

## Step 1: Learn the Basics

Lec 1: Things to know in C++ | Java | Python

### ① User Input/Output

→ Scanner for input | System.out for output.

→ Ex:

```
import java.util.Scanner;
```

```
Class Demo
```

```
String name[] =
```

```
Scanner sc = new Scanner(System.in);
```

```
System.out.println("Enter your name: ");
```

```
String name = sc.nextLine();
```

```
System.out.println("Enter your age: ");
```

```
int age = sc.nextInt();
```

```
System.out.println(name + " " + age);
```

}

Output::

### ② Data Types

→ Data types are categorized into primitive type and reference type.

- ① Primitive Data Type
- ② Reference Data Type

## (a) Primitive Data Types

→ There are the most basic data types for Java.

→ Ex:-

### Data Type

#### Size

#### Example

byte

1 byte

byte b = 100;

short

2 bytes

short s = 10000;

int

4 bytes

int x = 50000;

long

8 bytes

long l = 150000L;

float

4 bytes

float f = 5.75f;

double

8 bytes

double d = 19.99

char

2 bytes

char c = 'A';

boolean

1 bit

boolean b = true;

## (b) Reference Data Type

→ Therefore reference to objects.

→ Ex:-

### Type

#### Example

#### Object

String

String name = "Alice";

Array

int[] arr = {1, 2, 3};

custom class

Person p = new Person();

wrappers

Integer i = 5;

### ③ if else statement

→ Ex :-

class Demo

{  
    println("String arg")

}

int number = -10;

if (number >= 0)

    println("Positive number");

else

    println("Negative number");

}

?  
output: Negative number

### ④ switch

→ The switch statement is used to execute one block of code among many options based on the value of a variable.

→ Ex:-

String fruit = "Apple";

switch(fruit)

{  
    case "Apple":

        println("You choose Apple");

        break;

    case "Mango":

        println("You choose Mango");

        break;

    default:

        println("Unknown fruit");

}

?  
Output:- You choose Apple

⑤

## Array, String

→ **Array**: An array is a collection of elements of the same data type, stored in a contiguous memory location.

Ex:-

```
int arr[5] = {10, 20, 30, 40, 50};
```

```
int arr[5] = {90, 80, 70, 60, 50};
```

→ **String**: A string is an object that represents a sequence of characters.

Ex:-

```
String name = "Alice";
```

```
String city = new String("New York");
```

## ⑥ for loop

→ used when you know how many times you want to loop.

→ Ex. print 1 to 5

clear Demo

```
for (String s : arr)
```

```
{ for (int i = 1; i <= 5; i++)
```

```
    System.out.println(i);
```

```
}
```

```
}
```

Output:

1  
2  
3  
4  
5

## ⑦ while loop

→ Ex. Print 1 to 5

class Demo

{

perm(string[] args)

{

int i=1;

while (i<=5)

{

cout << i;

i++;

}

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## 9 Time & Space Complexity

### (a) Time complexity

→ It tells you how fast an algorithm runs as the input size increases.

→ Common time complexities:

Notation      Name

$O(1)$       constant time

$O(\log n)$       logarithmic time

$O(n)$       linear time

$O(n \log n)$       log-linear time

$O(n^2)$       quadratic time

$O(2^n)$       Exponential time

$O(n!)$       factorial time

#### Example

Accessing an array element:  $O(1)$

Binary search

Loop through Array,

Merge sort, Quick sort

Brute force

Nested loop (Bubble sort)

Recursive fibonacci

Brute-force permutation

Set partitions

### (b) Space complexity

→ It tells you how much memory an algorithm needs based on input size.

→ includes:

- variables

- Data structures (array, lists, maps etc.)

- function call stack (especially in recursion)

## Lec-2: Build up logical thinking

④ Pattern - Done

lec 3: Java collections : Done

lec 4: Basic Maths

① Count Digits

→  $N = 7789$  : extraction of digits

$$7789 \div 10 = 9$$

↓ it will give the remainder.

$$7780 \rightarrow 9$$

$$7789 / 10 = 778.9 = 778$$

$$778 \div 10 = 78 \quad (\Rightarrow 778 / 10 = 77)$$

$$77 \div 10 = 7 \quad (\Rightarrow 77 / 10 = 7)$$

$$7 \div 10 = 0$$

while ( $n > 0$ )

→ while ( $n > 0$ )  
{     lastDigit =  $n \div 10$ ;

$$n = n / 10;$$

    count++;

    ?     if (lastDigit == 0)  
        copyCount);

$$\log_{10}(7789) + 1$$

$$3.81 - + 1$$

4

→ TC →  $O(\log_{10}(N))$

## ② Reverse a number

→ Given an integer  $N$  return the reverse of given number.

