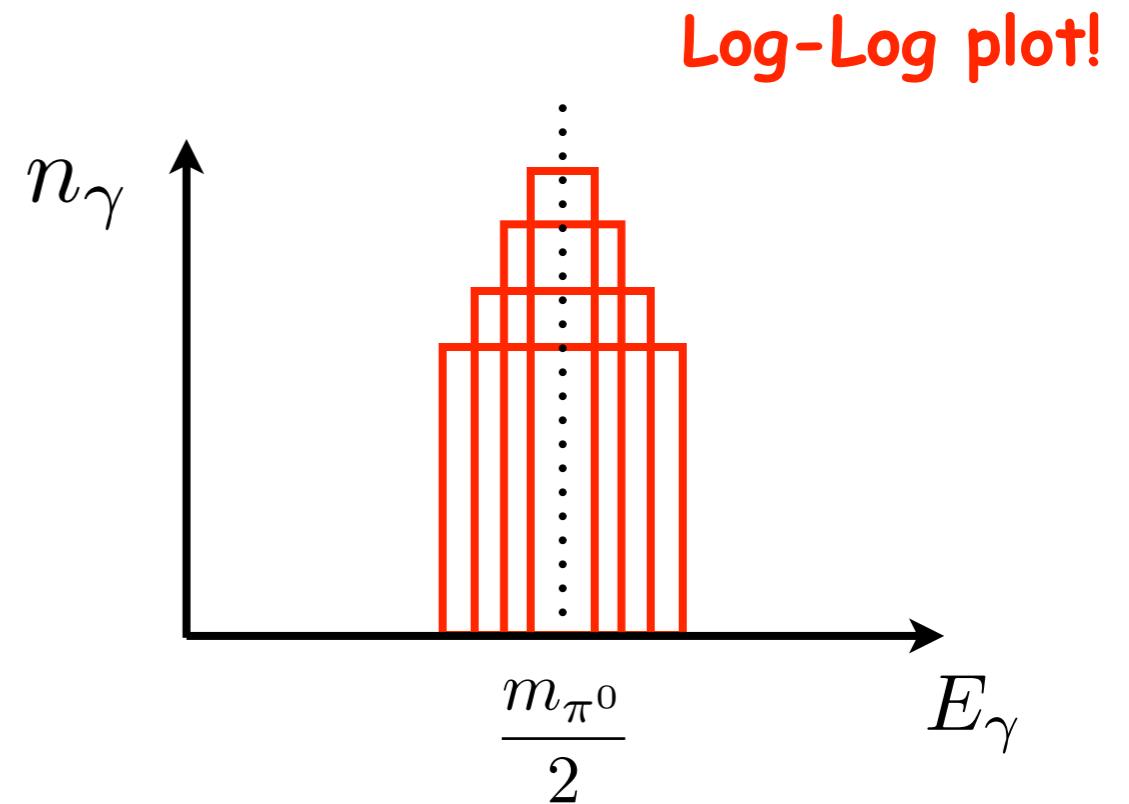
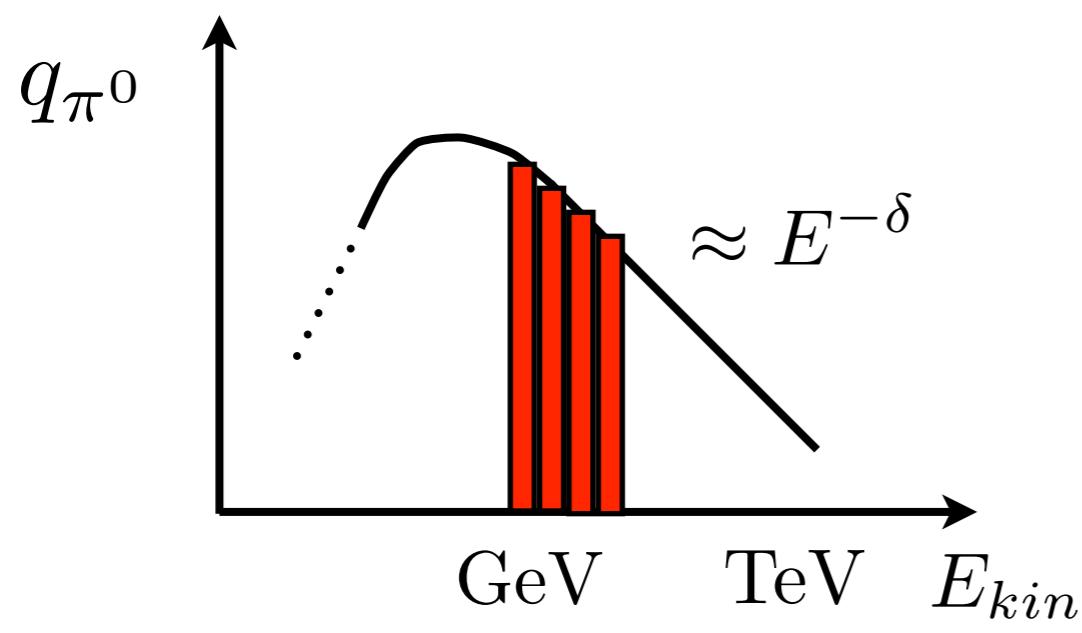
Gamma-Ray Astronomy: p-p interactions

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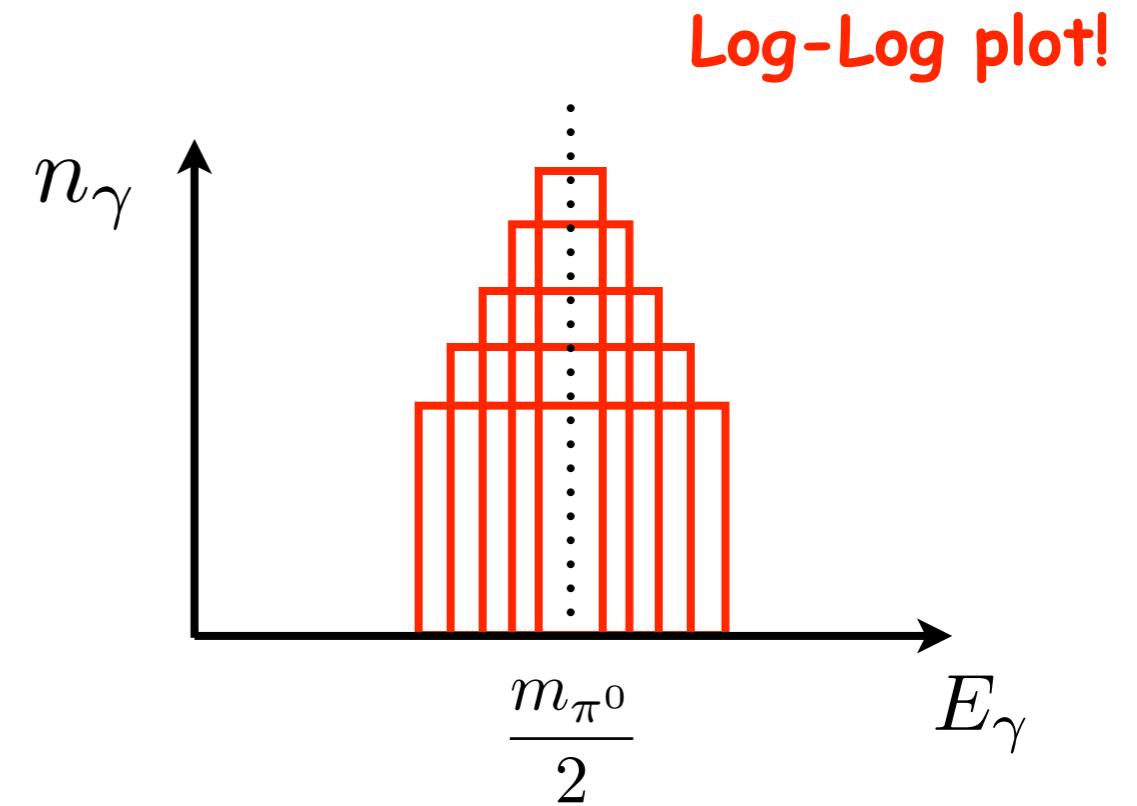
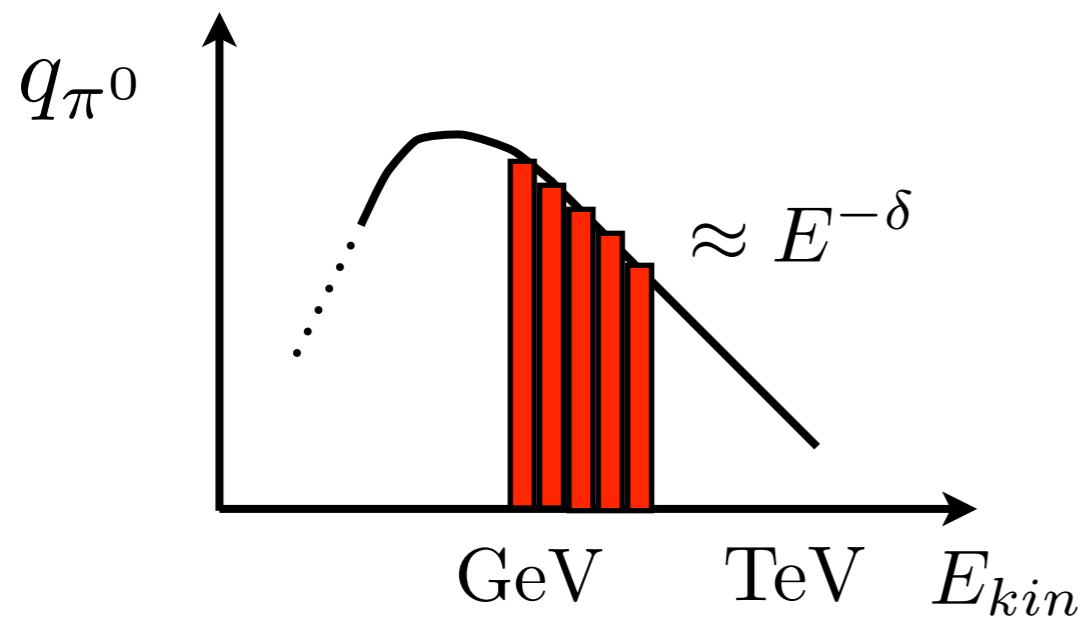
Gamma-Ray Astronomy: p-p interactions

Let's now calculate the spectrum of photons from pion decay - III



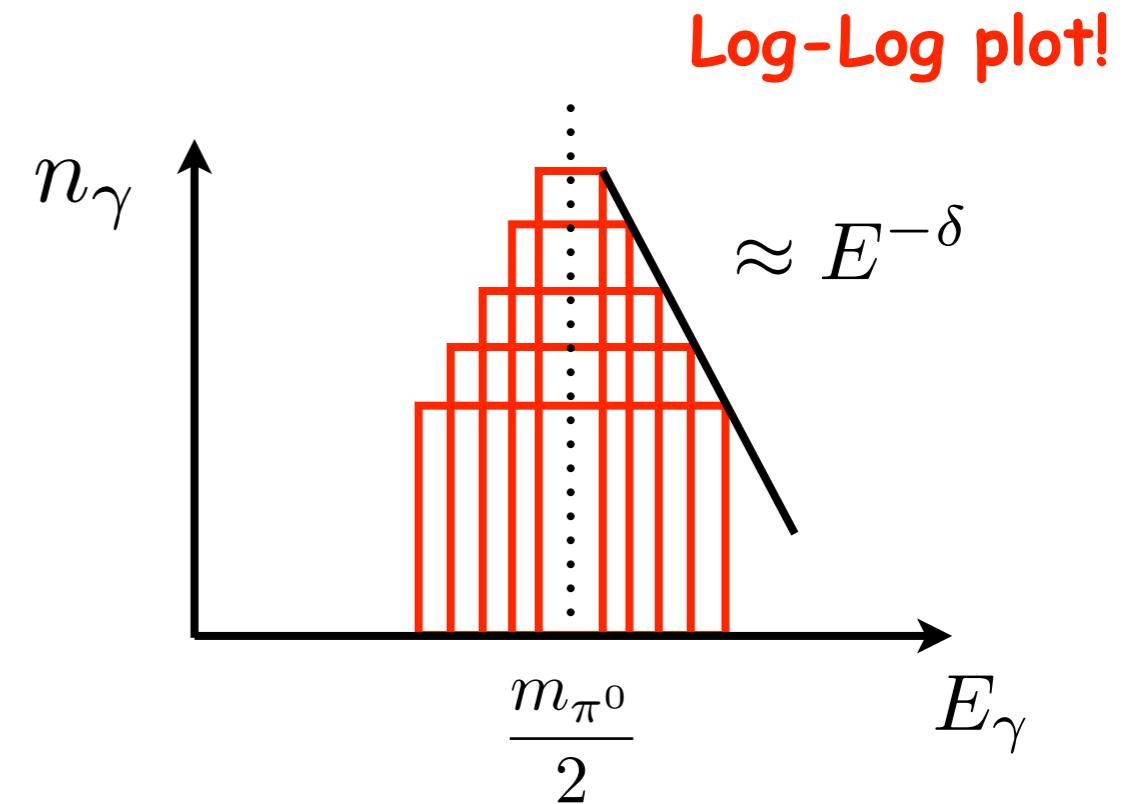
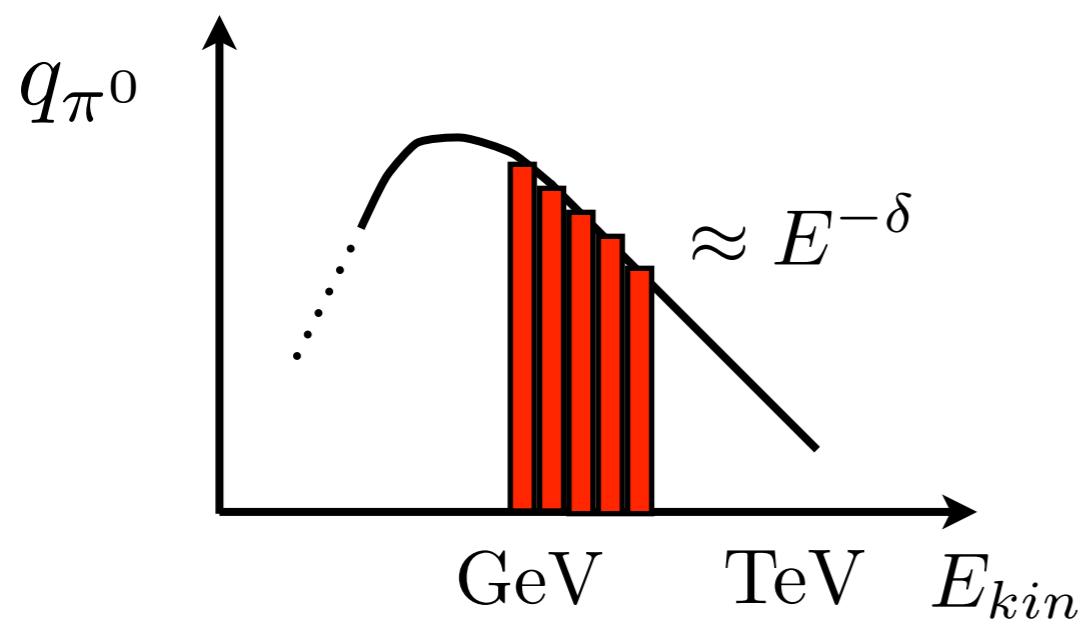
Gamma-Ray Astronomy: p-p interactions

Let's now calculate the spectrum of photons from pion decay - III



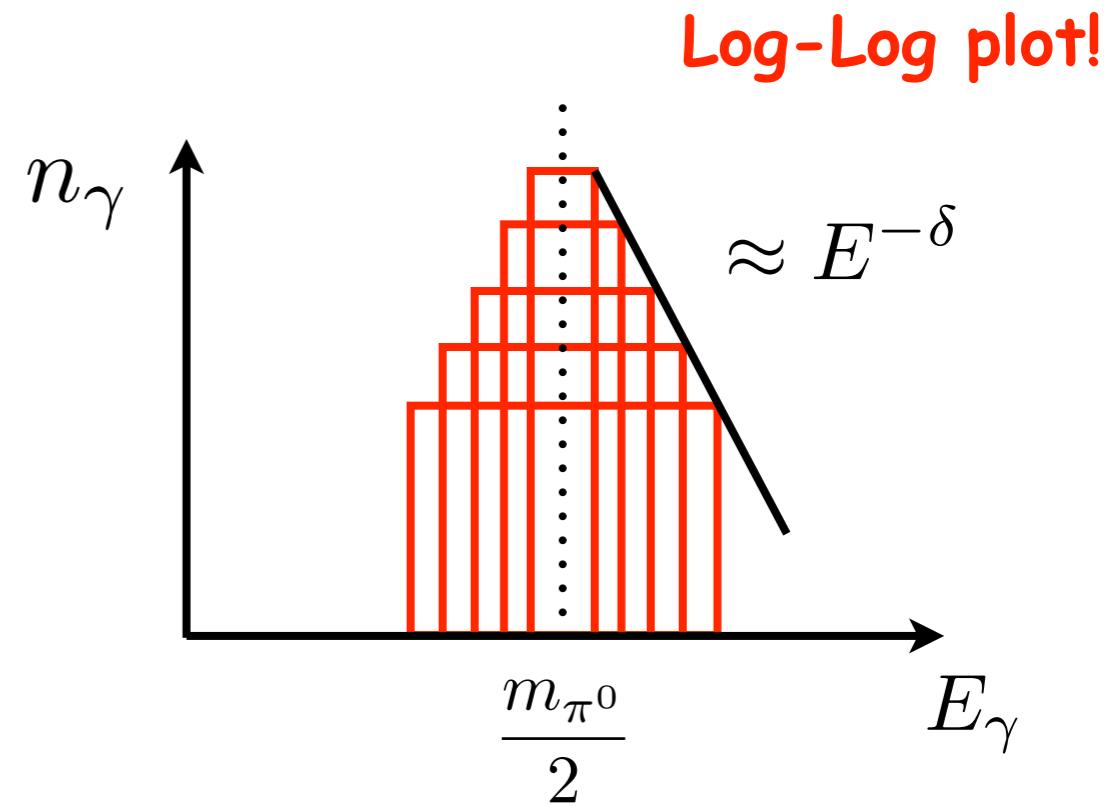
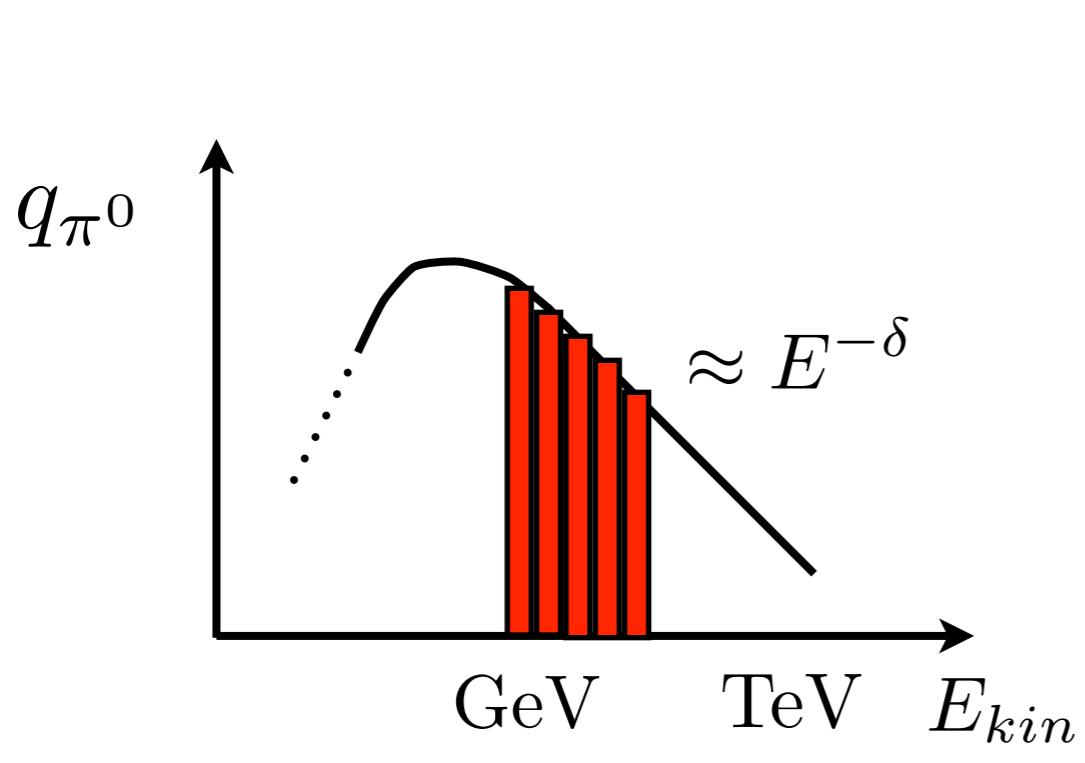
Gamma-Ray Astronomy: p-p interactions

Let's now calculate the spectrum of photons from pion decay - III



Gamma-Ray Astronomy: p-p interactions

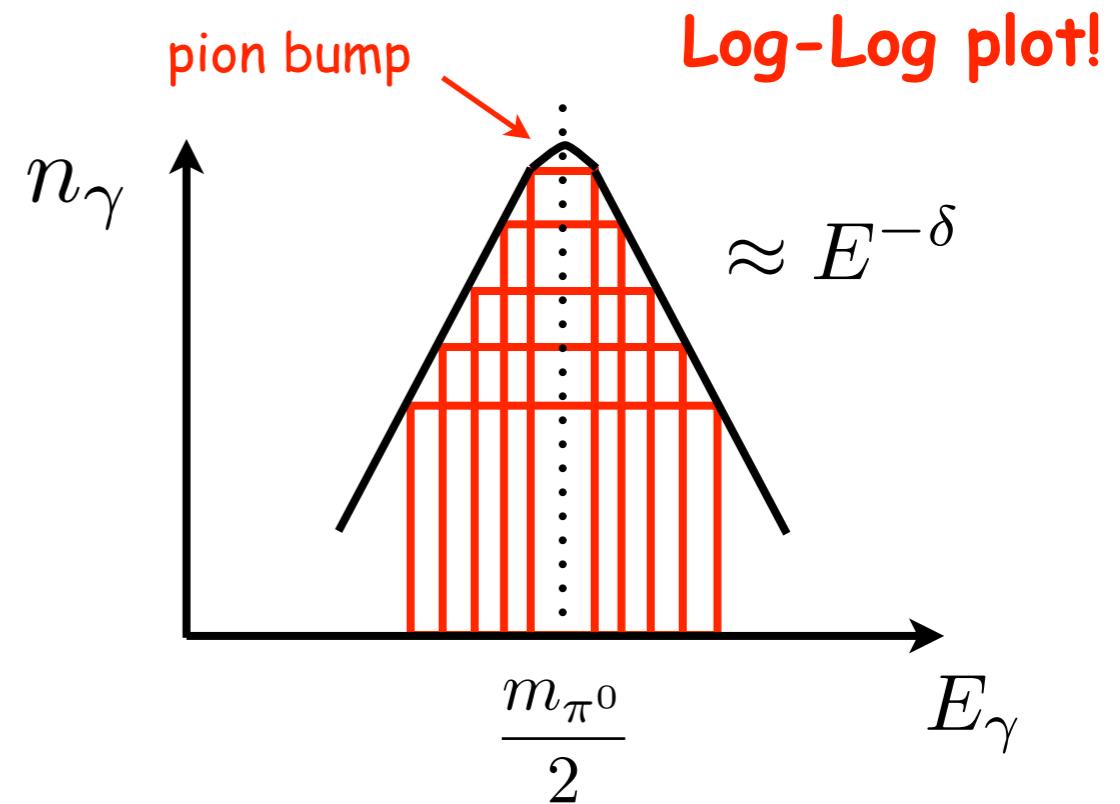
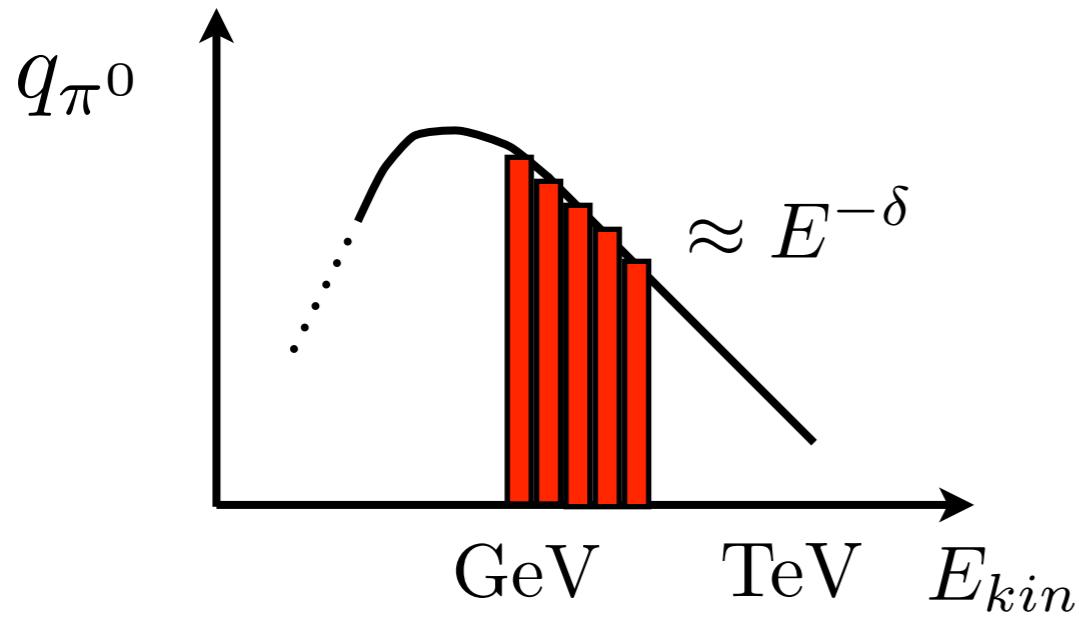
Let's now calculate the spectrum of photons from pion decay - III



- the gamma ray spectrum is symmetric (in log-log) with respect to: $\frac{m_{\pi^0}}{2} \sim 70 \text{ MeV}$
- at high energy the spectrum mimics the CR spectrum, with (roughly): $E_{\gamma} \approx \frac{E_{CR}}{10}$

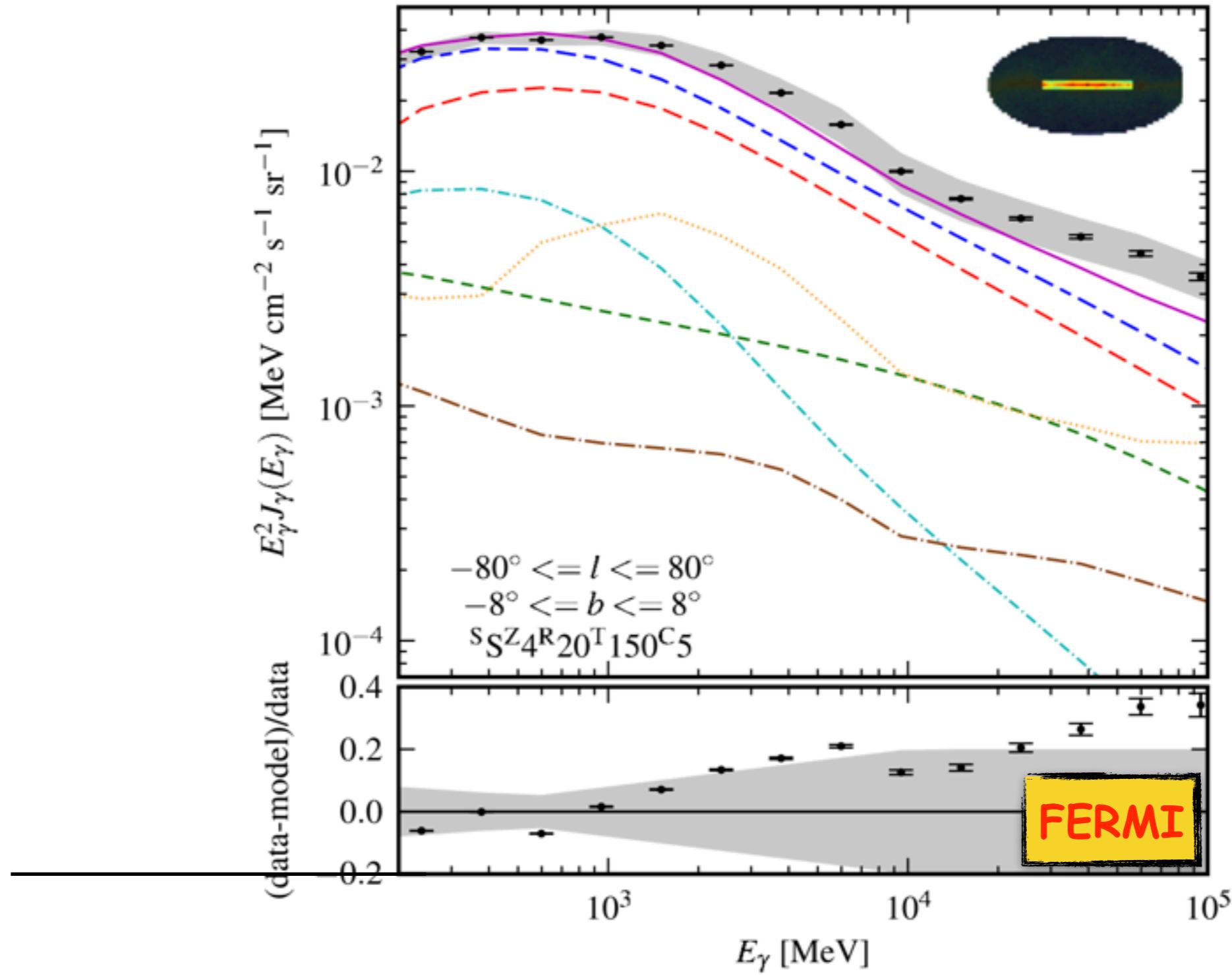
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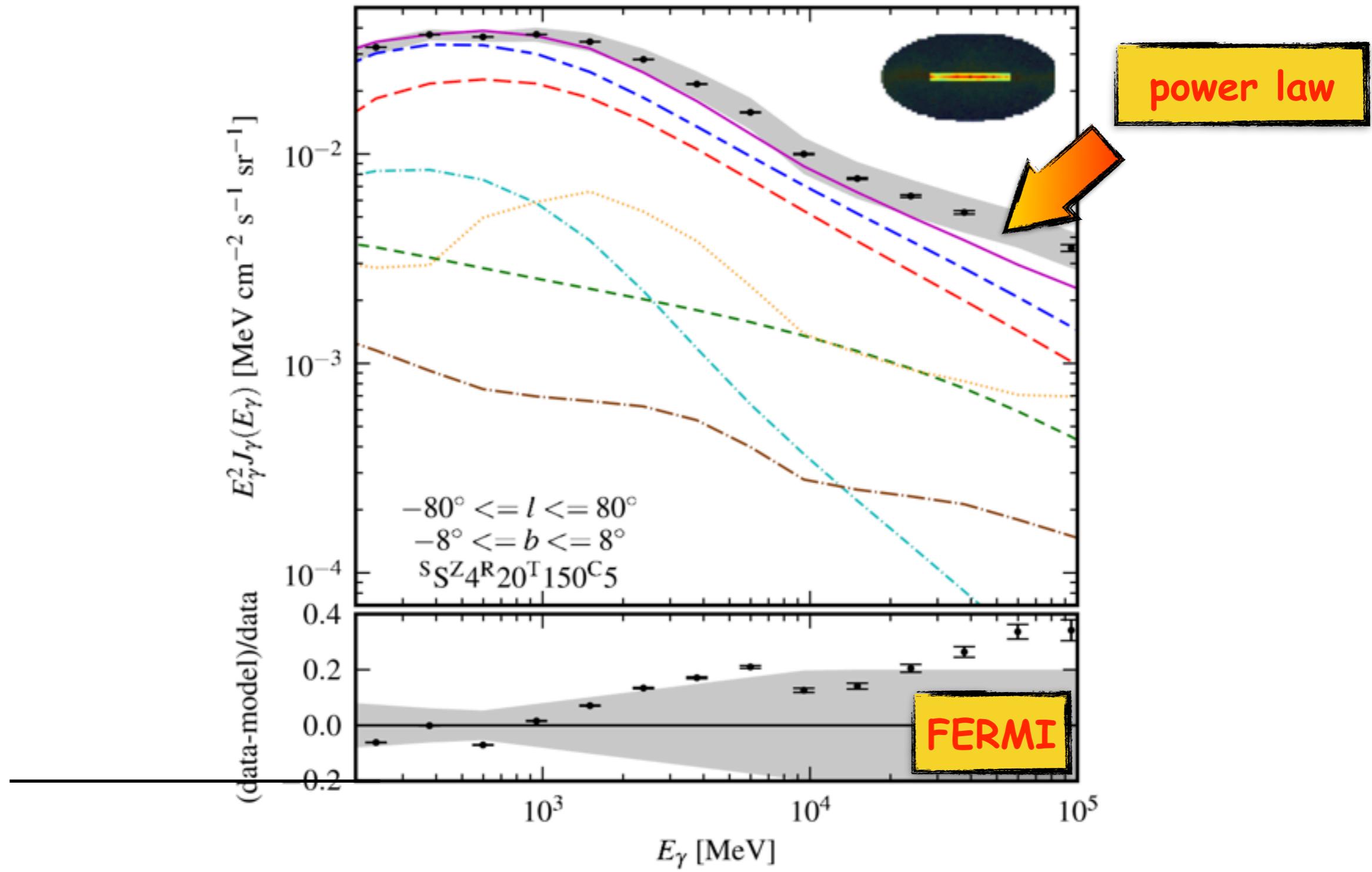


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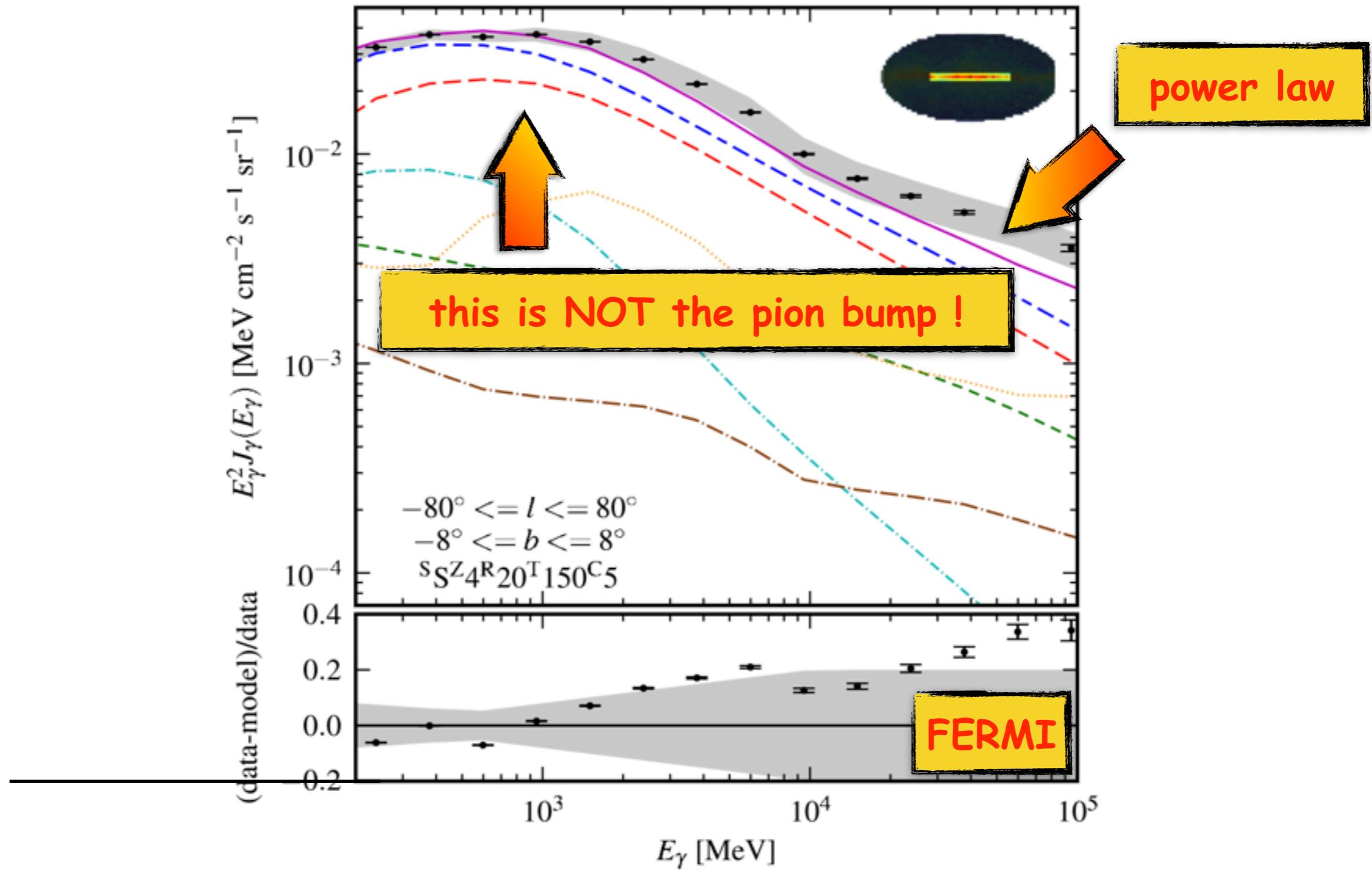
Diffuse emission from the inner Galaxy



