Document number:
 P0237R7

 Revises:
 P0237R6

 Date:
 2017-06-19

Project: ISO JTC1/SC22/WG21: Programming Language C++

Audience: LEWG

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Wording for fundamental bit manipulation utilities

Note: this is an early draft. It's known to be incomplet and incorrekt, and it has lots of bad formatting.

1 Bit manipulation library

[bit]

1.1 General [bit.general]

This Clause describes the contents of the header <bit> (1.2) that provides components that C++ programs may use to access, manipulate and process both individual bits and bit sequences.

1.2 Header

 synopsis

[bit.syn]

```
namespace std {
  // 1.4, class bit_value
  class bit_value;
  // 1.5, class template bit_reference
  template <class WordType> class bit_reference;
  // 1.6, class template bit_pointer
  template <class WordType> class bit_pointer;
  // 1.7, class template bit_iterator
  template <class Iterator> class bit_iterator;
  // 1.4.9, bit_value operations
  constexpr bit_value operator~(bit_value rhs) noexcept;
  constexpr bit_value operator&(bit_value lhs, bit_value rhs) noexcept;
  constexpr bit_value operator|(bit_value lhs, bit_value rhs) noexcept;
  constexpr bit_value operator^(bit_value lhs, bit_value rhs) noexcept;
  // 1.5.9, bit_reference swap
  template <class T, class U>
    void swap(bit_reference<T> lhs, bit_reference<U> rhs) noexcept;
  template <class T>
    void swap(bit_reference<T> lhs, bit_value& rhs) noexcept;
  template <class U>
    void swap(bit_value& lhs, bit_reference<U> rhs) noexcept;
  // 1.6.7, bit_pointer arithmetic
  template <class T>
    constexpr bit_pointer<T> operator+(typename bit_pointer<T>::difference_type n,
                                        bit_pointer<T> x);
  template <class T, class U>
    constexpr typename std::common_type<</pre>
      typename bit_pointer<T>::difference_type,
      typename bit_pointer<U>::difference_type
    >::type operator-(bit_pointer<T> lhs, bit_pointer<U> rhs);
  // 1.7.7, bit_iterator arithmetic
 template <class T>
    constexpr bit_iterator<T> operator+(typename bit_iterator<T>::difference_type n,
                                         const bit_iterator<T>& i);
  template <class T, class U>
    constexpr typename std::common_type<</pre>
```

§ 1.2

```
typename bit_iterator<T>::difference_type,
    typename bit_iterator<U>::difference_type
 >::type operator-(const bit_iterator<T>& lhs, const bit_iterator<U>& rhs);
// 1.4.9, bit_value comparisons
constexpr bool operator==(bit_value lhs, bit_value rhs) noexcept;
constexpr bool operator!=(bit_value lhs, bit_value rhs) noexcept;
constexpr bool operator<(bit_value lhs, bit_value rhs) noexcept;</pre>
constexpr bool operator<=(bit_value lhs, bit_value rhs) noexcept;</pre>
constexpr bool operator>(bit_value lhs, bit_value rhs) noexcept;
constexpr bool operator>=(bit_value lhs, bit_value rhs) noexcept;
// 1.6.7, bit_pointer comparisons
template <class T, class U>
  constexpr bool operator==(bit_pointer<T> lhs, bit_pointer<U> rhs) noexcept;
template <class T, class U>
 constexpr bool operator!=(bit_pointer<T> lhs, bit_pointer<U> rhs) noexcept;
template <class T, class U>
 constexpr bool operator<(bit_pointer<T> lhs, bit_pointer<U> rhs) noexcept;
template <class T, class U>
 constexpr bool operator<=(bit_pointer<T> lhs, bit_pointer<U> rhs) noexcept;
template <class T, class U>
  constexpr bool operator>(bit_pointer<T> lhs, bit_pointer<U> rhs) noexcept;
template <class T, class U>
  constexpr bool operator>=(bit_pointer<T> lhs, bit_pointer<U> rhs) noexcept;
// 1.7.7, bit_iterator comparisons
template <class T, class U>
  constexpr bool operator==(const bit_iterator<T>& lhs, const bit_iterator<U>& rhs);
template <class T, class U>
 constexpr bool operator!=(const bit_iterator<T>& lhs, const bit_iterator<U>& rhs);
template <class T, class U>
 constexpr bool operator<(const bit_iterator<T>& lhs, const bit_iterator<U>& rhs);
template <class T, class U>
 constexpr bool operator<=(const bit_iterator<T>& lhs, const bit_iterator<U>& rhs);
template <class T, class U>
  constexpr bool operator>(const bit_iterator<T>& lhs, const bit_iterator<U>& rhs);
template <class T, class U>
 constexpr bool operator>=(const bit_iterator<T>& lhs, const bit_iterator<U>& rhs);
// 1.4.9, bit_value input and output
template <class CharT, class Traits>
 basic_istream<CharT, Traits>& operator>>(basic_istream<CharT, Traits>& is,
                                           bit_value& x);
template <class CharT, class Traits>
 basic_ostream<CharT, Traits>& operator<<(std::basic_ostream<CharT, Traits>& os,
                                           bit_value x);
// 1.5.9, bit_reference input and output
template <class CharT, class Traits, class T>
 basic_istream<CharT, Traits>& operator>>(std::basic_istream<CharT, Traits>& is,
                                           bit_reference<T>& x);
template <class CharT, class Traits, class T>
  basic_ostream<CharT, Traits>& operator<<(std::basic_ostream<CharT, Traits>& os,
                                           bit_reference<T> x);
```

