Kristali

$$\begin{array}{l} \alpha_{M,i} = \sum_{j \neq i} \frac{Z_j}{r_j/a} \quad \text{(Madelungova konstanta)} \\ V_{C,i} = \frac{e_0 \alpha_{M,i}}{4 \pi \varepsilon_0 a} \\ W_{C,i} = Z_i e_0 V_{C,i} \\ V = \frac{N}{2} V_{C,i} + V_{\text{odb,k}} + \frac{N}{2} W_i - \frac{N}{2} W_a \end{array}$$

Blochov teorem

 $\psi = e^{i\mathbf{k}\cdot\mathbf{r}}u(\mathbf{r})$, kjer ima $u(\mathbf{r})$ enako periodo kot $V(\mathbf{r})$, torej $u(\mathbf{r} + \mathbf{r}_0) = u(\mathbf{r}) \implies \psi(\mathbf{r} + \mathbf{r}_0) = e^{i\mathbf{k}\cdot\mathbf{r}_0}\psi(\mathbf{r})$.

Kronig-Penny-ev model kovinske vezi

$$V(x) = \begin{cases} 0; & 0 \le x < a \\ V_0; & -b \le x < 0 \end{cases} & \text{in } V(x+a+b) = V(x)$$

$$\psi(x) = \begin{cases} Ae^{ikx} + Be^{-ikx}; & 0 \le x < a \\ Ce^{\kappa x} + Be^{-\kappa x}; & -b \le x < 0 \end{cases} & \text{in } \psi(x+a+b) = \psi(x)$$

$$k = \sqrt{\frac{2mE}{\hbar^2}} \qquad \kappa = \sqrt{\frac{2m(V_0 - E)}{\hbar^2}}$$

S približkom $b \to 0, V_0 \to \infty, P = \frac{\kappa^2 ab}{2} = konst.$ dobimo:

$$P\frac{\sin(ka)}{ka} + \cos(ka) = \cos(kla)$$
$$k_l = \frac{2\pi l}{Na}, \qquad l = 1, 2, \dots$$

Valenčni pas je najvišji energijski pas v katerem so pri $T \to 0$ energijski nivoji še zasedeni z elektroni.

Prevodni pas je najnižji energijski pas v katerem so pri $T \to 0$ vsi energijski nivoji nezasedeni.

$$P(\text{preskok med pasoma}) = \exp\left\{-\frac{E_g}{k_B T}\right\}$$

Izolator: valenčni pas popolnoma zapolnjen, prevodni pas prazen. $E_q \sim 10$ eV.

Prevodnik: valenčni in prevodni pas sta enaka.

Polprevodnik: tudi pri nizkih Tlahko elektroni preskočijo v prevodni pas. $E_g \sim 1 \ {\rm eV}.$

Fermijeva energija

$$F_{Fe}(E) = \left(\exp\left\{\frac{E-\mu}{k_BT}\right\} + 1\right)^{-1}$$

$$\rho_E = \frac{dg}{dE} = 4\pi(2m)^{\frac{3}{2}} \frac{V}{h^3} \sqrt{E}$$

$$N_{Fe} = \int_0^\infty \rho_E F_{Fe} dE \approx \int_0^{E_F} \rho_E dE$$

$$E_F = \mu(T \to 0) = \frac{h^2}{2m} \left(\frac{3N}{8\pi V}\right)^{\frac{2}{3}} = \frac{mv_F^2}{2}$$

Drudejev model prevodnosti

$$\begin{split} p(t) &= (p_0 - qE\tau)e^{-t/\tau} + eE\tau \\ j &= \frac{\mathrm{d}e}{\mathrm{Sd}t} = ne_0\langle v \rangle \\ \langle v \rangle &= \frac{p(t \to \infty)}{m} = \frac{eE\tau}{m} = \beta E \\ \sigma_0 &= \frac{j}{E} = \frac{ne_0^2\tau}{m} \\ \tau &= \frac{a}{\langle v \rangle} \approx a\sqrt{\frac{m}{3k_BT}} \\ \mathrm{Izmenični\ tok:} \ \sigma &= \frac{\sigma_0}{\sqrt{1+4c^2\tau^2}}e^{i\arctan(\omega\tau)} \end{split}$$

Efektivna masa

$$m^* = \hbar^2 / \frac{\mathrm{d}^2 E}{\mathrm{d}k^2}$$

 $E = \frac{p^2}{2m^*} = \frac{\hbar^2 k^2}{2m^*}$

Polprevodniki

Definiramo E=0 na vrhu valenčnega pasu.