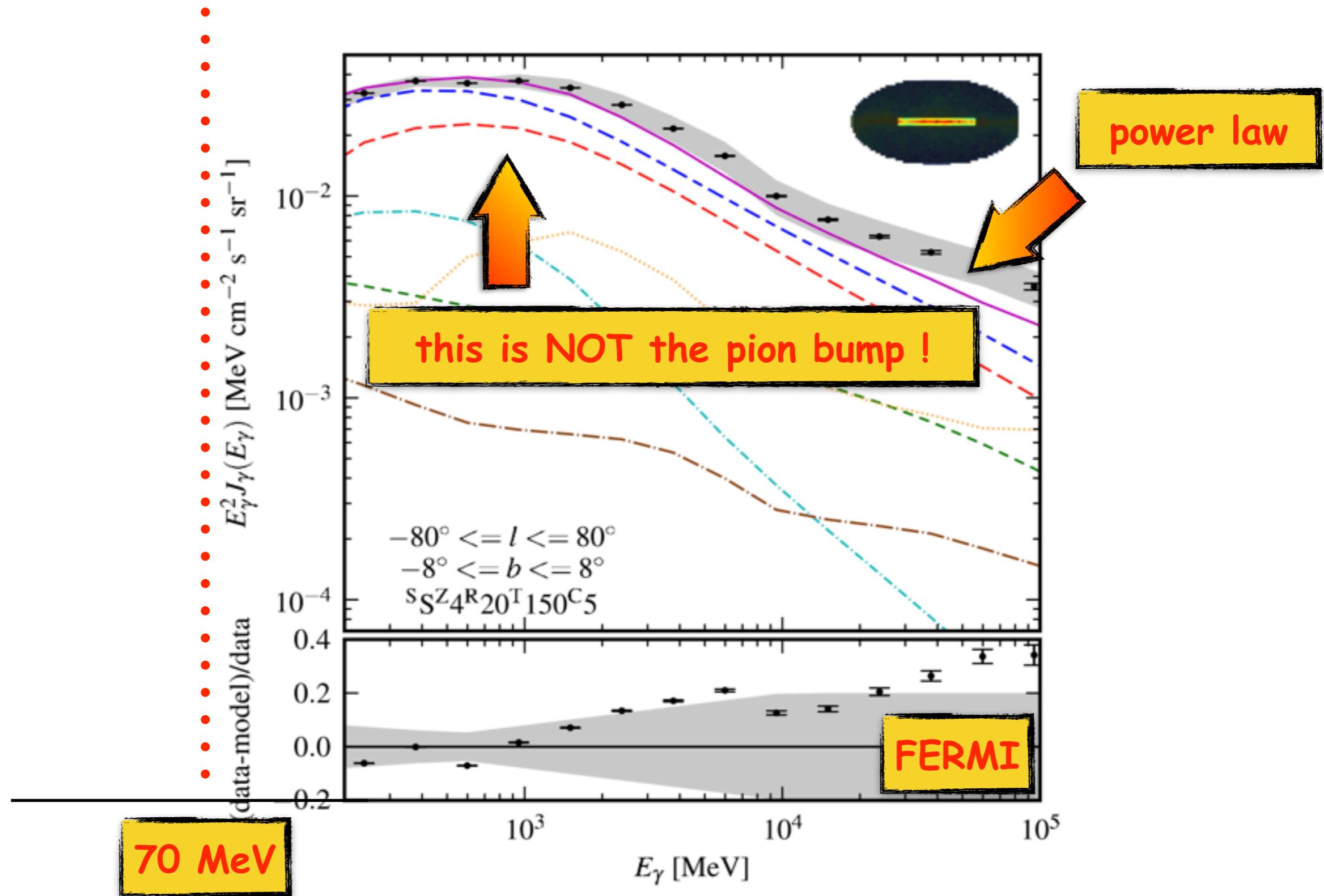
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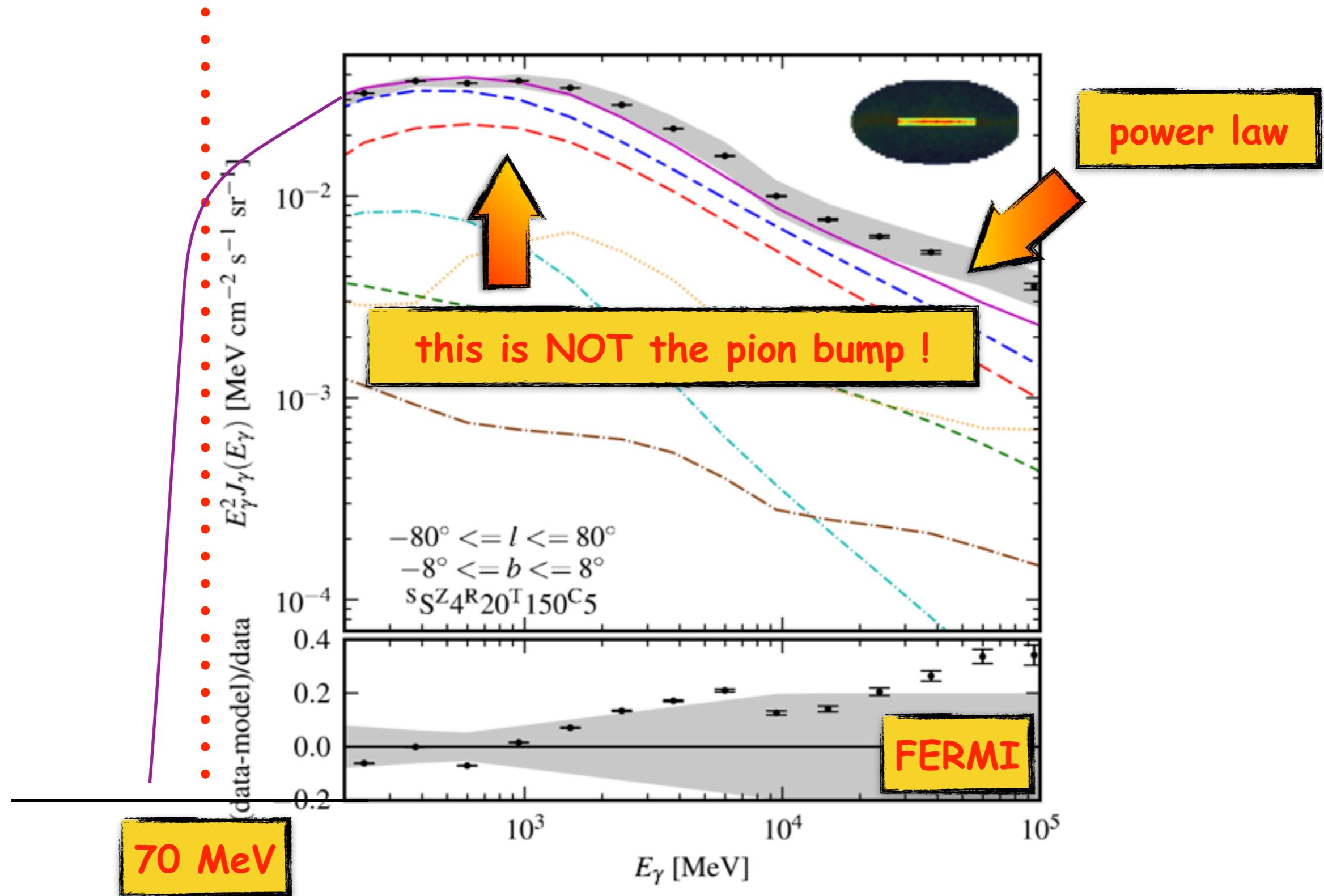
Diffuse emission from the inner Galaxy



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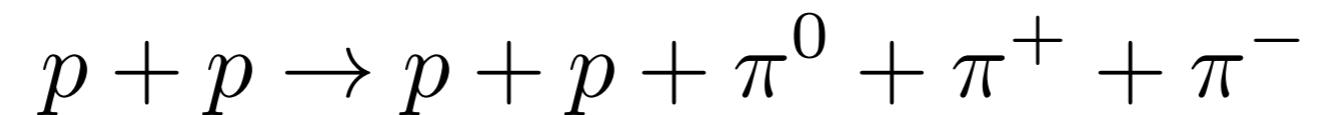


Diffuse emission from the inner Galaxy



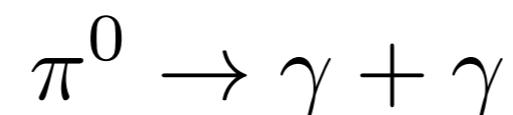
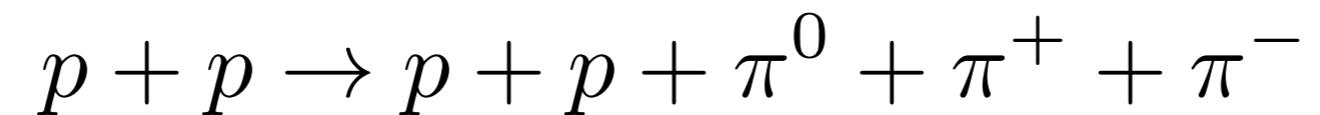
Not only gammas: neutrinos & electrons

Neutrinos/antineutrinos & electrons/positrons are also produced in pp interactions



Not only gammas: neutrinos & electrons

Neutrinos/antineutrinos & electrons/positrons are also produced in pp interactions



Not only gammas: neutrinos & electrons

Neutrinos/antineutrinos & electrons/positrons are also produced in pp interactions

$$p + p \rightarrow p + p + \pi^0 + \pi^+ + \pi^-$$

$$\pi^0 \rightarrow \gamma + \gamma$$

$$\left\{ \begin{array}{l} \pi^\pm \rightarrow \mu^\pm + \nu_\mu (\bar{\nu}_\mu) \\ \mu^\pm \rightarrow e^\pm + \bar{\nu}_\mu (\nu_\mu) + \nu_e (\bar{\nu}_e) \end{array} \right.$$

Not only gammas: neutrinos & electrons

Neutrinos/antineutrinos & electrons/positrons are also produced in pp interactions

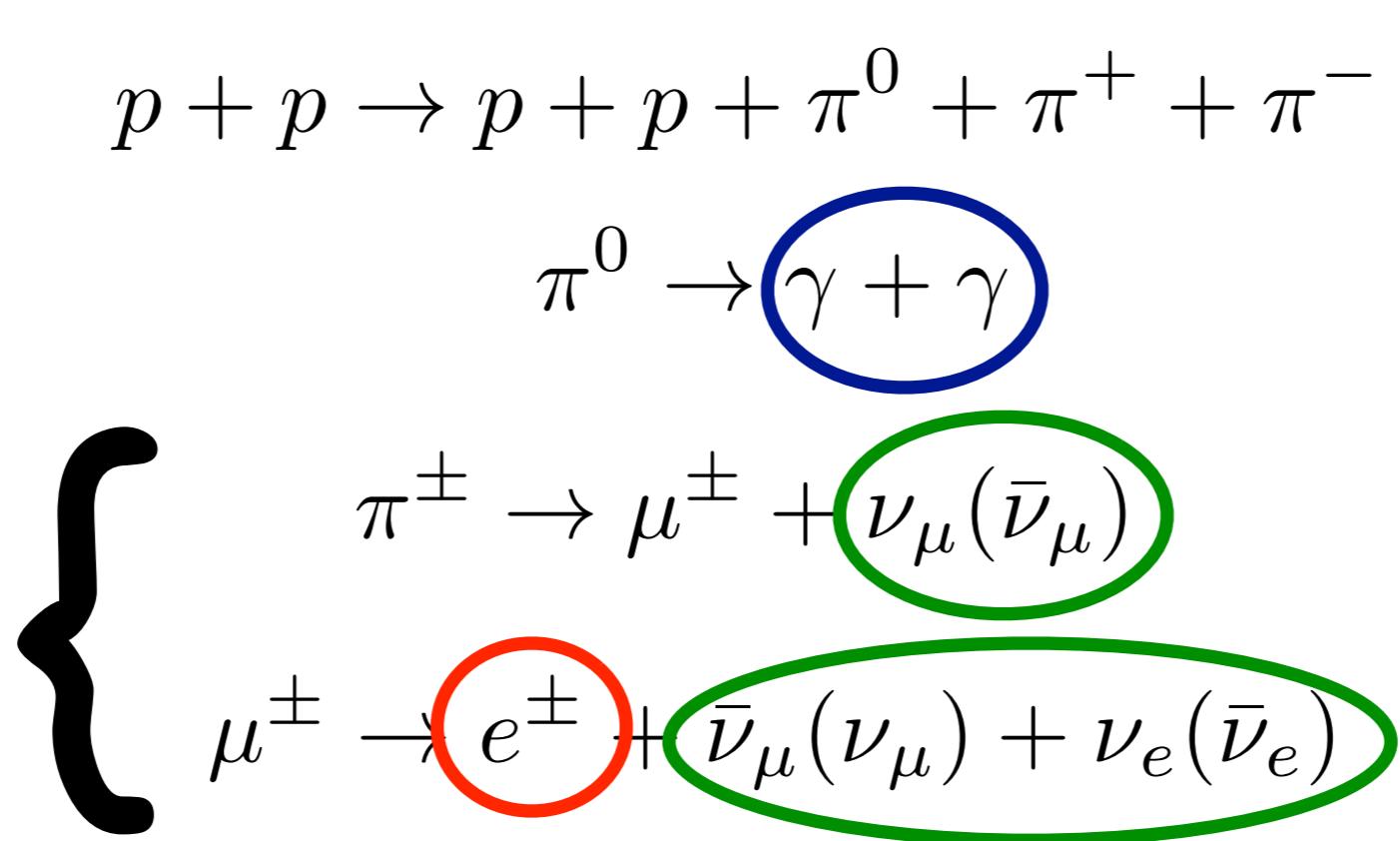
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Final products of proton-proton interactions are not only **gamma ray photons** but also **neutrinos, anti-neutrinos, electrons and positrons**

$$E_e \approx E_\nu \approx \frac{E_p}{20}$$

Not only gammas: neutrinos & electrons

Neutrinos/antineutrinos & electrons/positrons are also produced in pp interactions



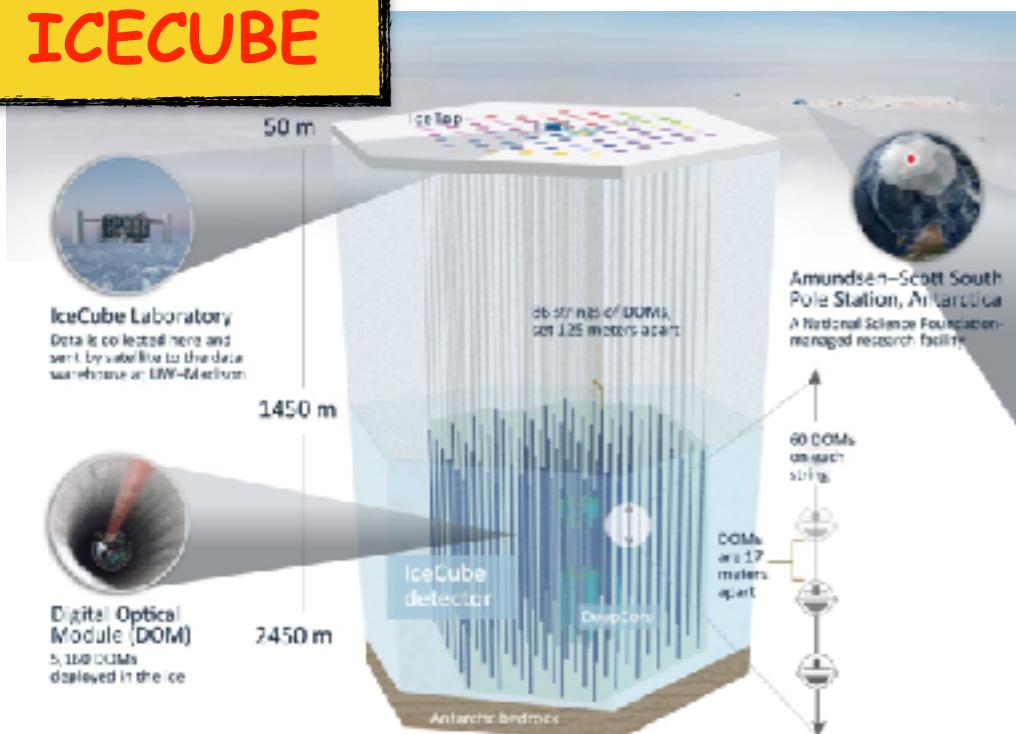
neutral and charged
pions produced with the
same probability
(1/3,1/3,1/3)

Final products of proton-proton interactions are not only **gamma ray photons** but
also **neutrinos, anti-neutrinos, electrons and positrons**

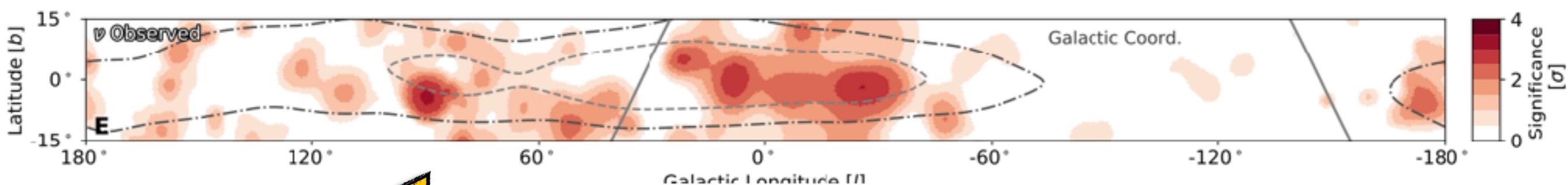
$$E_e \approx E_\nu \approx \frac{E_p}{20}$$

Neutrino telescopes

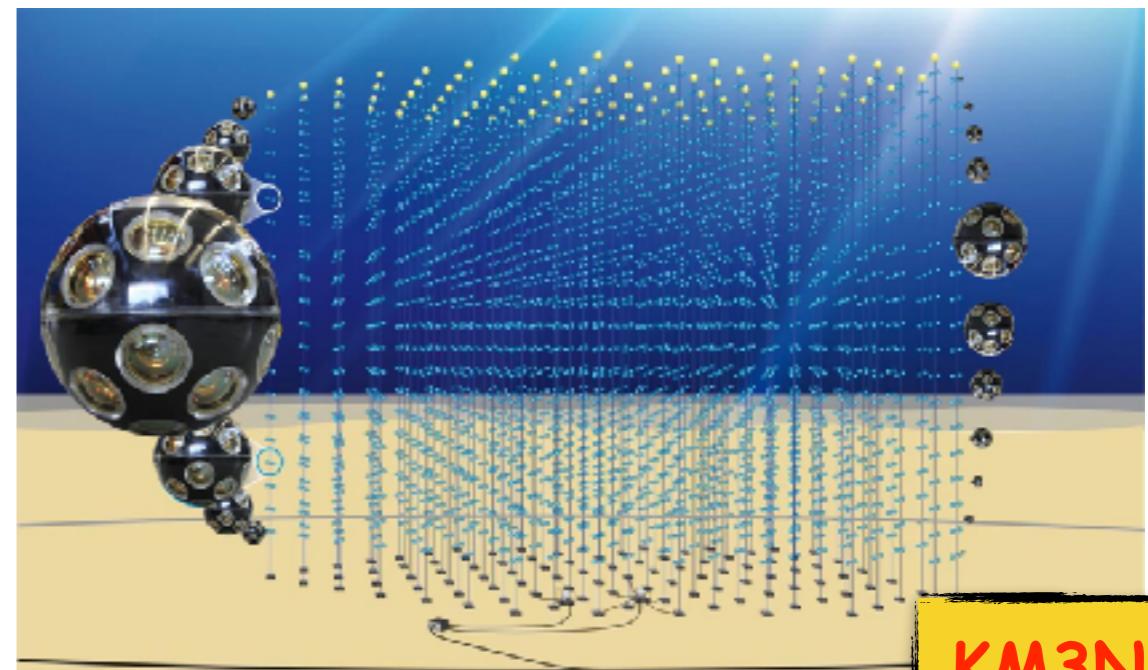
ICECUBE



Baikal



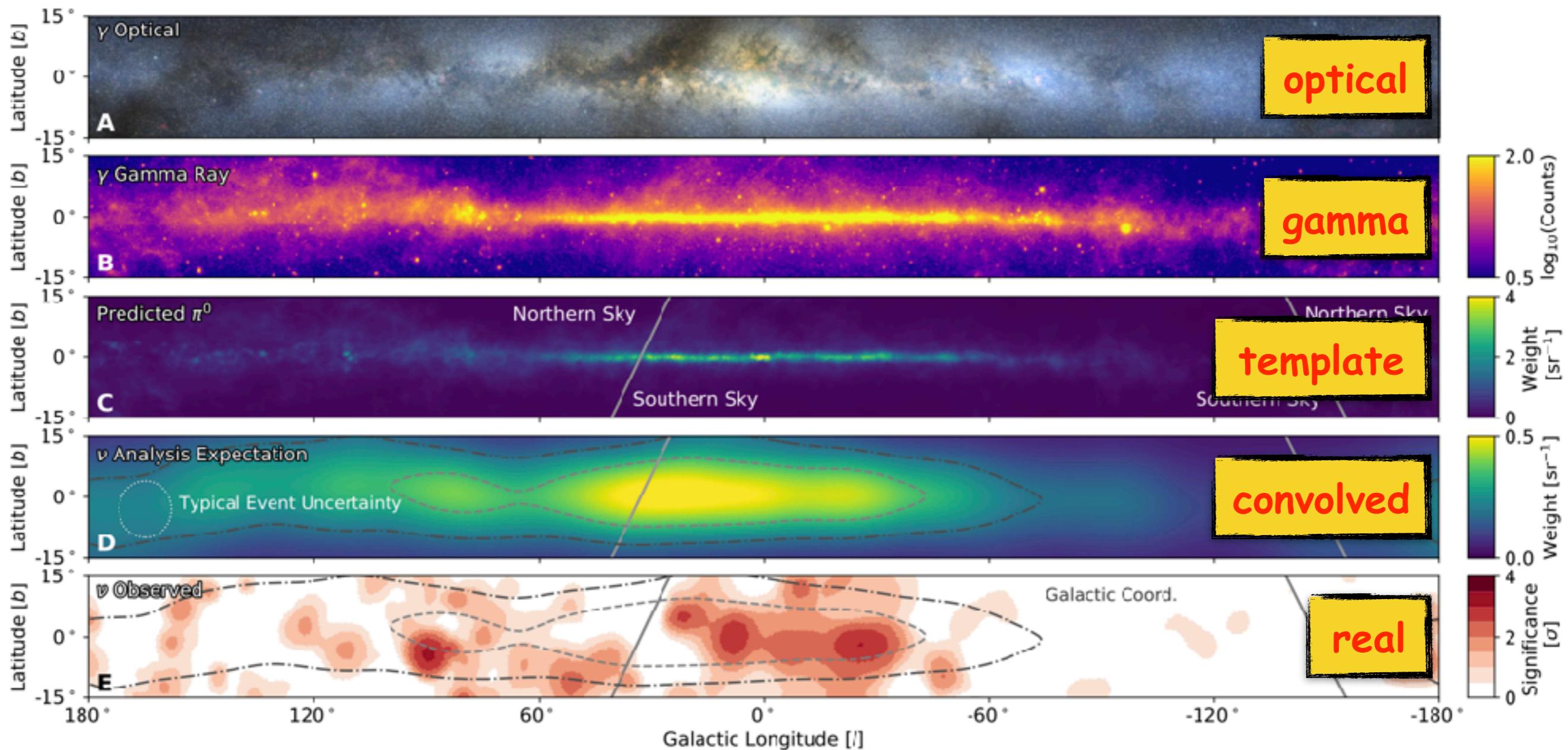
diffuse emission
from Galactic plane!



KM3NeT

The gamma-neutrino connection

a neutrino signal from the disk is unavoidable !



Simple order-of-magnitude calculations

gamma rays

valid at large energies

number of protons of
energy E_p produced per s

$$Q_p(E_p)$$


Simple order-of-magnitude calculations

gamma rays

valid at large energies

number of protons of
energy E_p produced per s

$$Q_p(E_p) E_p^2$$

A red bracket underlines the term E_p^2 , and a red arrow points from the text "power (energy per unit time)" to this bracket.

power (energy
per unit time)

Simple order-of-magnitude calculations

gamma rays

valid at large energies

fraction of the
energy converted
into pions...

number of protons of
energy E_p produced per s

$$\eta_\pi Q_p(E_p) E_p^2$$

power (energy
per unit time)

Simple order-of-magnitude calculations

gamma rays

valid at large energies

fraction of the
energy converted
into pions...

number of protons of
energy E_p produced per s

$$\eta_\pi Q_p(E_p) E_p^2$$

power (energy
per unit time)

$$\eta_\pi = 1 - e^{-\left(\frac{\tau_{res}}{\tau_{pp}}\right)} \rightarrow \frac{\tau_{res}}{\tau_{pp}} \quad \tau_{pp} \gg \tau_{res}$$
$$\rightarrow 1 \quad \tau_{pp} \ll \tau_{res}$$

Simple order-of-magnitude calculations

gamma rays

valid at large energies

$$f_\gamma \eta_\pi Q_p(E_p) E_p^2$$

fraction of the energy converted into pions...

...and into gamma rays ($1/3 \rightarrow \pi^0$)

number of protons of energy E_p produced per s

power (energy per unit time)

A diagram illustrating the components of the formula. A bracket is placed under the term $Q_p(E_p) E_p^2$. Red arrows point from the text "number of protons of energy E_p produced per s" and "power (energy per unit time)" to this bracketed term. Another red arrow points from the text "...and into gamma rays ($1/3 \rightarrow \pi^0$)" to the term $f_\gamma \eta_\pi$.

$$\eta_\pi = 1 - e^{-\left(\frac{\tau_{res}}{\tau_{pp}}\right)} \longrightarrow \frac{\tau_{res}}{\tau_{pp}} \quad \tau_{pp} \gg \tau_{res}$$
$$\longrightarrow 1 \quad \tau_{pp} \ll \tau_{res}$$

Simple order-of-magnitude calculations

gamma rays

valid at large energies

$$Q_\gamma(E_\gamma)E_\gamma^2 = f_\gamma \eta_\pi Q_p(E_p)E_p^2$$

emitted power in gamma rays

fraction of the energy converted into pions...

number of protons of energy E_p produced per s

...and into gamma rays ($1/3 \rightarrow \pi^0$)

power (energy per unit time)

$$\eta_\pi = 1 - e^{-\left(\frac{\tau_{res}}{\tau_{pp}}\right)} \rightarrow \frac{\tau_{res}}{\tau_{pp}} \quad \tau_{pp} \gg \tau_{res}$$
$$\rightarrow 1 \quad \tau_{pp} \ll \tau_{res}$$

Simple order-of-magnitude calculations

gamma rays

valid at large energies

$$Q_\gamma(E_\gamma)E_\gamma^2 = f_\gamma \eta_\pi Q_p(E_p)E_p^2$$

emitted power in gamma rays

fraction of the energy converted into pions...

number of protons of energy E_p produced per s

$E_\gamma \sim E_p/10$

...and into gamma rays ($1/3 \rightarrow \pi^0$)

power (energy per unit time)

The diagram illustrates the calculation of emitted power in gamma rays. It starts with the equation $Q_\gamma(E_\gamma)E_\gamma^2 = f_\gamma \eta_\pi Q_p(E_p)E_p^2$. Red arrows point from various parts of the equation to explanatory text: one arrow from $Q_\gamma(E_\gamma)E_\gamma^2$ points to 'emitted power in gamma rays'; another from $f_\gamma \eta_\pi$ points to 'fraction of the energy converted into pions...'; a third from $Q_p(E_p)E_p^2$ points to 'number of protons of energy E_p produced per s'. A horizontal red arrow below the equation points from E_γ to $E_p/10$, with the text ' $E_\gamma \sim E_p/10$ ' written below it. Another red arrow points from E_p to the text '...and into gamma rays ($1/3 \rightarrow \pi^0$)'. A final red arrow points from E_p^2 to the text 'power (energy per unit time)'.

$$\eta_\pi = 1 - e^{-\left(\frac{\tau_{res}}{\tau_{pp}}\right)} \rightarrow \frac{\tau_{res}}{\tau_{pp}} \quad \tau_{pp} \gg \tau_{res}$$

$$\rightarrow 1 \quad \tau_{pp} \ll \tau_{res}$$

Simple order-of-magnitude calculations

neutrinos

valid at large energies

The same as for gammas but:

$$\rightarrow f_\gamma \longrightarrow f_\nu = \frac{2}{3} \times \frac{3}{4} \times \frac{1}{3}$$

↑ ↑ ↑
fraction of fraction of per flavour (after
charged pions pion energy -> oscillations)

$$\rightarrow E_\gamma \longrightarrow E_\nu \sim 0.05 \times E_p$$

Simple order-of-magnitude calculations

valid at large energies

gamma rays

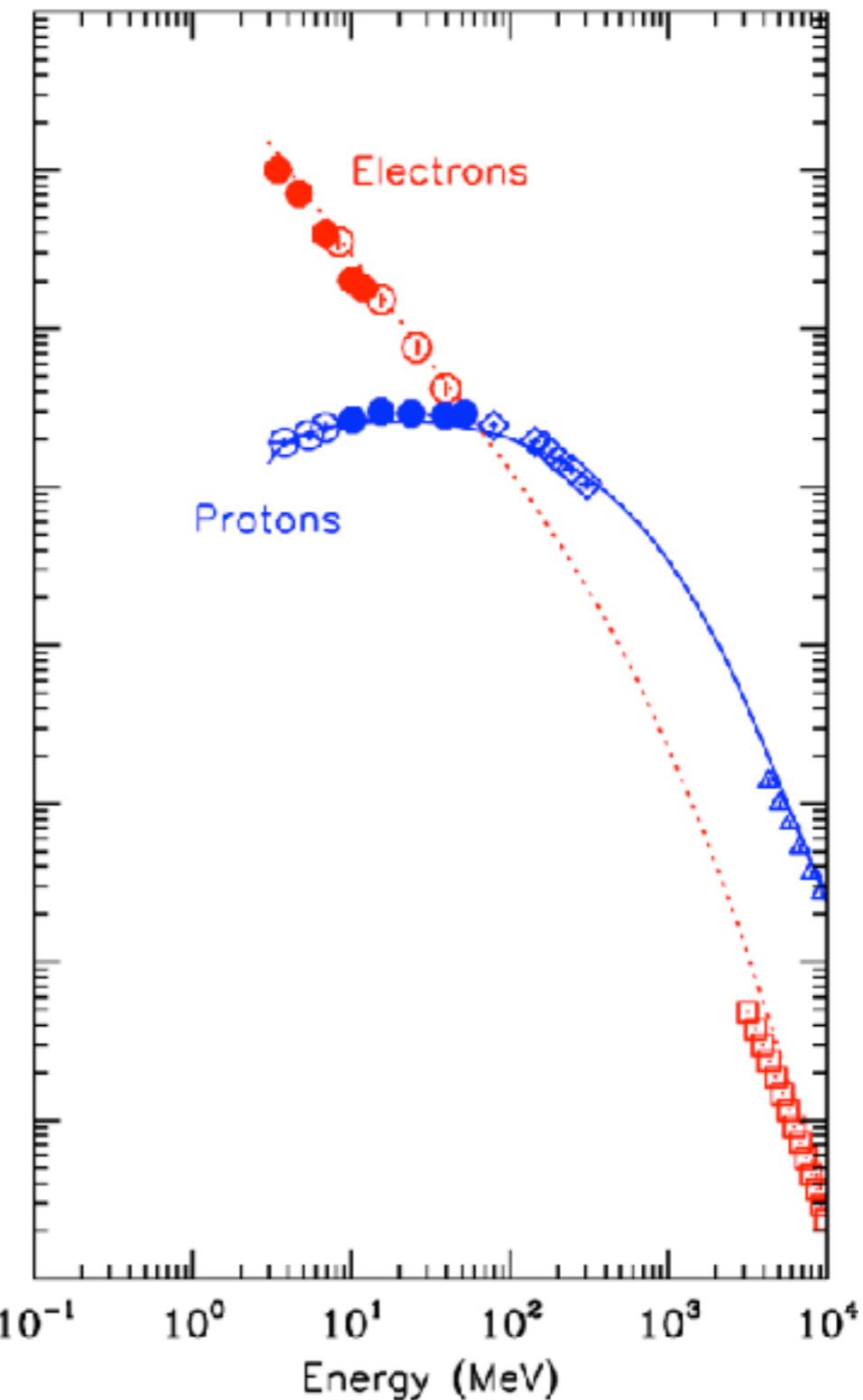
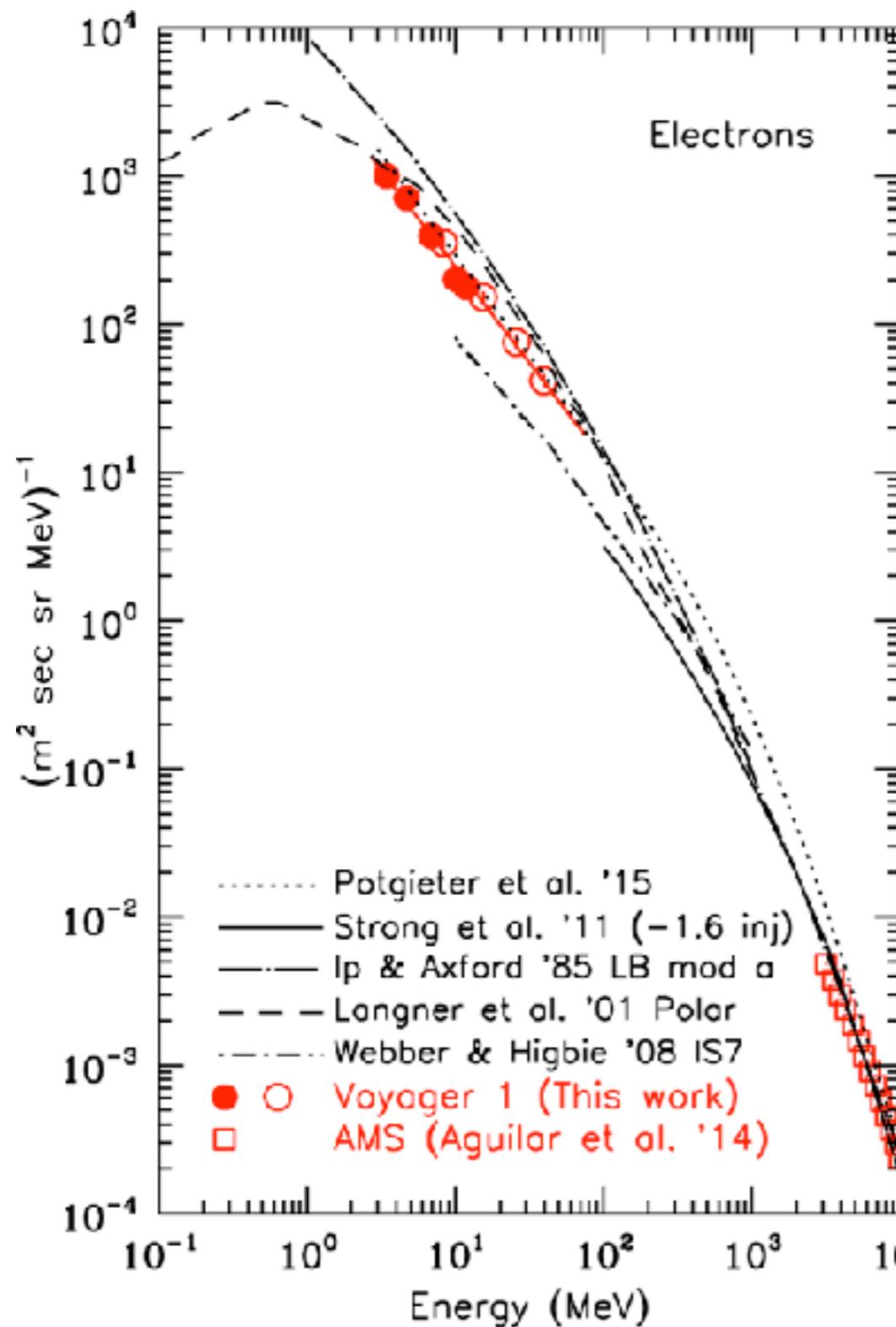
$$Q_\gamma(E_\gamma)E_\gamma^2 = \frac{\eta_\pi}{3}Q_p(E_p)E_p^2$$

neutrinos
(per flavour)

$$Q_\nu(E_\nu)E_\nu^2 = \frac{1}{2}Q_\gamma(E_\gamma)E_\gamma^2$$

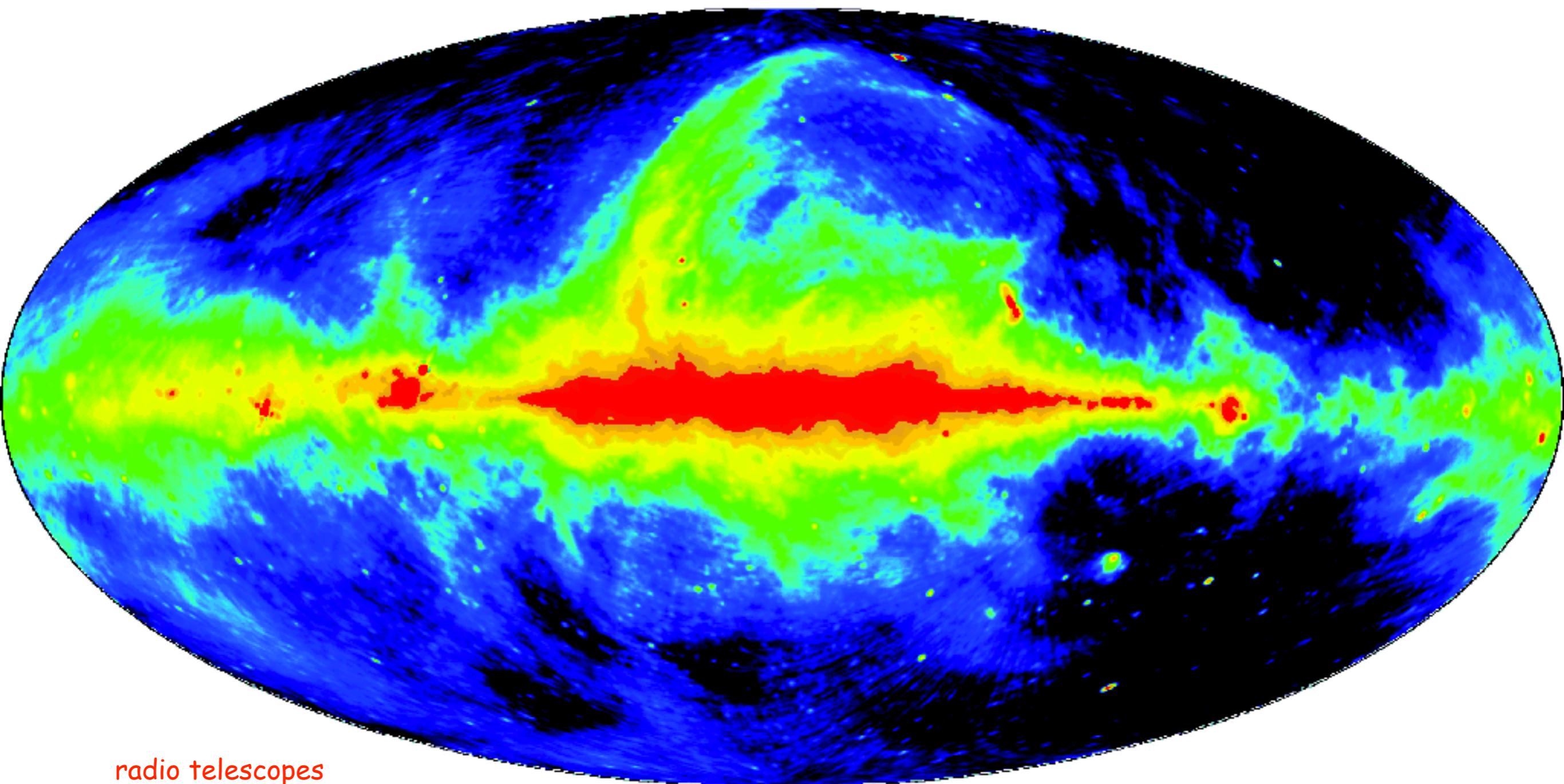
What about electrons?

false myths: the proton-to-electron ratio is ~ 100 in Galactic cosmic rays



Synchrotron emission from the Milky Way

radio domain → 408 MHz



radio telescopes

Jodrell-Bank 250-ft + Effelsberg 100-m + Parkes 64-m

Synchrotron emission from the Milky Way

radio domain → 408 MHz

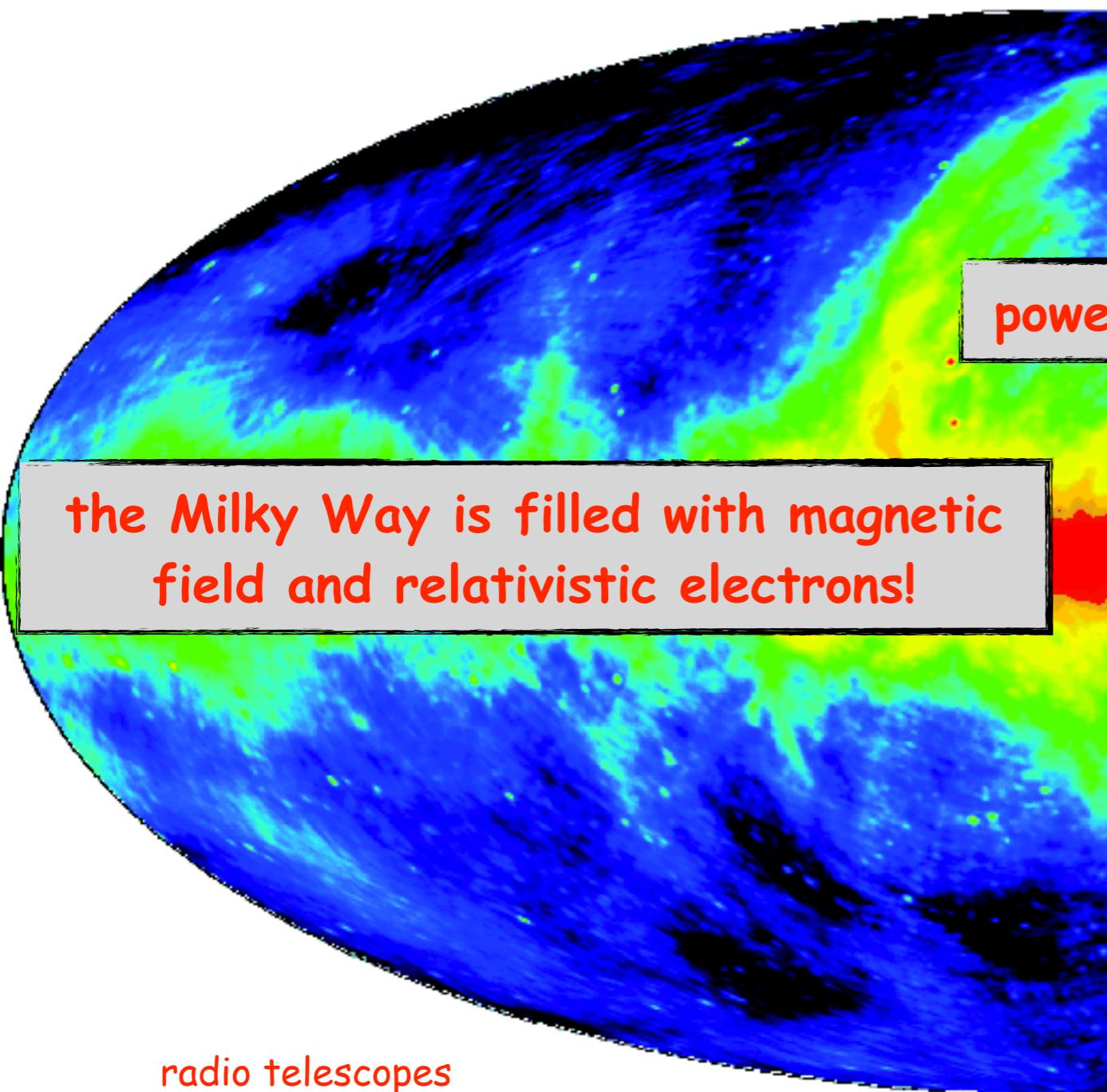
the Milky Way is filled with magnetic field and relativistic electrons!

