

Q1) Given  $N$  elements, point max subarray sum of  
len =  $k$ .

Ex1 arr[8] = {<sup>0</sup>-3 <sup>1</sup>2 <sup>2</sup>6 <sup>3</sup>4 <sup>4</sup>1 <sup>5</sup>-4 <sup>6</sup>5 <sup>7</sup>3}  
 $k=4$

s	e	sum
0	3	9
1	4	13
2	5	7
3	6	6
4	7	5

ans = 13

Pseudo Code !

int s = 0, e = k-1;  
max\_val = Integer.Min;

while (e < n) {

// iterate from s to e to  
get sum.

int sum = 0;

for (int i = s; i ≤ e; i++) {

sum = sum + arr[i];

}

max\_val ⇒ max(max\_val, sum);

s++, e++;

}

point max\_val;

Tc ⇒ no of subarrays  $\times k$

e = [k-1, n-1]

$n - (k-1) + 1$

⇒  $n - k + 1$

no of  
Subarrays =  $n - k + 1$



$$T_c : (n-k+1)(k)$$

↓

$$k=1$$

$$T_c = O(n)$$

↓

$$k = n/2$$

$$T_c : O(n^2)$$

$$S_c : O(1)$$

↓

$$k \neq N$$
$$T_c = O(n)$$

Approach 2:

1) Use Prefix Sum.

if  $(s == 0)$   
     $sum = pf[e];$

else  
     $sum = pf[e] - pf[s-1]$

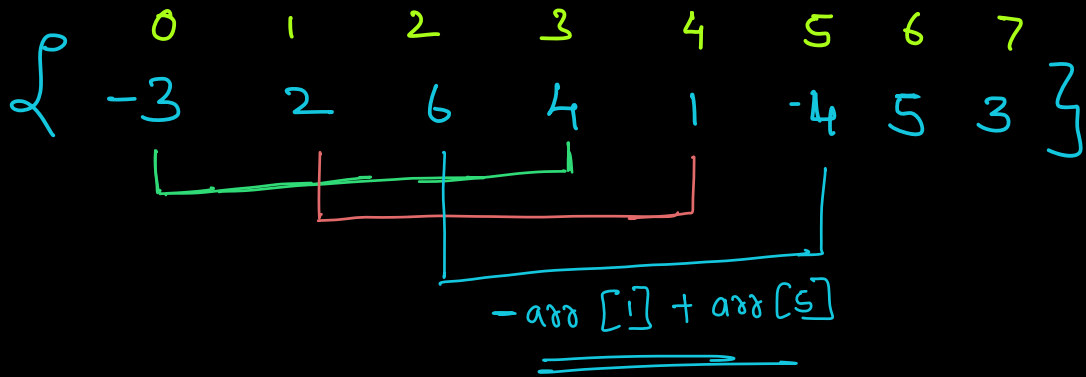
$$T_c : O(n), S_c : O(n)$$

$$T_c = \text{no of subarrays}$$
$$= (n-k+1)$$

$$T_c : O(n)$$

worst case

## Approach 2:



s e sum

0 3 9  $\Rightarrow$  loop & find sum.

1 4 13  $\Rightarrow$   $\text{sum} = \text{arr}[0] + \text{arr}[1] + \text{arr}[2]$   
 $9 - (-3) + 1 \Rightarrow \underline{13}$

2 5 7  $\Rightarrow$   $\text{sum} = \text{arr}[i] + \text{arr}[s] + \text{arr}[s+1]$   
 $\Rightarrow 13 - 2 + (-4) \Rightarrow 7$

3 6 6  $\Rightarrow$  Similar trick

4 7 5

for s & e :  $\text{sum} = \text{arr}[s-1] + \text{arr}[e]$

[ carry forward + subarrays of same length = SLIDING WINDOWS ]

## Pseudo Code

```
int s = 0, e = k-1;  
max_val = Integer.Min;  
sum = 0
```

```
for (int i = s; i ≤ e; i++) {  
    sum = sum + arr[i];
```

// first window

k iterations

```
}
```

```
max_val = sum;
```

```
s = 1, e = k;
```

```
while (e < n) {
```

```
    sum = sum - arr[s-1] + arr[e];
```

```
    max_val = max(max_val, sum);
```

```
    s++; e++;
```

```
}
```

```
return max_val;
```

→ [k, n-1]

~~n - 1~~ - ~~k + 1~~

= n - k

iterations.

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Tc:  $O(n)$

Sc:  $O(1)$

Q2 Given  $arr[]$  and a number  $B$ . Find and return minimum no of swaps to bring all numbers  $\leq B$  together.