§ 1.2

```
// 1.3, helper class binary_digits
template <class T> struct binary_digits;
template <class T> constexpr binary_digits_v = binary_digits<T>::value;

// 1.4.10, bit_value objects
static constexpr bit_value bit_zero = bit_value(0U);
static constexpr bit_value bit_one = bit_value(1U);
```

1.3 Helper class binary_digits

[bit.helper]

1.3.1 Class binary_digits overview

[bit.helper.overview]

```
template <class UIntType> struct binary_digits
: public integral_constant<size_t, numeric_limits<UIntType>::digits> { };
```

Requires: UIntType shall be a (possibly cv-qualified) unsigned integer type. [Note: This excludes (possibly cv-qualified) bool. —end note]

Remarks: Specialization of this helper class for a type T informs other library components that this type T corresponds to a word type whose bits can be accessed through bit_value, bit_reference, bit_pointer and bit_iterator.

1.3.2 Class binary digits specializations

[bit.helper.specializations]

```
template <> struct binary_digits<byte>
  : public integral_constant<size_t, numeric_limits<unsigned char>::digits> { };
template <> struct binary_digits<const byte>
  : public integral_constant<size_t, numeric_limits<const unsigned char>::digits> { };
template <> struct binary_digits<volatile byte>
  : public integral_constant<size_t, numeric_limits<volatile unsigned char>::digits> { };
template <> struct binary_digits<const volatile byte>
  : public integral_constant<size_t, numeric_limits<const volatile unsigned char>::digits> { };
```

The specialization of binary_digits for (possibly cv-qualified) byte makes byte a viable word type to hold bits.

1.3.3 Variable template binary_digits_v

[bit.helper.variable]

template <class T> constexpr binary_digits_v = binary_digits<T>::value;

The variable template binary_digits_v provides an access to the value member of binary_digits for convenience.

1.4 Class bit value

[bit.value]

1.4.1 Class bit_value overview

[bit.value.overview]

- A bit_value emulates the behavior an independent single bit, with no arithmetic behavior apart from bitwise compound assignment (1.4.5) and bitwise operators (1.4.9). It provides the bit modifier members (1.4.7) set, reset and flip. [Note: A bit_value is typically implemented as a wrapper around bool. —end note]
- ² A bit_value is implicitly convertible from a bit_reference (1.5), typically to create temporary values from references to bits.
- ³ To prevent implicit conversions to bool and int potentially leading to misleading arithmetic behaviors, a bit_value is explicitly, and not implicitly, convertible to bool (1.4.6).