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Jodrell-Bank 250-ft + Effelsberg 100-m + Parkes 64-m

Synchrotron emission from the Milky Way

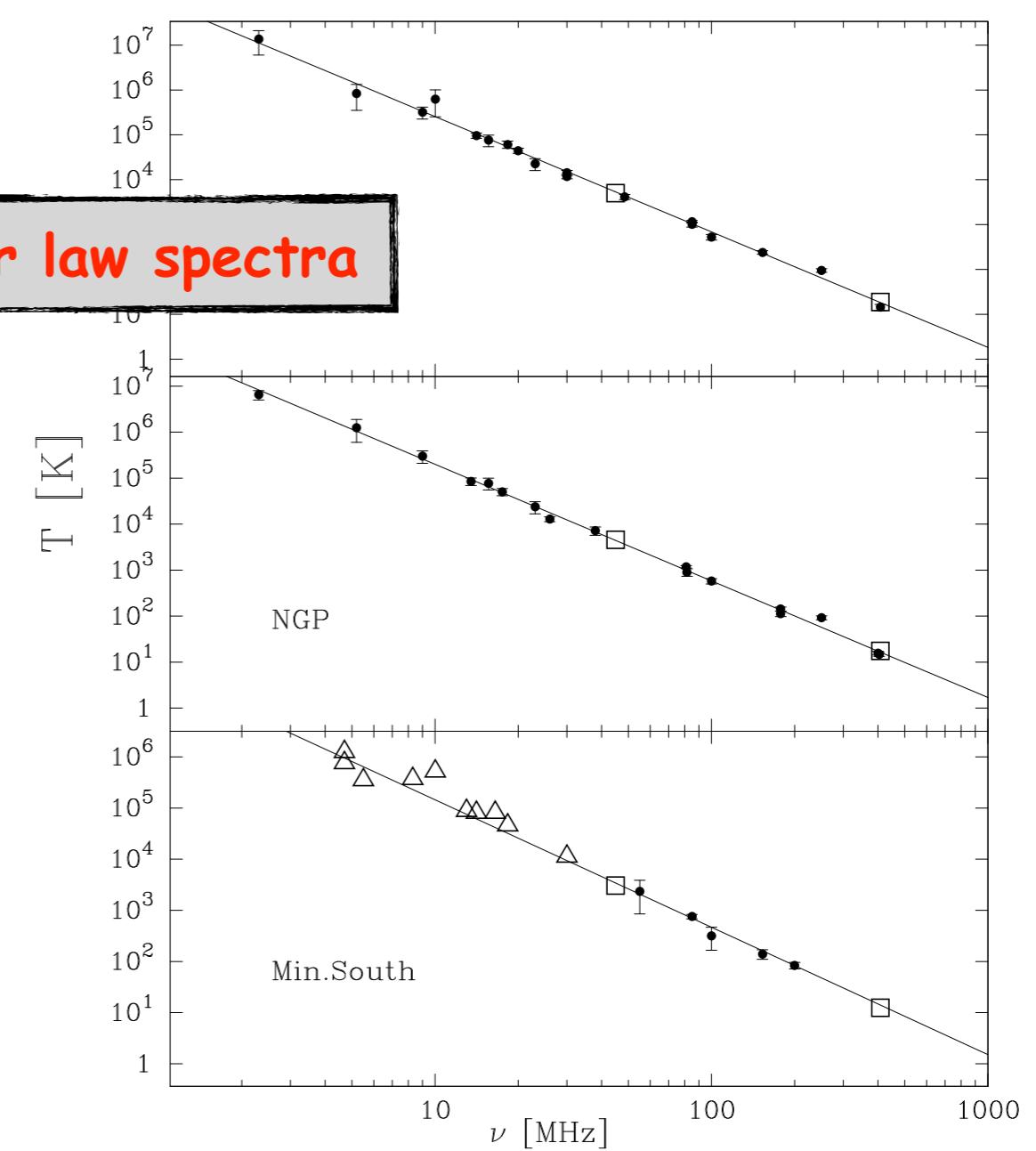
radio domain → 408 MHz



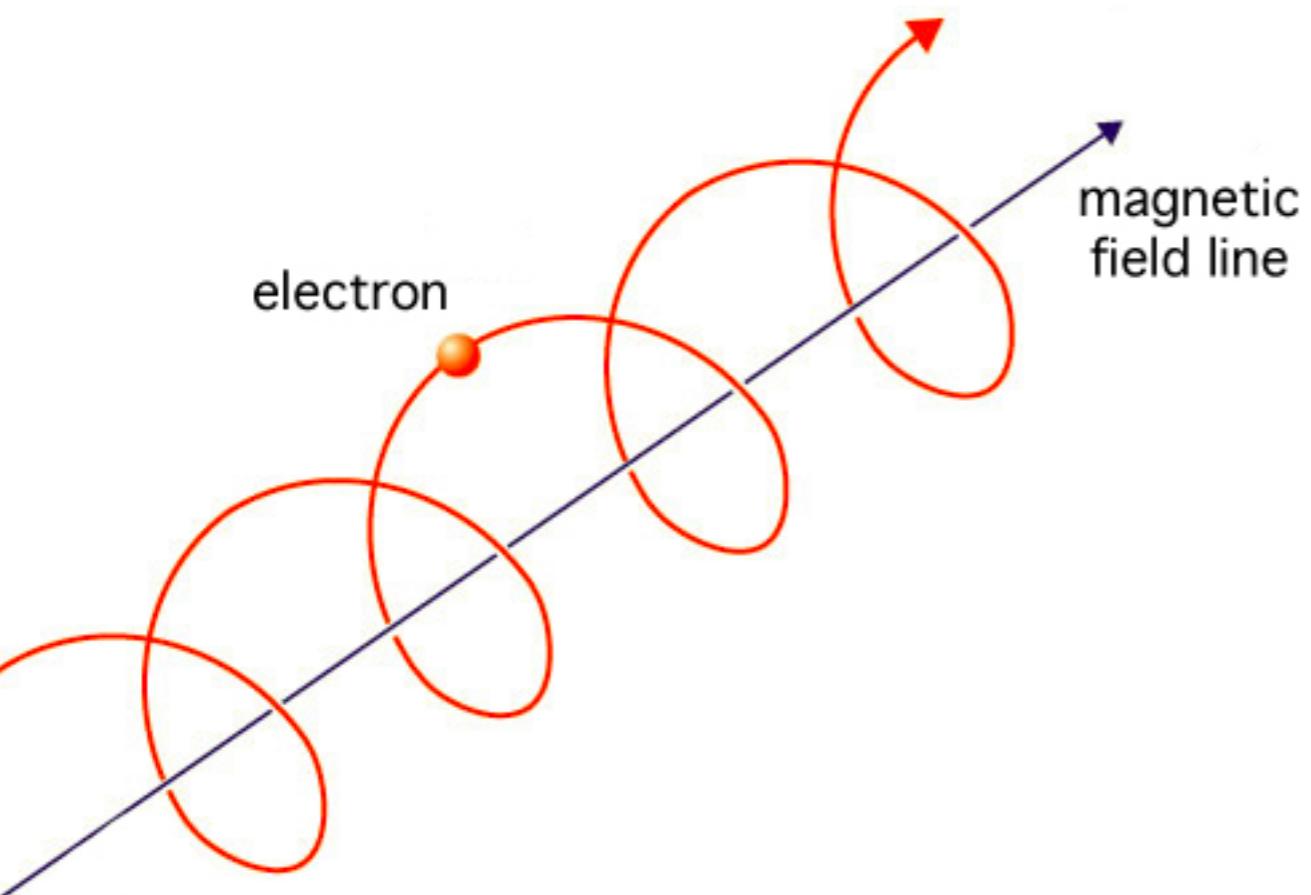
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Motion of a particle in a magnetic field

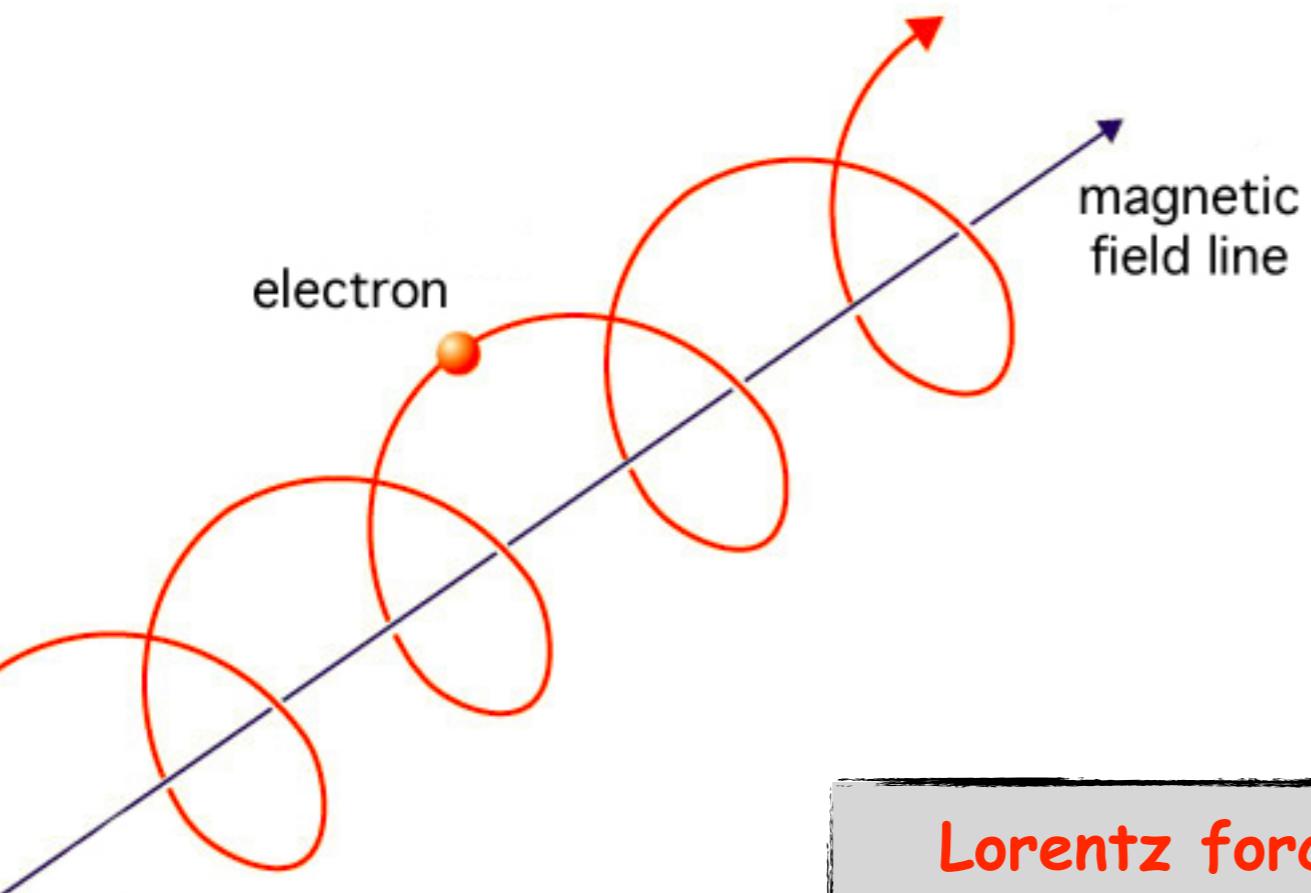


$$\mu = \cos \vartheta$$

pitch angle = angle between v and B

$$\begin{cases} v_{\parallel} &= \mu v \\ v_{\perp} &= (1 - \mu^2)^{1/2}v \end{cases}$$

Motion of a particle in a magnetic field



$$\mu = \cos \vartheta$$

pitch angle = angle between v and B

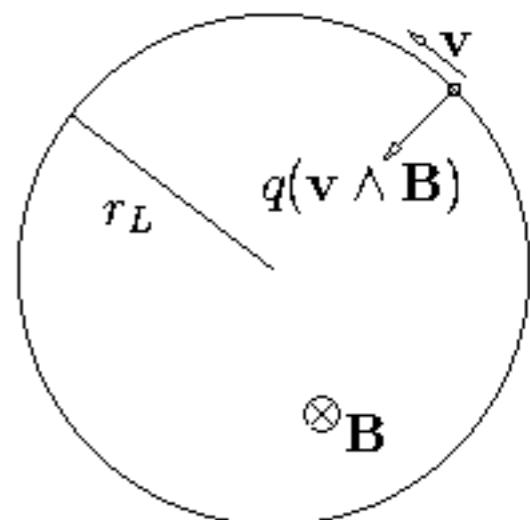
$$\begin{cases} v_{\parallel} &= \mu v \\ v_{\perp} &= (1 - \mu^2)^{1/2}v \end{cases}$$

Lorentz force

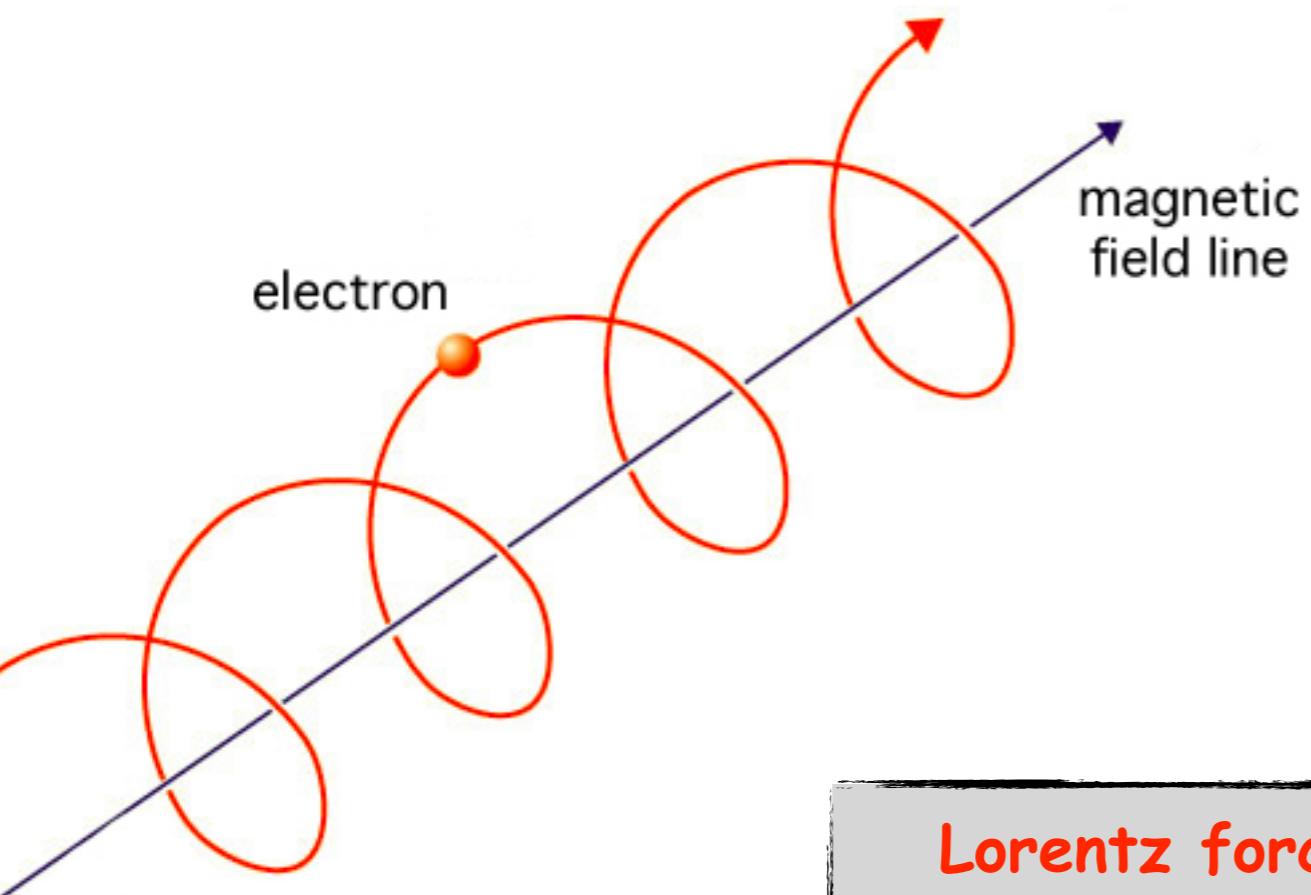
$$F_L = \frac{q}{c} \vec{v} \times \vec{B}$$

Larmor radius

$$R_L = \frac{p_{\perp} c}{q B}$$



Motion of a particle in a magnetic field



$$\mu = \cos \vartheta$$

pitch angle = angle between v and B

$$\begin{cases} v_{\parallel} &= \mu v \\ v_{\perp} &= (1 - \mu^2)^{1/2}v \end{cases}$$

Lorentz force

$$F_L = \frac{q}{c} \vec{v} \times \vec{B}$$

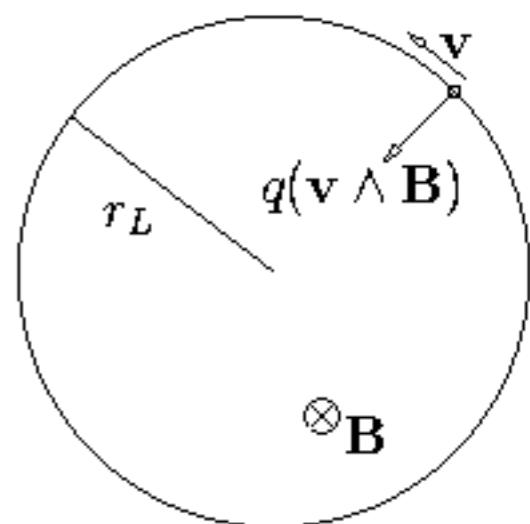
Larmor radius

$$R_L = \frac{p_{\perp} c}{q B}$$

gyration frequency

$$\nu_B = \frac{1}{t_g} = \frac{v_{\perp}}{2\pi R_L} = \frac{qB}{2\pi\gamma mc}$$

Lorentz factor



Power emitted by an electron*

non-relativistic

$$P = \frac{2e^2}{3c^3} a^2 \longrightarrow P = \frac{2e^2}{3c^3} \gamma^4 \left[\gamma^2 a_{\parallel}^2 + a_{\perp}^2 \right]$$

relativistic

* implicit assumption: the energy of the electron does not change during one gyration around the B-field

Power emitted by an electron*

non-relativistic

$$P = \frac{2e^2}{3c^3} a^2$$

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relativistic

Lorentz force is orthogonal to v

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Power emitted by an electron*

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$$P = \frac{2e^2}{3c^3} a^2$$



$$P = \frac{2e^2}{3c^3} \gamma^4 \left[\gamma^2 a_{\parallel}^2 + a_{\perp}^2 \right]$$

relativistic

Lorentz force is orthogonal to v

$$F_L = F_{L,\perp} = \frac{ev_{\perp}B}{c} \equiv \gamma m \frac{dv_{\perp}}{dt} \rightarrow a_{\perp} = \frac{ev_{\perp}B}{\gamma mc}$$

* implicit assumption: the energy of the electron does not change during one gyration around the B-field

Power emitted by an electron*

non-relativistic

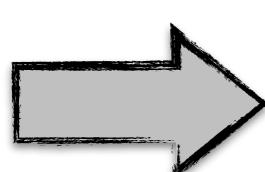
$$P = \frac{2e^2}{3c^3} a^2$$

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relativistic

Lorentz force is orthogonal to v

$$F_L = F_{L,\perp} = \frac{ev_{\perp}B}{c} \equiv \gamma m \frac{dv_{\perp}}{dt} \rightarrow a_{\perp} = \frac{ev_{\perp}B}{\gamma mc}$$



$$P = \frac{4}{3} \sigma_T c U_B \gamma^2$$

■ Thomson cross section

$$\sigma_T = \frac{8\pi}{3} \left(\frac{e^2}{mc^2} \right)^2 = 6.65 \times 10^{-25} \text{ cm}^2$$

■ magnetic field energy density $U_B = B^2/8\pi$

■ ultra relativistic electrons $\beta \rightarrow 1$

■ isotropic distribution of particles $\langle \sin^2 \vartheta \rangle = 2/3$

* implicit assumption: the energy of the electron does not change during one gyration around the B-field

Power emitted by an electron*

non-relativistic

$$P = \frac{2e^2}{3c^3} a^2$$

$$P = \frac{2e^2}{3c^3} \gamma^4 \left[\gamma^2 a_{\parallel}^2 + a_{\perp}^2 \right]$$

relativistic

Lorentz force is orthogonal to v

$$F_L = F_{L,\perp} = \frac{ev_{\perp}B}{c} \equiv \gamma m \frac{dv_{\perp}}{dt} \rightarrow a_{\perp} = \frac{ev_{\perp}B}{\gamma mc}$$



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* implicit assumption: the energy of the electron does not change during one gyration around the B-field

Characteristic frequency

as done for Bremsstrahlung: characteristic time ----> characteristic frequency

gyration frequency?

$$\nu_B = \frac{1}{t_g} = \frac{v_{\perp}}{2\pi R_L} = \frac{qB}{2\pi\gamma mc}$$

Characteristic frequency

as done for Bremsstrahlung: characteristic time ----> characteristic frequency

gyration frequency?

$$\nu_B = \frac{1}{t_g} = \frac{v_{\perp}}{2\pi R_L} = \cancel{\frac{qB}{2\pi c}}$$

Beaming

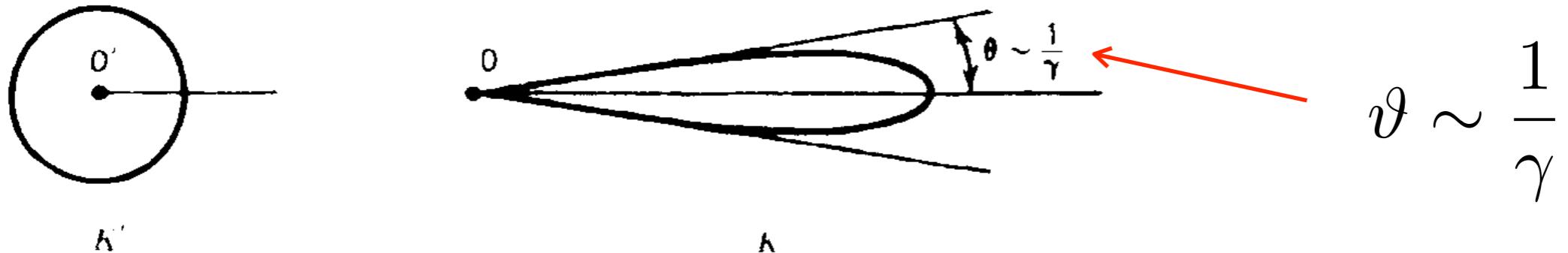


Figure 4.3 Relativistic beaming of radiation emitted isotropically in the rest frame K' .

the radiation emitted by a relativistic particle is concentrated within a cone of opening angle $1/\gamma$ entered along the particle velocity

Characteristic frequency

as done for Bremsstrahlung: characteristic time \longrightarrow characteristic frequency

gyration frequency?

$$\nu_B = \frac{1}{t_g} = \frac{v_{\perp}}{2\pi R_L} = \cancel{\frac{qP}{2\pi\gamma c}}$$

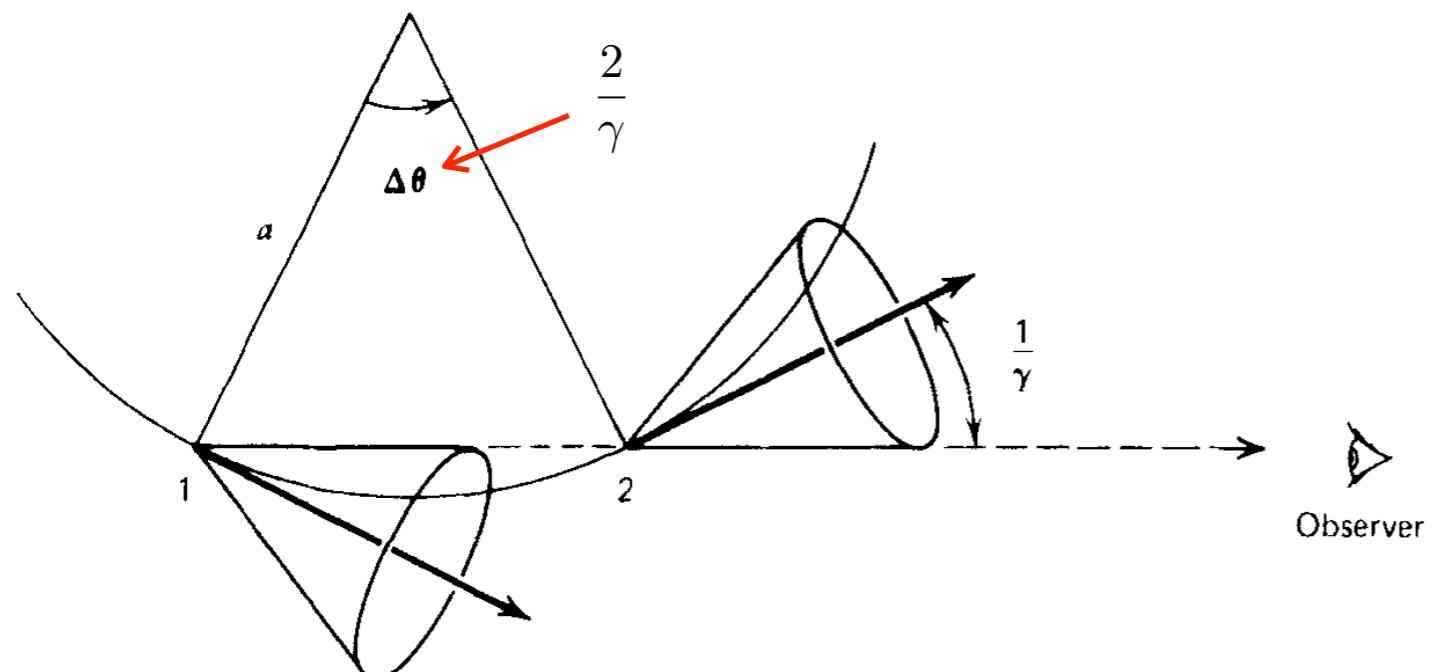


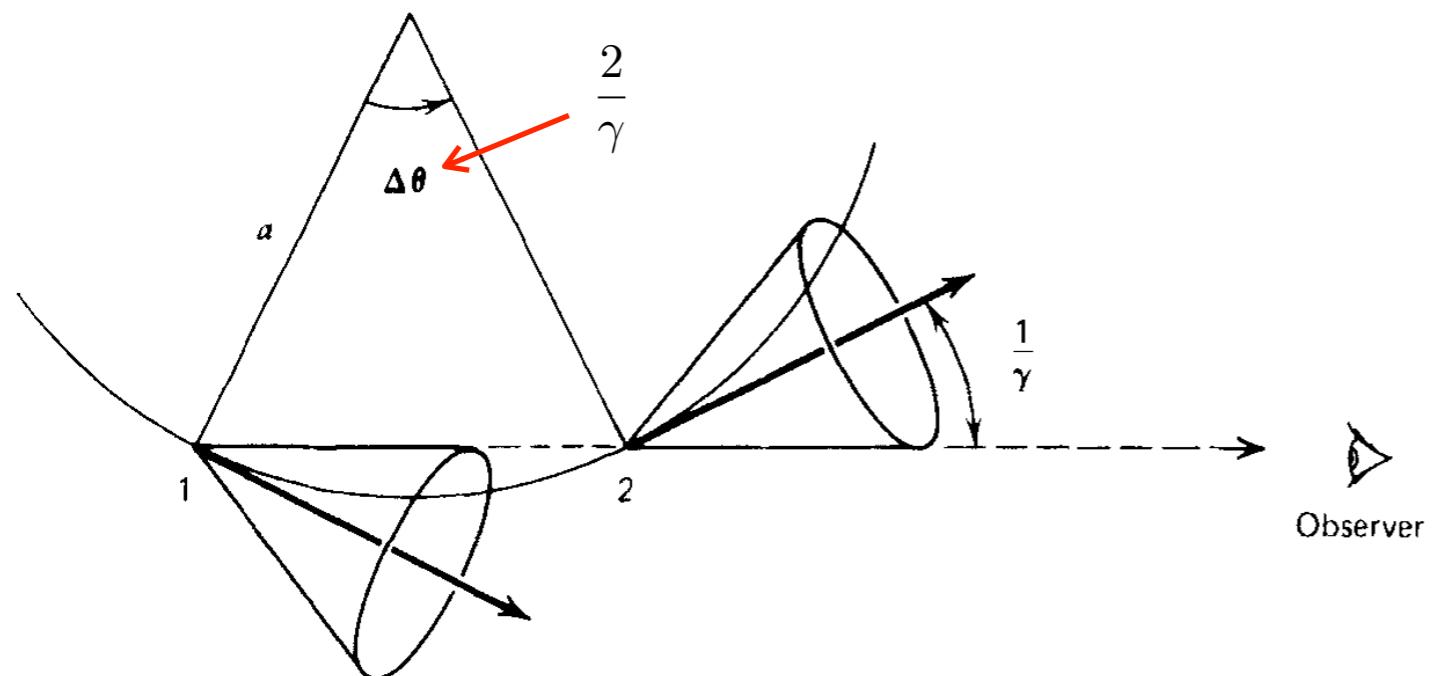
Figure 6.2 Emission cones at various points of an accelerated particle's trajectory.