Note: If a number has trailing zeros, then the reverse will not include them, for e.g. Reverse of 10400 will be 40 instead of 00401.

Ex:- I/P :  $N = 12345$

O/P : 54321

→

$rev = 0;$

while ( $N > 0$ )

{ int rem =  $N \% 10$ ;

$N = N / 10;$

$rev = rev \times 10 + rem;$

} // (P.B.F.F) loop  
Sopln(rev)

## ③ Palindrome number

→ Given an integer  $N$ , return true if it is a palindrome else return false.

A palindrome is a number that reads the same backward as forward.

for example : 121, 1331 & 4554

Ex:-

I/P : 4554

O/P : true

I/P : 7789

O/P : false

→ int n = 1991

int rev = 0;

int sum = 0;

while (n > 0)

{ int rem = n % 10; }  
operator % to calculate the remainder of division

n = n / 10;

rev = rev \* 10 + rem;

}

return sum == rev;

#### ④ Armstrong number

→ Given an integer N, return true if it is an Armstrong number otherwise return false.

An Armstrong number is a number that is equal to the sum of its own digits each raised to the power of the number of digits.

Ex:- 153

$$1^3 + 5^3 + 3^3 = 1 + 125 + 27 = 153$$

True

→ int n = 153; int count = 0; int sum = 0; int digit = 0;  
int count = 0; (int) Math.log10(n) + 1; To calculate the number of digits  
int sum = 0; operator + to add digits  
while (n > 0)

{ int rem = n % 10;

n = n / 10;

sum = sum + Math.pow(rem, count);

? System.out.println("Armstrong number");

## ⑤ Print all divisors:

→ Given an integer  $N$ , return all divisors of  $N$ .

A divisor of an integer  $N$  is a positive integer that divides  $N$  without leaving a remainder.

Ex:-  $n = 36$

OP:-  $[1, 2, 3, 4, 6, 9, 12, 18, 36]$

→ Ex:-

$n = 26$

for ( $i=1$ :  $i \leq n$ ;  $i++$ )

{ if ( $n \% i == 0$ )

cout  $\ll$  i;

}

→ Tc :-  $O(n)$

## ⑥ find gcd of two numbers

→ Given two integers  $n_1$  and  $n_2$ . find their

greatest common divisor.

The gcd of any two integers is the largest number that divides both integers.

Ex:-  $n_1 = 9$

$n_2 = 12$

OP:- 3

```

→ for int gcd = 1;
    for (int i = 1; i < Math.min(m1, m2); i++)
        if (m1 % i == 0 && m2 % i == 0)
            gcd = i;
    return gcd;
}

```

$\rightarrow$  for ( $i = \min(\sigma_1, \sigma_2)$ ;  $i >= 1$ ;  $i--$ )  
 { if ( $\sigma_1[i] == 0$  &  $\sigma_2[i] == 0$ )  
 { gcd = i;  
 break;  
 }  
 Tc = O(\min(\sigma\_1, \sigma\_2)) + t\_w

→ Euclidean Algorithm:-

$\text{gcd}(a, b) = \text{gcd}(a + -b, b)$   
 $\text{while } (a > 0 \text{ and } b > 0)$   
 \$ \quad \text{if } (a > b) \quad a = a - b;  
 else  $b = b - a$   
 if  $(a == 0) \quad \text{topin}(b)$   
 else  $\text{topin}(a)$

## 7 Check Prime number

Given an integer n, check whether it is prime or not.

A prime number is a number that is only divisible by 1 and itself, and the total number of divisors is 2.