§ 1.4.1 3

```
<sup>4</sup> For convenience, two global bit_value objects are provided (1.4.10): bit_zero and bit_one. <sup>1</sup>
     class bit_value {
    public:
      // 1.4.2, types
      using size_type = see below;
      // 1.4.3, constructors
      bit_value() noexcept = default;
      template <class T> constexpr bit_value(bit_reference<T> ref) noexcept;
      template <class WordType> explicit constexpr bit_value(WordType val) noexcept;
      template <class WordType> constexpr bit_value(WordType val, size_type pos);
      // 1.4.4, assignment
      template <class T> bit_value& operator=(bit_reference<T> ref) noexcept;
      template <class WordType> bit_value& assign(WordType val) noexcept;
      template <class WordType> bit_value& assign(WordType val, size_type pos);
      // 1.4.5, compound assignment
      bit_value& operator&=(bit_value other) noexcept;
      bit_value& operator|=(bit_value other) noexcept;
      bit_value& operator^=(bit_value other) noexcept;
      // 1.4.6, observers
      explicit constexpr operator bool() const noexcept;
      // 1.4.7, modifiers
      void set(bool b) noexcept;
      void set() noexcept;
      void reset() noexcept;
      void flip() noexcept;
      // 1.4.8, swap
      void swap(bit_value& other);
      template <class T> void swap(bit_reference<T> other);
    };
                                                                                       [bit.value.types]
  1.4.2 bit_value member types
  using size_type = see below;
        Type: An implementation-defined unsigned integer type capable of holding at least as many values as
        binary_digits_v<word_type>. Same as decltype(binary_digits_v<word_type>) (1.3).
                                                                                        [bit.value.cons]
  1.4.3 bit_value constructors
  bit_value() noexcept = default;
        Effects: Constructs an uninitialized object of type bit_value.
  template <class T> constexpr bit_value(bit_reference<T> ref) noexcept;
        Effects: Constructs an object of type bit_value from the value of the referenced bit ref.
  template <class WordType> explicit constexpr bit_value(WordType val) noexcept;
    1) The full spelling of numbers in the naming avoids the potential ambiguity between bit_1, bit_i, bit_I and bit_1 in
  certain fonts.
```

§ 1.4.3

certain folies.

- Requires: binary_digits_v<WordType> shall be defined and shall not be null (1.3).
- 4 Effects: Constructs an object of type bit_value from the value of the bit at position 0.
- Remarks: Contrarily to the more generic constructor that takes an arbitrary position as an argument, this constructor is marked noexcept.

```
template <class WordType> constexpr bit_value(WordType val, size_type pos);
```

- 6 Requires: binary_digits_v<WordType> shall be defined and shall not be null (1.3).
- 7 Requires: pos < binary_digits_v<WordType>.
- 8 Effects: Constructs an object of type bit_value from the value of the bit at position pos.
 - 1.4.4 bit value assignment [bit.value.assign] 1.4.5 bit_value compound assignment [bit.value.cassign] 1.4.6 bit_value observers [bit.value.observers] 1.4.7 bit_value modifiers [bit.value.modifiers] 1.4.8 bit_value swap [bit.value.swap] 1.4.9 bit value non-member operations [bit.value.nonmembers] [bit.value.objects] 1.4.10 bit value objects [bit.reference] 1.5 Class template bit_reference
 - 1.5.1 Class template bit_reference overview

[bit.reference.overview]

- A bit_reference emulates the behavior of a reference to a bit within an object, with no arithmetic behavior apart from bitwise compound assignment (1.5.5) and bitwise operators provided through implicit conversion to bit_value (1.4.9). Comparison operators are provided through implicit conversion to bit_value (1.4.9). As for bit_value (1.4.7), it provides the bit modifier members (1.5.7) set, reset and flip. [Note: A bit_reference is typically implemented in terms of a bit position or a mask, and in terms of a pointer or a reference to the object in which the bit is referenced. end note]
- ² The copy assignment operator = is overloaded to assign a new value to the referenced bit without changing the underlying reference itself. Specializations of swap are provided for the same reason, typically using a temporary bit_value (1.4) to ensure that the referenced values are swapped and not the references themselves.
- ³ The address-of operator & of bit_reference (1.5.6) is overloaded to return a bit_pointer (1.6) to the referenced bit. [Note: A pointer to a bit_reference can be obtained through the addressof function of the standard library. end note]
- 4 An access to the underlying representation of a bit_reference is provided through the function members address, position and mask (1.5.6).
- ⁵ To prevent implicit conversions to bool and int potentially leading to misleading arithmetic behaviors, a bit_reference is explicitly, and not implicitly, convertible to bool.
- ⁶ The template parameter type WordType shall be an unsigned integer type [Note: This does not include bool. end note] or a type such that binary_digits_v<WordType> is defined and is not null (1.3). A reference to a constant bit shall be obtained through bit_reference<const WordType>.

```
template <class WordType>
class bit_reference {
public:
   // 1.5.2, types
   using word_type = WordType;
```