Characteristic frequency

as done for Bremsstrahlung: characteristic time ----> characteristic frequency

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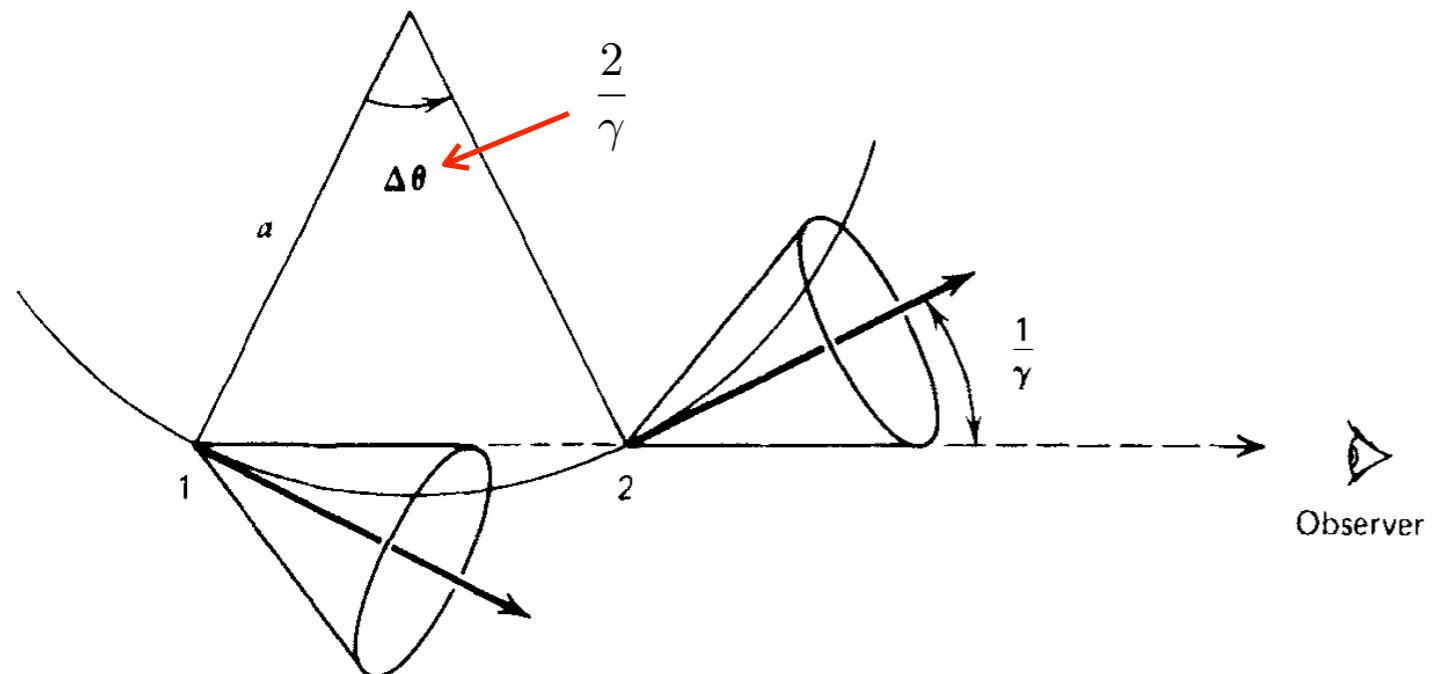
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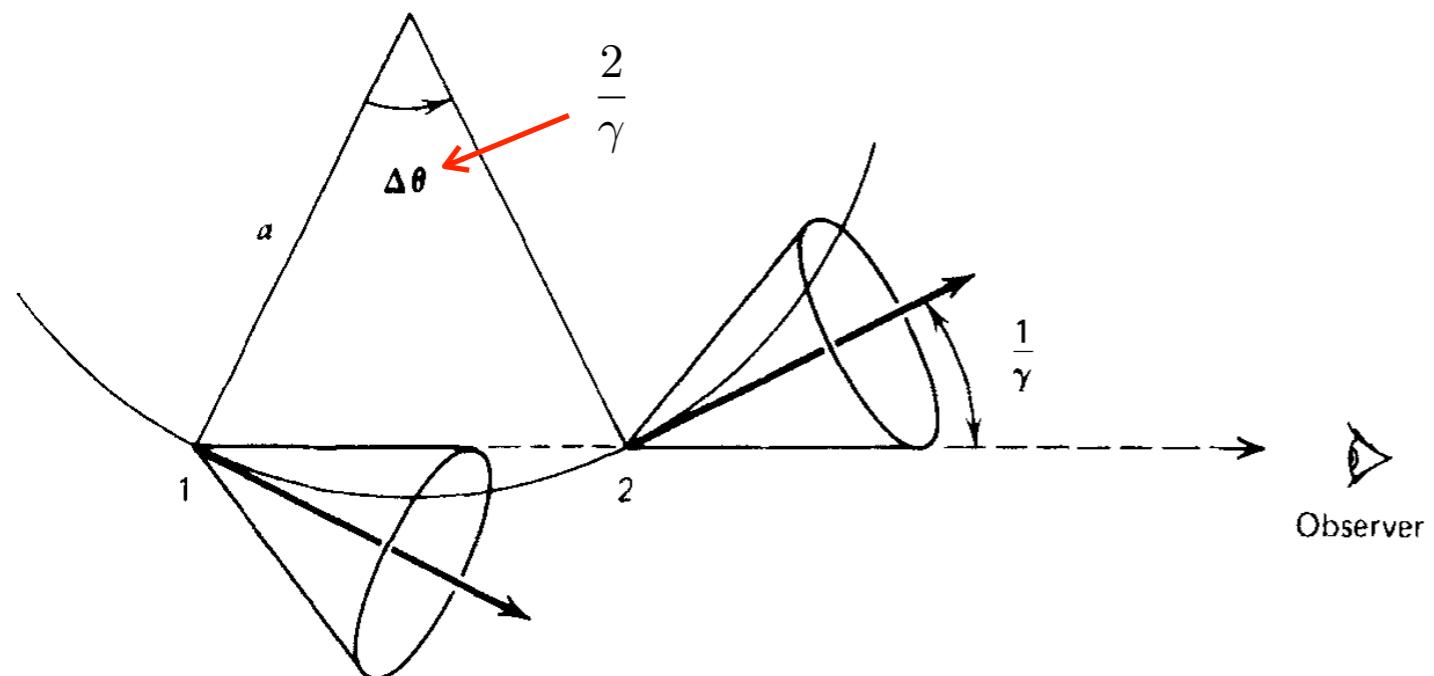
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$$\Delta t_a = \frac{c \Delta t_e - v_{\perp} \Delta t_e}{c} \approx \Delta t_e (1 - \beta) = \Delta t_e \frac{1 - \beta^2}{1 + \beta} \approx \frac{\Delta t_e}{2\gamma^2}$$

Emission from one and many electrons

duration of the
received pulse

$$\Delta t_a \approx \frac{\Delta t_e}{2\gamma^2} = \frac{1}{2\pi\gamma^3\nu_B} = \frac{1}{\gamma^2} \frac{mc}{qB}$$

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POWER LAW

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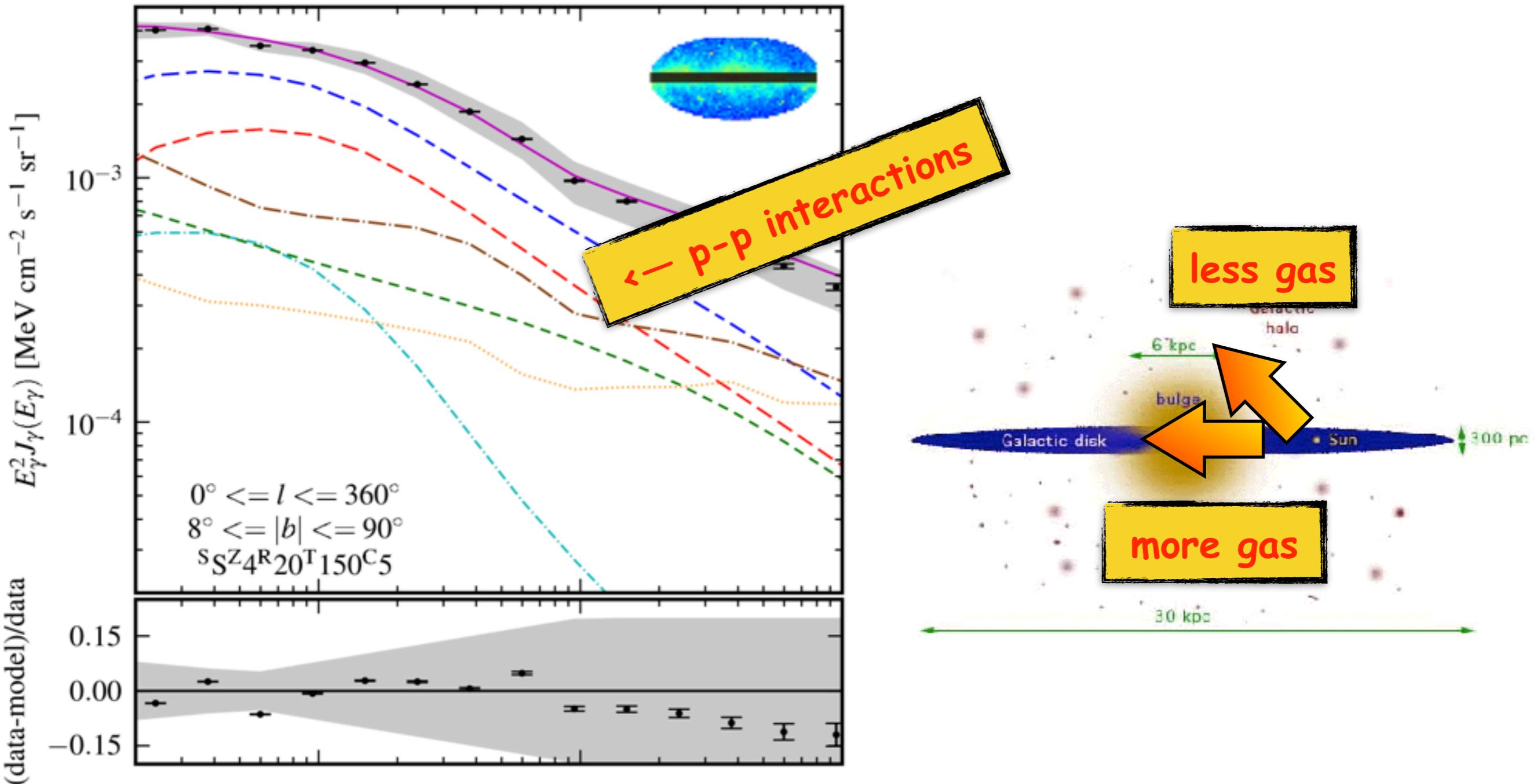
several ways to measure B exist, and they indicate $B \sim 3 \mu G$ in the Milky Way

$$\nu_s = \gamma^2 \frac{qB}{2\pi mc} \left\{ \begin{array}{l} E_e = 10 \text{ GeV} \rightarrow \nu_s \sim 3 \text{ GHz} \\ E_e = 100 \text{ TeV} \rightarrow \nu_s \sim 1 \text{ keV} \end{array} \right.$$

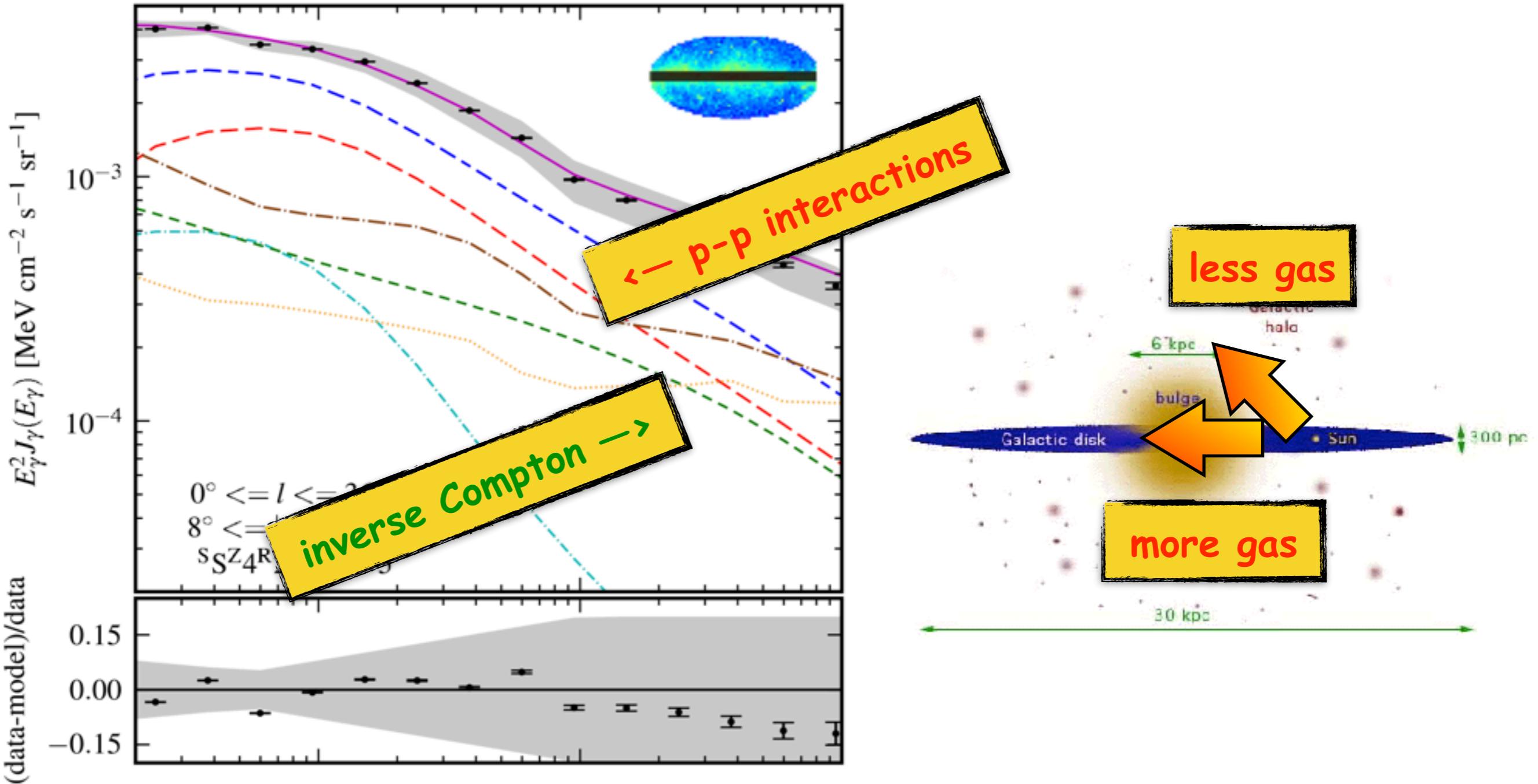
radio

X-rays

Diffuse emission, large Galactic latitudes

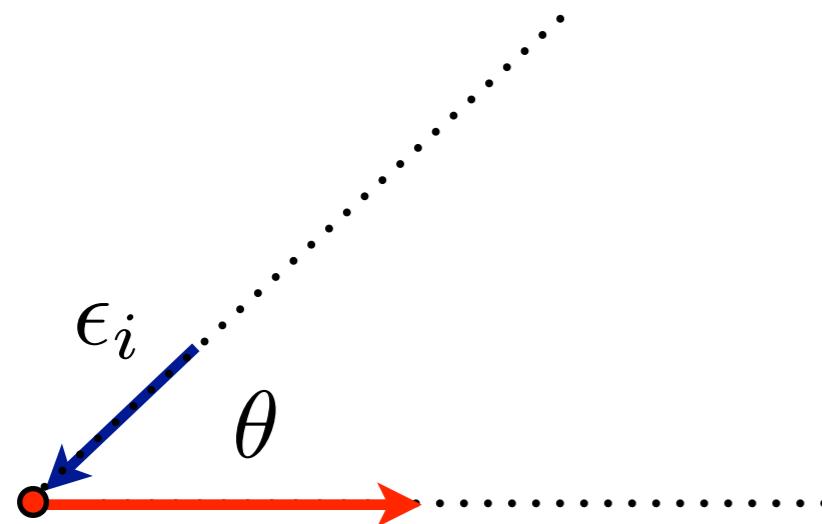


Diffuse emission, large Galactic latitudes



Leptonic Gamma-Rays: Inverse Compton

Relativistic **electrons** can interact with soft background photons
(Cosmic Microwave Background, IR and Optical galactic background...)



Leptonic Gamma-Rays: Inverse Compton

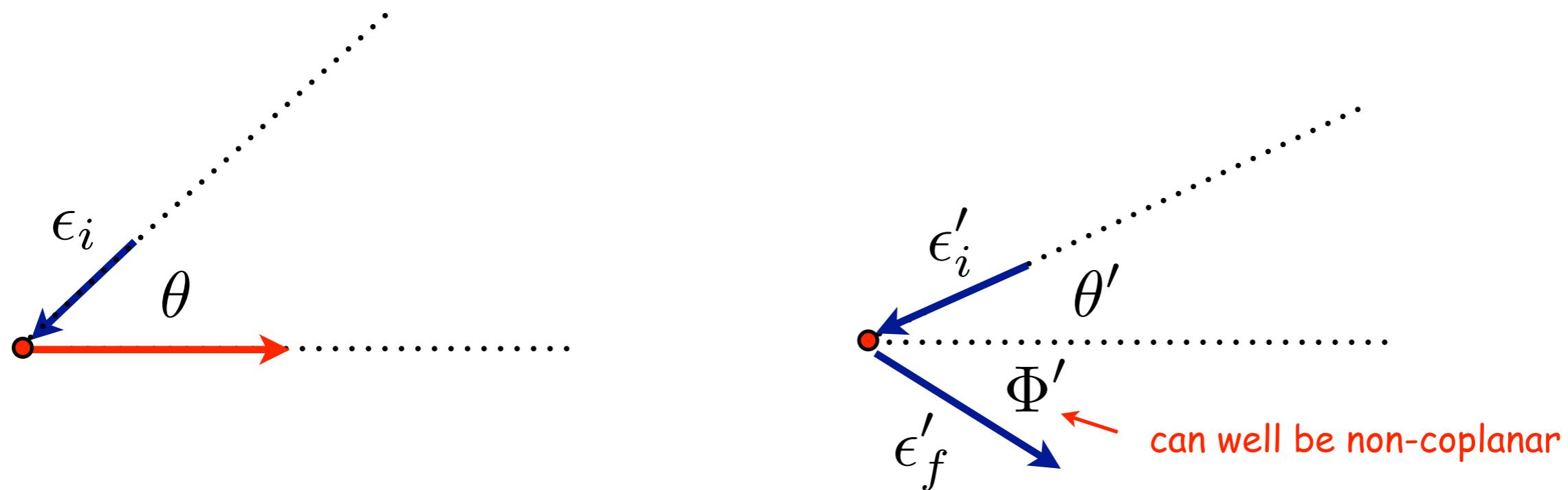
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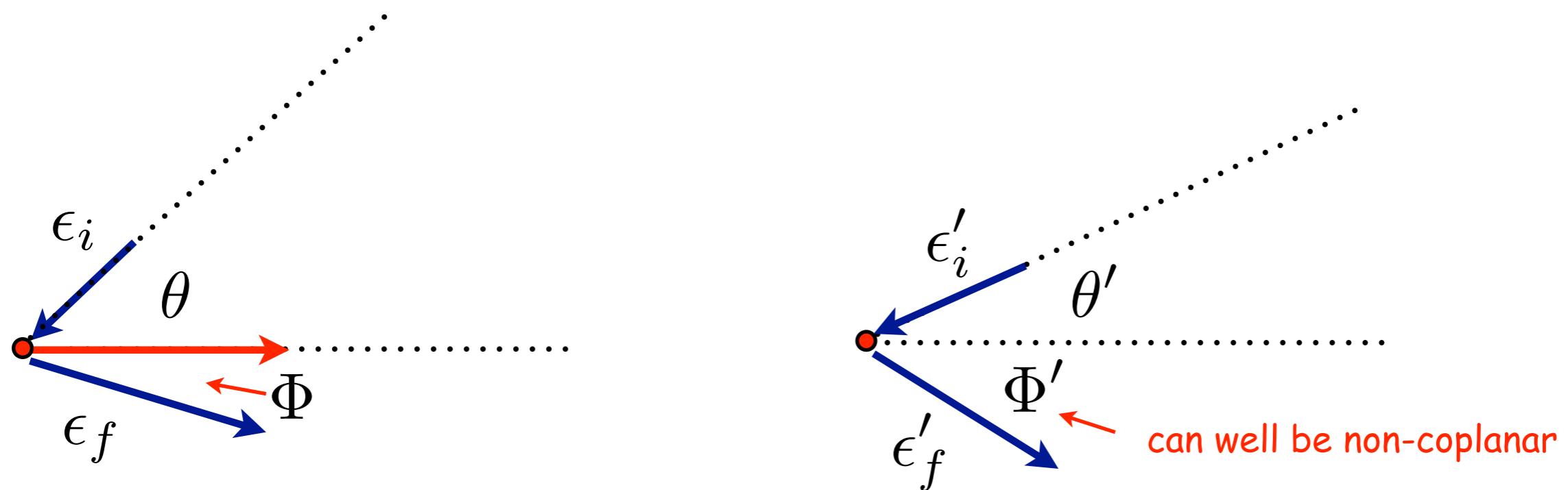


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In the lab rest frame the (final) photon energy is: $\epsilon_f = \epsilon'_f \gamma (1 + \beta \cos \Phi)$

Leptonic Gamma-Rays: Inverse Compton

$$\epsilon_f = \gamma^2 \epsilon_i G(\theta, \Phi)$$

After averaging over angles (tedious...):

$$\epsilon_f = \frac{4}{3} \gamma^2 \epsilon_i$$

Leptonic Gamma-Rays: Inverse Compton

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Example:

Cosmic Microwave Background $\rightarrow T \sim 3 \text{ K}$ $kT \approx 3 \times 10^{-4} \text{ eV}$

- $E_e = 1 \text{ GeV} \rightarrow \epsilon_\gamma = 1,5 \text{ keV}$ X-rays
- $E_e = 1 \text{ TeV} \rightarrow \epsilon_\gamma = 1,5 \text{ GeV}$ gamma rays (FERMI)
- $E_e = 25 \text{ TeV} \rightarrow \epsilon_\gamma = 1 \text{ TeV}$ gamma rays (Cherenkov Telescopes)

Leptonic Gamma-Rays: Inverse Compton

is there a maximum energy for
the up-scattered photons?

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energy conservation...

above a given energy Inverse Compton scattering becomes ineffective

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Thomson scattering ONLY if:

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if $\gamma \epsilon_i \sim mc^2$ we must use the quantum relativistic (Klein-Nishina) cross section

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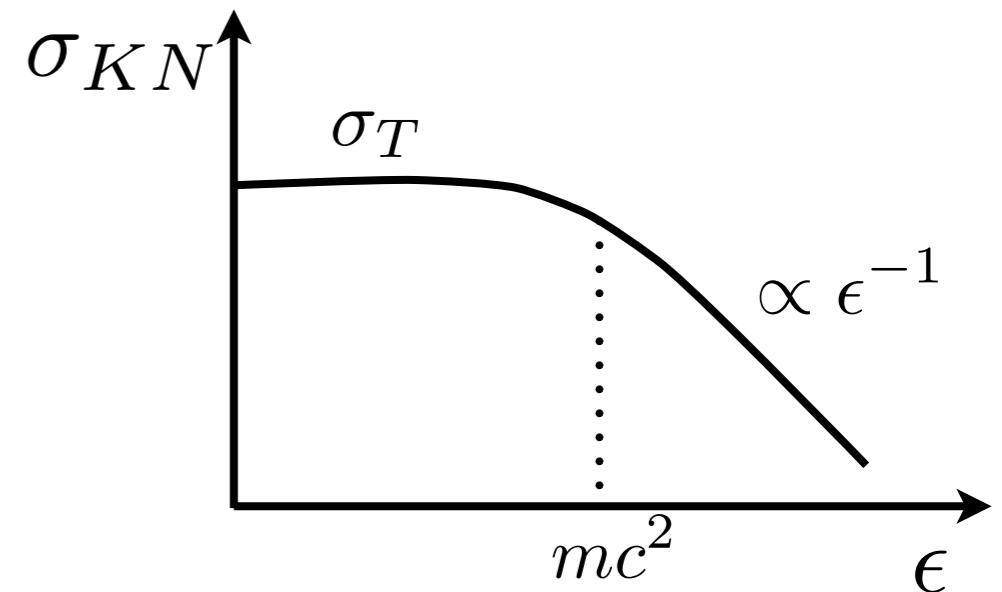
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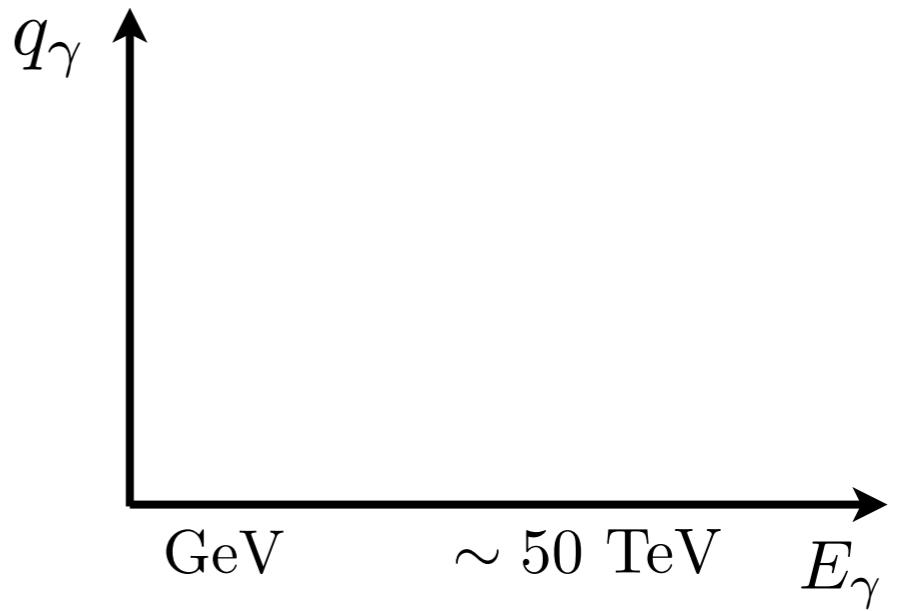
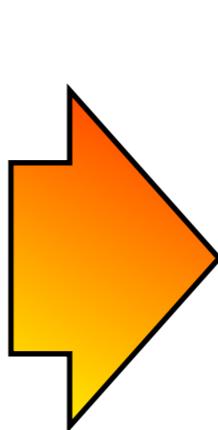
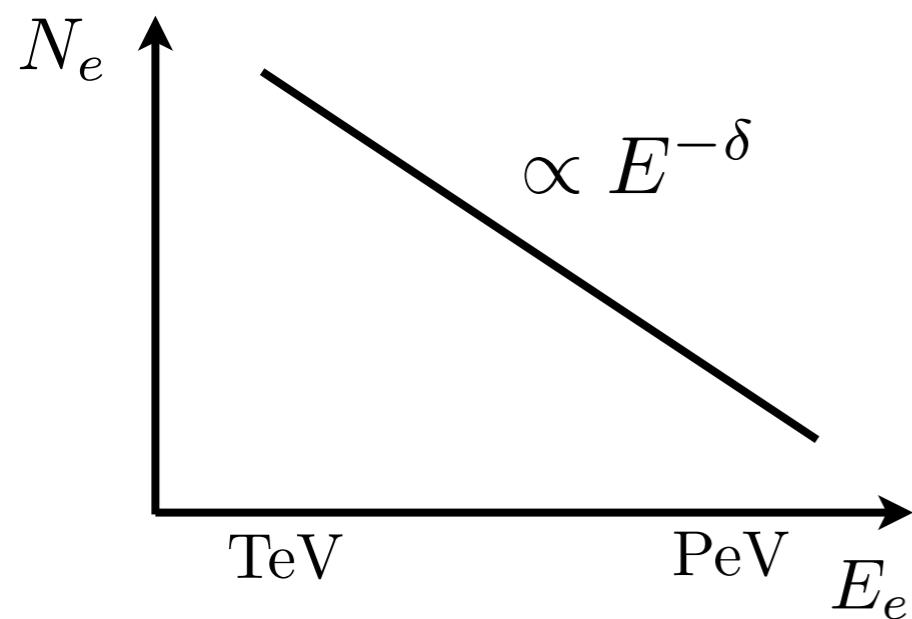
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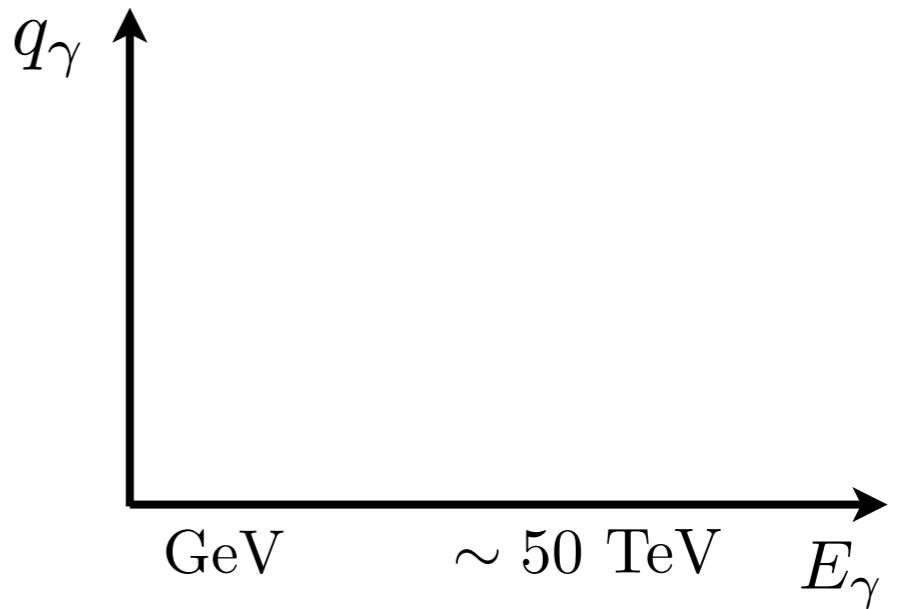
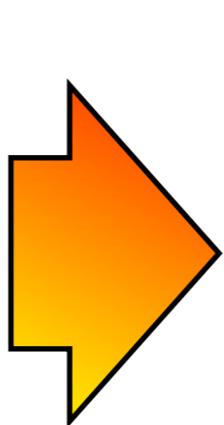
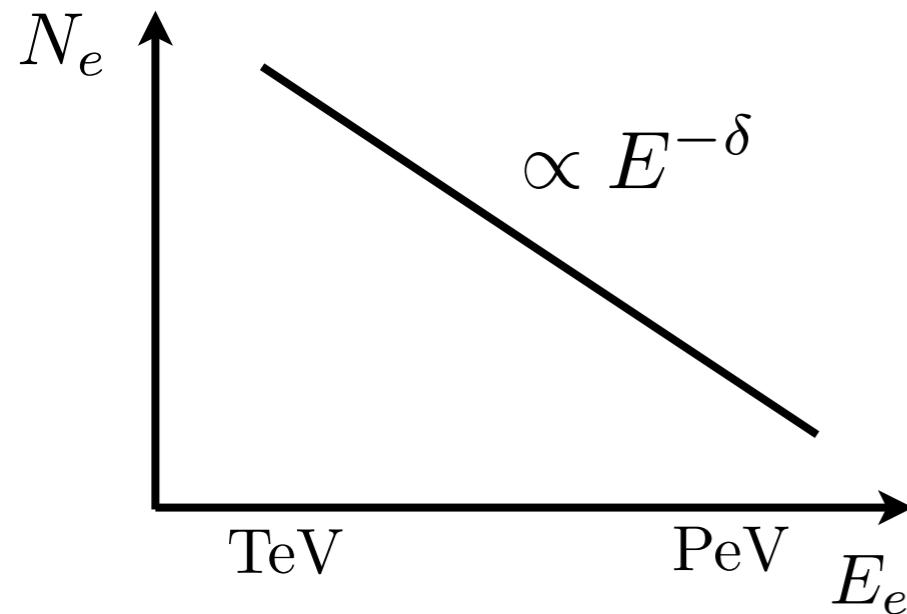
Photon spectrum:



$$q_\gamma(E_\gamma) = \int dE_e N_e(E_e) \delta(E_\gamma - \frac{4}{3}\gamma^2 \epsilon_{CMB})(n_{CMB} \sigma_T c)$$

Leptonic Gamma-Rays: Inverse Compton

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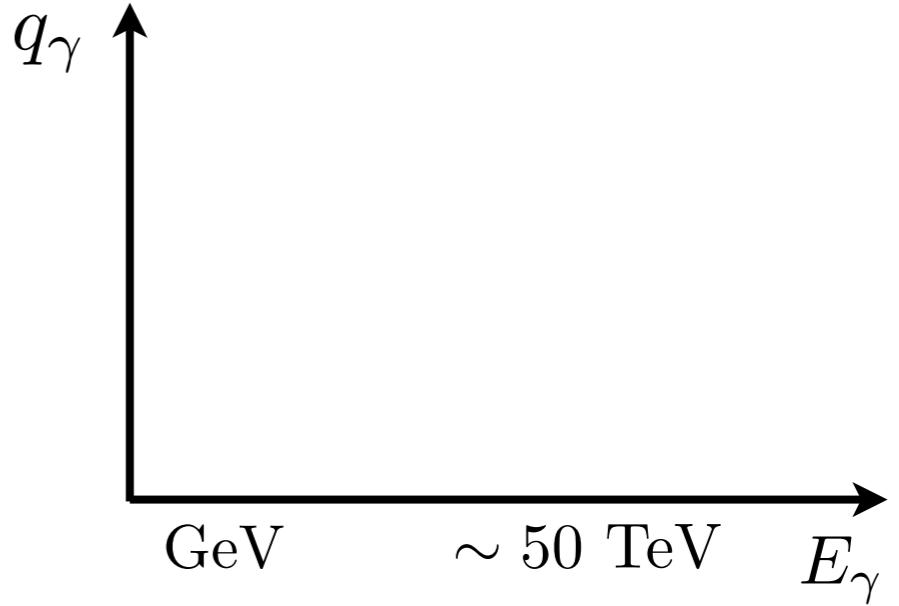
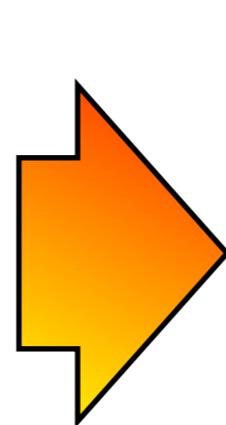
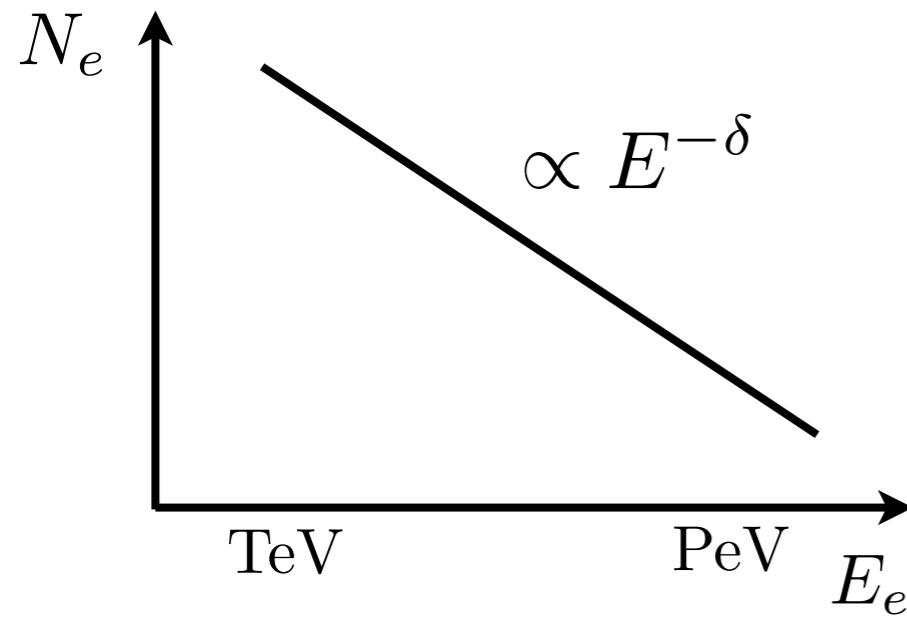
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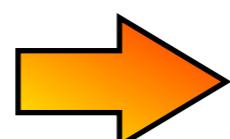
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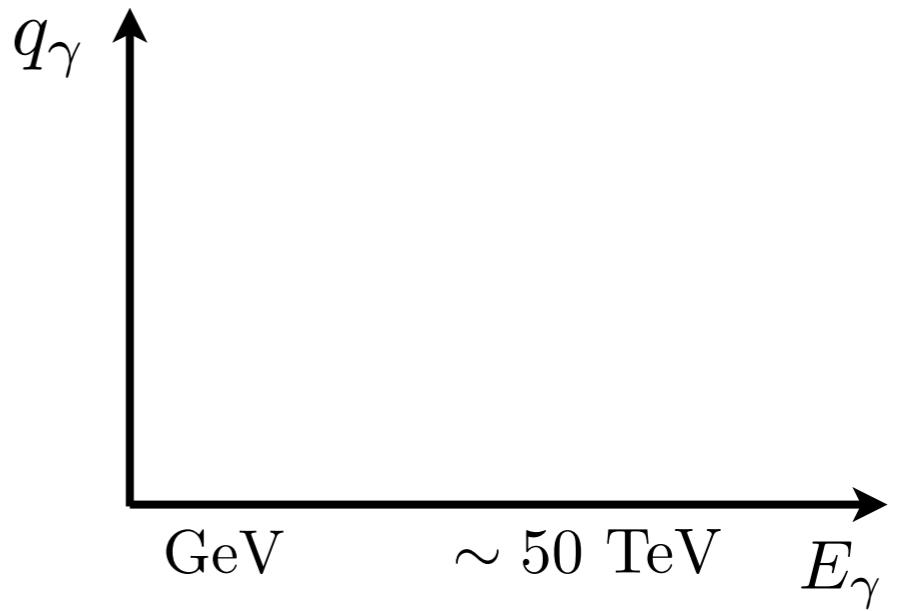
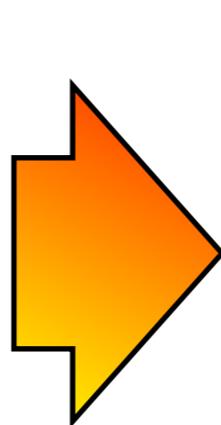
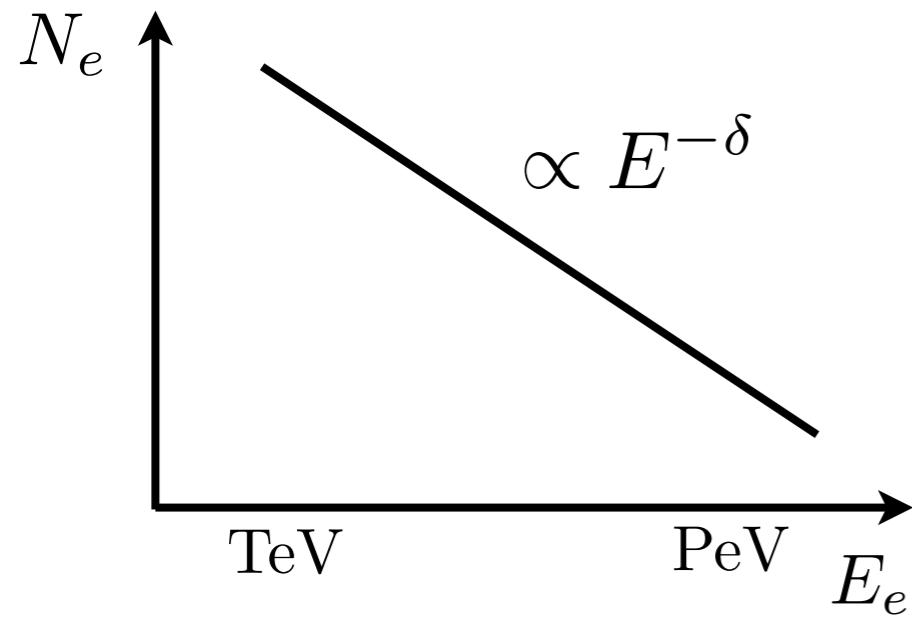
$$\delta \left(E_\gamma - \frac{4}{3} \left(\frac{E_e}{mc^2} \right)^2 \epsilon_{CMB} \right)$$

Annotations below the equation:

- $x_0 \propto E_\gamma^{1/2}$ with a red arrow pointing to the term E_e in the equation.
- $g' \propto E_e$ with a red arrow pointing to the term E_e in the equation.