Elektroni v prevodnem pasu
$$(E - E_f \gg k_B T)$$
: $\rho_e \propto \sqrt{E - E_g}$

$$F_e = e^{-(E - E_F)/k_B T}$$

$$n_e = \frac{N_e}{V} = 2\left(\frac{2\pi m^* k_B T}{h^2}\right)^{\frac{3}{2}} e^{-(E_g - E_F)/k_B T}$$
 $v_e = \beta_e E$

Vrzeli v valenčnem pasu $(E - E_f \gg k_B T)$:

$$\begin{aligned} & \rho_v \propto \sqrt{-E} \\ & F_v = 1 - F_e = e^{-(E_F - E)/k_B T} \\ & n_v = \frac{N_v}{V} = 2 \left(\frac{2\pi m^* k_B T}{h^2}\right)^{\frac{3}{2}} e^{-E_F/k_B T} \\ & v_v = \beta_v E \end{aligned}$$

$$n_e n_v \propto e^{-E_g/kT} \neq f(E_F)$$

Čisti polprevodnik: $n_e = n_v \implies E_F = \frac{1}{2}E_g - \frac{3}{4}k_BT \ln \frac{m_e^*}{m^*}$

$$\begin{split} j &= ne_0v = j_e + j_v = \sigma E \\ \sigma &= 2\left(\frac{2\pi m^* k_B T}{h^2}\right)^{\frac{3}{2}} e_0(\beta_e + \beta_v) e^{-E_g/2k_B T} \end{split}$$

Dopirani polprevodniki

Akceptorji imajo en elektron manj kot čisti polprevodnik. Donorji imajo en elektron več kot čisti polprevodnik.

$$\begin{array}{ll} n_{e_i} = n_{v_i} & \Longrightarrow & n_e - n_D = n_v - n_A \\ \text{n-tip: } n_e \approx n_D \\ \text{p-tip: } n_v \approx n_A \end{array}$$

p-n stik

$$U(x) = \begin{cases} -\frac{e_0 n_D}{2\varepsilon\varepsilon_0} (x - x_n)^2 + U_0; & 0 \le x \le x_n \\ \frac{e_0 n_A}{2\varepsilon\varepsilon_0} (x + x_p)^2; & -x_p \le x \le 0 \end{cases}$$

$$U_0 = \frac{e_0}{2\varepsilon\varepsilon_0} (n_D x_n^2 + n_A x_p^2)$$

$$x_n = \left[\frac{2\varepsilon\varepsilon_0 U_0}{e_0 n_D \left(1 + \frac{n_D}{n_A}\right)} \right]^{1/2}, \quad x_p = \left[\frac{2\varepsilon\varepsilon_0 U_0}{e_0 n_A \left(1 + \frac{n_A}{n_D}\right)} \right]^{1/2}$$

$$d = x_n + x_p = \left[\frac{2\varepsilon\varepsilon_0 U_0}{e_0} \frac{n_A + n_D}{n_A n_D} \right]^{1/2} \text{ (depletirana plast)}$$

$$U_0 = \frac{k_B T}{e_0} \ln \frac{n_e n_v}{n_{e_i} n_{v_i}} \text{ (kontaktna napetost)}$$

$$d \propto \sqrt{U_b + U_0} \approx \sqrt{U_b}$$

$$I = I_0 \left(e^{e_0 U/k_b T} - 1 \right)$$

$$C = \frac{\mathrm{d}e}{\mathrm{d}U} = S\sqrt{\frac{\varepsilon\varepsilon_0 n_D e_0}{2(U_0 + U_b)}} \quad (n_a \gg n_d \implies d_n \gg d_p)$$

Fotodioda

$$I = I_0 \left(e^{e_0 U/k_b T} - 1 \right) - I_f$$

$$I_f = \eta 2 \frac{\mathrm{d} n_f}{\mathrm{d} t} e_0$$

Tranzistor

$$\begin{split} I_c &= \alpha I_e \\ I_b &= (1 - \alpha) I_e \\ I_b &\approx I_0 e^{e_0 U_{be}/k_B T} \\ I_c &= \frac{\alpha}{1 - \alpha} I_0 e^{e_0 U_{be}/k_B T} \end{split}$$

Jedra

$$\begin{split} & \text{Rutherfordov eksperiment: } \frac{\mathrm{d}N}{\mathrm{d}\Omega} \propto \sin^{-4}\frac{\vartheta}{2} \\ & r_{j} \sin\beta = n\lambda_{b} \\ & r_{j} = r_{0}A^{1/3} \\ & \rho_{e}(r) = \frac{\rho_{0}}{e^{(r-r_{j})/s}+1} \\ & M = Zm_{p} + Nm_{n} + E_{v}/c^{2} \\ & E_{v} = -w_{0}A + w_{1}A^{2/3} + w_{2}\frac{Z^{2}}{A^{1/3}} + w_{3}\frac{(A-2Z)^{2}}{A} + w_{4}\frac{\delta_{ZN}}{A^{3/4}} \\ & \delta_{ZN} = \begin{cases} -1; & Z \operatorname{sod}, N \operatorname{sod} \\ 0; & \operatorname{en \operatorname{sod} en \ lih} \\ 1; & Z \operatorname{lih}, N \operatorname{lih} \end{cases}$$

Lupinski model jedra

$$\hat{H} = -\frac{\hbar^2}{2\mu} \left(\frac{\partial^2}{\partial r^2} + \frac{2}{r} \frac{\partial}{\partial r} - \frac{l(l+1)}{r^2} \right) + V(r)$$

$$V(r) = -V_0 / \left[e^{(r-r_j)/s} + 1 \right] \qquad \text{(Saxon-Woodsov potencial)}$$

$$\hat{H}_{ls} = -\eta \, \hat{\mathbf{l}} \cdot \hat{\mathbf{s}}$$

Nukleona imata $s = \frac{1}{2}$.