Ex:-  $n=2$  |  $1 \leq i \leq 10$   
O/P:- True       $O/P = \text{false}$

$\rightarrow$  init.  $cnt = 0;$

for ( $i=1; i*i <= n; i++$ )

if ( $n \% i == 0$ )

{  
 $cnt++;$   
 $if ((n \% i) != i)$   
 $cnt++;$

3

if ( $cnt == 2$ ) return true;

else return false;

$(2, 0) \text{ top} = (2, 21) \text{ base}$

$(2, 0) \text{ top} = (2, 21) \text{ top}$

$(2, 21) \text{ top} = (2, 0) \text{ top}$

$(2, 0) \text{ top} = (2, 21) \text{ top}$

(solution)

$(d, d+n) \text{ top} = (d, n) \text{ base}$

$(d, d+n) \text{ top} = (d, n) \text{ base}$

$d \cdot d = d \quad (d > 0)$

$d \cdot d = d \quad (d > 0)$

$(d, d+n) \text{ top} = (d, n) \text{ base}$

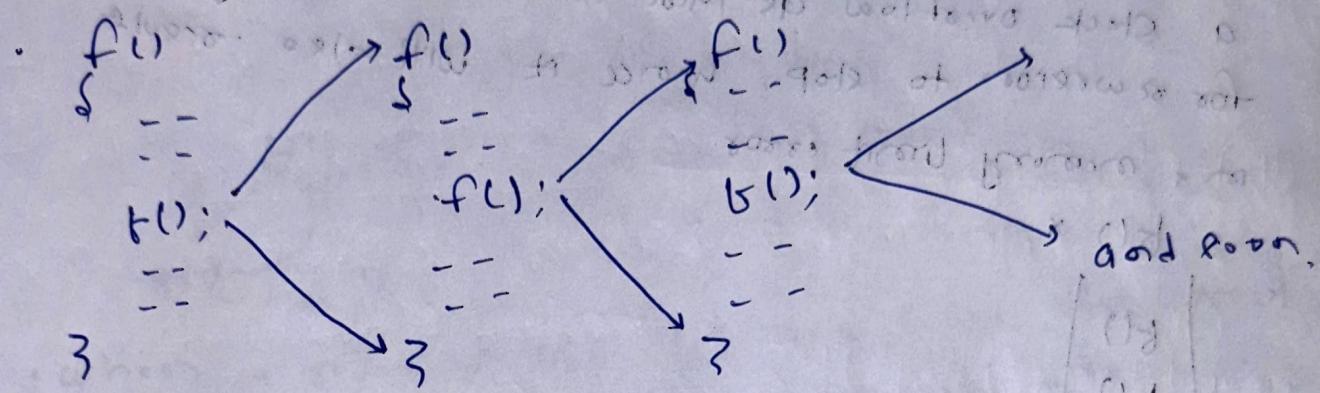
$(d, d+n) \text{ top} = (d, n) \text{ base}$

## Lec 5: Learn Basic Recursion

- ① Understanding recursion by point something N times

→ What is Recursion?

- It is a phenomenon when a function calls itself indefinitely until a specified condition is fulfilled.



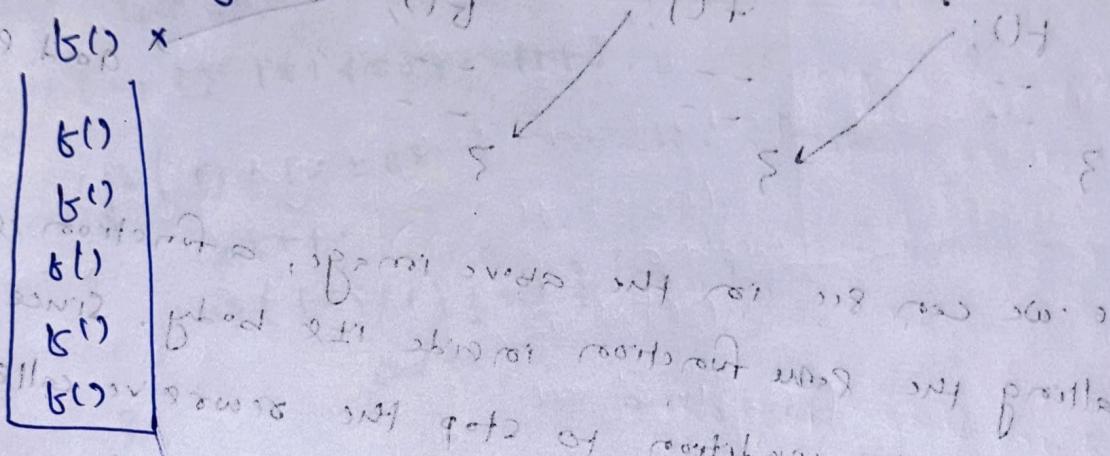
- As we can see in the above image, a function is calling the same function inside its body. Since there is no condition to stop the recursive calls, the calls will run indefinitely until the stack runs out of memory (stack overflow).