Leptonic Gamma-Rays: Inverse Compton

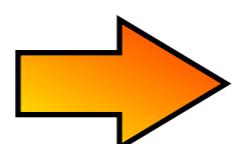
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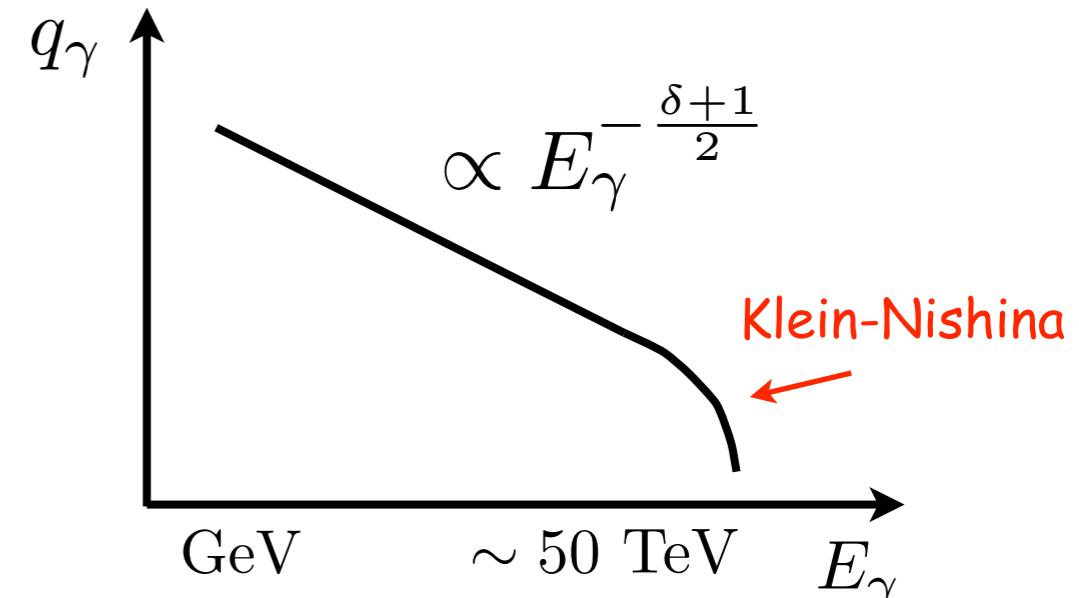
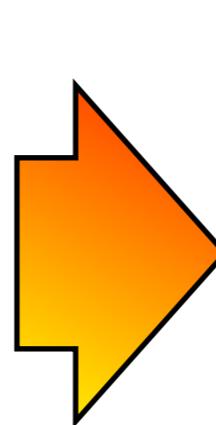
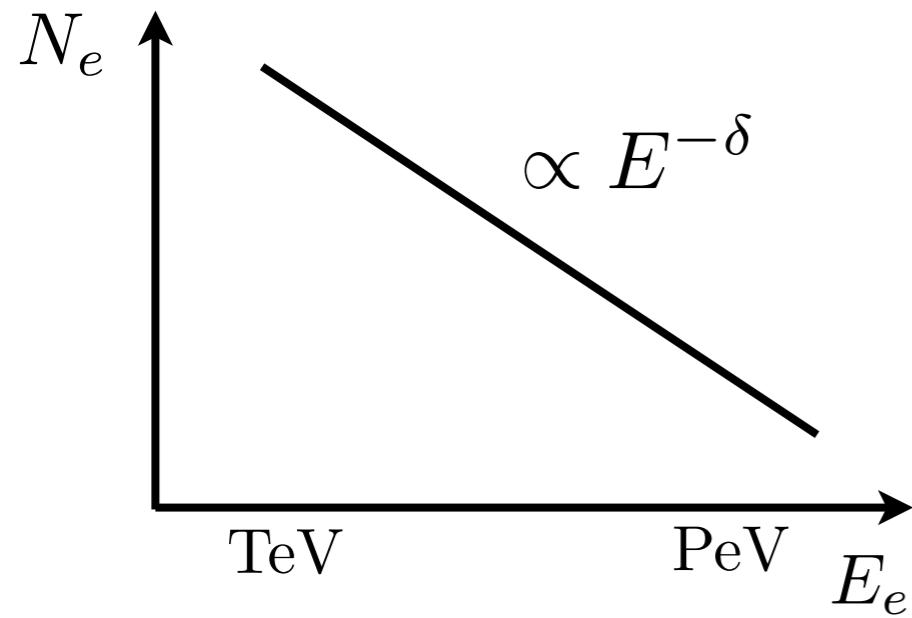
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$g(x)$

$x_0 \propto E_\gamma^{1/2}$ $g' \propto E_e$

Leptonic Gamma-Rays: Inverse Compton

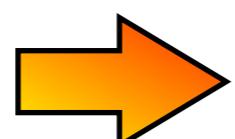
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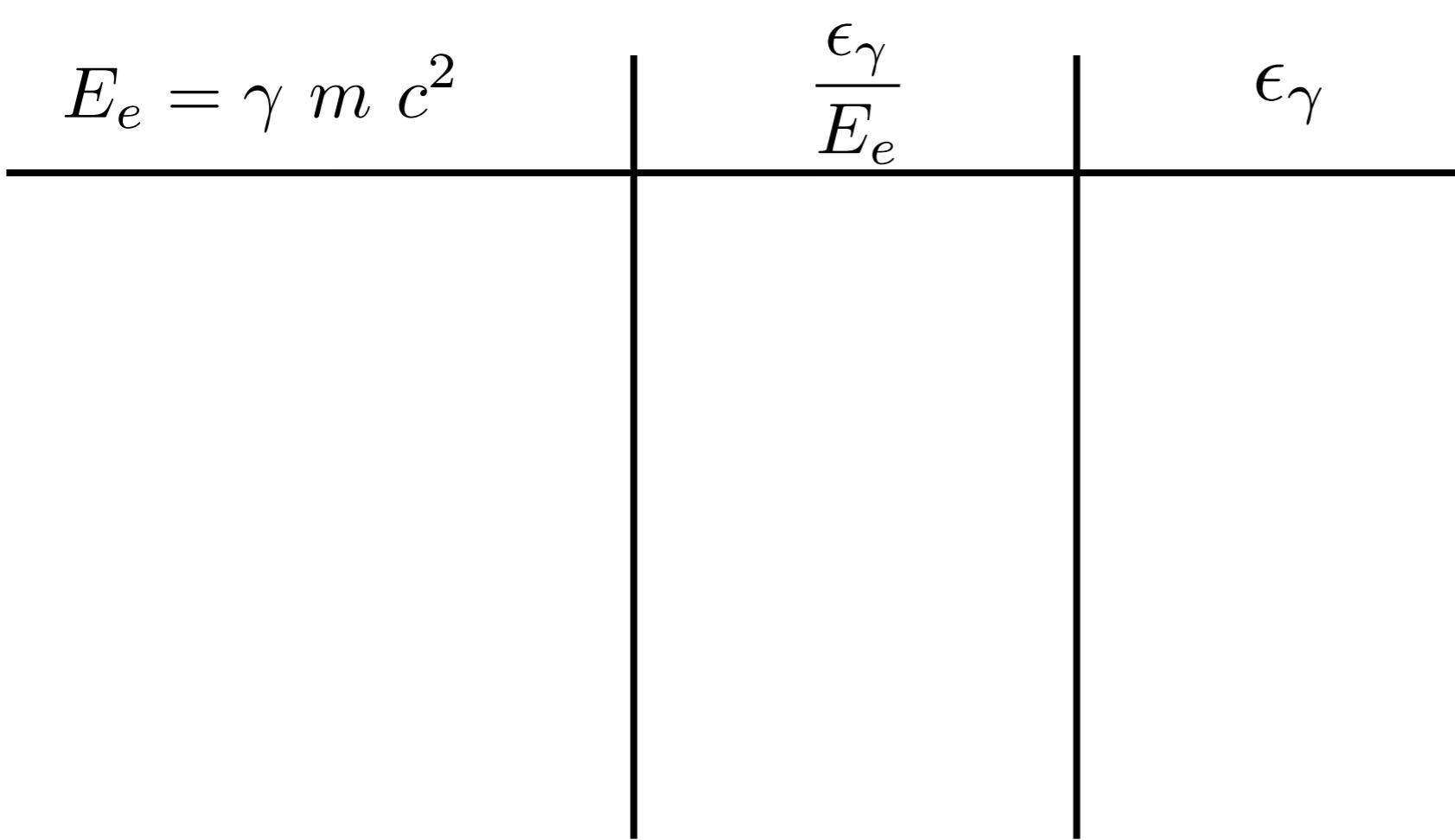
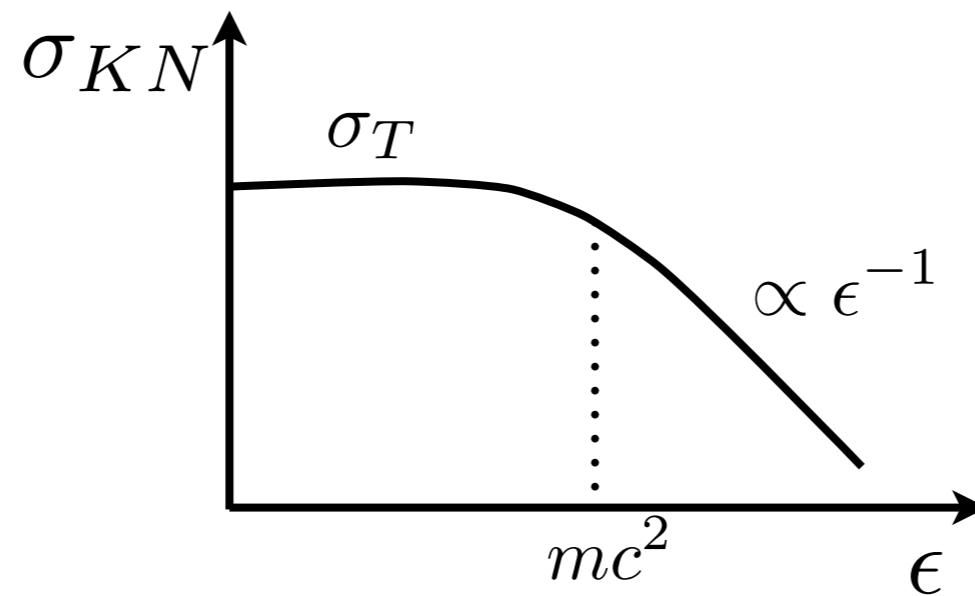


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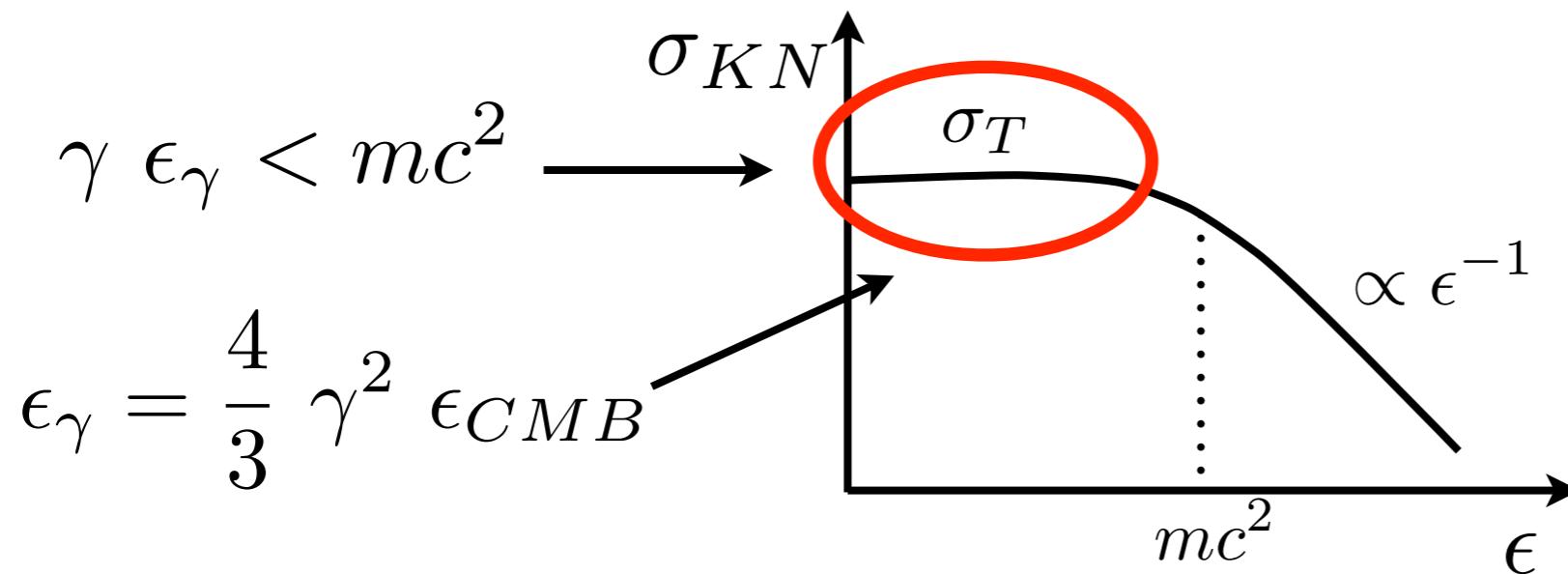
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Leptonic Gamma-Rays: Inverse Compton



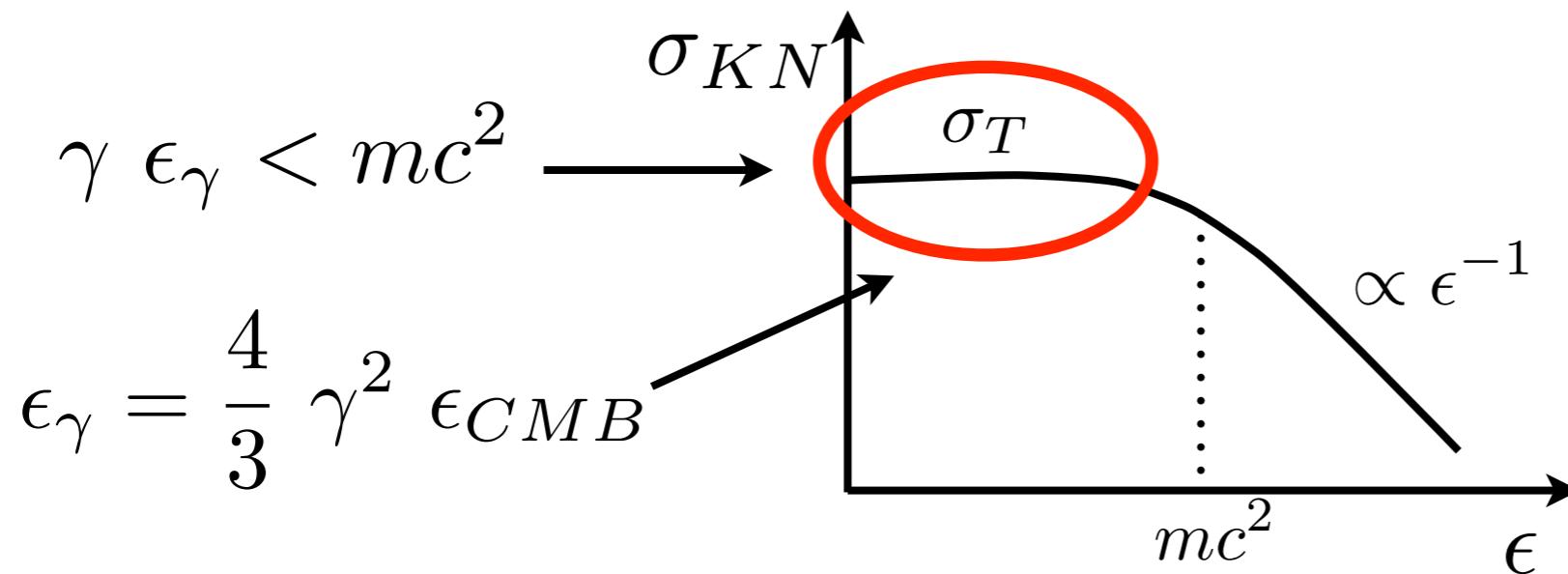
Leptonic Gamma-Rays: Inverse Compton



$E_e = \gamma m c^2$	$\frac{\epsilon_\gamma}{E_e}$	ϵ_γ
1 TeV	~0.2%	~1.5 GeV
25 TeV	~4%	~1 TeV
100 TeV	~15%	~15 TeV

Thomson

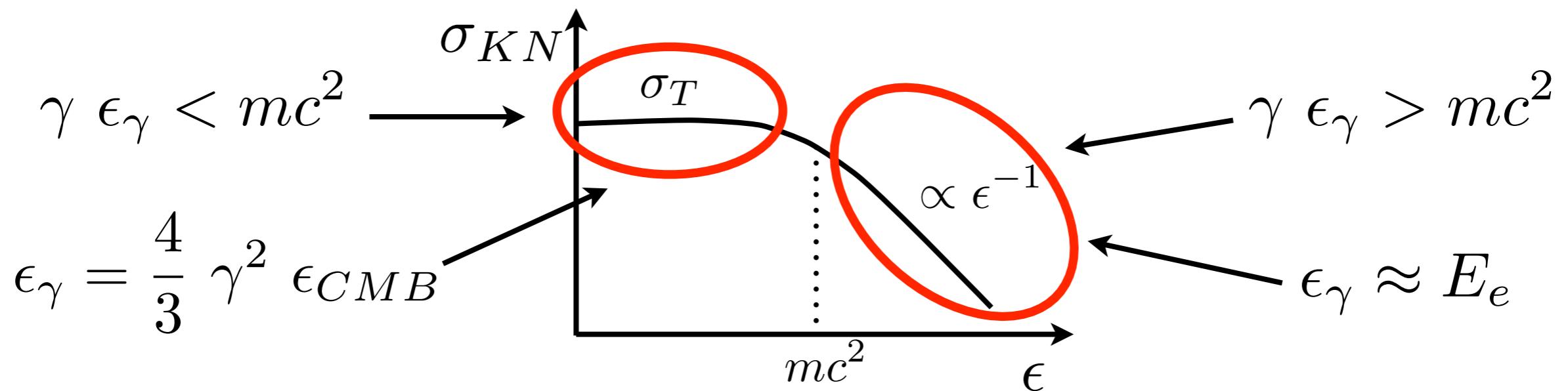
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Thomson

Leptonic Gamma-Rays: Inverse Compton

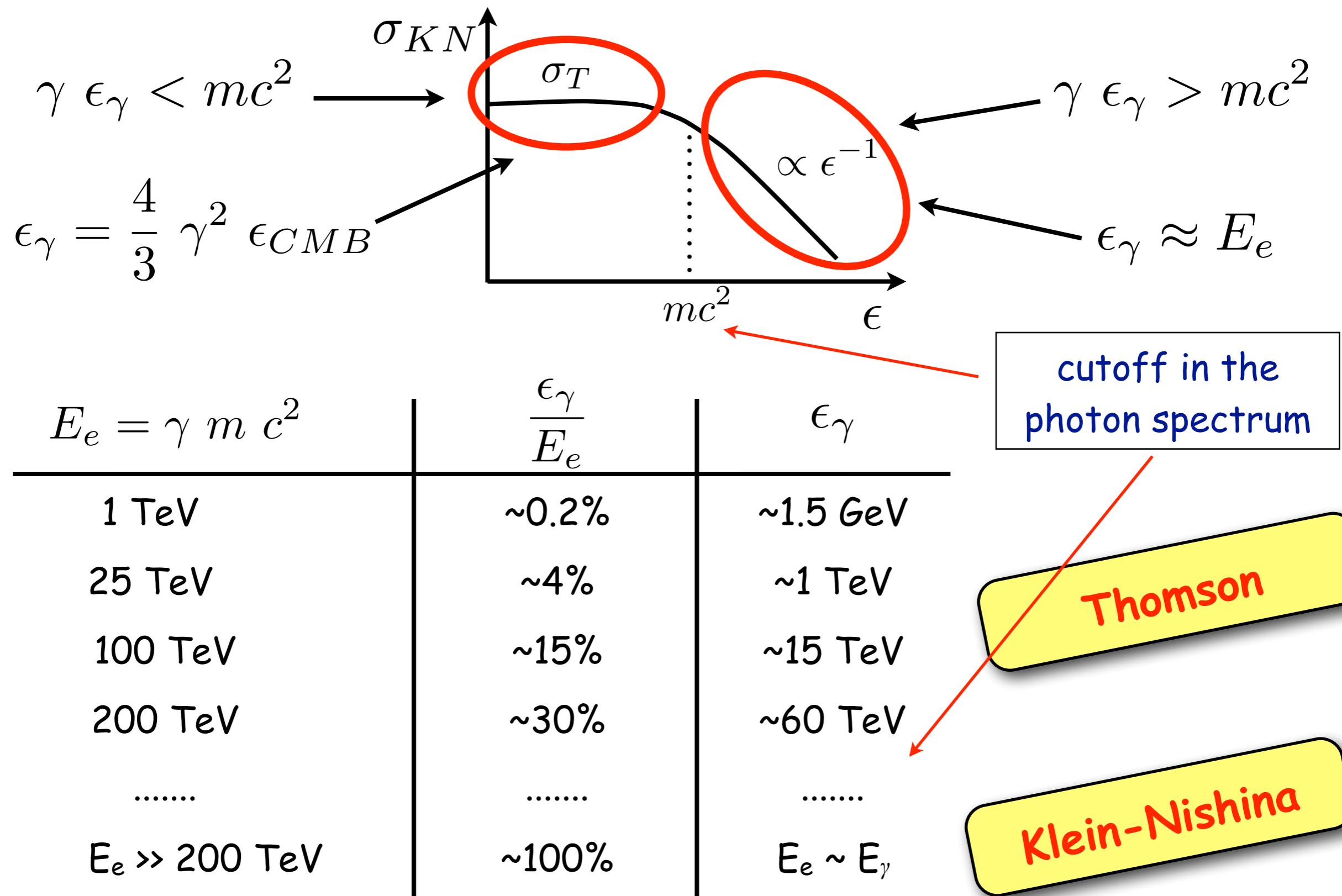


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$E_e \gg 200$ TeV	~100%	$E_e \sim E_\gamma$

Thomson

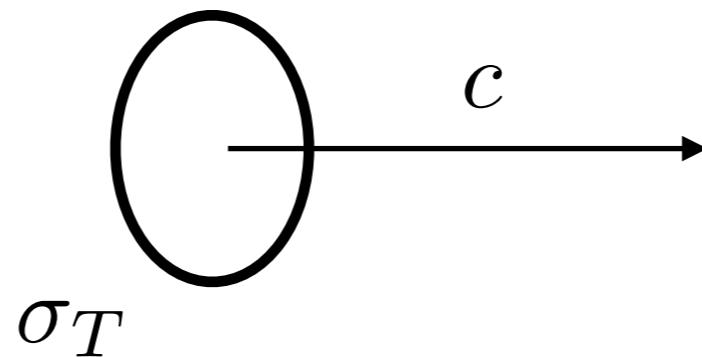
Klein-Nishina

Leptonic Gamma-Rays: Inverse Compton



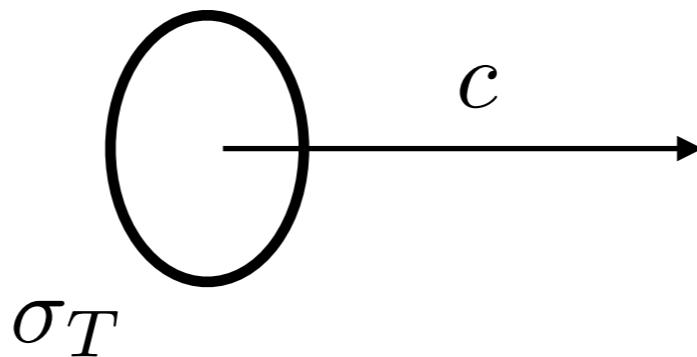
Inverse Compton: energy loss rate

Scattering rate



Inverse Compton: energy loss rate

Scattering rate

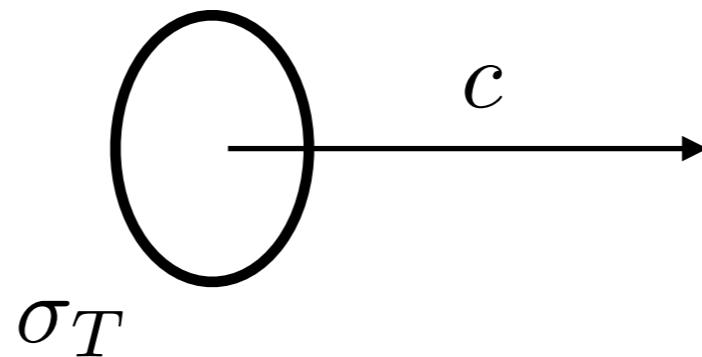


σ_T

Volume swept per second $\sigma_T c$

Inverse Compton: energy loss rate

Scattering rate



σ_T

Volume swept per second $\sigma_T c$

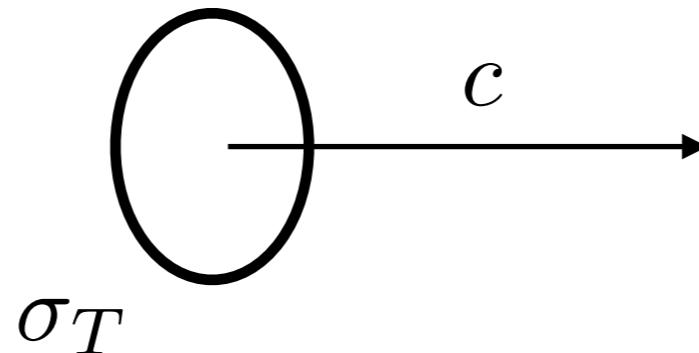
Interaction rate

$$\sigma_T c n_{CMB}$$

$$n_{CMB} = \frac{\omega_{CMB}}{\langle \epsilon \rangle}$$

Inverse Compton: energy loss rate

Scattering rate



σ_T

Volume swept per second $\sigma_T c$

Interaction rate

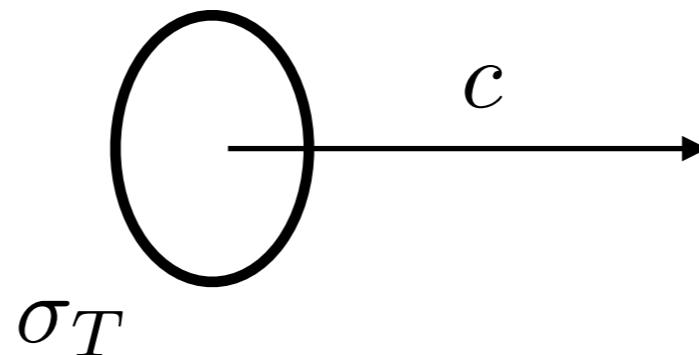
$$\sigma_T c n_{CMB}$$

$$n_{CMB} = \frac{\omega_{CMB}}{\langle \epsilon \rangle}$$

Radiated power $P_{IC} = \left(\sigma_T c \frac{\omega_{CMB}}{\langle \epsilon \rangle} \right) \left(\frac{4}{3} \gamma^2 \langle \epsilon \rangle \right) = \frac{4}{3} \sigma_T c \gamma^2 \omega_{CMB}$

Inverse Compton: energy loss rate

Scattering rate



$$\sigma_T$$

Volume swept per second $\sigma_T c$

Interaction rate

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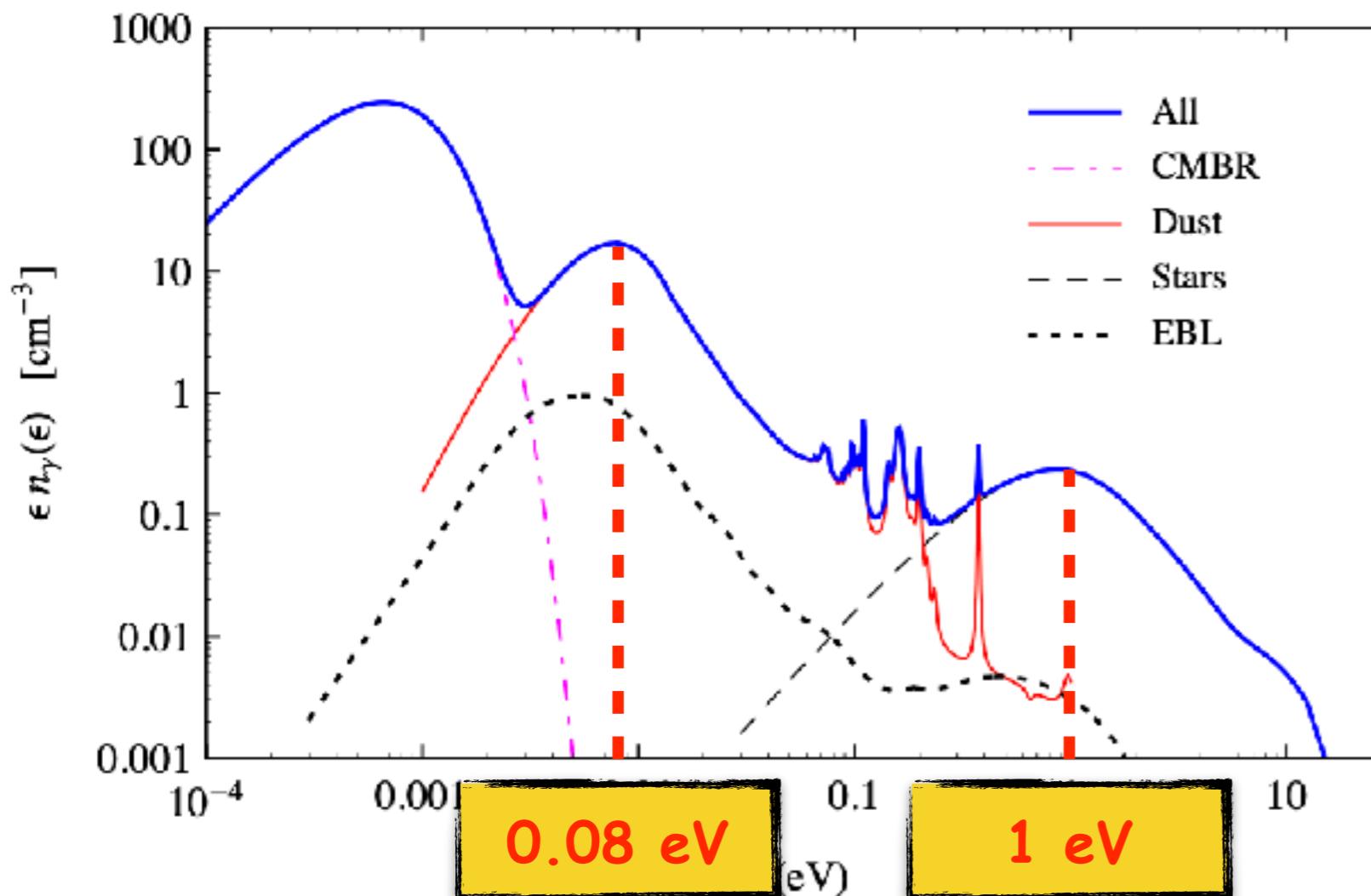
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Same expression as synchrotron!

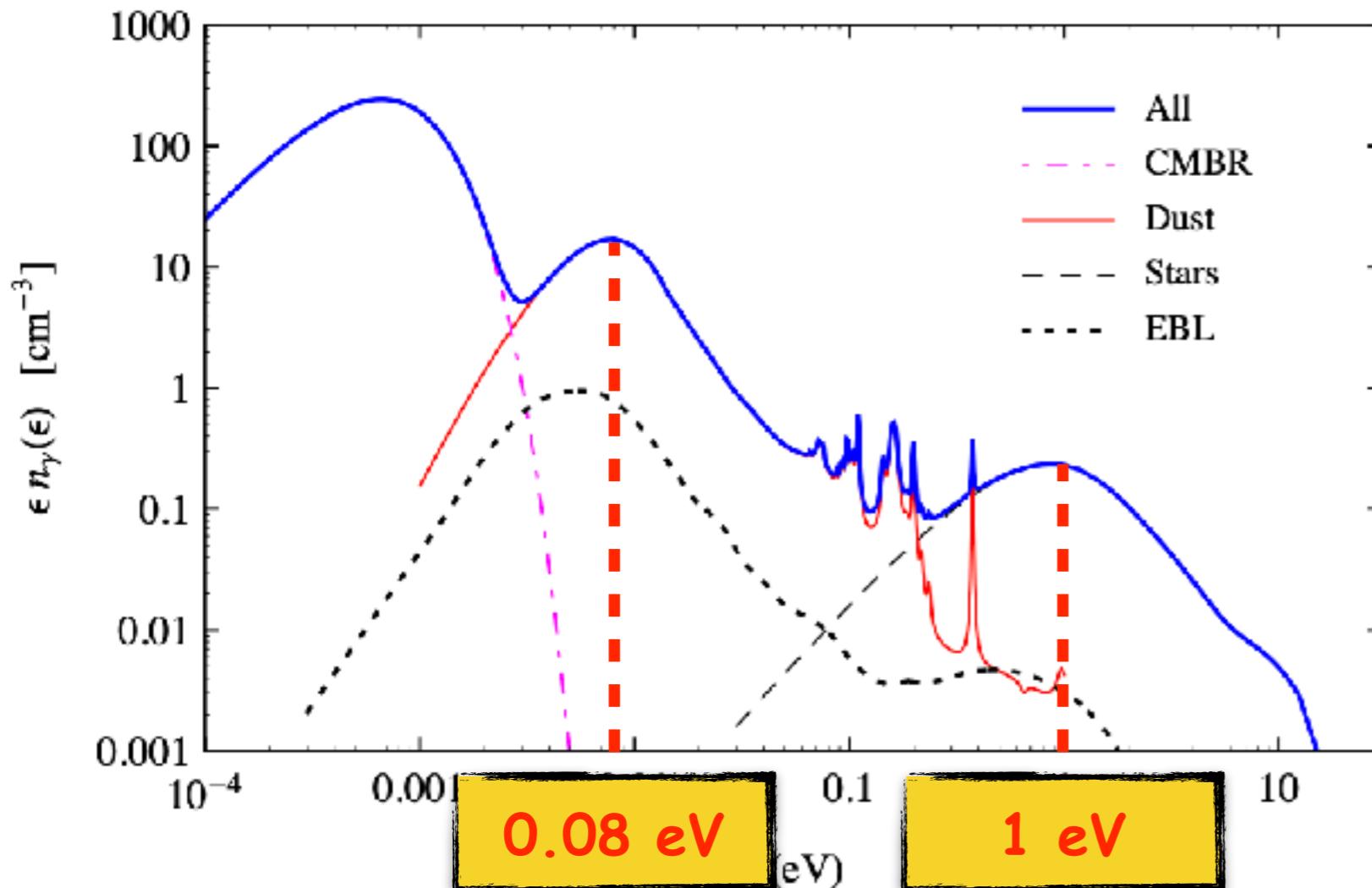
Note on the K-N regime

Lipari & Vernetto 2018



Note on the K-N regime

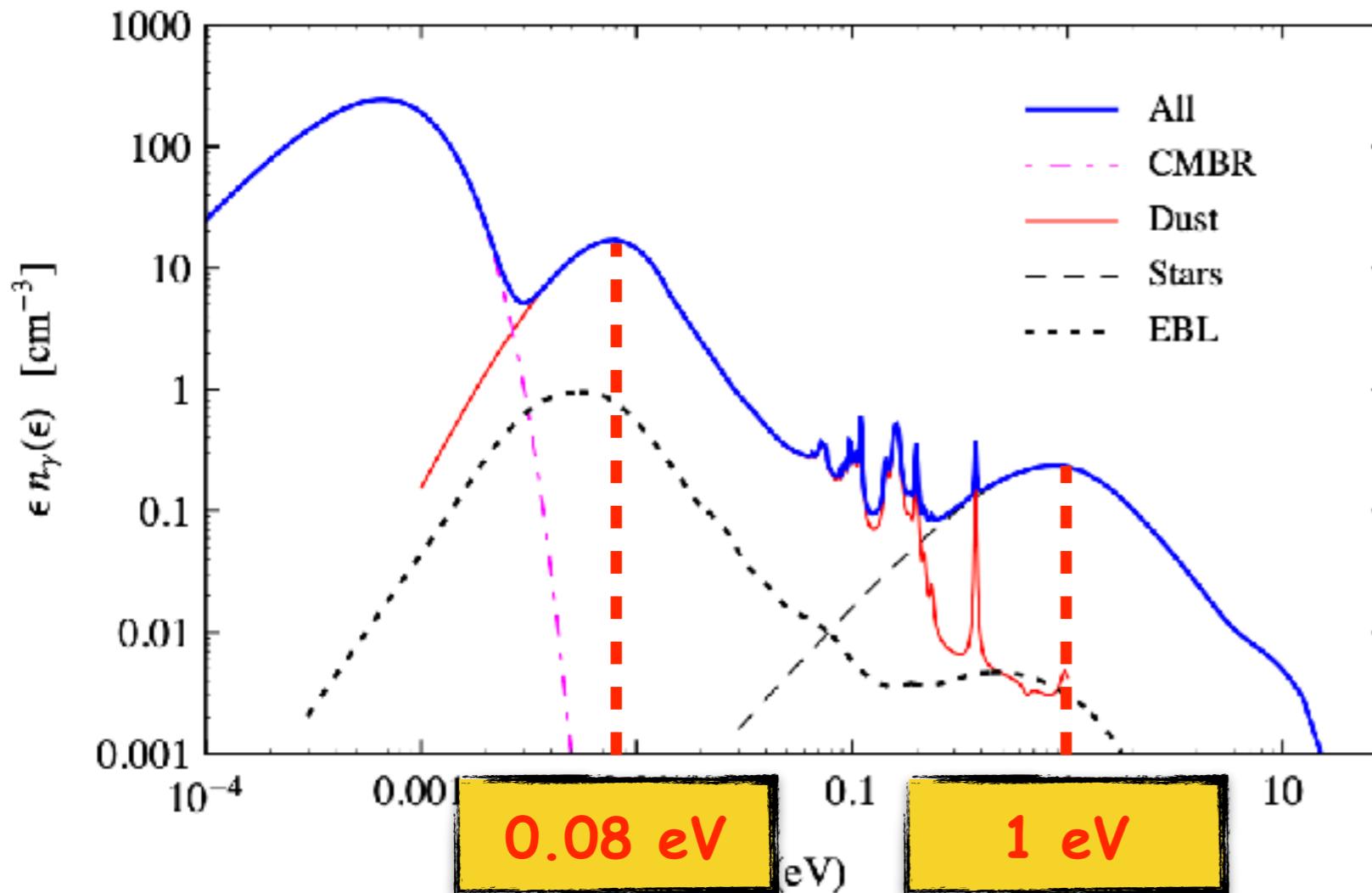
Lipari & Vernetto 2018



$$\gamma \epsilon_\gamma > mc^2$$

Note on the K-N regime

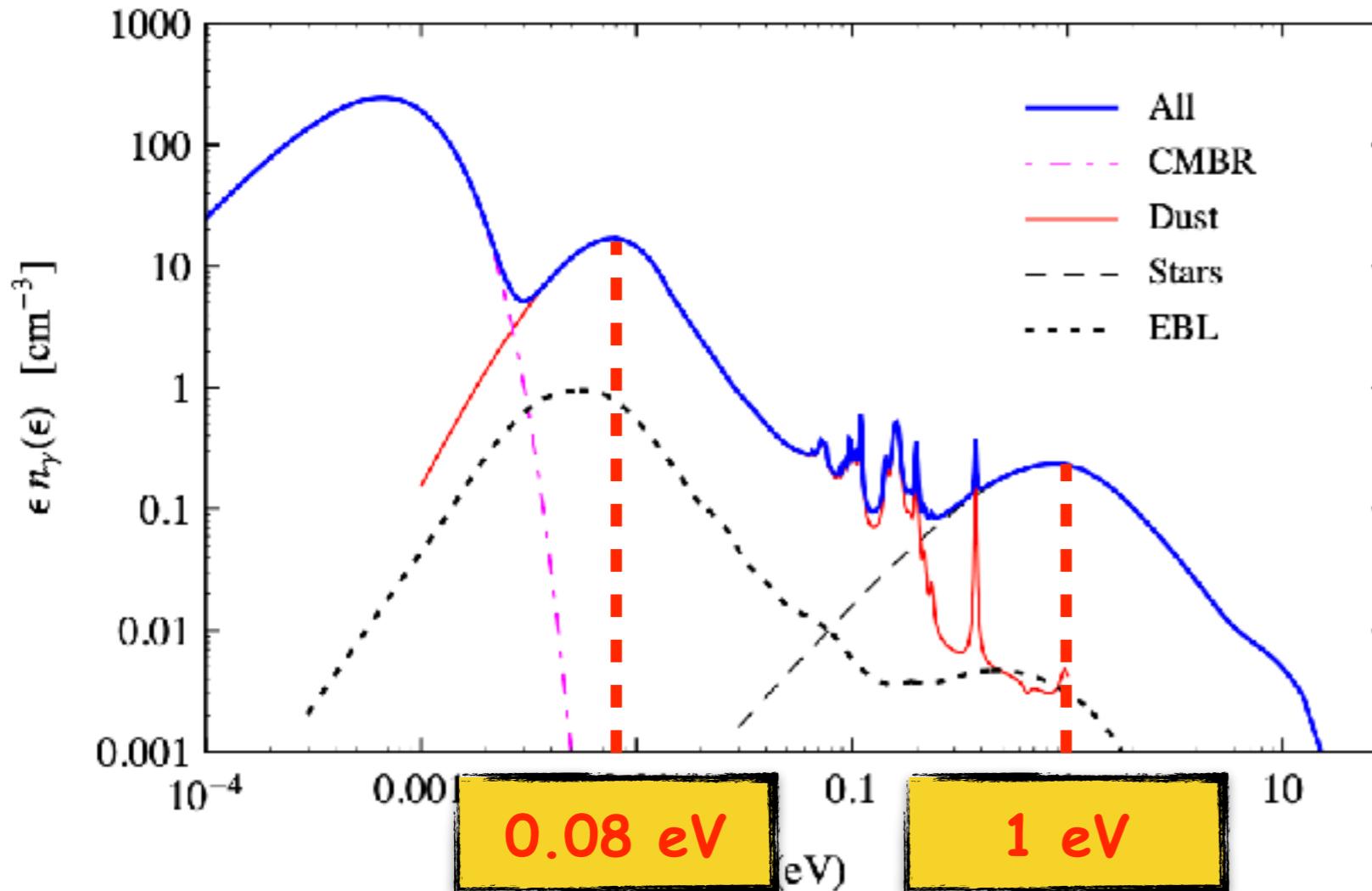
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$$\gamma \epsilon_\gamma > mc^2$$
$$E_e > \frac{(mc^2)^2}{\epsilon_\gamma}$$

