average-minimum-distance

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amd.calculate.**AMD** ($periodic_set$: Union[amd.PeriodicSet.PeriodicSet, Tuple[numpy.ndarray, numpy.ndarray]], <math>k: int) \rightarrow numpy.ndarray

Computes an AMD vector up to k from a periodic set.

Parameters

- periodic_set (amd.PeriodicSet or tuple of ndarrays (motif, cell)) Representation of the periodic set, in Cartesian coordinates. amd.Cif-Reader yields PeriodicSets which can be given here. Otherwise pass a tuple of arrays (motif, cell) in Cartesian form.
- \mathbf{k} (int) A m_b by k PDD matrix (with weights in the first column).

Returns AMD of periodic_set up to k.

Return type ndarray

 $\verb| amd.calculate.AMD_estimate| (periodic_set: Union[amd.PeriodicSet.PeriodicSet, Tuple[numpy.ndarray]], k: int) \rightarrow numpy.ndarray$

Calculates an estimate of AMD based on the PPC.

amd.calculate.PDD ($periodic_set$: Union[amd.PeriodicSet.PeriodicSet, Tuple[numpy.ndarray, numpy.ndarray]], k: int, order: bool = True, collapse: bool = True, $collapse_tol$: float = 0.0001) \rightarrow numpy.ndarray

Computes a PDD up to k from a periodic set.

Parameters

- periodic_set (amd.PeriodicSet or tuple of ndarrays (motif, cell)) Representation of the periodic set, in Cartesian coordinates. amd.Cif-Reader yields PeriodicSets which can be given here. Otherwise pass a tuple of arrays (motif, cell) in Cartesian form.
- **k** (*int*) A m_b by k PDD matrix (with weights in the first column).
- order (bool, optional) Whether or not to lexicographically order the rows. Default True.
- **collapse** (bool, optional) Whether or not to collapse identical rows (within a tolerance). Default True.
- **collapse_tol** (*float*) If two rows have all entries closer than collapse_tol, they get collapsed. Default 1e-4.

Returns PDD of periodic_set up to k.

Return type ndarray

amd.calculate.PDD_to_AMD (pdd: numpy.ndarray) \rightarrow numpy.ndarray Calculates AMD from a PDD.

amd.calculate.PPC (periodic_set: Union[amd.PeriodicSet.PeriodicSet, Tuple[numpy.ndarray, numpy.ndarray]])

Calculate the point packing coefficient (ppc) of periodic_set.

The ppc is a constant of any periodic set determining the asymptotic behaviour of its AMD/PDD as k -> infinity.

As $k \rightarrow infinity$, the ratio AMD_k / (n-th root of k) approaches the ppc (as does any row of a PDD).

For a unit cell U and m motif points in n dimensions, $ppc = \sqrt{n} \{Vol[U] / (m * V_n) \}$, where V_n is the volume of a unit sphere in n dimensions.

amd.compare.AMD_cdist (amds: Union[int, float, complex, str, bytes, numpy.generic, Sequence[Sequence[Any]], Sequence[Union[int, float, complex, bytes, numpy.generic]], str, numpy.typing._array_like._SupportsArray], amds_: Union[int, float, complex, str, bytes, numpy.generic, Sequence[Sequence[Any]], Sequence[Union[int, float, complex, str, bytes, numpy.generic]], numpy.typing._array_like._SupportsArray], k: Optional[int] = None, low_memory: bool = False, metric: str = 'chebyshev', **kwargs) \rightarrow numpy.ndarray

Compare two sets of AMDs with each other. Returns a distance matrix.

Parameters

- amds (ndarray or list of ndarrays) An m_a by n array (of m_a vectors/AMDs).
- amds An m_b by n array (of m_b vectors/AMDs).
- **k** (*int*, *optional*) If None, compare whole AMDs (largest k). Set k to an int to compare for a specific k (less than the maximum).
- **low_memory** (bool, optional) Optionally use a slightly slower but more memory efficient method for large collections of AMDs (Chebyshev/l-inf distance only).
- **metric** (*str* or *callable*, *optional*) Usually AMDs are compared with the Chebyshev/l-infinity distance. Can take any metric + kwargs accepted by scipy.spatial.distance.cdist.

Returns Returns a m_a by m_b distance matrix. The ij th entry is the distance between amds[i] and amds_[j] given by the metric.