→ What is Recursive Stack Overflow in Recursion?

- Whenever recursive calls are executed, they are simultaneously stored in a workspace stack where they wait for the completion of the recursive function. A recursive function can be only be completed if a base condition is fulfilled and the control returns to the parent function.

- But, when there is no base condition given for a particular recursive function, it gets called indefinitely which results in a stack overflow i.e., exceeding the memory limit of the recursion stack and hence the program terminates giving a segmentation fault error.

- The illustration above also represents the case of a stack overflow as there is no terminating condition for recursion to stop, hence it will also result in a memory limit error.



### Base condition

- Stating the condition that is written in a recursive function in order for it to get completed and not to run indefinitely. After encountering the base condition, the function terminates and returns back to its parent function simultaneously.

Ex:

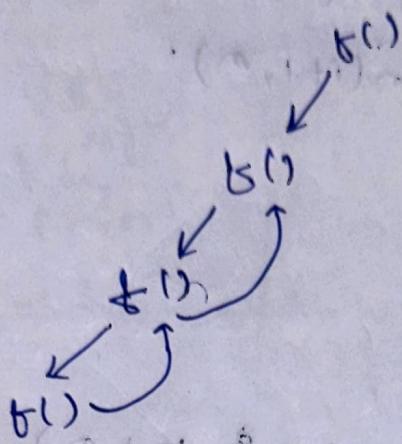
```

    int count = 0;
    f()
    {
        if(count == 3)
            return;
        cout << count;
        count++;
        f();
    }
  
