

## CESM2 (TSMLT) Feedforward and Feedback Estimates

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**Table 1: Temperature Targets**

	T0	T1	T2
Member 1	288.62	2.60	-29.52
Member 2	288.61	2.57	-29.55
Member 3	288.68	2.74	-29.30
Member 4	288.65	2.59	-29.50
Member 5	288.62	2.63	-29.38
<b>Ensemble average</b>	<b>288.64 ± 0.01</b>	<b>2.63 ± 0.03</b>	<b>-29.45 ± 0.05</b>

Targets are defined as the average over the 2020-2039 period in the SSP 245 runs (CESM2, full chemistry).

**Table 2: Sensitivity Estimates (includes significant digits)**

	My CESM 2				My CESM 1				GLENS CESM 1		
	$\ell_0^{-1}$	$\ell_1^{-1}$	$\ell_2^{-1}$		$\ell_0^{-1}$	$\ell_1^{-1}$	$\ell_2^{-1}$		$\ell_0^{-1}$	$\ell_1^{-1}$	$\ell_2^{-1}$
T <sub>0</sub>	-7.95				-6.66				-5.2		
T <sub>1</sub>	-4.8	-7.6			-2.43	-3.7			-3.7	-4.4	
T <sub>2</sub>	-2.6	0.0	-2		-2.29	-2.0	-2.49		-2.4	-2.2	-1.6

My estimates for CESM2 sensitivities are drawn from the data of Tilmes et al 2020.

**Table 3: Temperature increase seen in SSP 245 relative to temperature targets, beginning from ~0 in 2030 (in other words, how much temperature increase needs to be offset)**

Metric	Behavior	Forcing required to offset
$T_0$	+0.0276 K per year	enough $\ell_0$ to offset this change
$T_1$	erratic - assume no detectable change	enough $\ell_1$ to cancel out whatever $\ell_0$ is doing to $T_1$
$T_2$	+0.0080 K per year	enough $\ell_2$ to offset this change, minus the influence of $\ell_0$ (neglect influence of $\ell_1$ on $T_2$ - see table 2 above)

#### Feedforward calculations

- $\ell_0$ :
  - $-0.0276 \text{ K/yr} \div -7.95 \text{ K}/\ell_0 = \mathbf{0.0035 \ell_0 \text{ per year}}$
- $\ell_1$ :
  - $-4.8 \text{ K}/\ell_0 \times 0.0035 \ell_0/\text{yr} = -0.0165 \text{ K/yr to offset}$
  - $0.0165 \text{ K/yr} \div -7.6 \text{ K}/\ell_1 = \mathbf{-0.0022 \ell_1 \text{ per year}}$
- $\ell_2$ :
  - -0.0080 K/year required in total
  - $-2.6 \text{ K}/\ell_0 \times 0.035 \ell_0/\text{yr} = -0.0091 \text{ K/yr from } \ell_0$
  - 0.0011 K/yr of  $T_2$  leftover  $\rightarrow$  the desired  $\ell_0$  already overcompensates  $T_2$  by a small amount
  - $0.0011 \text{ K/yr} \div 2.14 \text{ K}/\ell_2 = \mathbf{-0.0005 \ell_2 \text{ per year}}$

**Table 4: Injection rates**

Latitude	Equation	$\ell_0$ and $\ell_1$ feeds	$\ell_0$ feed only
30N	$20\ell_1^N + 40\ell_2$	0	0
15N	$30(\ell_0 - \ell_1^N - \ell_1^S - \ell_2) + 45\ell_1^N$	$0.0388*(t-2030) \text{ Tg/yr}$	$0.1041*(t - 2030) \text{ Tg/yr}$
15S	$30(\ell_0 - \ell_1^N - \ell_1^S - \ell_2) + 45\ell_1^S$	$0.1367*(t-2030) \text{ Tg/yr}$	$0.1041*(t - 2030) \text{ Tg/yr}$
30S	$20\ell_1^S + 40\ell_2$	$0.0435*(t-2030) \text{ Tg/yr}$	0

**Table 5: Feedback gains**

<b>Metric</b>	<b>Old Gain</b>	<b>GLENS sens.</b>	<b>New sens.</b>	<b>Ratio</b>	<b>New gain</b>
$\ell_0$	0.028	-5.2	-7.95	0.66	0.0183
$\ell_1$	0.13	-4.4	-7.6	0.58	0.0753
$\ell_2$	0.39	-1.6	-2	0.8	0.3120