Note on the K-N regime

Lipari & Vernetto 2018



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\downarrow

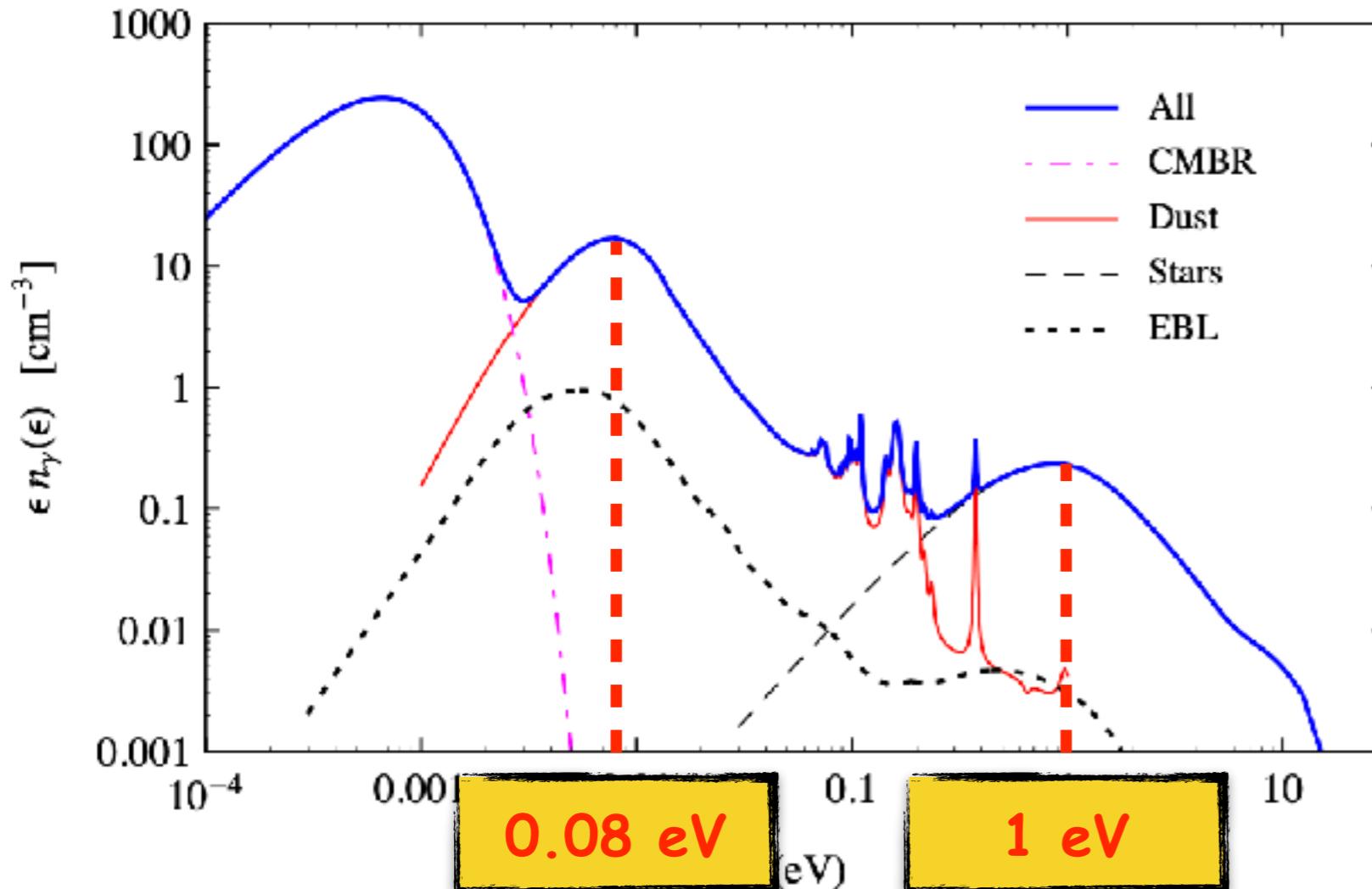
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$$E_\gamma = \frac{4}{3} \gamma^2 \epsilon_\gamma \quad \rightarrow \quad E_\gamma > \frac{4}{3} \frac{(mc^2)^2}{\epsilon_\gamma} \sim 0.3 \left(\frac{\epsilon_\gamma}{\text{eV}} \right) \text{TeV}$$

Note on the K-N regime

Lipari & Vernetto 2018



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↓

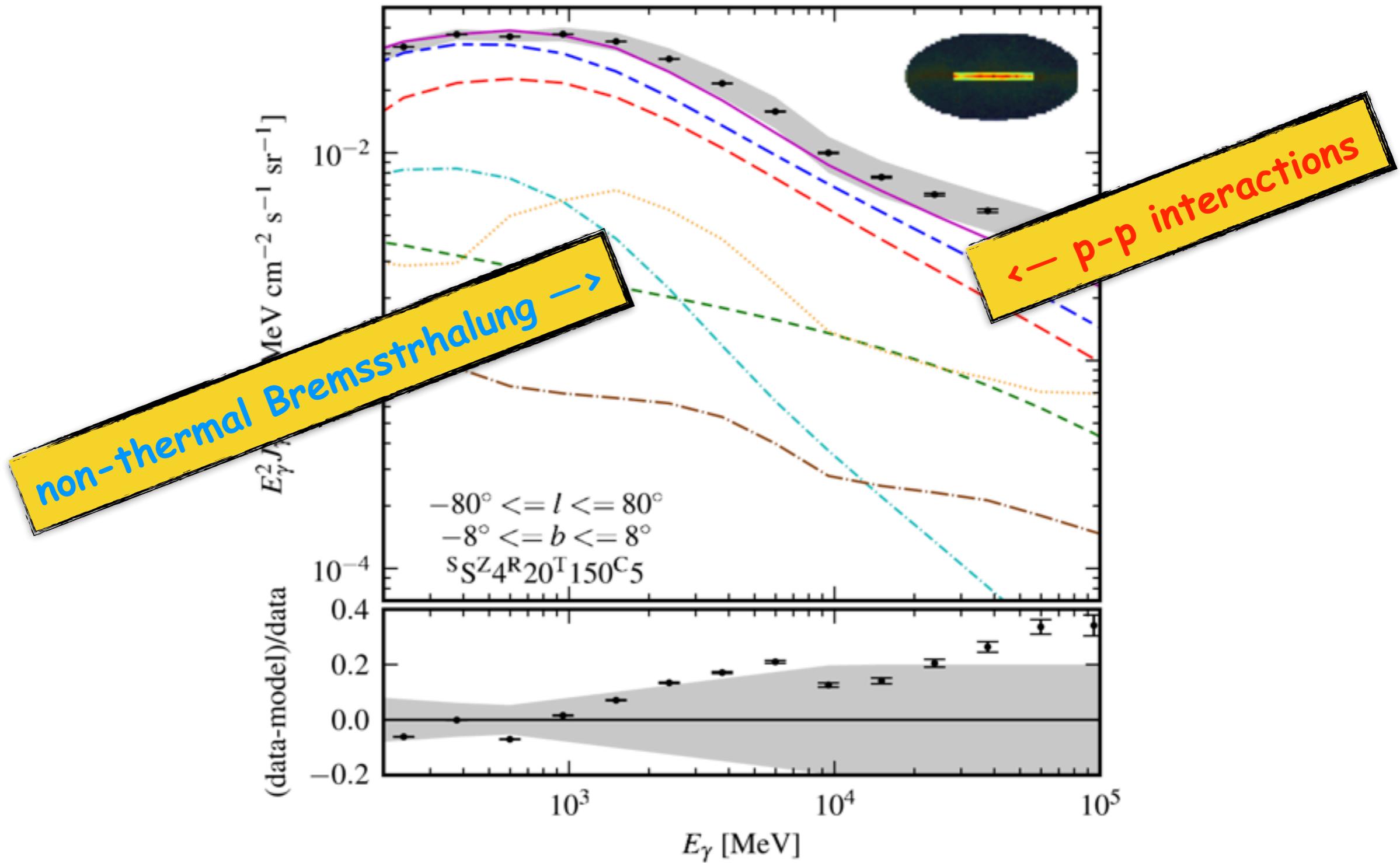
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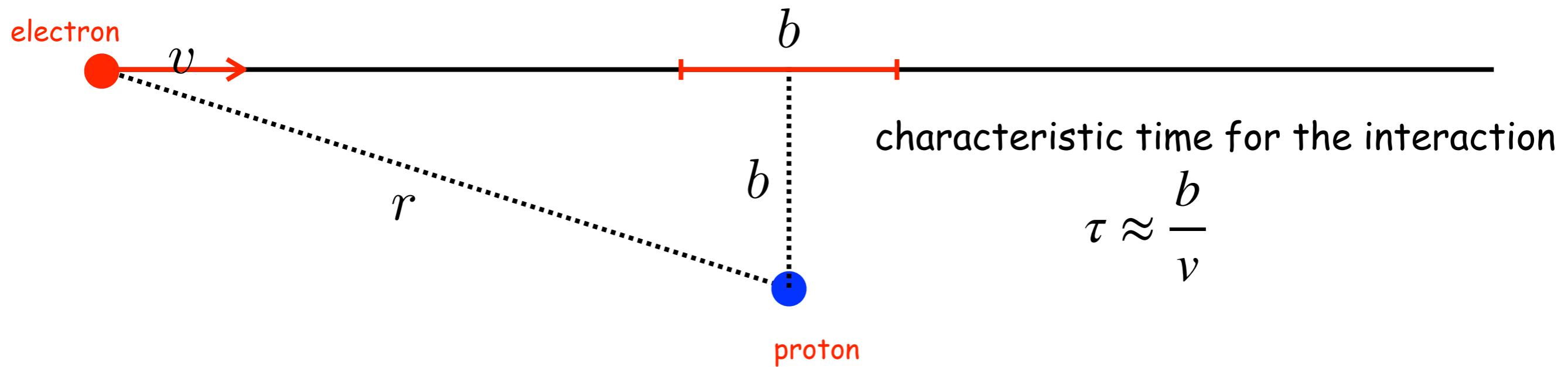
in first approximation: if you are a TeV astronomer just CMB matters for ICS

Non-thermal bremsstrahlung



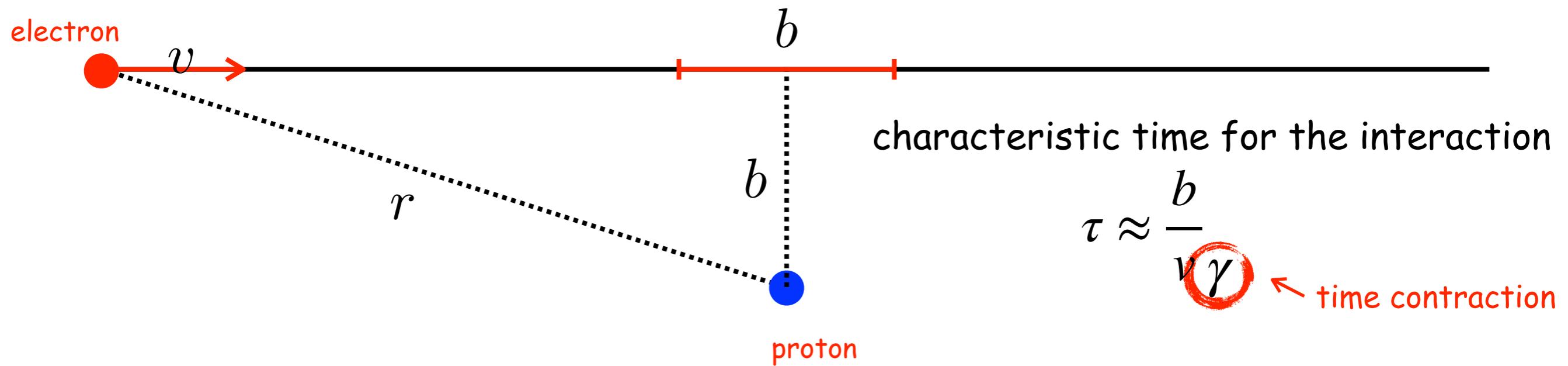
Non-thermal Bremsstrahlung

remember what we did for the thermal Bremsstrahlung



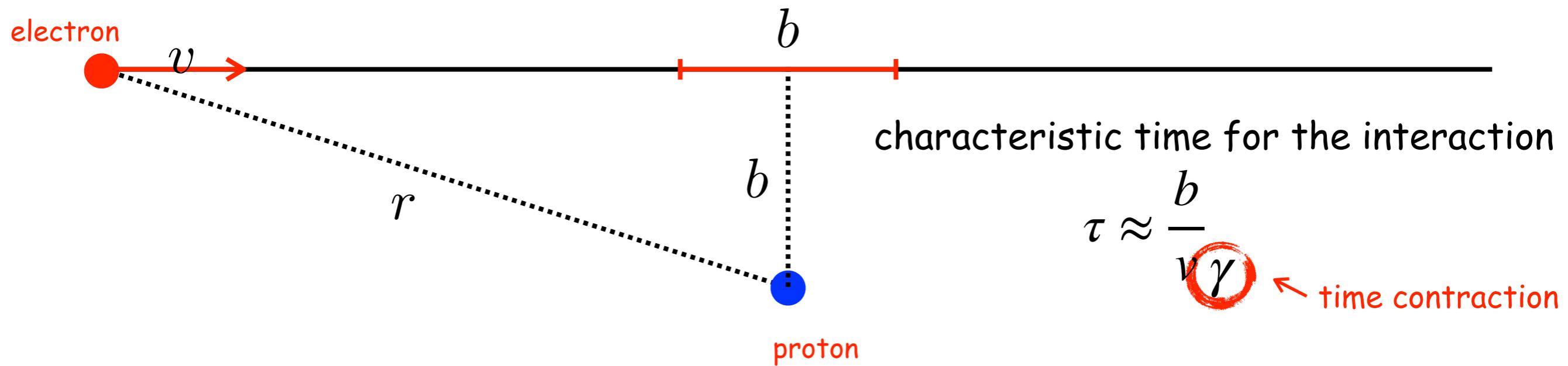
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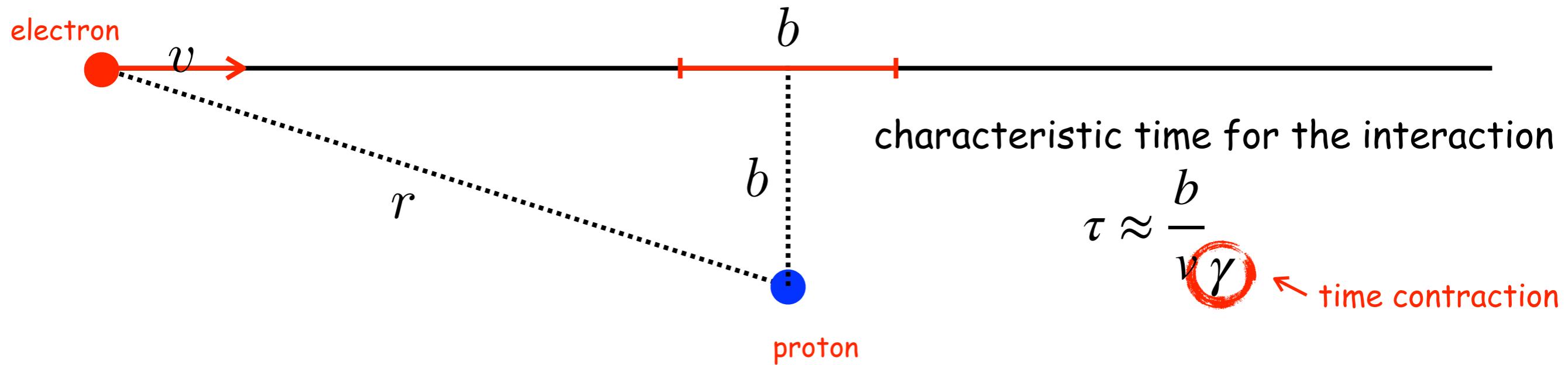
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→ in its rest frame, the e^- sees the proton's E field contracted into a very fast pulse

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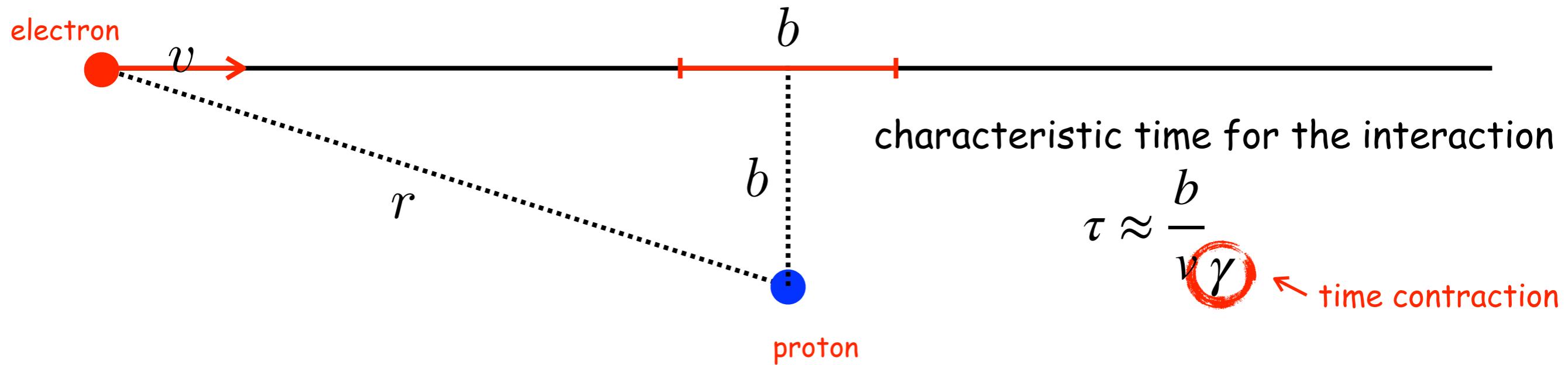
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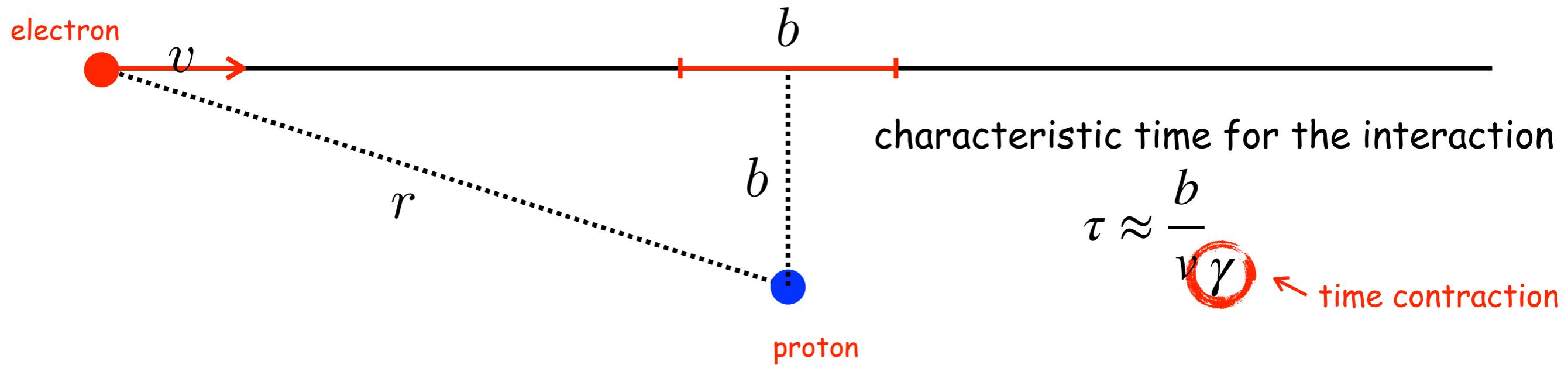
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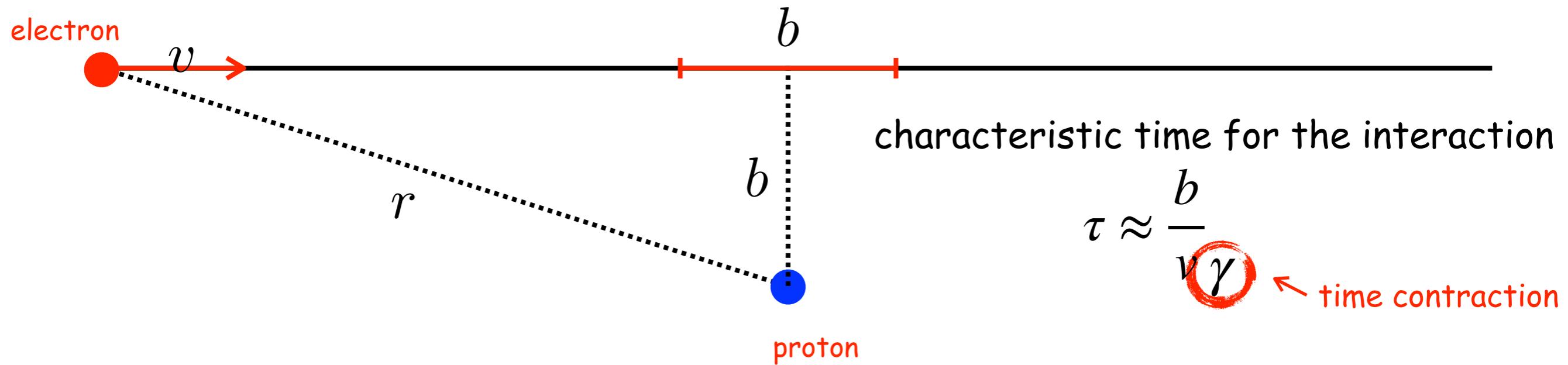
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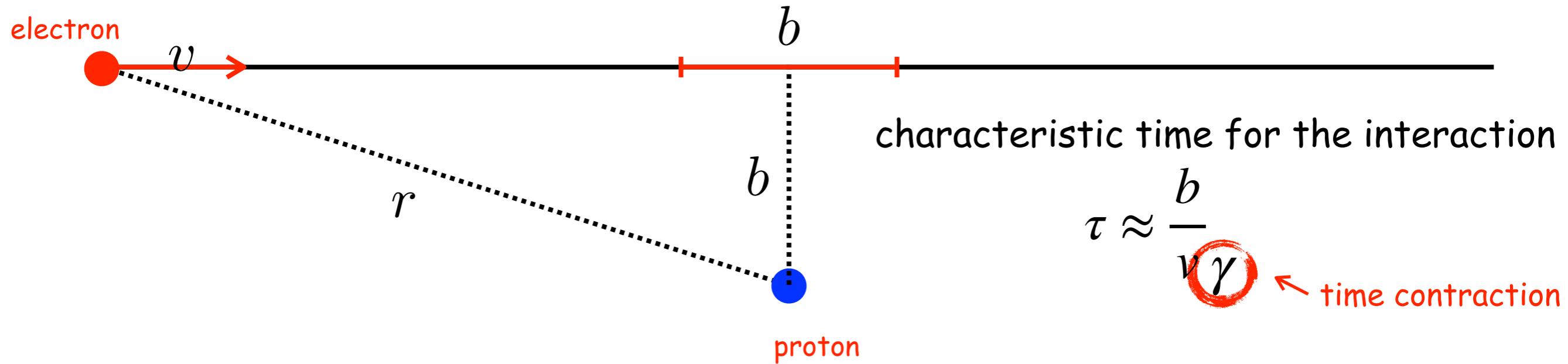
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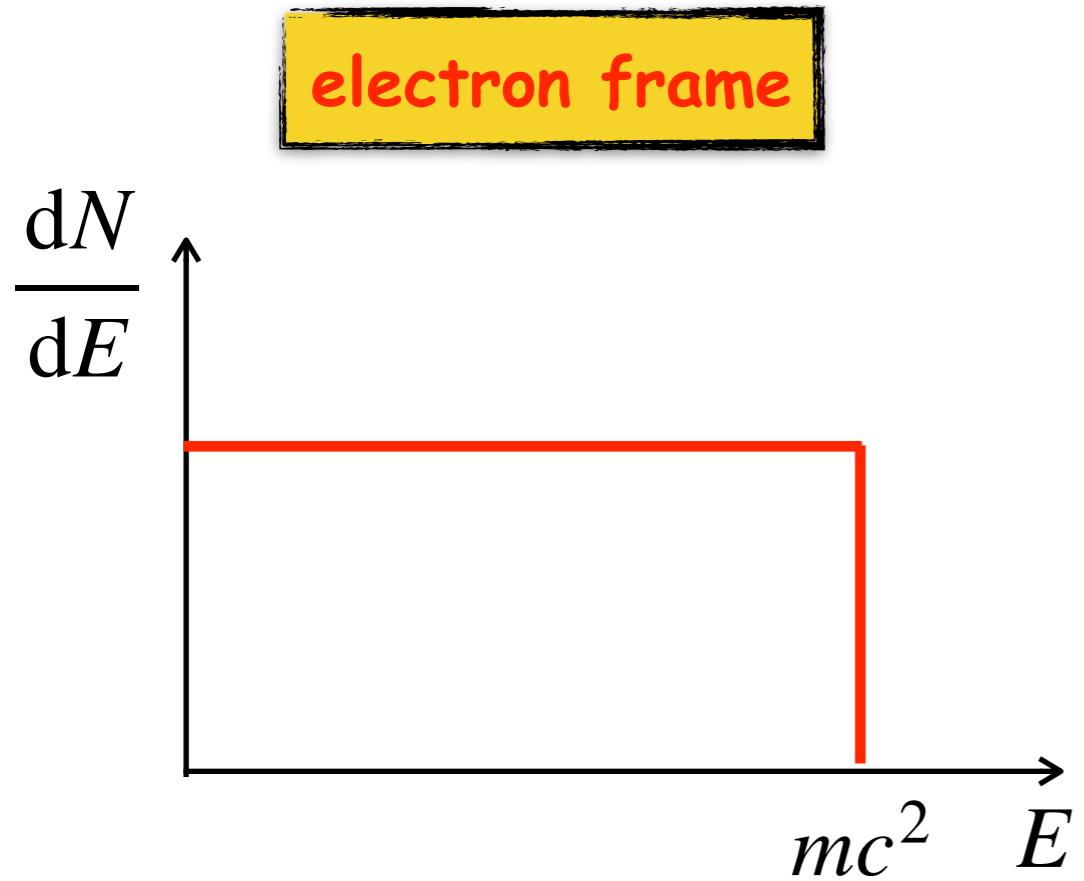
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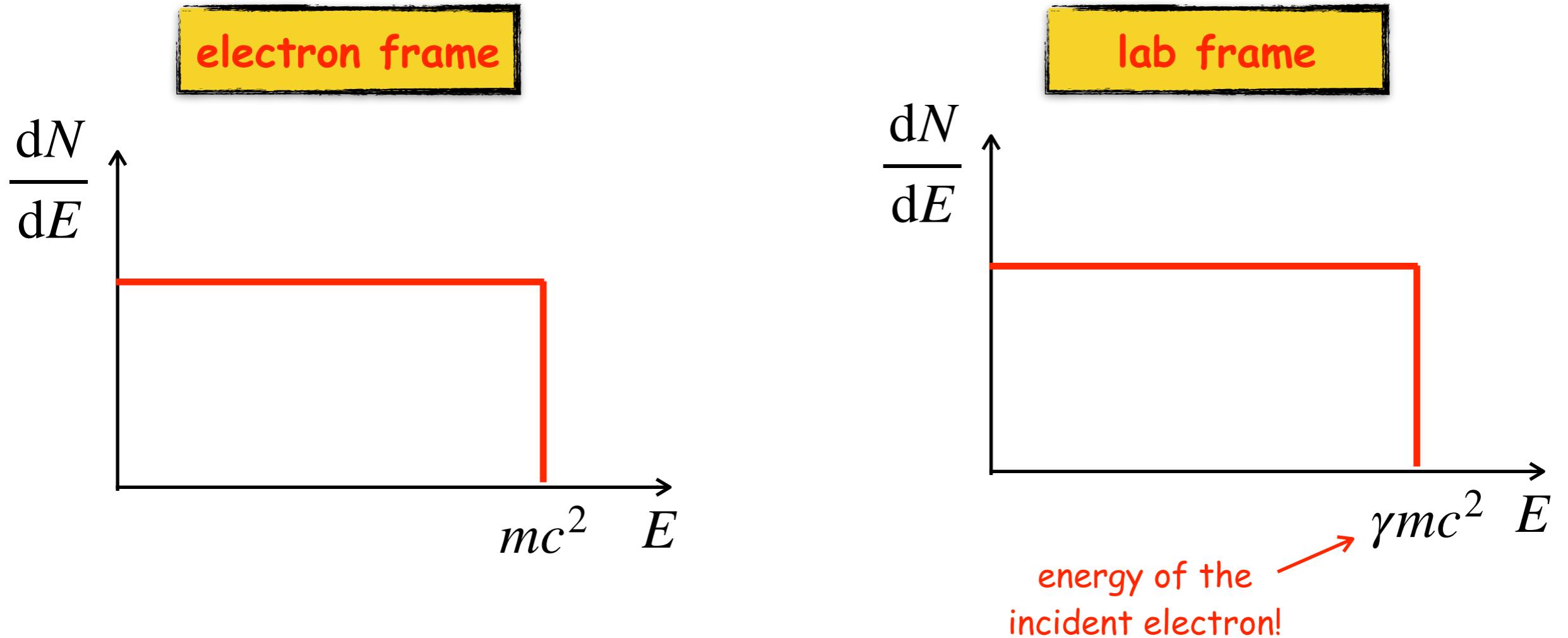


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- the pulse can be approximated as a spectrum of plane waves, i.e., "virtual" photons
 - the e^- will Compton scatter the virtual photon
 - Compton cross section drops beyond photon energies equal to mc^2
- the spectrum of scattered photons (in the e^- rest frame) extends up to mc^2
 - in the lab frame the spectrum extends up to γmc^2 !

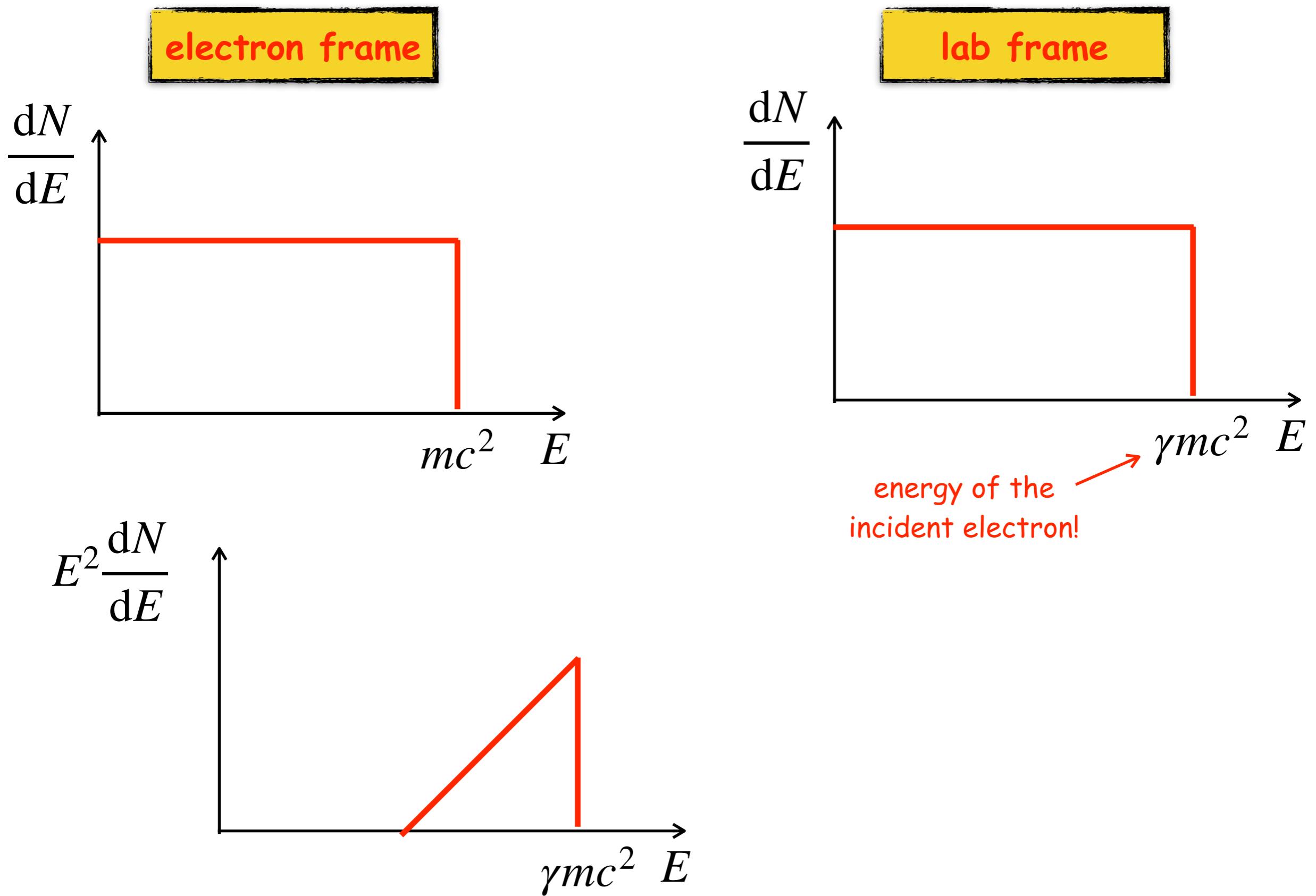
Non-thermal bremsstrahlung



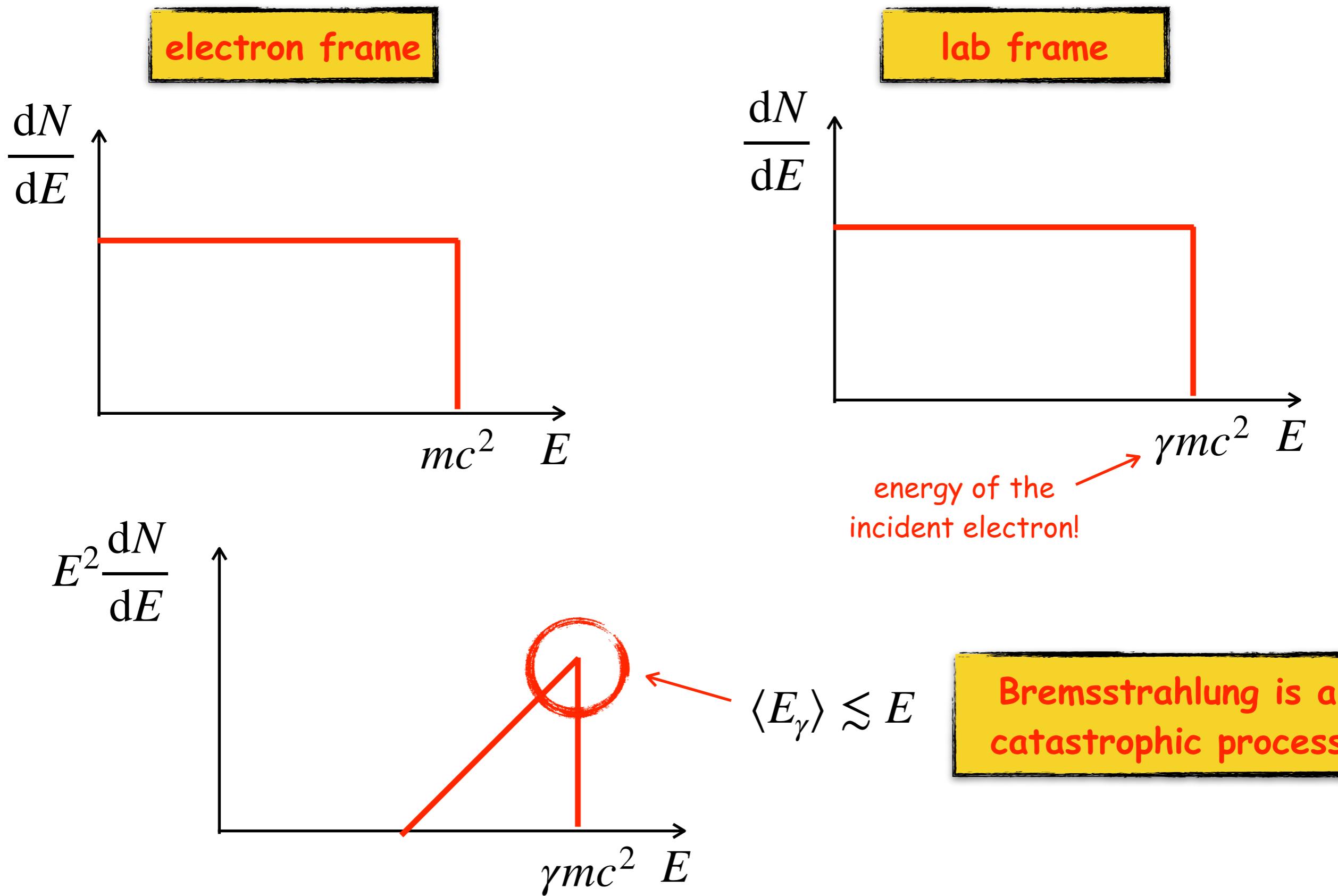
Non-thermal bremsstrahlung



Non-thermal bremsstrahlung



Non-thermal bremsstrahlung



Energy loss times in the ISM...

continuous losses →

$$\frac{dE}{dt} = \frac{4}{3} \sigma_T c \gamma^2 (\omega_B + \omega_{CMB})$$

synchrotron inverse Compton
↓ ↓
same importance
in the ISM !