```

O/P: 0 1 2

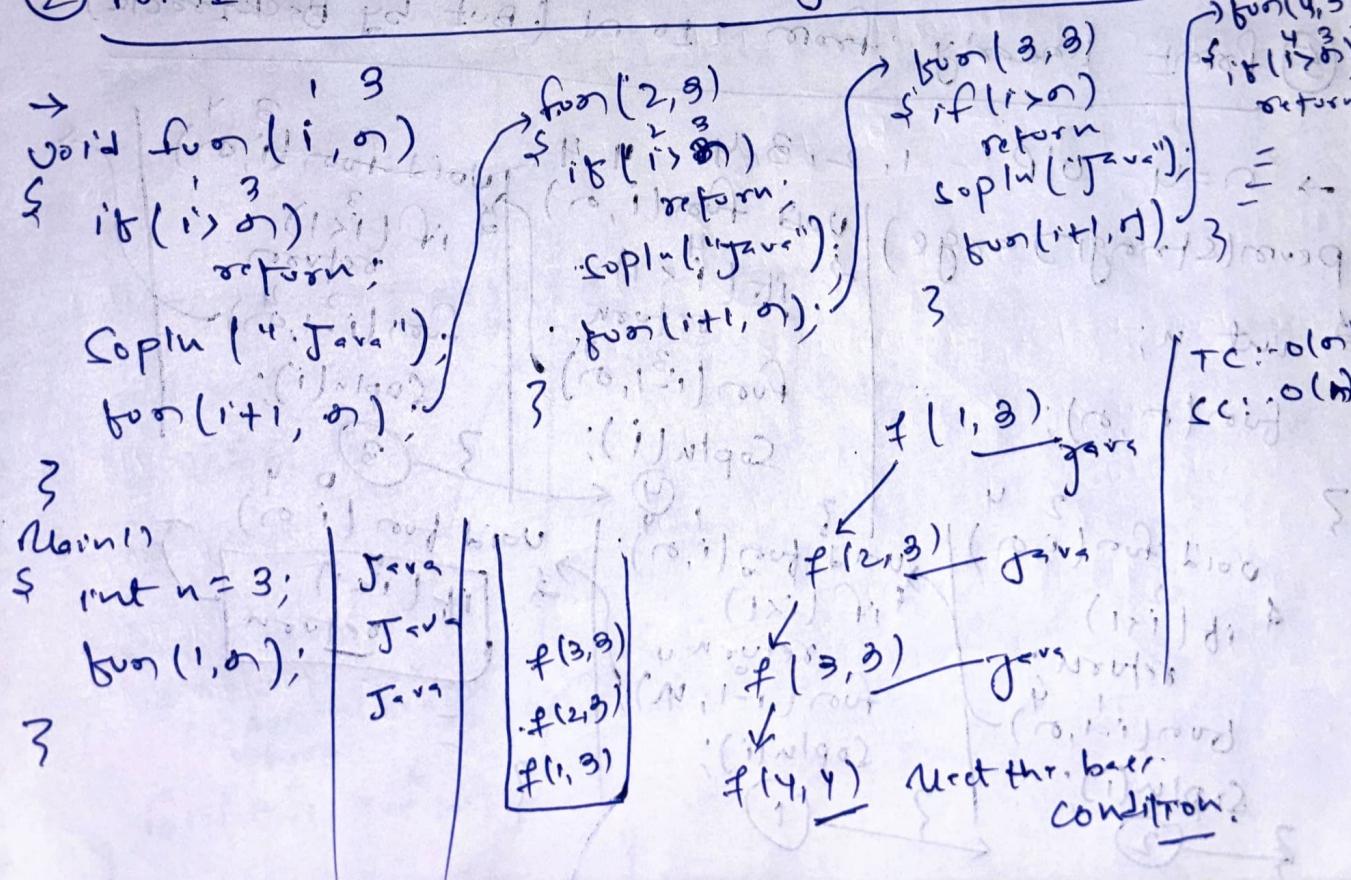
## → Recursive Function

- A recursive function is basically a representative form of recursion which depicts how functions are called and returned back in terms of execute happening recursively. It's a pictorial description of the process of recursion as below:



- When a recursive call gets completed, the control returns back to the parent function which is then further executed until the last function waiting in the recursive stack returns.

## ② Point name or times using Recursion



③ Point linearly from 1 to n.

$\rightarrow n=4$ ,  $OP = 1, 2, 3, 4$

perm(string range)

```
int n=4;
fun(1, n);
{
```

void fun(int i, int n)

```
if (i > n)
    return;
cout(i);
fun(i+1, n);
}
```

④ Point ~~in~~ from n to 1.

$\rightarrow n=4$ ,  $OP = 4 3 2 1$

perm(string range)

```
int n=4;
fun(n, n);
{
```

void fun(int n, int m)

```
if (n < m)
    return;
cout(m);
fun(m-1, n);
}
```

⑤ Point linearly from 1 to n (But by Backtracking).

$\rightarrow n=4$ ,  $OP = 1, 2, 3, 4$

perm(string range)

```
int n;
fun(n, n);
{
```

void fun(i, n)

```
if (i > n)
    return;
cout(i);
fun(i+1, n);
}
```

void fun(i, n)

```
if (i > n)
    return;
cout(i);
fun(i-1, n);
}
```

void fun(i, n)

```
if (i > n)
    return;
cout(i);
fun(i-1, n);
}
```

if (i > n)
 return;

①      ②      ③      ④

## ⑥ Point $\alpha \rightarrow 1$ (using back track)

4.3  
function  
d if (ison)  
    &erson;

7) Sum of first  $n$  numbers

(a) Parameterized w/ J

$$\underline{N=3} \quad \underline{0P:-6}$$

~~return (long) a[0]~~

~~int n = 3;~~

~~if (n == 0)~~

~~return 0;~~

~~return n + f(n-1);~~

~~3~~

~~3 0~~

~~f(0, even)~~

perm (strong) org x if fin (n, 8 um)

10

int u=3;  
~~cout < u;~~

~~Specimen~~,  
Fig 1 (or 0).

$$3 \in \left( \frac{1}{6}, \frac{5}{8} \right)$$

2 if( $\alpha \geq 1$ )  
copinlsum;

return; 6

3 ~~+0.1~~ -0.1, 3

3 3

for ( $i, m$ )

if ( $i > m$ )  
return;

if ( $i \leq m$ )  
for ( $i, m$ )  
if ( $i > m$ )  
return;  
if ( $i \leq m$ )  
fun( $i+1, m$ )