Return type ndarray

amd.compare.**AMD_mst** (amds: Union[int, float, complex, str, bytes, numpy.generic, Sequence[Union[int, float, complex, str, bytes, numpy.generic]], Sequence[Sequence[Any]], numpy.typing._array_like._SupportsArray], k: Optional[int] = None, low_memory: bool = False, metric: $str = 'chebyshev', **kwargs) \rightarrow List[Tuple[int, int, float]]$

Return list of edges in a minimum spanning tree based on AMDs.

Parameters

- amds (ndarray or list of ndarrays) An m_a by n array (of m_a vectors/AMDs).
- **k** (*int*, *optional*) If None, compare whole PDDs (largest k). Set k to an int to compare for a specific k (less than the maximum).
- **metric** (str or callable, optional) Usually PDD rows are compared with the Chebyshev/l-infinity distance. Can take any metric + kwargs accepted by scipy.spatial.distance.cdist.

Returns Each tuple (i,j,w) is an edge in the mimimum spanning tree, where i and j are the indices of nodes and w is the weight on the edge connecting them.

Return type list of tuples

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amd.compare.**AMD_pdist** (amds: Union[int, float, complex, str, bytes, numpy.generic, Sequence[Union[int, float, complex, str, bytes, numpy.generic]], Sequence[Sequence[Any]], numpy.typing_array_like_SupportsArray], k: Optional[int] = None, low_memory: bool = False, metric: str = 'chebyshev', **kwargs') \rightarrow numpy.ndarray

Do a pairwise comparison on one set of AMDs.

Parameters

- amds (ndarray or list of ndarrays) An m_a by n array (of m_a vectors/AMDs).
- **k** (*int*, *optional*) If None, compare whole AMDs (largest k). Set k to an int to compare for a specific k (less than the maximum).
- **low_memory** (bool, optional) Optionally use a slightly slower but more memory efficient method for large collections of AMDs (Chebyshev/l-inf distance only).
- metric (str or callable, optional) Usually AMDs are compared with the Chebyshev/l-infinity distance. Can take any metric + kwargs accepted by scipy.spatial.distance.cdist.

Returns

Returns a condensed distance matrix. Collapses a square distance matrix into a vector just keeping the upper traingle. scipy's squareform will convert to a square distance matrix.

Return type ndarray

amd.compare.**PDD_cdist** (pdds: List[numpy.ndarray], $pdds_{:}$: List[numpy.ndarray], k: Optional[int] = None, metric: <math>str = 'chebyshev', $verbose: bool = False, **kwargs) \rightarrow numpy.ndarray$

Compare two sets of PDDs with each other. Returns a distance matrix.

Parameters

- **pdds** (*ndarray* or *list* of *ndarrays*) A list of PDDs (ndarrays whose last/second dimension agree). If a 2D array, is interpreted as one PDD.
- **pdds** A list of PDDs (ndarrays whose last/second dimension agree). If a 2D array, is interpreted as one PDD.
- **k** (*int*, *optional*) If None, compare whole PDDs (largest k). Set k to an int to compare for a specific k (less than the maximum).
- **metric** (*str* or *callable*, *optional*) Usually PDD rows are compared with the Chebyshev/l-infinity distance. Can take any metric + kwargs accepted by scipy.spatial.distance.cdist.
- **verbose** (bool, optional) Optionally print progress as for large sets this can be long.

Returns Returns a m_a by m_b distance matrix. The ij th entry is the distance between pdds[i] and pdds_[j] given by earth mover's distance.

Return type ndarray

amd.compare.PDD_mst (pdds: List[numpy.ndarray], amd_filter_cutoff : Optional[int] = None, k: Optional[int] = None, metric: str = 'chebyshev', verbose: bool = False, **kwargs) $\rightarrow List[Tuple[int, int, float]]$ Return list of edges in a minimum spanning tree based on PDDs.

Parameters

- **pdds** (*ndarray* or *list* of *ndarrays*) A list of PDDs (*ndarrays* whose last/second dimension agree). If a 2D array, is interpreted as one PDD.
- amd_filter_cutoff (int, optional) If specified, apply the AMD filter behaviour of the filter() function. The int specified is the n passed to filter(), the number of neighbours to connect in the neighbourhood graph.
- **k** (*int*, *optional*) If None, compare whole PDDs (largest k). Set k to an int to compare for a specific k (less than the maximum).
- metric (str or callable, optional) Usually PDD rows are compared

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with the Chebyshev/l-infinity distance. Can take any metric + kwargs accepted by scipy.spatial.distance.cdist.