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$$\tau_{syn/IC} \sim \frac{E}{dE/dt} \approx 1 \left(\frac{\omega_{TOT}}{0.25 \text{ eV/cm}^3} \right)^{-1} \left(\frac{E}{\text{TeV}} \right)^{-1} \text{Myr}$$

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$$\tau_{loss} \sim \left(\kappa n_{gas} \sigma c \right)^{-1}$$

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$$\tau_{pp} \sim 60 \left(\frac{n_{gas}}{\text{cm}^{-3}} \right)^{-1} \text{Myr}$$

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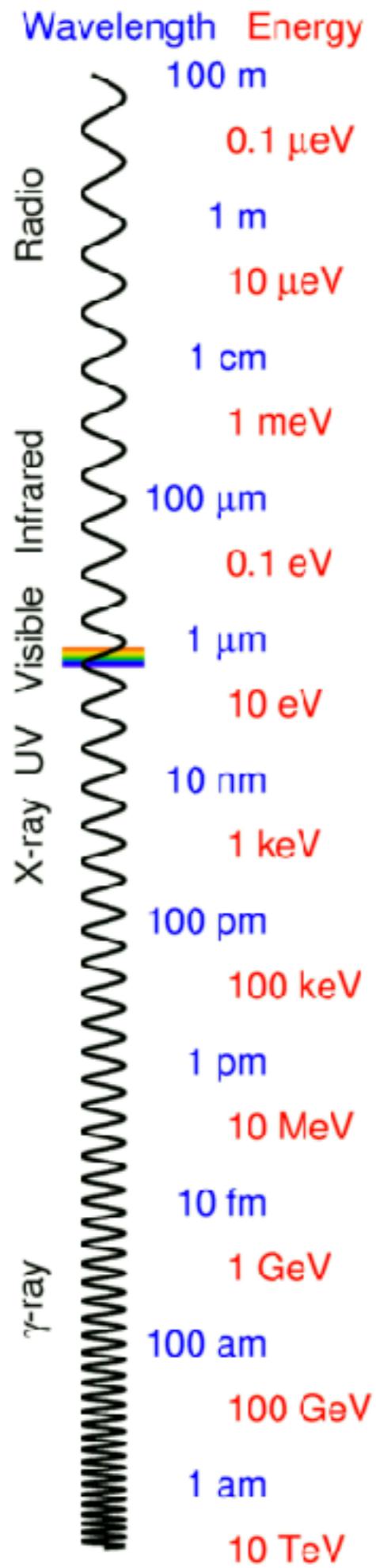
$$\tau_{pp} \sim 60 \left(\frac{n_{gas}}{\text{cm}^{-3}} \right)^{-1} \text{Myr}$$

relativistic Bremsstrahlung →

$$\tau_{Brem} \sim 30 \left(\frac{n_{gas}}{\text{cm}^{-3}} \right)^{-1} \text{Myr}$$

ICS more
 effective in the
 TeV domain

GALACTIC NON-THERMAL EMISSIONS



$E > 280 \text{ MeV}$
pp interactions
protons

$E \sim 10 \text{ GeV}$
 100 TeV

synchrotron emission
electrons in gal. B

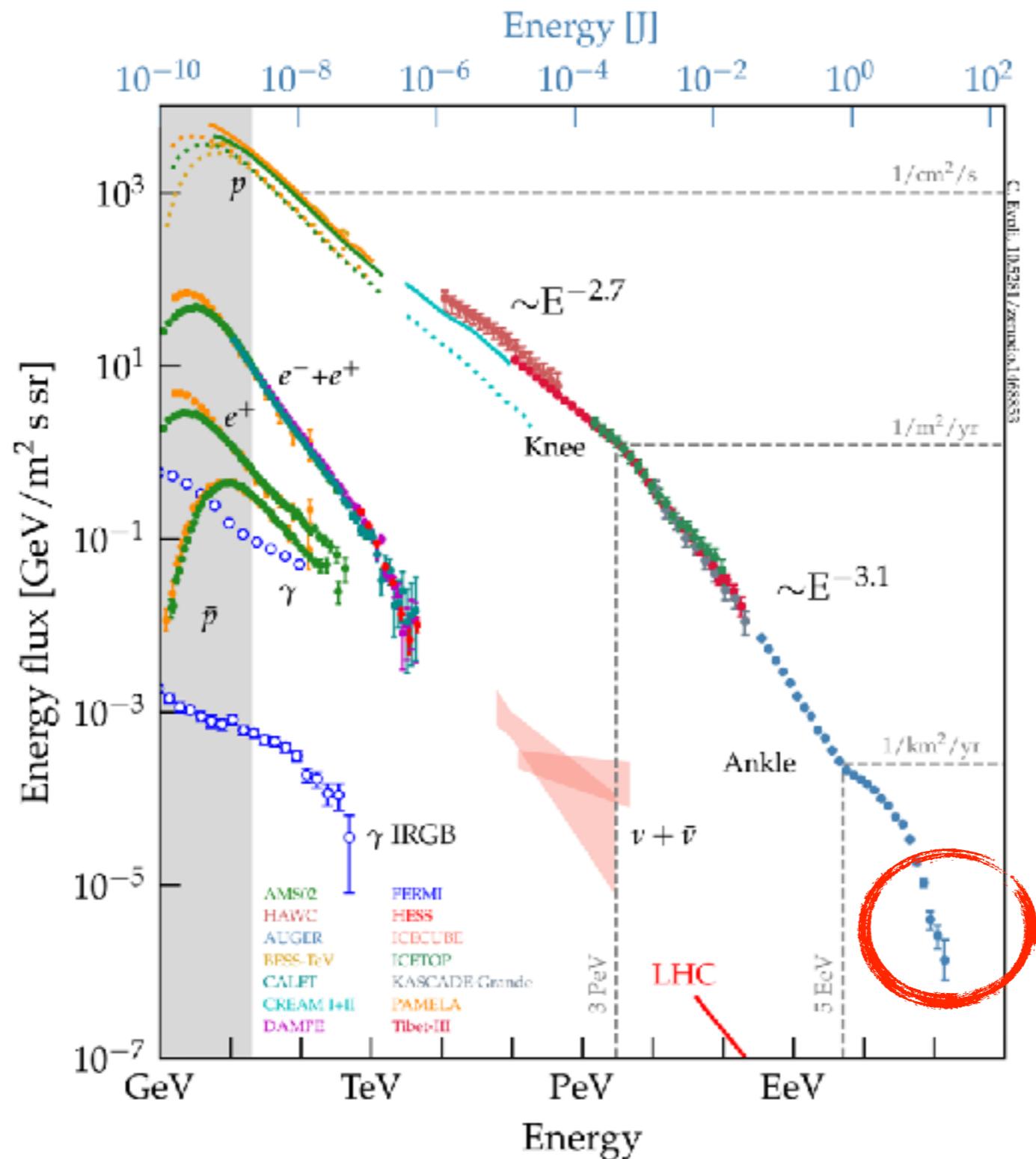
$E \sim \text{keV}$
 MeV
 GeV
 TeV

Bremsstrahlung emission
electrons

$E \sim \text{GeV}$
 TeV
 30 TeV

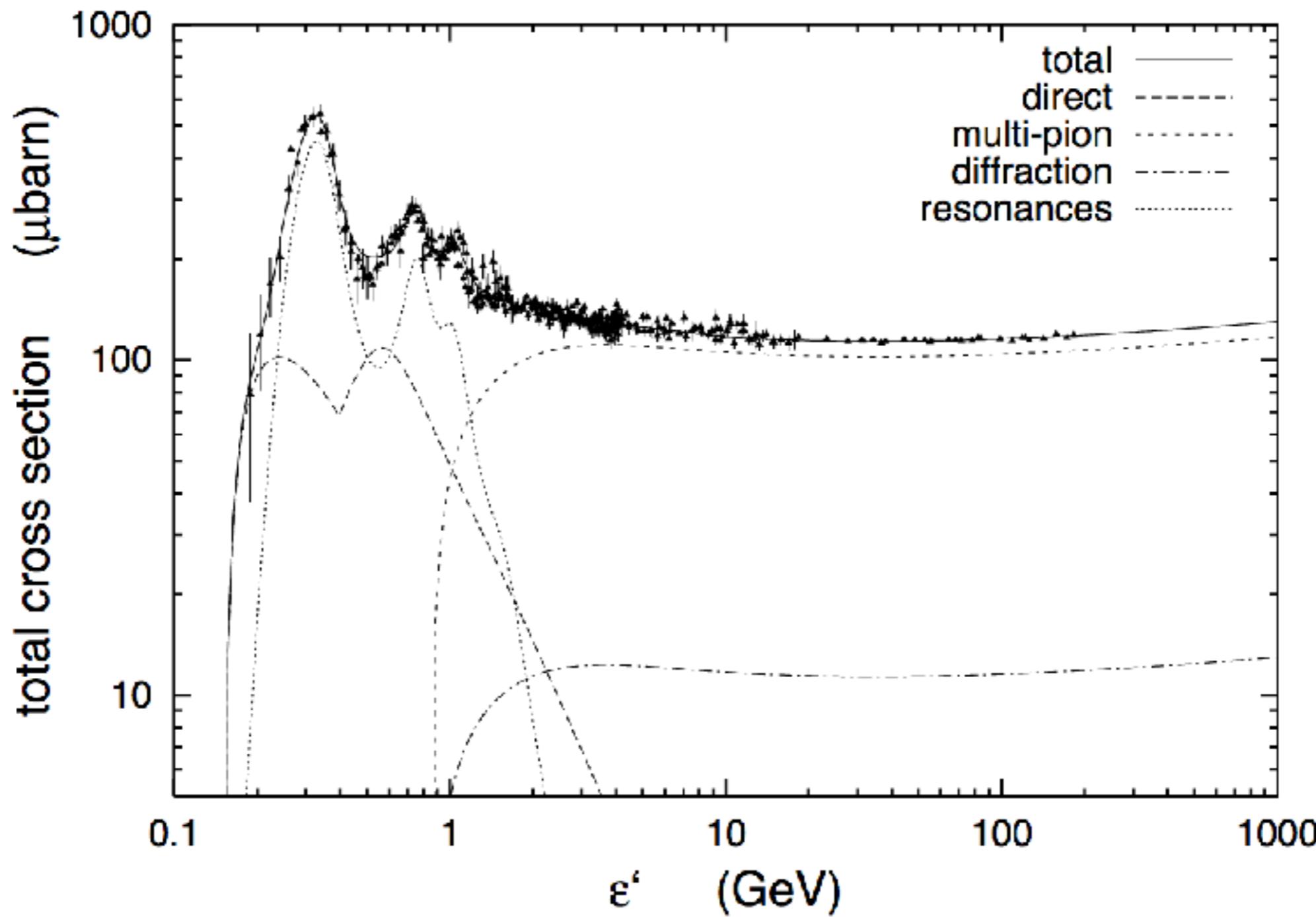
inverse Compton scattering
electrons in CMB

Question: where does the cosmic ray spectrum ends?



Photomeson production:

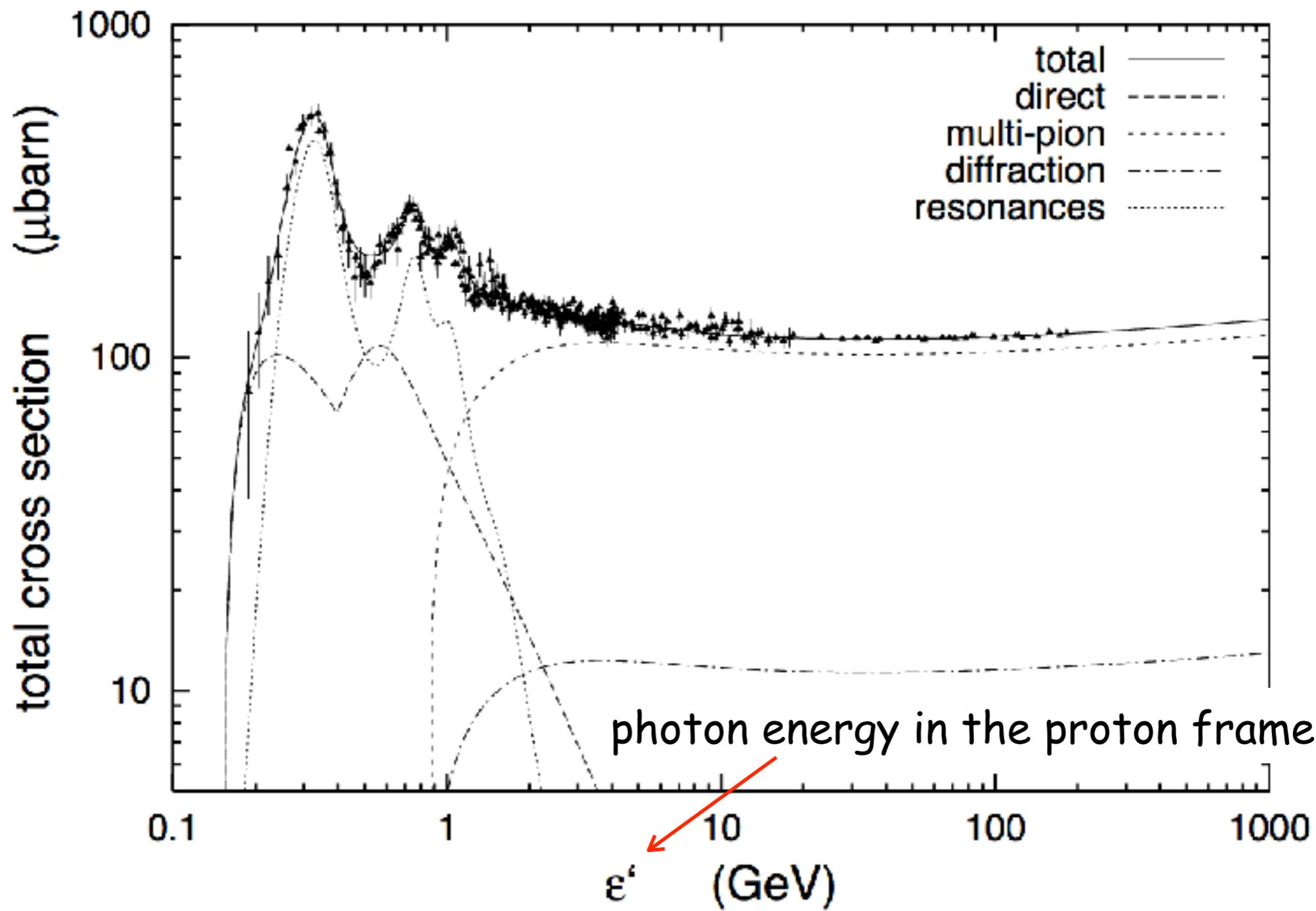
$p\gamma \rightarrow n\pi^+$ or $p\pi^0$



Mucke+ 1999

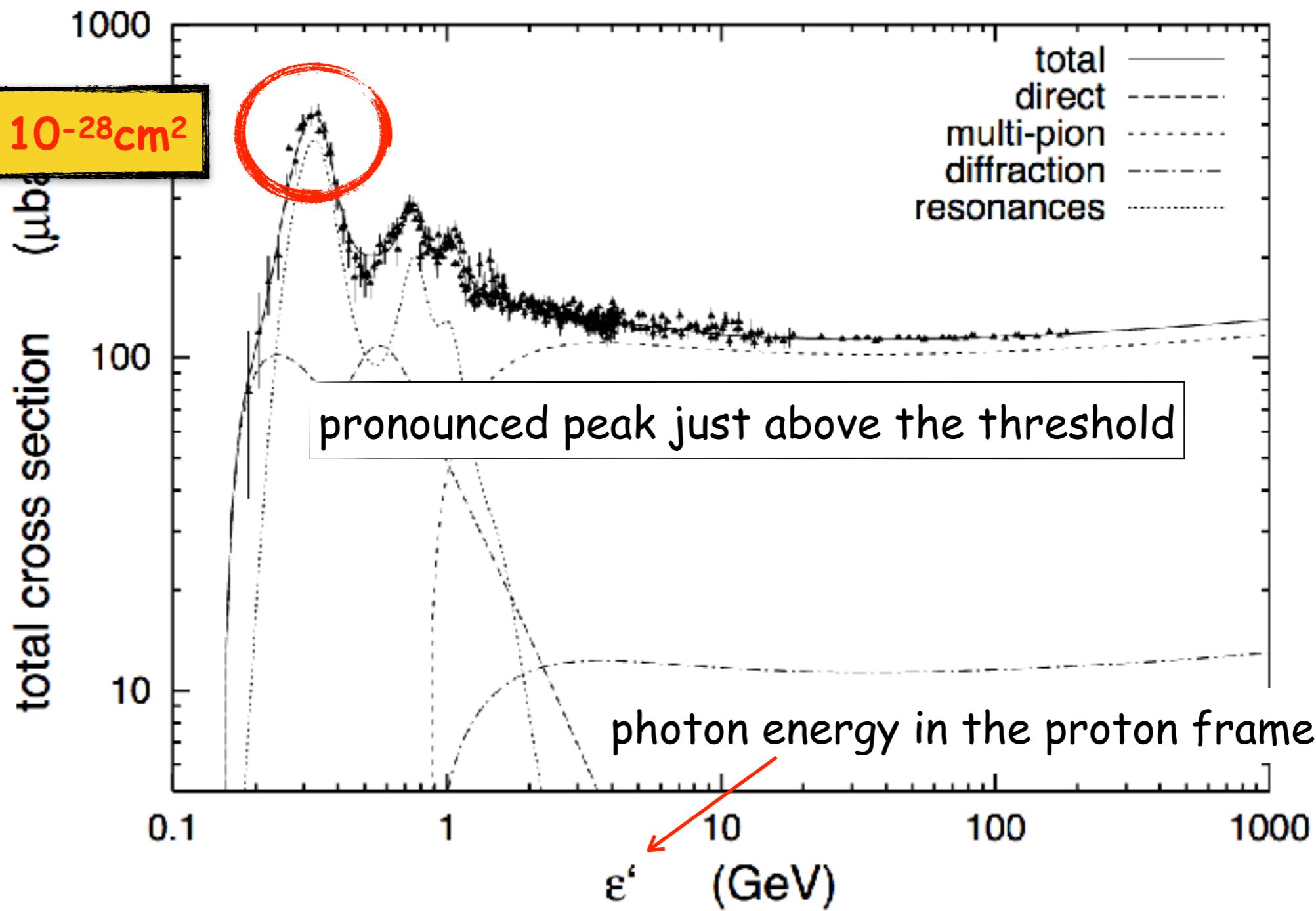
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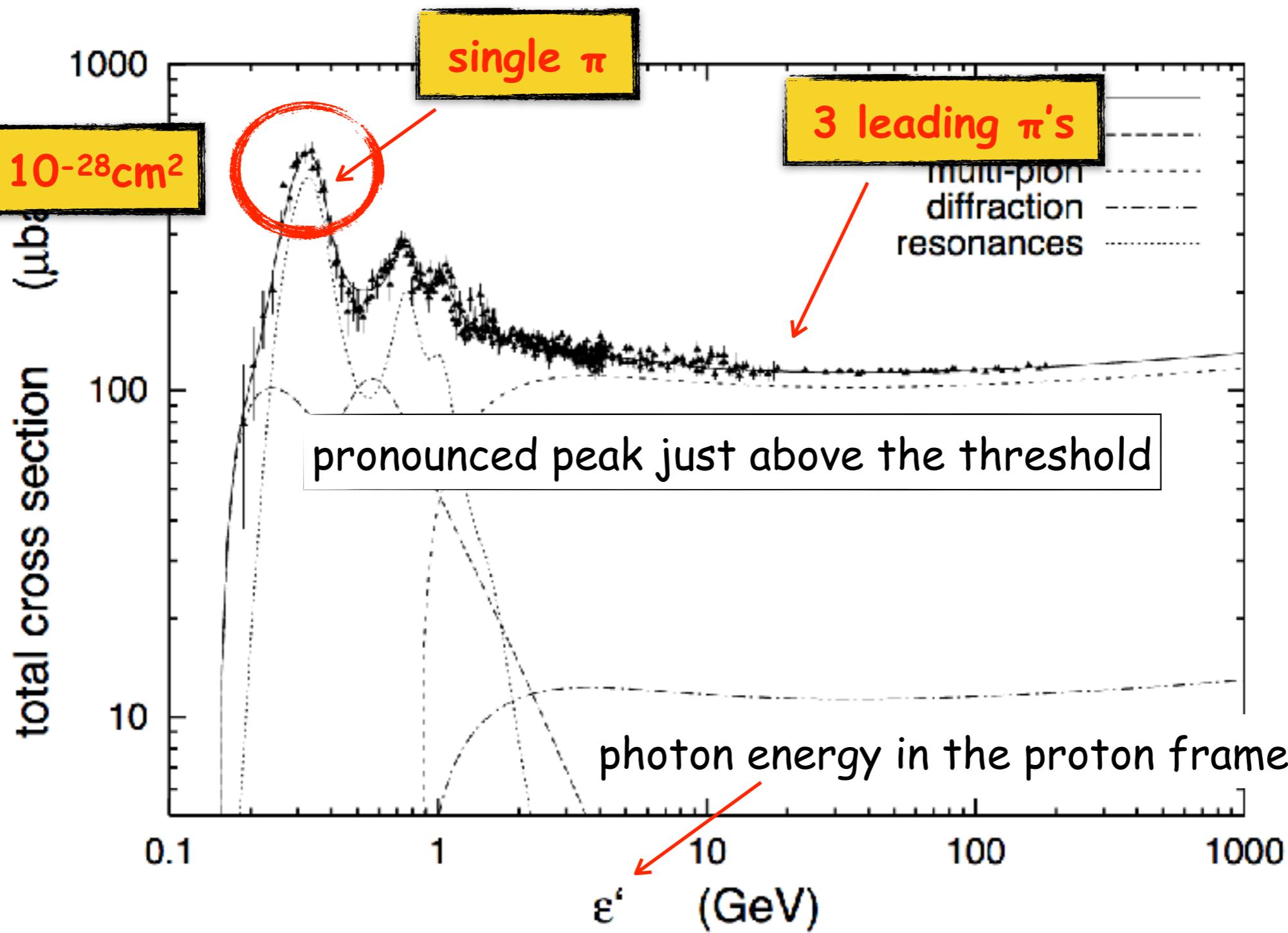


Photomeson production:

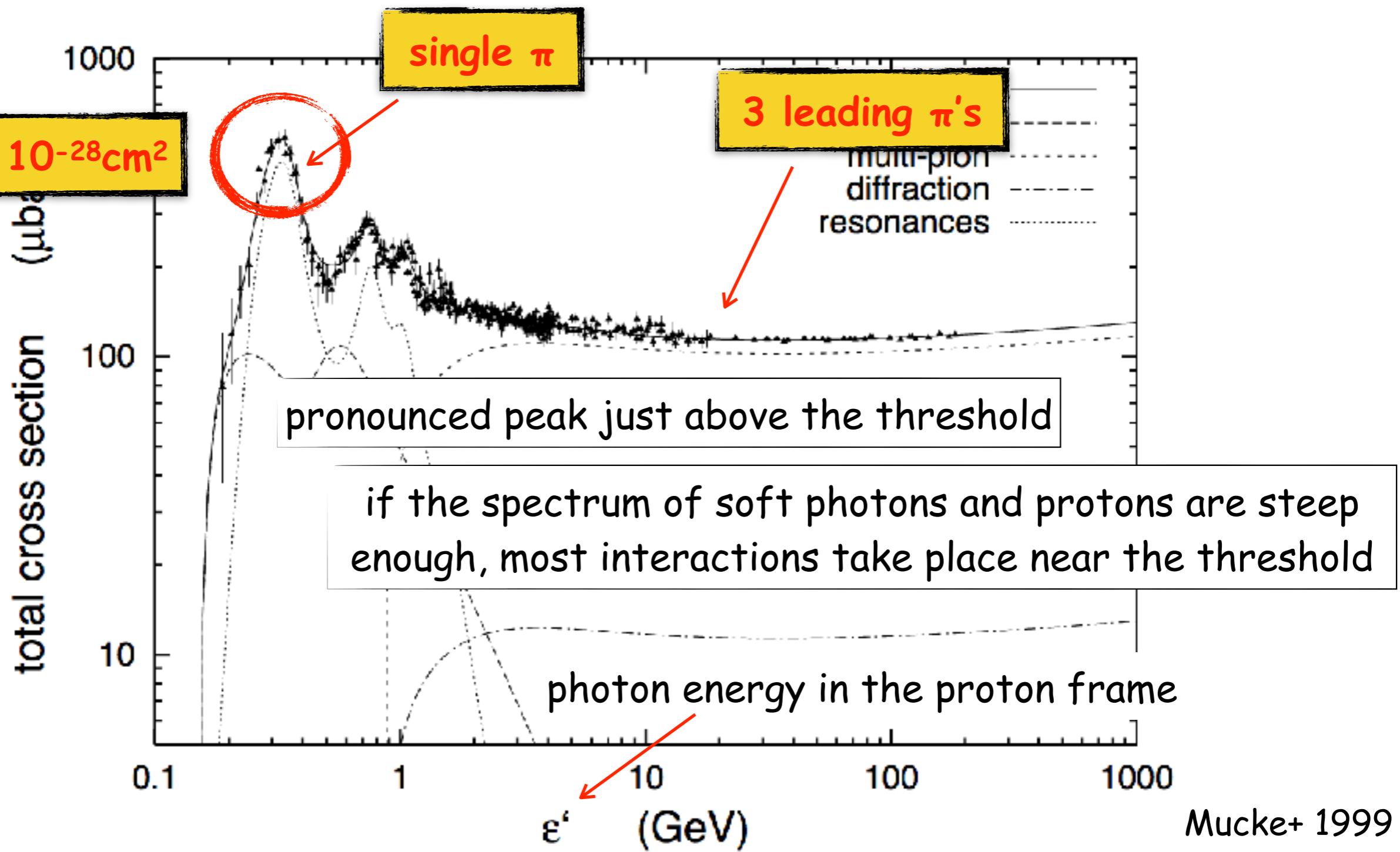
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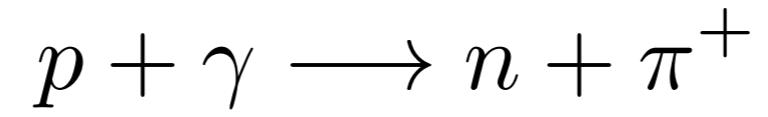
Photomeson production:



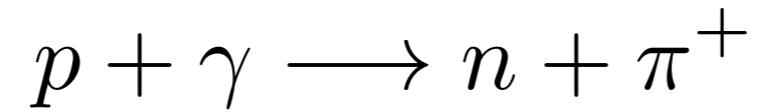
Photomeson production:



Photomeson production: threshold

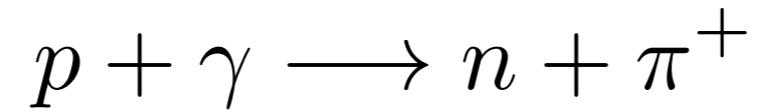


Photomeson production: threshold



energy in the center of mass frame

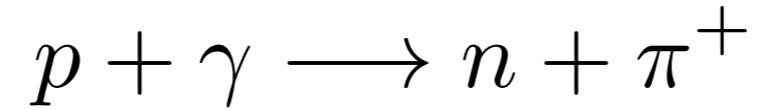
Photomeson production: threshold



energy in the center of mass frame

before the collision \rightarrow $s^2 = (E_p + \epsilon_\gamma)^2 - (\vec{p}_p + \vec{p}_\gamma)^2$

Photomeson production: threshold



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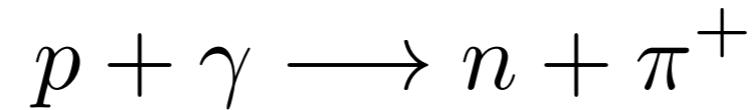
after the collision

and

$$\rightarrow s_{th} = m_p + m_\pi$$

at the threshold

Photomeson production: threshold



energy in the center of mass frame

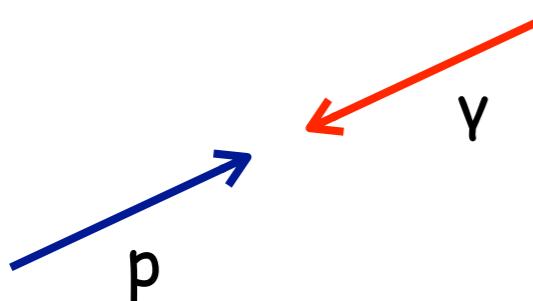
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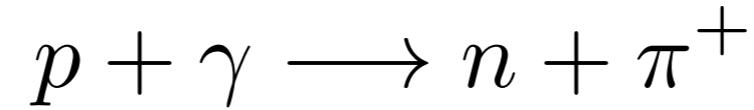
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Photomeson production: threshold



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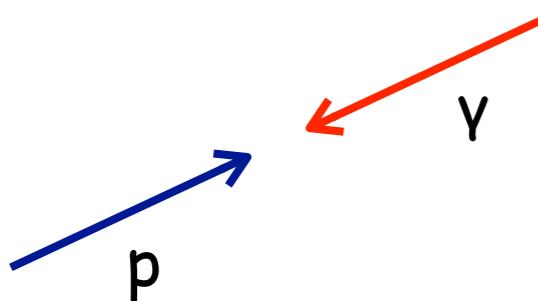
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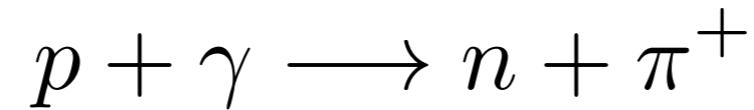
$$\rightarrow s_{th} = m_p + m_\pi$$

at the threshold



$$E_p^{min} \approx 60 \left(\frac{\epsilon_\gamma}{\text{eV}} \right)^{-1} \text{PeV}$$

Photomeson production: threshold



energy in the center of mass frame

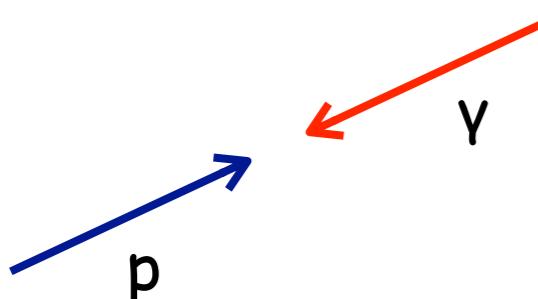
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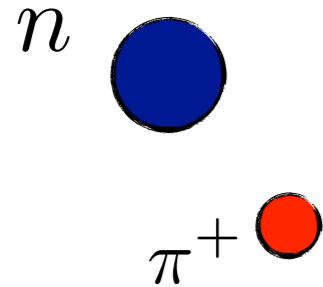
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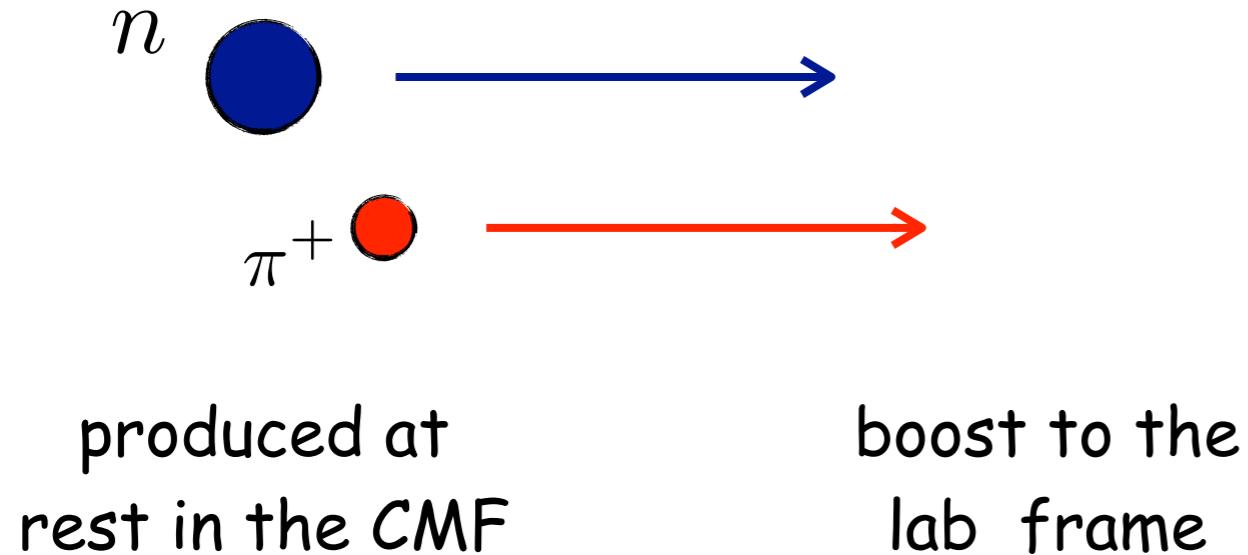
for CMB photons this is $\sim 10^{20}$ eV !