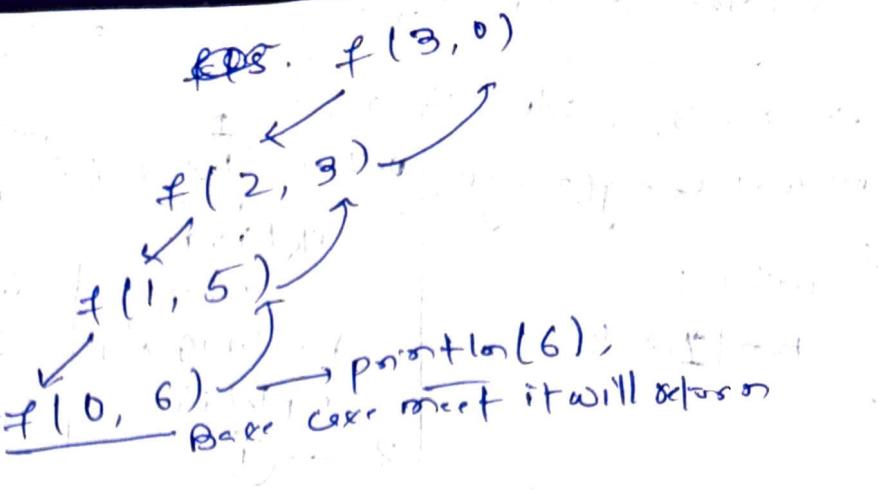
fun( $i+1, m$ )

copy( $i$ );

3 3

## ⑥ Parameters

(b) functional



## b) functional

$$\rightarrow n=3, \text{ sum}=6$$

prevon(strong argu)

point  $n=3;$

$\text{Sopl(fun}(n));$

3

$f(n)$

if( $n==0$ )  
return 0;

return  $\text{int}+f(n-1);$

?

$\boxed{1+0}$

(and so) root

(and so) right

(and so) left

fun(3, 1-0), out 2 + f(0)

(and so) right

(and so) left

fun(2, 1-1), out 1 + f(1)

(and so) right

(and so) left

fun(1, 1-2), out 0 + f(2)

(and so) right

(and so) left

X

fun(n)

if( $n==0$ )  
return 0;

return  $\text{int}+f(n-1);$

$\boxed{3+3}$

$f(n)$

if( $n==0$ )  
return 0;

$\boxed{3+0}$

$f(n)$

if( $n==0$ )  
return 0;

$\boxed{3+0}$

$f(3)$

$\boxed{6}$

$3+f(2)$

$\boxed{9}$

$2+f(1)$

$\boxed{1}$

$1+f(0)$

$\boxed{0}$

fun(n)

if( $n==0$ )  
return 0;