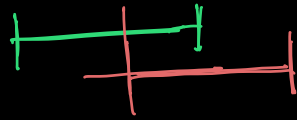
Ex1  $arr = \{ \underline{1} \ 12 \ 10 \ \underline{3} \ 14 \ 10 \ \underline{5} \}$ ,  $B=8$   
ans = 2

Ex2  $arr[] = \{ 19 \ 11 \ \underline{3} \ \underline{9} \ \underline{7} \ 25 \ \underline{6} \ 20 \ \underline{4} \}$ ,  $B=10$   
ans = 1

- 1) Find the count of elements  $\leq B$ . Let's say it is  $R$ . This is the window size
- 2) good elements  $\Rightarrow$  elements  $\leq B$ .
- 3) For a subarray of len  $R$ . If number good element =  $X$

$$\text{Swaps} \Rightarrow \underline{R - X}$$

{ 1 12 10 3 14 10 5 } , B = 8



1<sup>st</sup> window : no of good elements (ng)  $\Rightarrow$  1

2<sup>nd</sup> window : if (arr[s-1]  $\leq$  B)  
ng--;

if (arr[e]  $\leq$  B)  
ng++;

Pseudo code!

```
1) // find size of window.
for (int i=0 ; i < n ; i++) {
    if (arr[i]  $\leq$  B)
        k++;
}
```

// k is the  
size of  
window.

3

2) // Edge Cases.

```
if (k == 0 || k == 1 || k == n)
    return 0;
```

3) // first window

```
ng = 0
for (int i = 0; i < k - 1; i++) {
    if (arr[i] < B)
        ng++;
}
```

```
min_val = k - ng;
```

4) // Sliding window.

```
int s = 1, int e = k;
```

```
while (e < n) {
    if (arr[s - 1] < B)
        ng--;
```

```
    if (arr[e] < B)
        ng++;
```

```
    ans = k - ng;
```

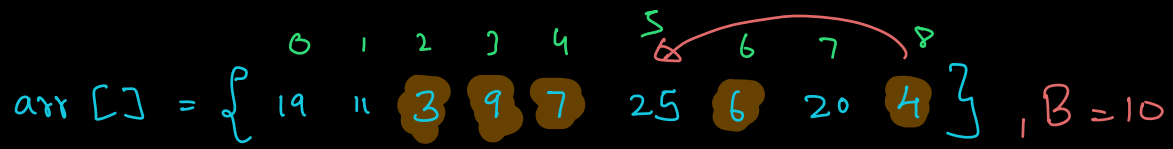
```
    min_val = min(ans, min_val);
```

```
    s++, e++
}
```

Tc:  $O(n)$

Sc:  $O(1)$

arr[] = { 19 11 3 9 7 25 6 20 4 } , B = 10



ans = 1 , s = 2, e = 6

⇒ [0, s-1] ⇒ no good elements

[e+1, n-1] ⇒ [8]

⇒ [s, e]



Q3 Given  $mat[n][n]$ , print boundary in clockwise direction.

1	2	3	4	5
6	7	8	9	10
11	12	13	14	15
16	17	18	19	20
21	22	23	24	25

→  $n-1$  elements in the first row.

→  $n-1$  elements in the last column.

→  $n-1$  elements in the last row.

→  $n-1$  elements in the first column.

Tc:  $O(m+n)$

Sc:  $O(1)$

Pseudo code

int i=0, int j=0

```
for (k=1 ; k < n ; k++) {  
    print (mat[i][j]);  
    j++;  
}
```



i=0, j=n-1

3

```
for (k=1 ; k < n ; k++) {  
    print (mat[i][j]);  
    i++;  
}
```

3



i=n-1, j=n-1

```
for (k=1 ; k < n ; k++) {  
    print (mat[i][j]);  
    j--;  
}
```

3



i=n-1, j=0

```
for (k=1 ; k < n ; k++) {  
    print (mat[i][j]);  
    i--;  
}
```

3



i=0, j=0

# Q4 Spiral printing

1	2	3	4	5	26
6	7	8	9	10	27
11	12	13	14	15	28
16	17	18	19	20	29
21	22	23	24	25	30
31	32	33	34	35	36

$$n \Rightarrow 6 \Rightarrow k=5$$

↓

$$n \Rightarrow 4 \Rightarrow k=3$$

↓

$$n=2 \Rightarrow k=1$$

↓

$$n=0 \Rightarrow \text{terminating condition}$$

1	2	3	4	5
6	7	8	9	10
11	12	13	14	15
16	17	18	19	20
21	22	23	24	25

$$n=5, k \Rightarrow 4$$

$$n=3, k=2$$

$$n=1, k=0$$

↓

print (mat[i][j])

Pseudo code

int i=0, int j=0

while (n > 1) {

for (k=1; k < n; k++) {  
    print (mat[i][j]);  
    j++;

}

for (k=1; k < n; k++) {  
    print (mat[i][j]);  
    i++;

}

for (k=1; k < n; k++) {  
    print (mat[i][j]);  
    j--;

}

for (k=1; k < n; k++) {  
    print (mat[i][j]);  
    i--;

}

n = n-2; i++; j++;

}

if (n == 1)  
    print (mat[i][j]);

}

Tc:  $O(n^2)$

Sc:  $O(1)$