§ 1.5.1 5

```
using size_type = see below;
    // 1.5.3, constructors
    template <class T> constexpr bit_reference(const bit_reference<T>& other) noexcept;
    explicit constexpr bit_reference(word_type& ref) noexcept;
    constexpr bit_reference(word_type& ref, size_type pos);
    // 1.5.4, assignment
    bit_reference& operator=(const bit_reference& other) noexcept;
    template <class T> bit_reference& operator=(const bit_reference<T>& other) noexcept;
    bit_reference& operator=(bit_value val) noexcept;
    bit_reference& assign(word_type val) noexcept;
    bit_reference& assign(word_type val, size_type pos);
    // 1.5.5, compound assignment
    bit_reference& operator&=(bit_value other) noexcept;
   bit_reference& operator|=(bit_value other) noexcept;
   bit_reference& operator^=(bit_value other) noexcept;
    // 1.5.6, observers
    explicit constexpr operator bool() const noexcept;
    constexpr bit_pointer<WordType> operator&() const noexcept;
    constexpr word_type* address() const noexcept;
    constexpr size_type position() const noexcept;
    constexpr word_type mask() const noexcept;
   // 1.5.7, modifiers
    void set(bool b) noexcept;
    void set() noexcept;
   void reset() noexcept;
    void flip() noexcept;
    // 1.5.8, swap
    template <class T> void swap(bit_reference<T> other);
   void swap(bit_value& other);
 };
1.5.2 bit_reference member types
                                                                             [bit.reference.types]
using word_type = WordType;
     Type: Refers to the underlying word type that is being provided as a template parameter.
using size_type = see below;
     Type: An implementation-defined unsigned integer type capable of holding at least as many values as
     binary_digits_v<word_type>. Same as decltype(binary_digits_v<word_type>) (1.3).
```

§ 1.5.2

2

```
1.5.3
                                                                  [bit.reference.cons]
     bit reference constructors
1.5.4 bit reference assignment
                                                                 [bit.reference.assign]
                                                                [bit.reference.cassign]
1.5.5 bit reference compound assignment
                                                             [bit.reference.observers]
1.5.6 bit reference observers
1.5.7
     bit_reference modifiers
                                                             [bit.reference.modifiers]
                                                                  [bit.reference.swap]
1.5.8 bit_reference swap
1.5.9 bit_reference non-member operations
                                                          [bit.reference.nonmembers]
1.6 Class template bit_pointer
                                                                         [bit.pointer]
      Class template bit pointer overview
```

1.6.1

- [bit.pointer.overview]
- A bit_pointer emulates the behavior of a pointer to a bit within an object. [Note: A bit_reference can be implemented in terms of a pointer to a bit_reference (1.5). — end note]
- ² The indirection operator * of bit_pointer (1.6.5) is overloaded to return a bit_reference (1.5) to the pointed bit, while the arrow operator -> is overloaded to return a pointer to a bit reference (1.5). Bit modifiers (1.5.7) can be accessed through this interface, as well as the underlying representation (1.5.6).
- 3 A null bit pointer can be created from a nullptr (1.6.3). Deferencing a null bit pointer leads to an undefined behavior. The explicit conversion to bool (1.6.5) shall return false for a null bit pointer, and true otherwise.
- ⁴ Arithmetic of bit pointers 1.6.6 rely on the following ordering: a bit pointer ptr2 is considered to be the next bit pointer of ptr1 if both of them are not null and if either of the following is true:

```
(4.1)
      — ptr2->address() - ptr1->address() == 0
         && ptr2->position() - ptr1->position() == 1
(4.2)
      — ptr2->address() - ptr1->address() == 1
         && binary_digits_v<typename decltype(ptr1)::word_type> - ptr1->position() == 1
         && ptr2->position() == 0
```

Comparison operators for bit_pointer (1.6.7) rely on the same ordering, first comparing the addresses of the underlying values and then comparing bit positions in case of equality.