return  $\text{int}+f(n-1);$

$\boxed{2+1}$

$2+f(1)$

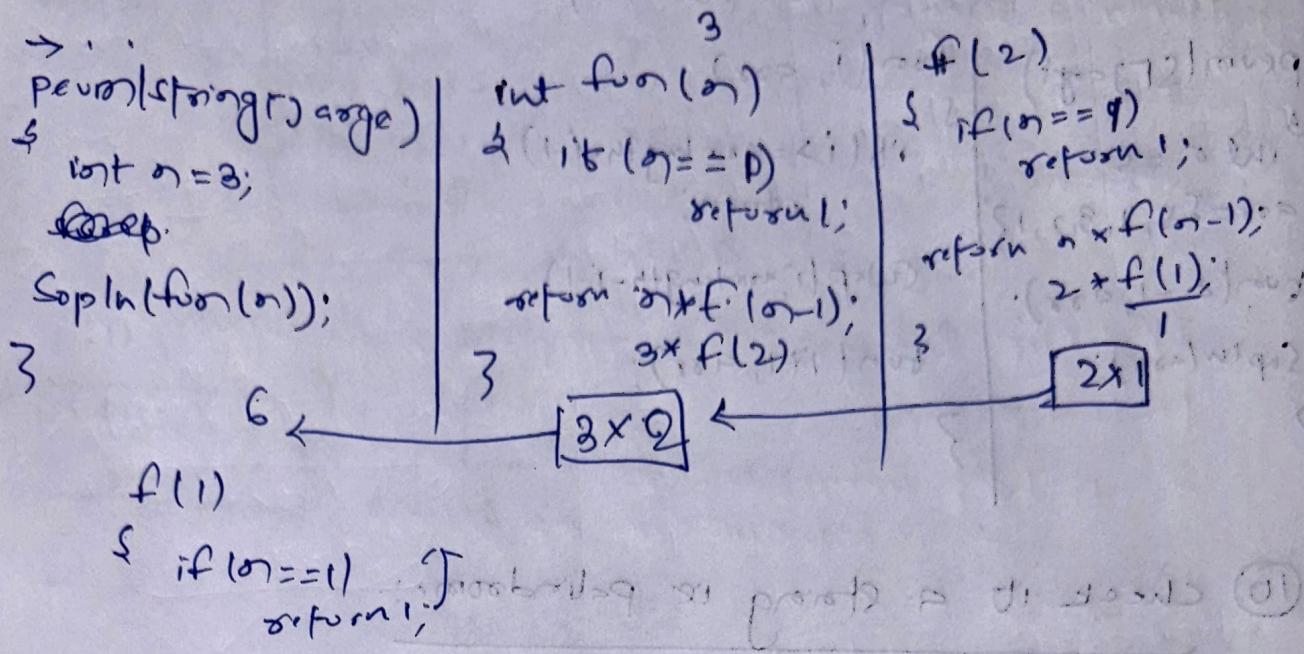
$\boxed{3+1}$

$3+f(0)$

$\boxed{3+0}$

## ⑧ factorial of N

$\rightarrow n = 3, \text{ O/P: } 1 \times 2 \times 3 = 6$



{ if ( $n == 1$ )  
return;

• = ~~ans = ans + 2 \* n~~ ~~for loop~~ ~~ans = ans + 2 \* n~~

}

## ⑨ Reverse a given array

### ⓐ Using two pointers

$\bullet n = 5, \text{ arr} = \{5, 4, 3, 2, 1\}$

O/P:  $\{1, 2, 3, 4, 5\}$

$\rightarrow$  `perm(string &arr)`

{ int n = 5;

int l = 0, r = n - 1;

swap(l, r, arr);

fun(l + 1, r - 1, arr);

swap(l, r, arr);

fun(l + 1, r - 1, arr);

swap(l, r, arr);

fun(l + 1, r - 1, arr);

swap(l, r, arr);

fun(l + 1, r - 1, arr);

swap(l, r, arr);

fun(l + 1, r - 1, arr);

swap(l, r, arr);

fun(l + 1, r - 1, arr);

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fun(l + 1, r - 1, arr);

swap(l, r, arr);

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fun(l + 1, r - 1, arr);

swap(l, r, arr);

fun(l + 1, r - 1, arr);

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swap(l, r, arr);

fun(l + 1, r - 1, arr);

⑥ Using single pointer

(ii) P:  $n=5$ ;  $a_{88} = \{5, 4, 3, 2, 1\}$

```

Pewon(&arr)
{
    int n = 5;
    arr = {5, 4, 3, 2, 1};
    fun(0, arr);
    swap(arr, 0);
}
}

fun(i, arr)
{
    if(i >= arr.length - i - 1)
        return;
    swap(i, arr.length - i - 1);
    fun(i + 1, arr);
}

swap(i, j)
{
    arr[i] = arr[i] ^ arr[j];
    arr[j] = arr[i] ^ arr[j];
    arr[i] = arr[i] ^ arr[j];
}

```

⑩ Check if a string is palindrome.

→ A strong on reversal reads the same.

$\rightarrow \text{NP} = e = \text{"UADAM"}$

```

    prev1)
    {
        if(strong == "NADAM")
            cout << f(0, s);
        else
            cout << f(0, 0, 1, s);
    }
}

int f(int i, string s)
{
    if(i == s.length())
        return true;
    if(s[i] != s[s.length() - i - 1])
        return false;
    if(i + 1 == s.length())
        return true;
    if(s[i] == s[i + 1])
        return f(i + 2, s);
    else
        return f(i + 1, s) || f(i + 2, s);
}

```

## ⑪ Fibonacci numbers

→ Given An integer  $N$ . Print the upto the  $N$ th term.

N=5

0|0: 0, 1, 1, 2, 3, 5

$$f_{i,b}(i) = f_{i,b}(i-1) + f_{i,b}(i-2);$$

```

prvmt()
{
    int n=4;
    fun(n)
}

int fun(int i)
{
    if (i<=1)
        return i;
    else
        {
            int laet = fun(i-1);
            int slret = fun(i-2);
            return laet+slret;
        }
}

```

$f(0) \rightarrow f(1)$   
 $f(1) \rightarrow f(2)$   
 $f(2) \rightarrow f(3)$   
 $f(3) \rightarrow f(4)$   
 $f(4) \rightarrow f(5)$

if ( $i <= 1$ )  
 return i;  
 $\downarrow$   
 $\downarrow$   
 $\downarrow$   
 $\downarrow$   
 $\downarrow$

