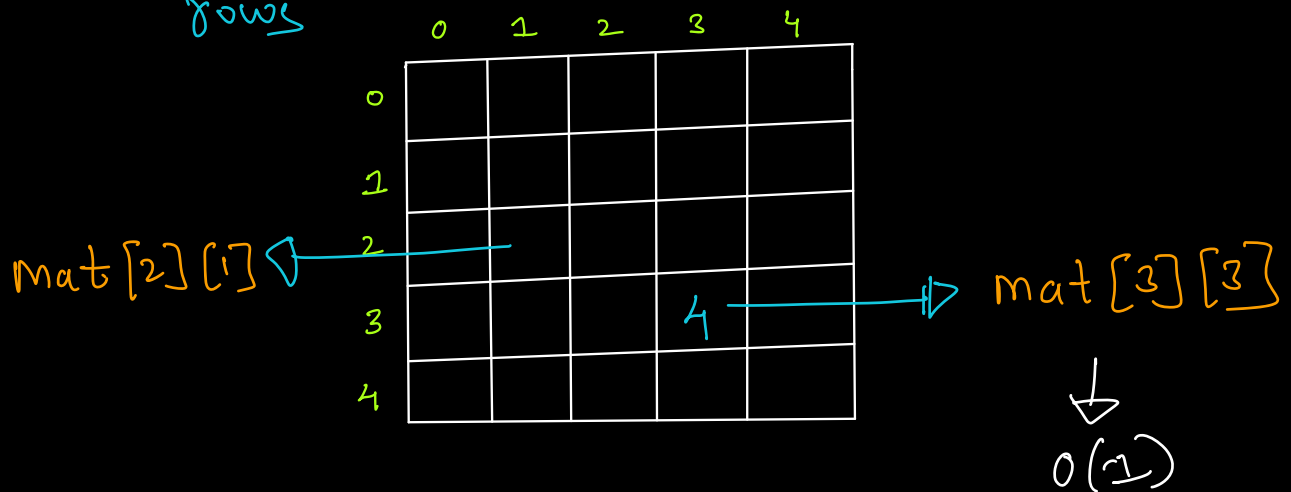
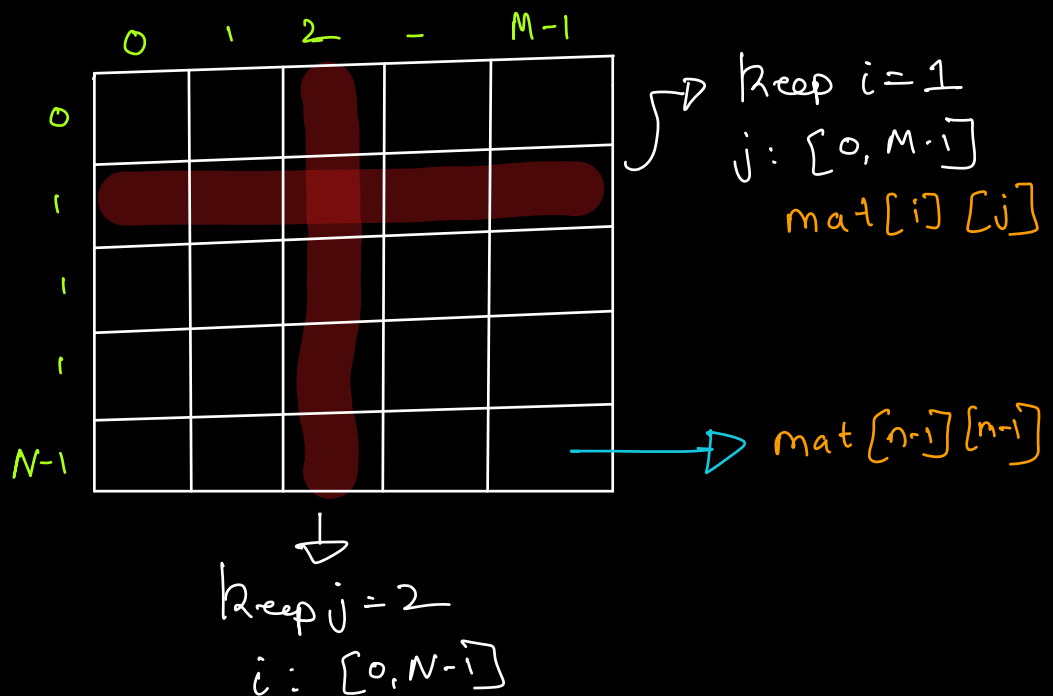


2D Arrays [BASICS]

`int mat[5][5]`
↓
rows
→ columns



`int mat[N][M]`



Q1) Given a $\text{mat}[N][M]$, print row-wise sum.

$\text{mat}[3][4]$

	0	1	2	3	
0	3	8	9	2	22
1	1	2	3	6	12
2	4	10	11	17	42

int sum \Rightarrow 0

for (int i = 0; i < n; i++) {
sum \Rightarrow 0

for (int j = 0; j < m; j++) {
sum = sum + mat[i][j]

}
print sum; Tc: $O(mn)$
gc: $O(1)$

Q2) Given $\text{mat}[N][M]$, find max column sum.