Photomeson production: threshold

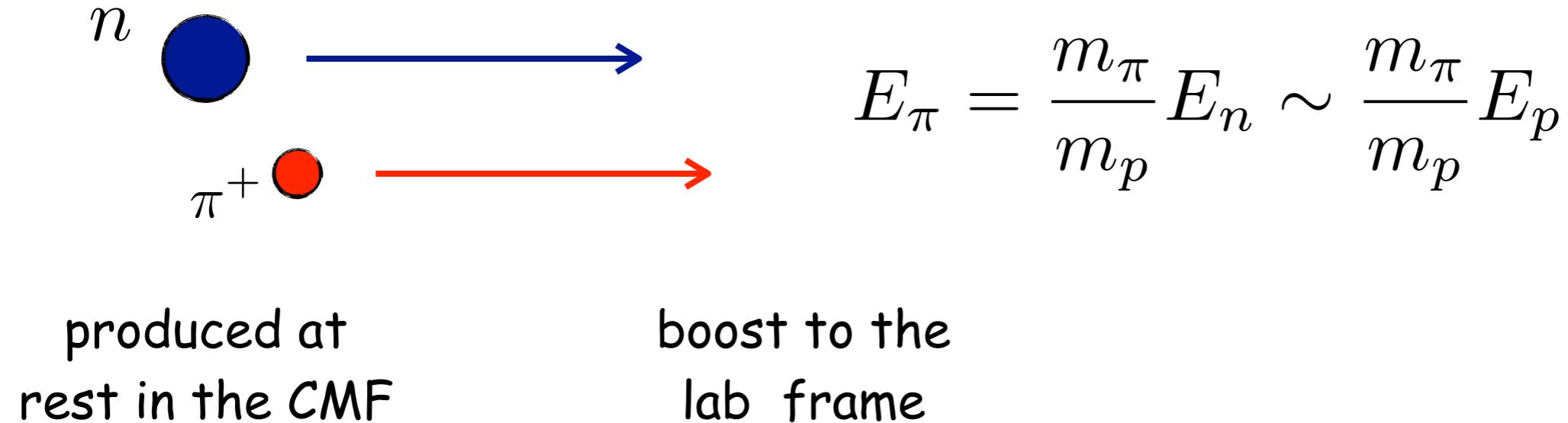


produced at
rest in the CMF

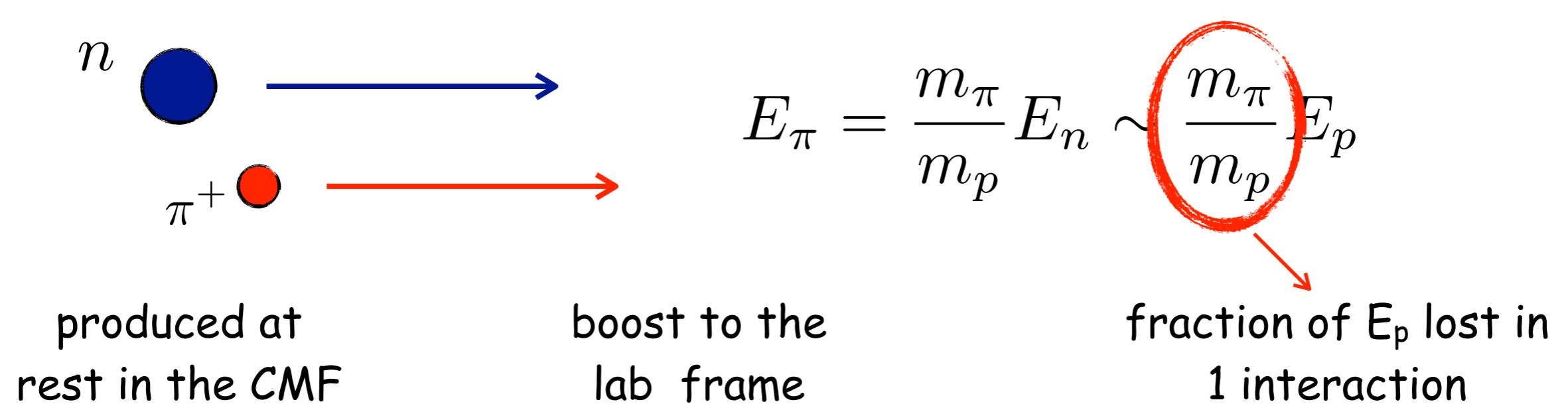
Photomeson production: threshold



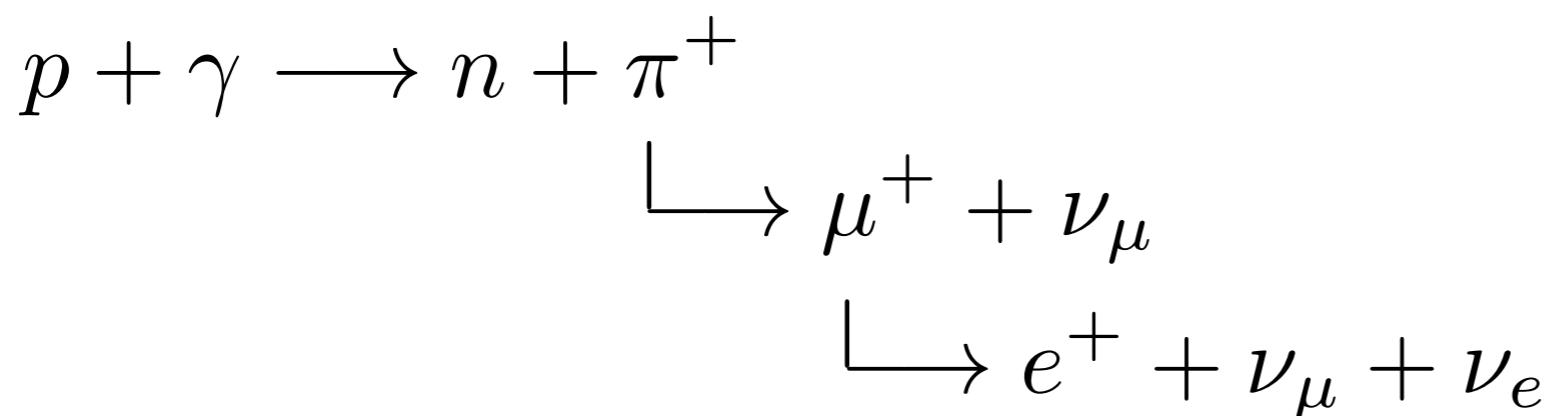
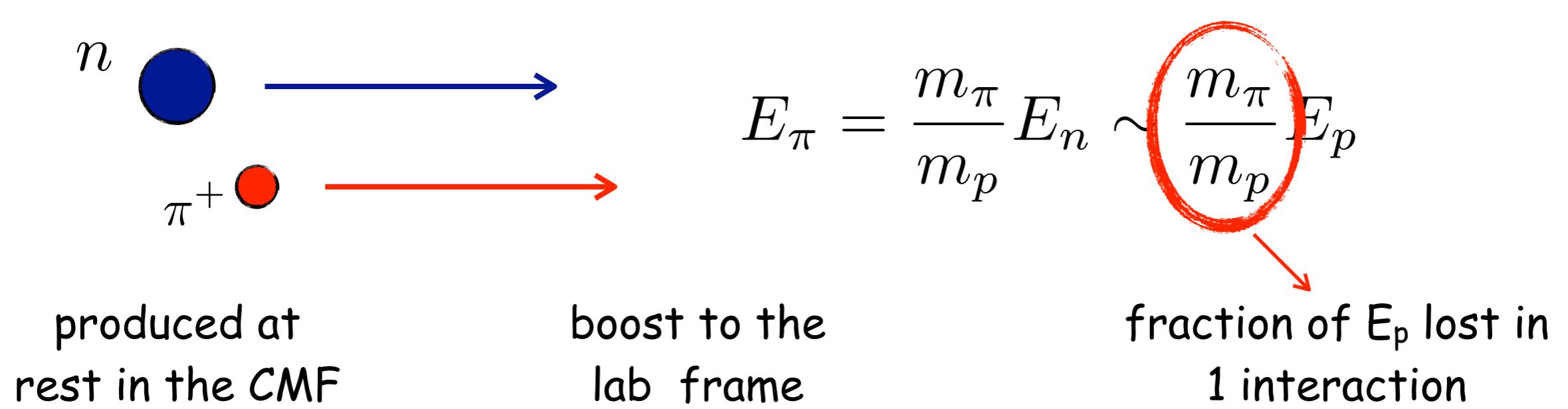
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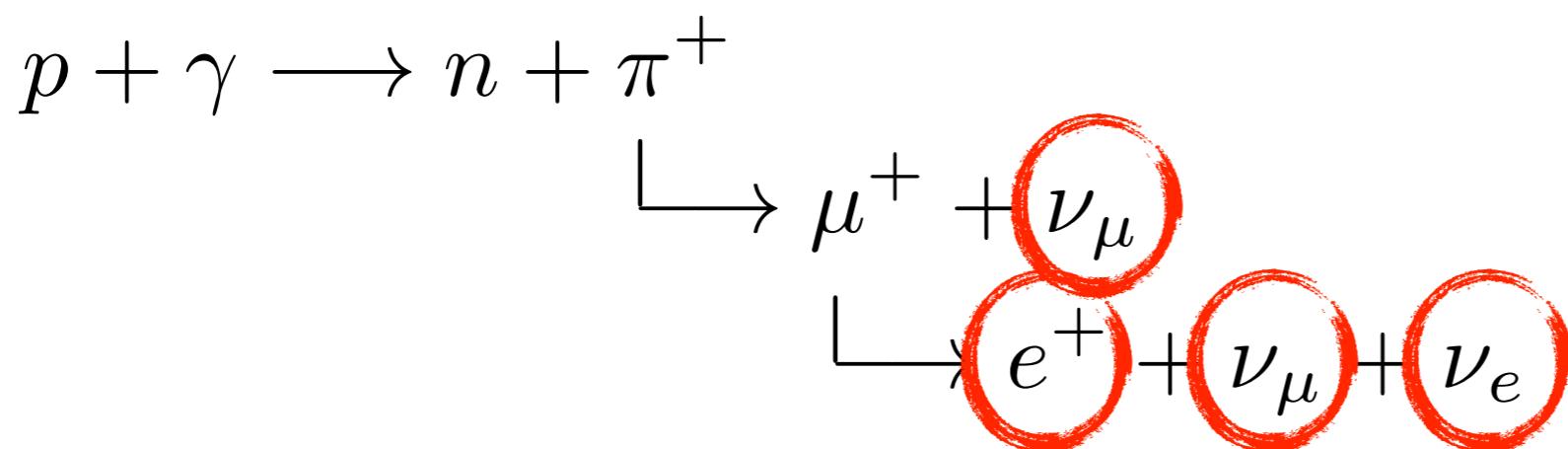
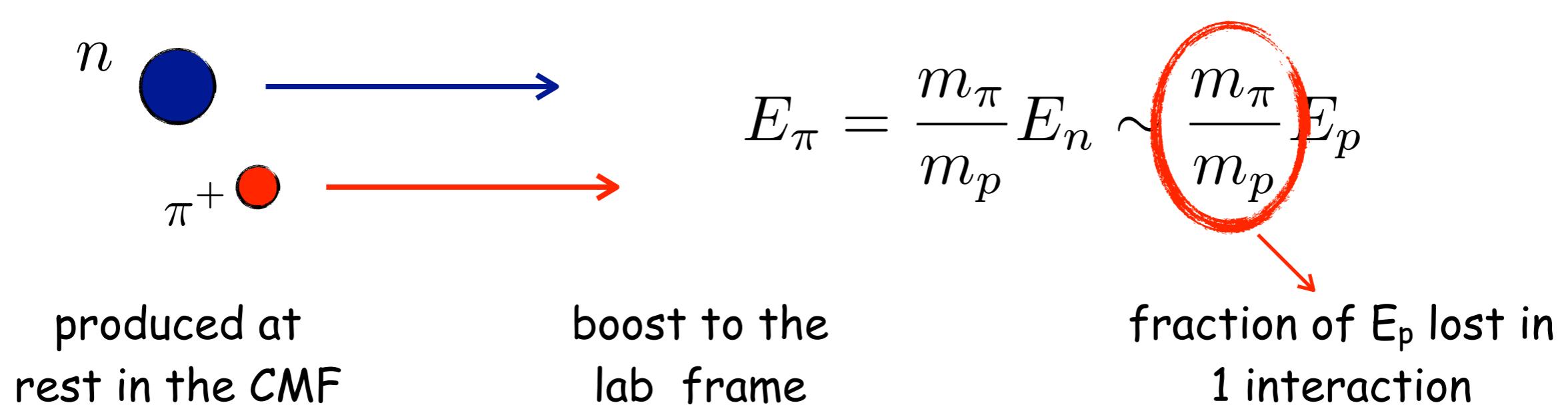
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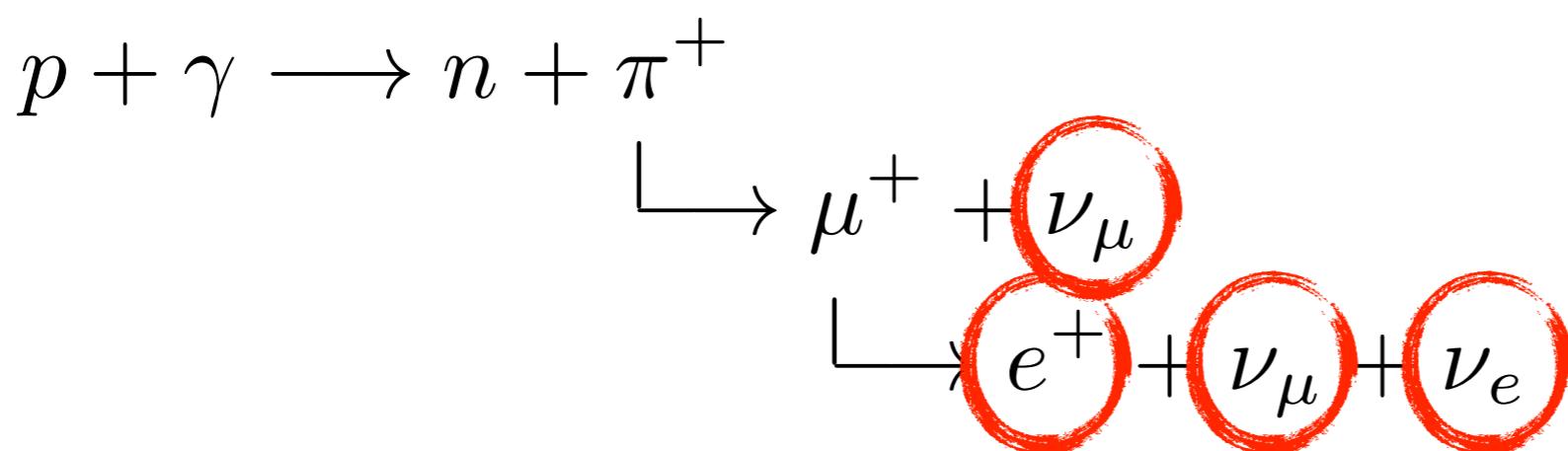
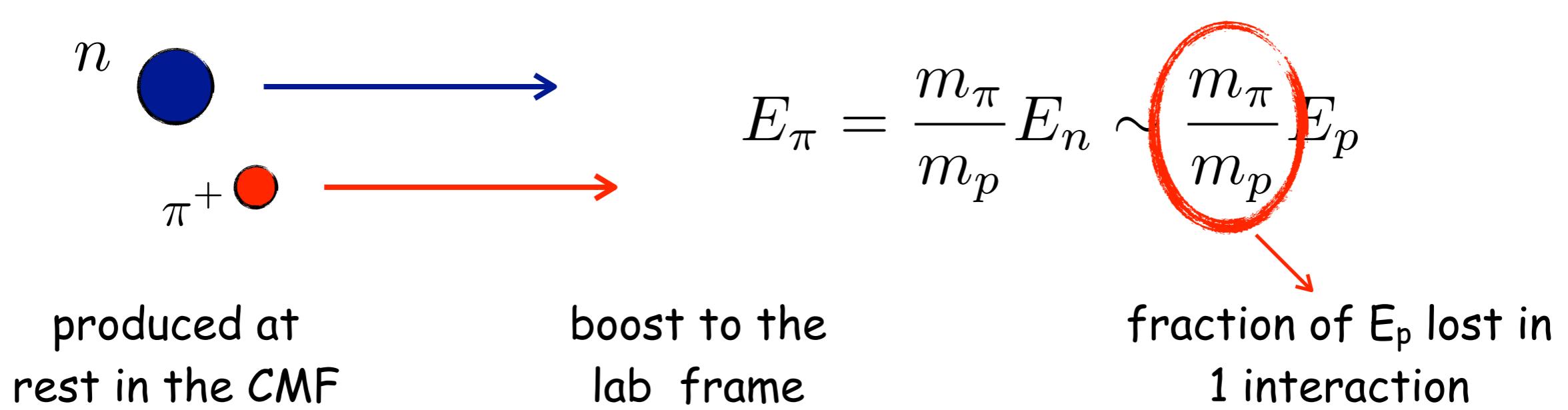


Photomeson production: threshold



4 stable particles carrying ~the same energy

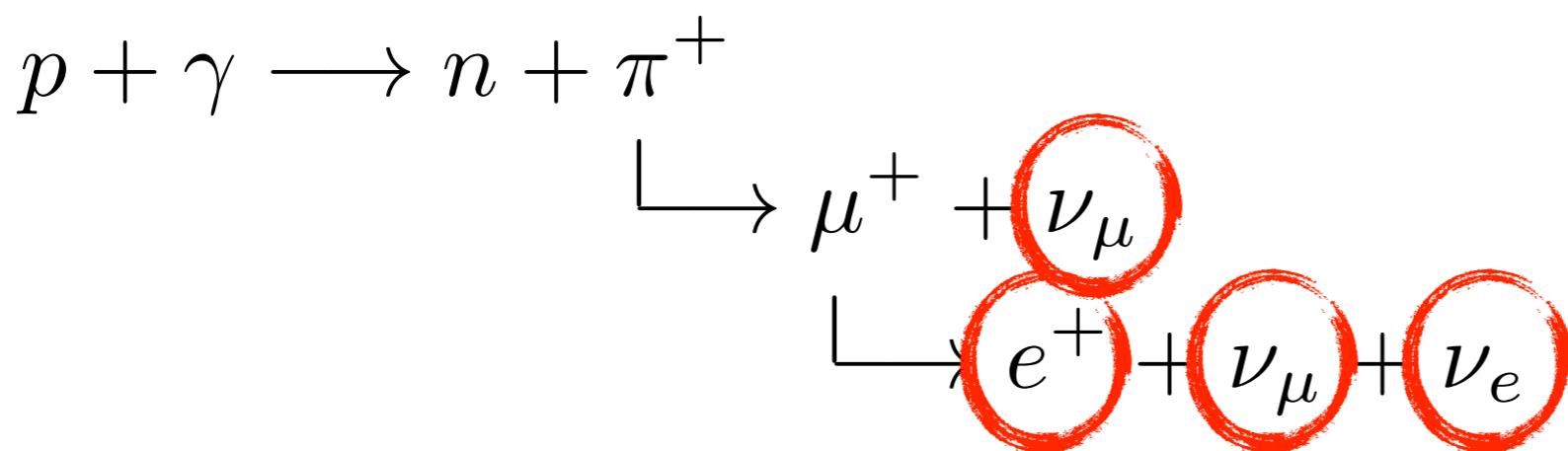
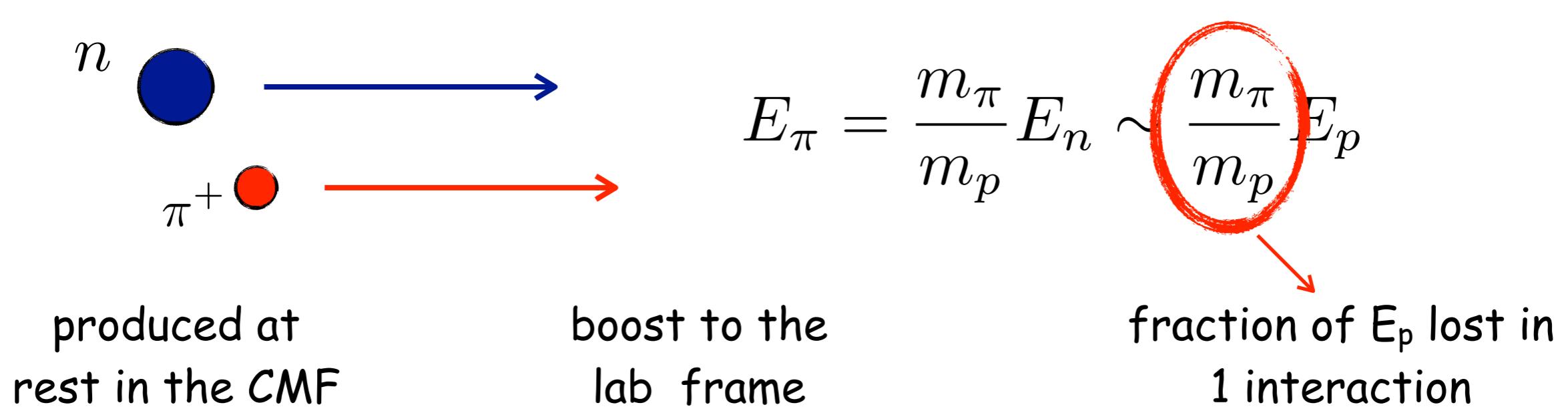
Photomeson production: threshold



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~the same energy

$$E_\nu \sim \left(\frac{m_\pi}{4m_p} \right) E_p$$

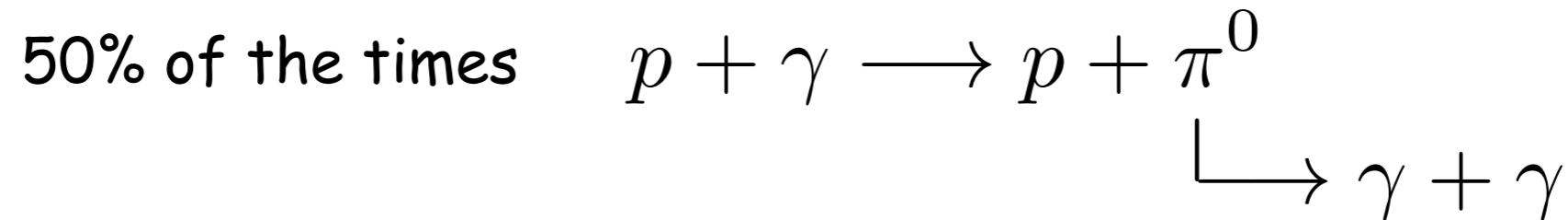
Photomeson production: threshold



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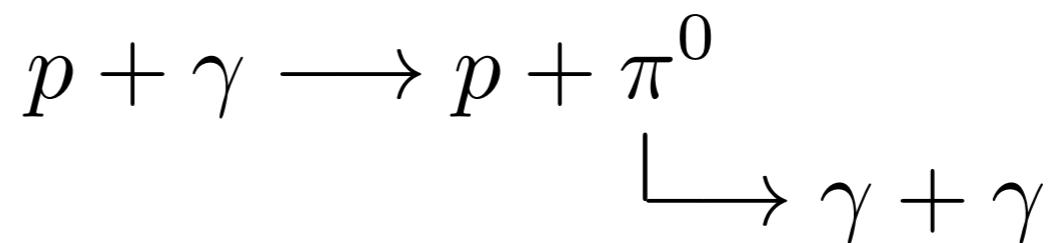
$$E_\nu \sim \left(\frac{m_\pi}{4m_p} \right) E_p \approx 0.04 E_p$$

Absorption of gamma rays



Absorption of gamma rays

50% of the times



- the π^0 carries a fraction of the proton energy equal to $\frac{m_\pi}{m_p}$

Absorption of gamma rays

50% of the times $p + \gamma \longrightarrow p + \pi^0$

$$\downarrow \rightarrow \gamma + \gamma$$

■ the π^0 carries a fraction of the proton energy equal to $\frac{m_\pi}{m_p}$

■ 2 stable particles of average energy

$$E_\gamma \sim \left(\frac{m_\pi}{2m_p} \right) E_p \sim 2 E_\nu$$

Absorption of gamma rays

50% of the times $p + \gamma \longrightarrow p + \pi^0$

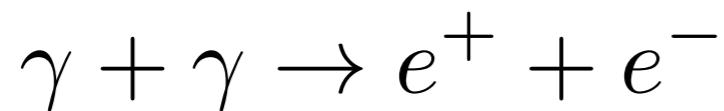
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■ 2 stable particles of average energy

threshold energy pair production

$$E_\gamma \sim \left(\frac{m_\pi}{2m_p} \right) E_p \sim 2 E_\nu$$



$$E_\gamma \epsilon_\gamma (1 - \cos \vartheta) > 2 m_e^2$$

Absorption of gamma rays

50% of the times $p + \gamma \longrightarrow p + \pi^0$

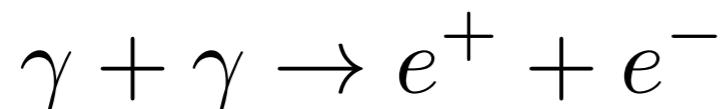
$$\downarrow \rightarrow \gamma + \gamma$$

■ the π^0 carries a fraction of the proton energy equal to $\frac{m_\pi}{m_p}$

■ 2 stable particles of average energy

threshold energy pair production

$$E_\gamma \sim \left(\frac{m_\pi}{2m_p} \right) E_p \sim 2 E_\nu$$

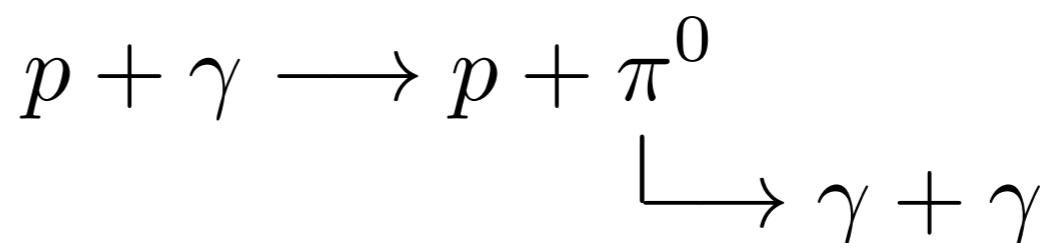


$$E_\gamma \epsilon_\gamma (1 - \cos \vartheta) > 2 m_e^2$$

$$E_\gamma^{min} \approx 0.3 \left(\frac{\epsilon_\gamma}{\text{eV}} \right)^{-1} \text{TeV}$$

Absorption of gamma rays

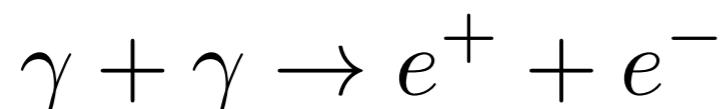
50% of the times



- the π^0 carries a fraction of the proton energy equal to $\frac{m_\pi}{m_p}$

- 2 stable particles of average energy

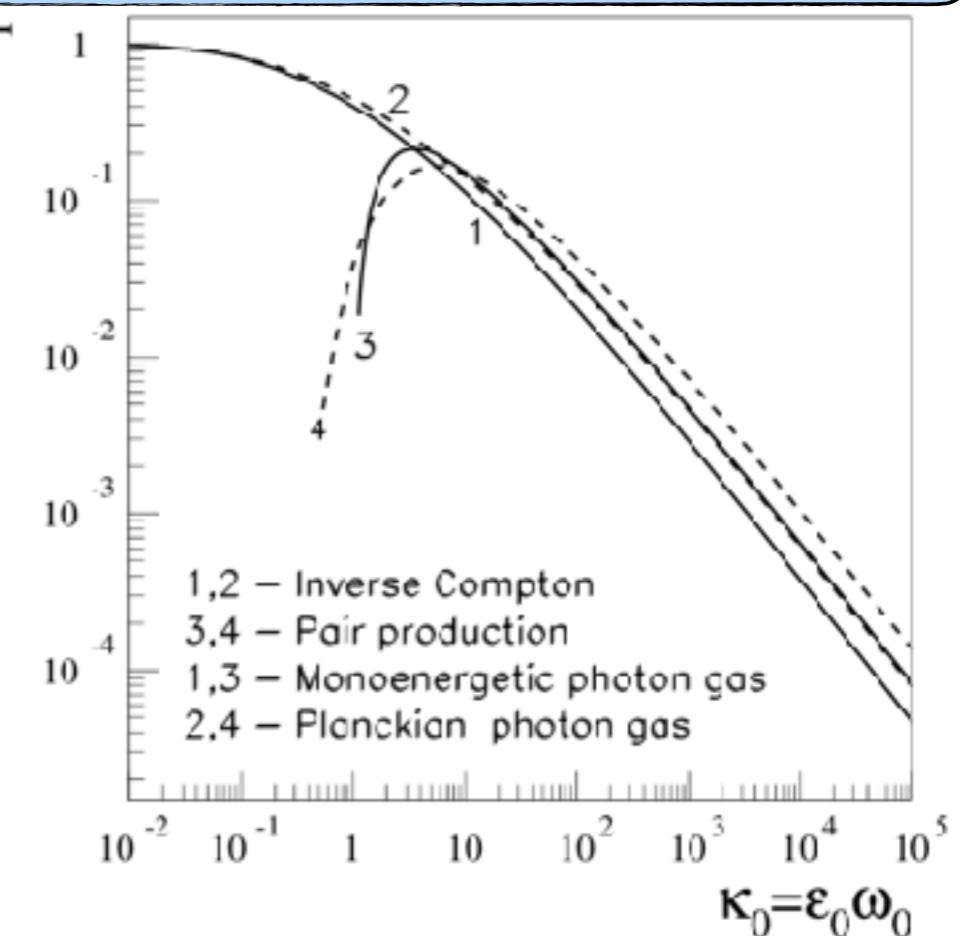
threshold energy pair production



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$$E_\gamma \sim \left(\frac{m_\pi}{2m_p} \right) E_p \sim 2 E_\nu$$



Aharonian's book

Absorption of gamma rays

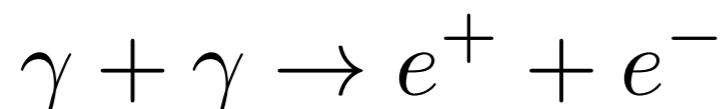
50% of the times $p + \gamma \longrightarrow p + \pi^0$

$$\downarrow \rightarrow \gamma + \gamma$$

■ the π^0 carries a fraction of the proton energy equal to $\frac{m_\pi}{m_p}$

■ 2 stable particles of average energy

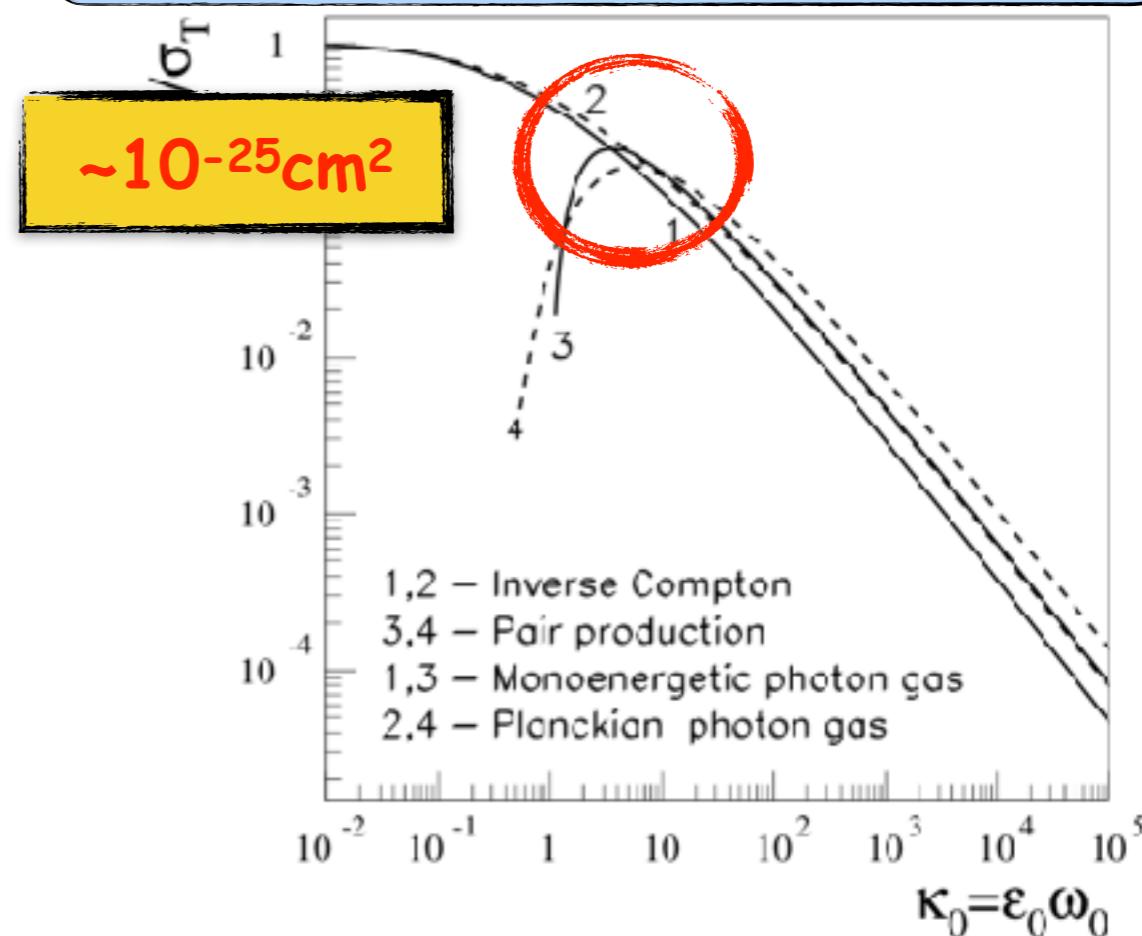
threshold energy pair production



$$E_\gamma \epsilon_\gamma (1 - \cos \vartheta) > 2 m_e^2$$

$$E_\gamma^{\min} \approx 0.3 \left(\frac{\epsilon_\gamma}{\text{eV}} \right)^{-1} \text{TeV}$$

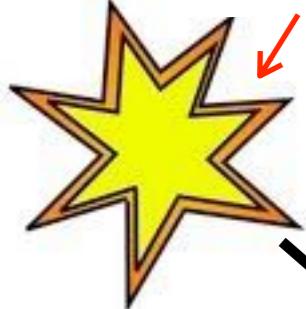
$$E_\gamma \sim \left(\frac{m_\pi}{2m_p} \right) E_p \sim 2 E_\nu$$



Where do photons go?



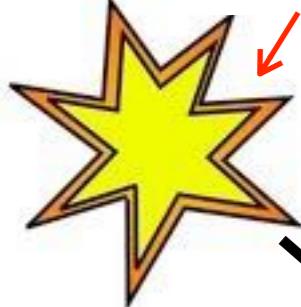
CR source



Where do photons go?



CR source



Where do photons go?

electron

photon

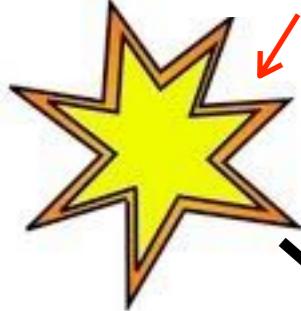
Klein-Nishina
cascade

$$E_\gamma \epsilon_\gamma \gg m_e^2$$

inverse Compton + pair production



CR source



Where do photons go?

electron

photon

Klein-Nishina
cascade

$E_\gamma \epsilon_\gamma \gg m_e^2$

inverse Compton + pair production

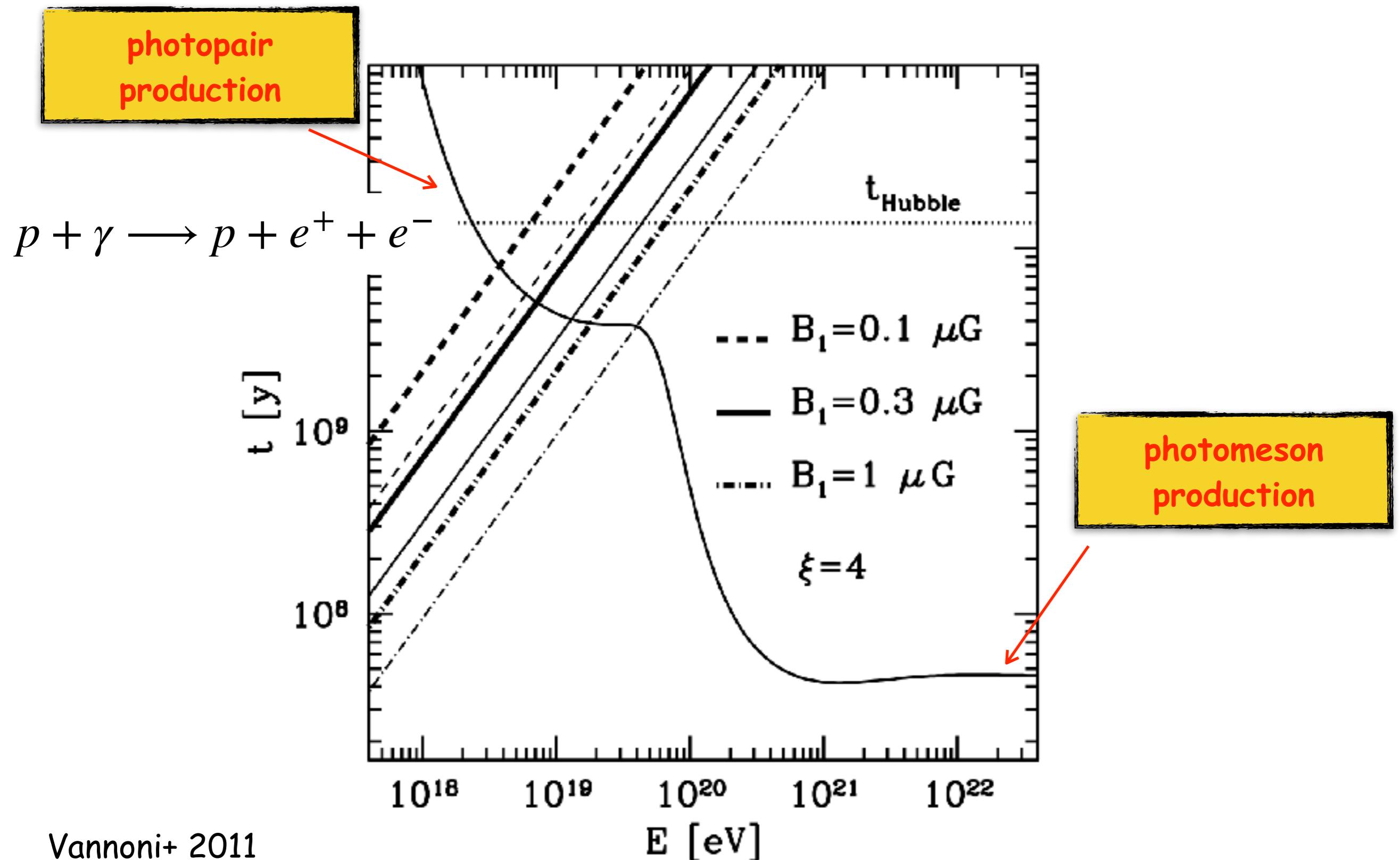
$E_\gamma \epsilon_\gamma \gtrsim m_e^2$

Thompson cascade

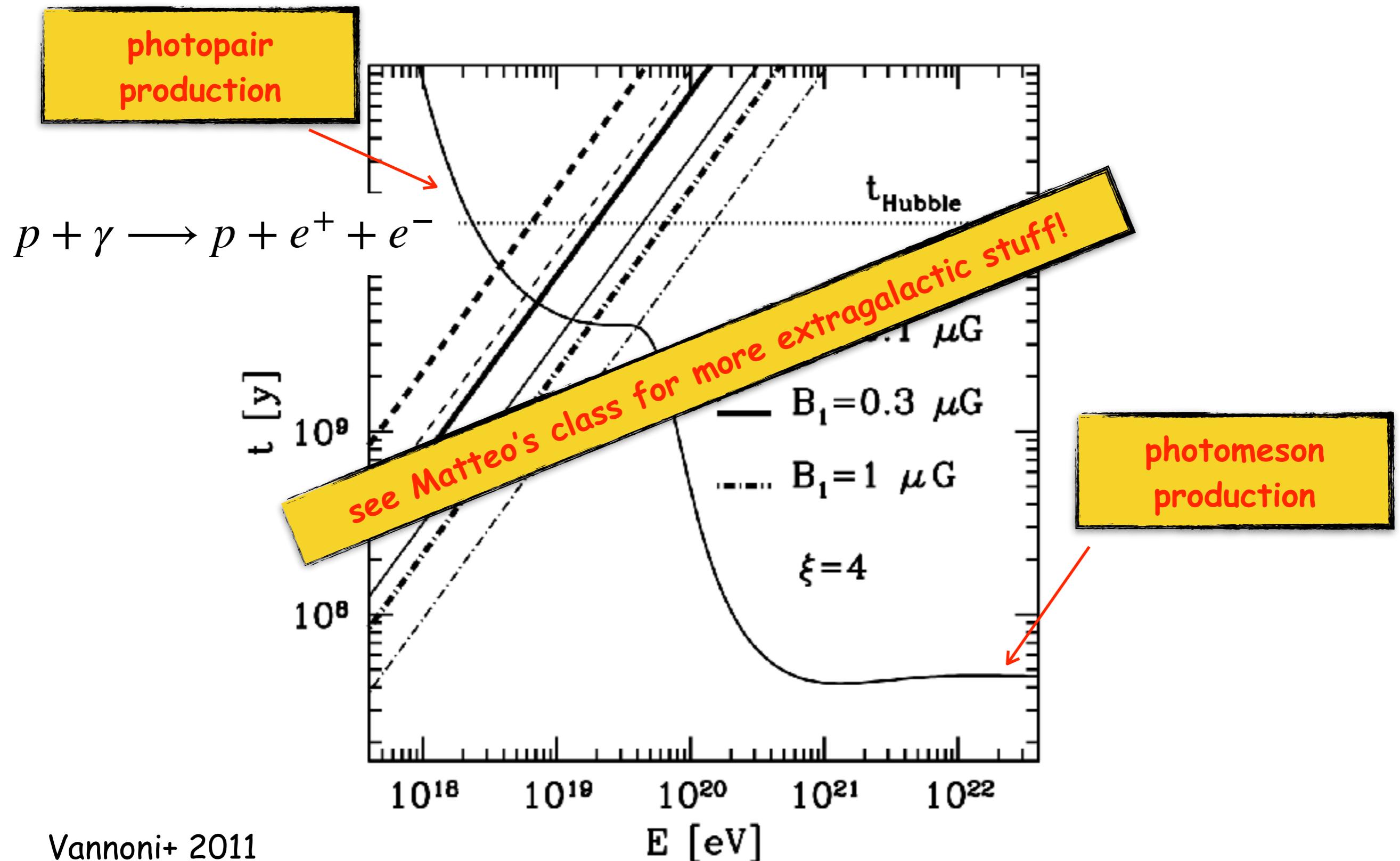
<100 GeV



Photopair production



Photopair production



next class: apply all this to "Galactic sources"...