• **verbose** (bool, optional) – Optionally print progress as for large sets this can be long.

Returns

Each tuple (i,j,w) is an edge in the mimimum spanning tree, where i and j are the indices of nodes and w is the weight on the edge connecting them.

Return type list of tuples

amd.compare.PDD_pdist ($pdds: List[numpy.ndarray], k: Optional[int] = None, metric: str = 'chebyshev', verbose: bool = False, **kwargs') <math>\rightarrow$ numpy.ndarray

Do a pairwise comparison on one set of PDDs.

Parameters

- **pdds** (*list of ndarrays*) A list of PDDs (ndarrays whose last/second dimension agree). If a 2D array, is interpreted as one PDD.
- **k** (*int*, *optional*) If None, compare whole PDDs (largest k). Set k to an int to compare for a specific k (less than the maximum).
- **metric** (*str or callable*, *optional*) Usually PDD rows are compared with the Chebyshev/l-infinity distance. Can take any metric + kwargs accepted by scipy.spatial.distance.cdist.
- **verbose** (bool, optional) Optionally print progress as for large sets this can be long.

Returns

Returns a condensed distance matrix. Collapses a square distance matrix into a vector just keeping the upper traingle. scipy's squareform will convert to a square distance matrix.

Return type ndarray

amd.compare.emd (pdd,pdd_, metric='chebyshev', **kwargs)

Earth mover's distance between two PDDs.

Parameters

- pdd (ndarray) A m_a by k PDD matrix (with weights in the first column).
- pdd A m_b by k PDD matrix (with weights in the first column).
- **metric** (*str* or *callable*, *optional*) Usually rows are compared with the Chebyshev/l-infinity distance. Can take any metric + kwargs accepted by scipy.spatial.distance.cdist.

Returns

Earth mover's distance between PDDs, where rows of the PDDs are compared with metric.

Return type float

Raises

ValueError – Thrown if reference and comparison do not have number of columns.

amd.compare.filter (n: int, pdds: List[numpy.ndarray], pdds_: Optional[List[numpy.ndarray]] = None,
k: Optional[int] = None, low_memory: bool = False, metric: str = 'chebyshev', verbose: bool = False, **kwargs)

→ Tuple[numpy.ndarray, numpy.ndarray]

For each item in pdds, get the n nearest items in pdds_ by AMD, then compare references to these nearest items with PDDs. Tries to comprimise between the speed of AMDs and the accuracy of PDDs.

If pdds_ is None, essentially sets pdds_ = pdds, i.e. do an 'AMD neighbourhood graph' for one set whose weights are PDD distances.

If n is smaller than the comparison set (pdds_ if it is not None and pdds if pdds_ is None), the AMD filter doesn't happen, this is essentially the same behaviour as pdd_cdist or pdd_pdist.

Parameters

• n (int) – Number of nearest neighbours to find.

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- **pdds** (*ndarray* or *list* of *ndarrays*) A list of PDDs (*ndarrays* whose last/second dimension agree). If a 2D array, is interpreted as one PDD.
- **pdds**_(ndarray or list of ndarrays) A list of PDDs (ndarrays whose last/second dimension agree). If a 2D array, is interpreted as one PDD.
- **k** (*int*, *optional*) If None, compare whole PDDs (largest k). Set k to an int to compare for a specific k (less than the maximum).
- **low_memory** (bool, optional) Optionally use a slightly slower but more memory efficient method for large collections of AMDs (Chebyshev/l-inf distance only).
- **metric** (*str or callable*, *optional*) Usually PDD rows are compared with the Chebyshev/l-infinity distance. Can take any metric + kwargs accepted by scipy.spatial.distance.cdist.
- **verbose** (bool, optional) Optionally print progress as for large sets this can be long.

Returns

For the i-th item in reference and some j < n, distance_matrix[i][j] is the distance from reference i to its j-th nearest neighbour in comparison (after the AMD filter). indices[i][j] is the index of said neighbour in comparison.

Return type tuple of ndarrays (distance_matrix, indices)

```
amd.compare.linf (v, v_{-})
```

l-infinity distance between vectors (AMDs).

amd.compare.neighbours_from_distance_matrix (n: int, dm: numpy.ndarray) ->
Tuple[numpy.ndarray, numpy.ndarray]

Given a distance matrix, find the n nearest neighbours of each item.

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