	0	1	2	3
0	3	8	9	2
1	1	2	3	6
2	4	10	11	17
	8	20	23	25

Tc: $O(mn)$
gc: $O(1)$

int sum \Rightarrow 0

int max-Sum = INT.MIN;

for (int j = 0; j < m; j++) {
sum \Rightarrow 0

for (int i = 0; i < n; i++) {
sum = sum + mat[i][j];

}
max-Sum = max(max-Sum, sum);

}
print max-Sum

Q3 Given a $mat[N][N]$, print diagonals.

Case 1: Left \rightarrow Right

Case 2: Right \rightarrow Left

CASE 1

$mat[4][4]$

	0	1	2	3
0	(0,0)			
1		(1,1)		
2			(2,2)	
3				(3,3)

L-R

for (int i=0; i<n; i++) {

for (int j=0; j<n; j++) {

if (i==j)

print mat[i][j]

}

}

Tc: $O(n^2)$
Sc: $O(1)$

Optimized solution.

int i=0;

while (i<n) {

print mat[i][i];

i++;

}

Tc: $O(n)$
Sc: $O(1)$

CASE 2

	0	1	2	3
0				(0,3)
1			(1,2)	
2		(2,1)		
3	(3,0)			

R-L

i	j
0	3
1	2
2	<u>1</u>
3	0
<u>3</u>	(n-i-1)

i=0, j=n-1

while (i < n) {

print mat[i][j];

i++;

j--;

}

i=0,

while (i < n) {

print mat[i][n-i-1]

i++;

}

Tc: $O(N)$

Sc: $O(1)$

Diagonals in a Rectangle

Row = n
Column = m

	0	1	2	3	4
0	↖	↗	↘	↙	↕
1	↖	↗	↘	↙	↕
2	↖	↗	↘	↙	↕

no of diagonals = $(m + n - 1)$

Q4 Given $mat[N][M]$, print all diagonals going R-L.

$mat[3][5]$

	0	1	2	3	4
0	1	2	3	4	5
1	6	7	8	9	10
2	11	12	13	14	15

row	column
0	4
1	3
2	2
3	1

row	column
0	1
1	0
2	-1

$[1]$
 $[2, 6]$
 $[3, 7, 11]$
 $[4, 8, 12]$
 $[5, 9, 13]$
 $[10, 14]$
 $[15]$

i, j
$i++$ $j--$

$i < n$ $\&\&$ $j \geq 0$

Terminating condition.

Pseudo code

$i = 0$

for (int $j = 0$; $j \leq m$; $j++$) {

int row = i

int col = j

while (row $< n$ && col ≥ 0) {

print mat[row][col];

row++; col--;

3 3

$T_c: O(mn)$

$Sc: O(1)$

$j = m - 1$

for (int $i = 1$; $i \leq n$; $i++$) {

int row = i

int col = j

while (row $< n$ && col ≥ 0) {

print mat[row][col];

row++; col--;

3 3

8:12am

Q5 Given a $\text{mat}[N][N]$, find the transpose in place. Given input $\text{mat}[] []$ should get updated. No extra space has to be used.
 SC: $O(1)$

$\text{mat}[5][5]$

	0	1	2	3	4
0	1	2	3	4	5
1	6	7	8	9	10
2	11	12	13	14	15
3	16	17	18	19	20
4	21	22	23	24	25

Original

	0	1	2	3	4
0	1	6	11	16	21
1	2	7	12	17	22
2	3	8	13	18	23
3	4	9	14	19	24
4	5	10	15	20	25

Transpose

	0	1	2	3	4
0	1	2	3	4	5
1	6	7	8	9	10
2	11	12	13	14	15
3	16	17	18	19	20
4	21	22	23	24	25

Swap [mat[i][j], mat[j][i]]

Pseudo Code:

for (int i=0 ; i < n ; i++) {

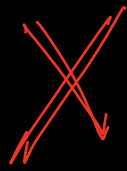
for (int j=0 ; j < n ; j++) {

if (i != j)

swap (mat[i][j], mat[j][i]);

}

}



We get original array in the end.

	0	1	2	3	4
0	1	6	11	16	21
1	2	7	12	17	22
2	3	8	13	18	23
3	4	9	14	19	24
4	5	10	15	20	25

Transpose

TODO:

Iterate on upper/lower triangle and swap.

What if the matrix is a rectangle.

2	1	3
5	6	4.

2×3

2	5
1	6
3	4

3×2

Cannot be solved in $O(1)$ space.

Q6) Given a mat $[N][N]$, rotate by 90° clockwise. Inplace. SC: $O(1)$

	0	1	2
0	1	2	3
1	4	5	6
2	7	8	9

	0	1	2
0	↙	↗	-
1	↘	↖	-
2	-	-	-

↓ Transpose

	0	1	2
0	1	4	7
1	2	5	8
2	3	6	9

→ reverse each row

	0	1	2
0	7	4	1
1	8	5	2
2	9	6	3

Step 1: Transpose : TC: $O(n^2)$

Step 2: Reverse each row : TC: $O(n^2)$

TC: $O(n^2)$

SC: $O(1)$

(Inplace)