- ⁵ The template parameter type WordType shall be an unsigned integer type [Note: This does not include bool. $-end \ note$ or a type such that binary digits v-WordType> is defined and is not null (1.3). A pointer to a constant bit shall be obtained through bit_pointer<const WordType>. A constant pointer to a mutable bit shall be obtained through const bit_pointer<WordType>. A constant pointer to a constant bit shall be obtained through const bit_pointer<const WordType>.
- The return type of the difference between two bit pointers (1.6.2) shall be an implementation-defined signed integer type capable of holding at least as many values as ptrdiff_t.

```
template <class WordType>
class bit_pointer {
public:
 // 1.6.2, types
 using word_type = WordType;
 using size_type = see below;
 using difference_type = see below;
  // 1.6.3, constructors
 bit_pointer() noexcept = default;
 template <class T> constexpr bit_pointer(const bit_pointer<T>& other) noexcept;
 constexpr bit_pointer(std::nullptr_t) noexcept;
 explicit constexpr bit_pointer(word_type* ptr) noexcept;
```

§ 1.6.1 7

```
constexpr bit_pointer(word_type* ptr, size_type pos);
      // 1.6.4, assignment
      bit_pointer& operator=(std::nullptr_t) noexcept;
      bit_pointer& operator=(const bit_pointer& other) noexcept;
      template <class T> bit_pointer& operator=(const bit_pointer<T>& other) noexcept;
      // 1.6.5, observers
      explicit constexpr operator bool() const noexcept;
      constexpr bit_reference<WordType> operator*() const noexcept;
      constexpr bit_reference<WordType>* operator->() const noexcept;
      constexpr bit_reference<WordType> operator[](difference_type n) const;
      // 1.6.6, arithmetic
      bit_pointer& operator++();
      bit_pointer& operator--();
      bit_pointer operator++(int);
      bit_pointer operator--(int);
      constexpr bit_pointer operator+(difference_type n) const;
      constexpr bit_pointer operator-(difference_type n) const;
      bit_pointer& operator+=(difference_type n);
      bit_pointer& operator-=(difference_type n);
    };
  1.6.2 bit_pointer member types
                                                                                [bit.pointer.types]
  using word_type = WordType;
        Type: Refers to the underlying word type that is being provided as a template parameter.
  using size_type = see below;
        Type: An implementation-defined unsigned integer type capable of holding at least as many values as
       binary_digits_v<word_type>. Same as decltype(binary_digits_v<word_type>) (1.3).
  using difference_type = see below;
        Type: An implementation-defined signed integer type capable of holding at least as many values as
       ptrdiff_t. Same as bit_pointer<word_type>::difference_type1.6.2.
                                                                                 [bit.pointer.cons]
  1.6.3 bit_pointer constructors
                                                                               [bit.pointer.assign]
  1.6.4 bit_pointer assignment
  1.6.5 bit_pointer observers
                                                                           [bit.pointer.observers]
                                                                          [bit.pointer.arithmetic]
  1.6.6 bit pointer arithmetic
  1.6.7 bit_pointer non-member operations
                                                                       [bit.pointer.nonmembers]
  1.7 Class template bit_iterator
                                                                                      [bit.iterator]
  1.7.1
          Class template bit_iterator overview
                                                                            [bit.iterator.overview]
<sup>1</sup> A bit_iterator is an iterator adaptor to iterate over the bits of a range of underlying values. The value_-
  type (1.7.2) of a bit_iterator is defined as a bit_value, the reference type (1.7.2) is defined as a
  bit_reference and the pointer type (1.7.2) is defined as a bit_pointer. [Note: A bit_iterator is
  typically implemented in terms of a bit position or a mask, and in terms of an underlying iterator. — end
  note
```

² Arithmetic of bit iterators 1.7.6 rely on the following ordering: a bit iterator it2 is considered to be the next bit iterator of it1 if either of the following is true:

Comparison operators for bit_iterator (1.7.7) rely on the same ordering, first comparing the underlying iterator and then comparing bit positions in case of equality.