Lupine pri Saxon-Woodsu z dovolj veliko η (nl_i) :

- 1. $1s_{1/2} \implies magično število 2$
- 2. $1p_{3/2}$, $1p_{1/2}$ \Longrightarrow magično število 8
- 3. $1d_{5/2}$, $2s_{1/2}$, $1d_{3/2}$ \Longrightarrow magično število 20
- 4. $1f_{7/2} \implies \text{magično število } 28$
- 5. $2p_{3/2}$, $1f_{5/2}$, $1p_{1/2}$, $1g_{9/2}$ \Longrightarrow magično število 50
- 6. $1g_{7/2}$, $2d_{5/2}$, $1d_{3/2}$, $3s_{1/2}$, $1h_{11/2} \implies$ magično število 82
- 7. $1h_{9/2}$, $2f_{7/2}$, $2f_{5/2}$, $3p_{3/2}$, $3p_{1/2}$, $1i_{13/2} \implies mš 126$

Spin sodo-lihega (oz. liho-sodega) jedra je enak celotni vrtilni količini zadnjega neparnega nukleona.

Spin sodo-sodega jedra je 0.

Spin liho-lihega jedra ne moremo natančno določiti, možne so vse kombinacije VK zadnjih dveh nukleonov.

Parnost sodo-lihega (oz. liho-sodega) jedra je $(-1)^l$, kjer l pripada zadnjemu neparnemu nukleonu.

Parnost sodo-sodega jedra je +.

Parnost liho-lihega jedra je $(-1)^{l_p}(-1)^{l_n},$ kjer l_p,l_n pripadata zadnjima nukleonoma.

Fizikalne konstante

$$\begin{split} R &= 8\ 310\ \frac{\mathrm{J}}{\mathrm{kmol\ K}} \\ N_A &= 6.02 \cdot 10^{26}\ \frac{1}{\mathrm{kmol}} \\ k_B &= \frac{R}{N_A} = 1.38 \cdot 10^{-23}\ \frac{\mathrm{J}}{\mathrm{K}} \\ e_0 &= 1.602 \cdot 10^{-19}\ \mathrm{As} \\ \varepsilon_0 &= 8.85 \cdot 10^{-12}\ \frac{\mathrm{As}}{\mathrm{Vm}} \\ \mu_0 &= 4\pi \cdot 10^{-7}\ \frac{\mathrm{Vs}}{\mathrm{Am}} \\ c_0 &= 3.0 \cdot 10^8\ \frac{\mathrm{m}}{\mathrm{s}} \\ \sigma &= 5.67 \cdot 10^{-8}\ \frac{\mathrm{W}}{\mathrm{m}^2\mathrm{K}^4} \\ k_W &= 2.90 \cdot 10^{-3}\ \mathrm{m \cdot K} \\ u &= 1.66 \cdot 10^{-27}\ \mathrm{kg} = 931.5\ \frac{\mathrm{MeV}}{\mathrm{c}^2} \\ m_e &= 9.1 \cdot 10^{-31}\ \mathrm{kg} = 0.511\ \frac{\mathrm{MeV}}{\mathrm{c}^2} \end{split}$$

$$m_p = 1,673 \cdot 10^{-27} \text{ kg} = 938,3 \frac{\text{MeV}}{\text{c}^2} = 1,00728u$$

 $m_n = 1,675 \cdot 10^{-27} \text{ kg} = 939,6 \frac{\text{MeV}}{\text{c}^2} = 1,00866u$

$$\begin{array}{l} h = 6{,}626 \cdot 10^{-34} \text{ Js} \\ hc = 1240 \text{ eV nm} \\ r_B = 5{,}291 \cdot 10^{-2} \text{ nm} \\ E_0 = 13{,}6 \text{ eV} \end{array}$$

$$\alpha_{EM} = \frac{e_0^2}{4\pi\varepsilon_0\hbar c} = \frac{1}{137}$$

$$b = 100 \text{ fm}^2$$

$$r_0 \approx 1.1 \text{ fm}$$

$$w_0 = 15.6 \text{ MeV}$$

$$w_1 = 17.3 \text{ MeV}$$

$$w_2 = 0.7 \text{ MeV}$$

$$w_3 = 23.3 \text{ MeV}$$

 $w_4 = 33.5 \text{ MeV}$

$$|V_{\text{CKM}}| = \begin{bmatrix} 0.97428 & 0.2253 & 0.00347 \\ 0.2252 & 0.97345 & 0.0410 \\ 0.00862 & 0.0403 & 0.999152 \end{bmatrix}$$