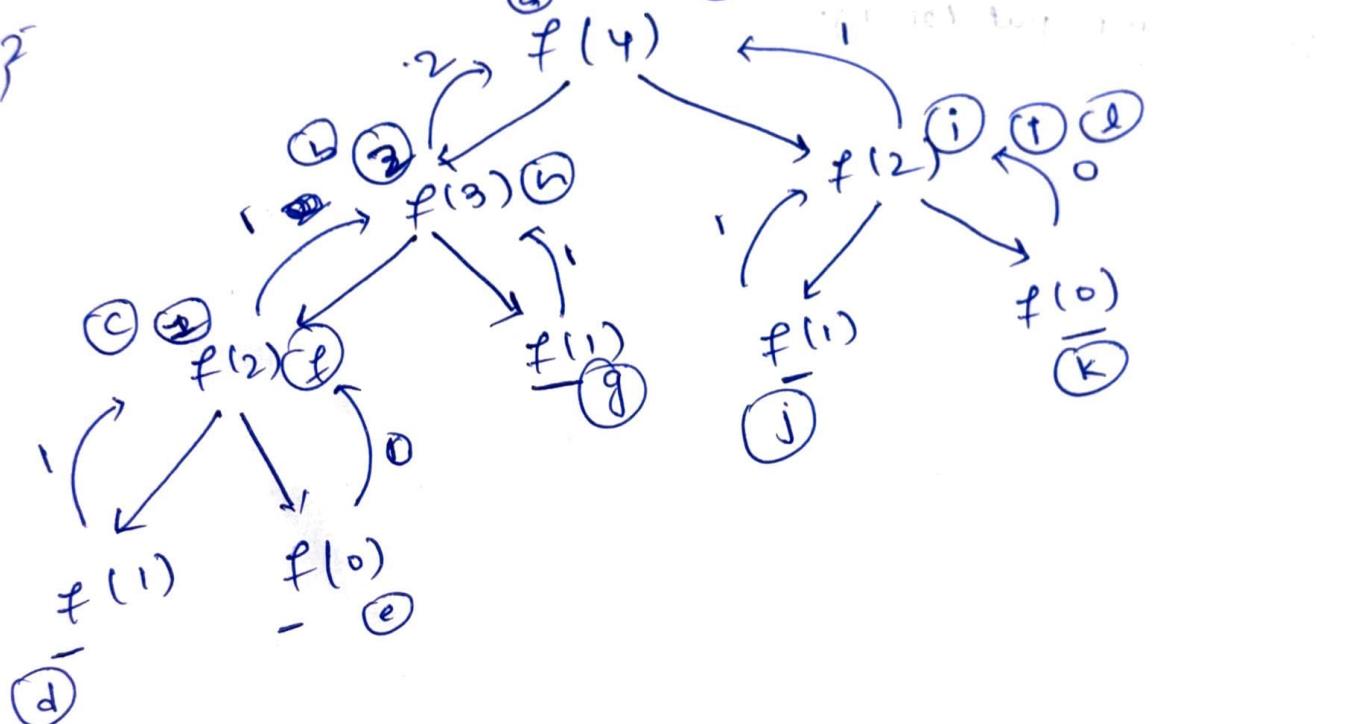
$f(1) \rightarrow f(0)$   
 $f(2) \rightarrow f(1)$   
 $f(3) \rightarrow f(2)$   
 $f(4) \rightarrow f(3)$   
 $f(5) \rightarrow f(4)$

```

f(1)
{
    if (i<=1)
        return i;
}

```

$f(0) \rightarrow f(1)$   
 $f(1) \rightarrow f(0)$   
 $f(1) \rightarrow f(2)$   
 $f(2) \rightarrow f(1)$   
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 $f(99) \rightarrow f(100)$



## lec6: Learn Basic Hashing

### ① Hashing Theory:

→ ~~Hash~~ →  $\text{hash} = \{1, 5, 2, 9, 7, 2, 3, 13\}$   
Hash Map: Integer, Integer → mp = new HashMap<1>;  
for (int n: hash)  
if (mp.containsKey(n))

{ if (mp.get(n) < 1)  
    mp.put(n, mp.get(n) + 1);

else {

    mp.put(n, 1);

② ③ ④

(1) 2 3