3 The template parameter type Iterator shall be an iterator such that the following types are the same:

```
(3.1) — iterator_traits<Iterator>::value_type
```

- (3.2) remove_cv_t<remove_reference_t<typename iterator_traits<Iterator>::reference>>
- (3.3) remove_cv_t<remove_pointer_t<typename iterator_traits<Iterator>::pointer>> , such that the following types are the same:
- $(3.4) \qquad \texttt{remove_reference_t<typename iterator_traits<Iterator>::reference>>}$
- (3.5) remove_pointer_t<typename iterator_traits<Iterator>::pointer>> and such that:
- (3.6) bit_reference<remove_reference_t<typename iterator_traits<Iterator>::reference>>
- $(3.7) \qquad -\ \, \text{bit_pointer} < \text{remove_pointer_t} < \text{typename iterator_traits} < \text{Iterator} > :: \text{pointer} > :: \text{pointe$

can be instantiated. [Note: This does not include bool. — end note] The member type word_- type (1.7.2) keeps track of the cv-qualification of the underlying type. [Note: For this reason, the types of iterator_traits<Iterator>::value_type and bit_iterator<Iterator>::word_type may have different cv-qualifiers. Implementations may use remove_reference_t<typename iterator_traits<Iterator>::reference> to propagate cv-qualifiers. — end note]

- ⁴ An access to the underlying representation of a bit_iterator is provided through the function members base, position and mask (1.7.5).
- ⁵ The return type of the difference between two bit iterator (1.6.2) shall be an implementation-defined signed integer type capable of holding at least as many values as ptrdiff_t.

```
template <class Iterator>
class bit_iterator {
public:
  // 1.7.2, types
  using iterator_type = Iterator;
  using word_type = see below;
  using iterator_category = typename std::iterator_traits<Iterator>::iterator_category;
  using value_type = bit_value;
  using difference_type = see below;
  using pointer = bit_pointer<word_type>;
 using reference = bit_reference<word_type>;
  using size_type = see below;
  // 1.7.3, constructors
  constexpr bit_iterator();
  template <class T> constexpr bit_iterator(const bit_iterator<T>& other);
  explicit constexpr bit_iterator(iterator_type i);
  constexpr bit_iterator(iterator_type i, size_type pos);
```

```
// 1.7.4, assignment
      template <class T> bit_iterator& operator=(const bit_iterator<T>& other);
      // 1.7.5, observers
      constexpr reference operator*() const noexcept;
      constexpr pointer operator->() const noexcept;
      constexpr reference operator[](difference_type n) const;
      constexpr iterator_type base() const;
      constexpr size_type position() const noexcept;
      constexpr word_type mask() const noexcept;
      // 1.7.6, arithmetic
      bit_iterator& operator++();
      bit_iterator& operator--();
      bit_iterator operator++(int);
      bit_iterator operator--(int);
      constexpr bit_iterator operator+(difference_type n) const;
      constexpr bit_iterator operator-(difference_type n) const;
      bit_iterator& operator+=(difference_type n);
      bit_iterator& operator-=(difference_type n);
    };
                                                                                  [bit.iterator.types]
  1.7.2 bit_iterator member types
  using iterator_type = Iterator;
1
        Type: Refers to the Iterator template type parameter that is being adapted.
  using word_type = see below;
2
        Type: Refers to the cy-qualified type on which the underlying iterator is iterating, which is equivalent
       to remove reference t<typename iterator traits<Iterator>::reference> according to 1.7.1.
  using iterator_category = typename std::iterator_traits<Iterator>::iterator_category;
3
        Type: Refers to the same iterator category as the one of the underlying iterator.
  using value_type = bit_value;
        Type: bit value.
  using difference_type = see below;
        Type: An implementation-defined signed integer type capable of holding at least as many values as
       ptrdiff_t. Same as bit_pointer<word_type>::difference_type (1.6.2).
  using pointer = bit_pointer<word_type>;
        Type: bit_pointer<word_type>.
  using reference = bit_reference<word_type>;
7
        Type: bit_reference<word_type>.
  using size_type = see below;
        Type: An implementation-defined unsigned integer type capable of holding at least as many values as
       binary_digits_v<word_type>. Same as decltype(binary_digits_v<word_type>) (1.3).
```

1.7.3	bit_iterator constructors	$[{ m bit.iterator.cons}]$
1.7.4	bit_iterator assignment	$[{\it bit.iterator.assign}]$
1.7.5	bit_iterator observers	$[{\it bit.iterator.observers}]$
1.7.6	bit_pointer arithmetic	$[{\it bit.iterator.arithmetic}]$
1.7.7	bit_iterator non-member operations	$[{\bf bit.iterator.nonmembers}]$