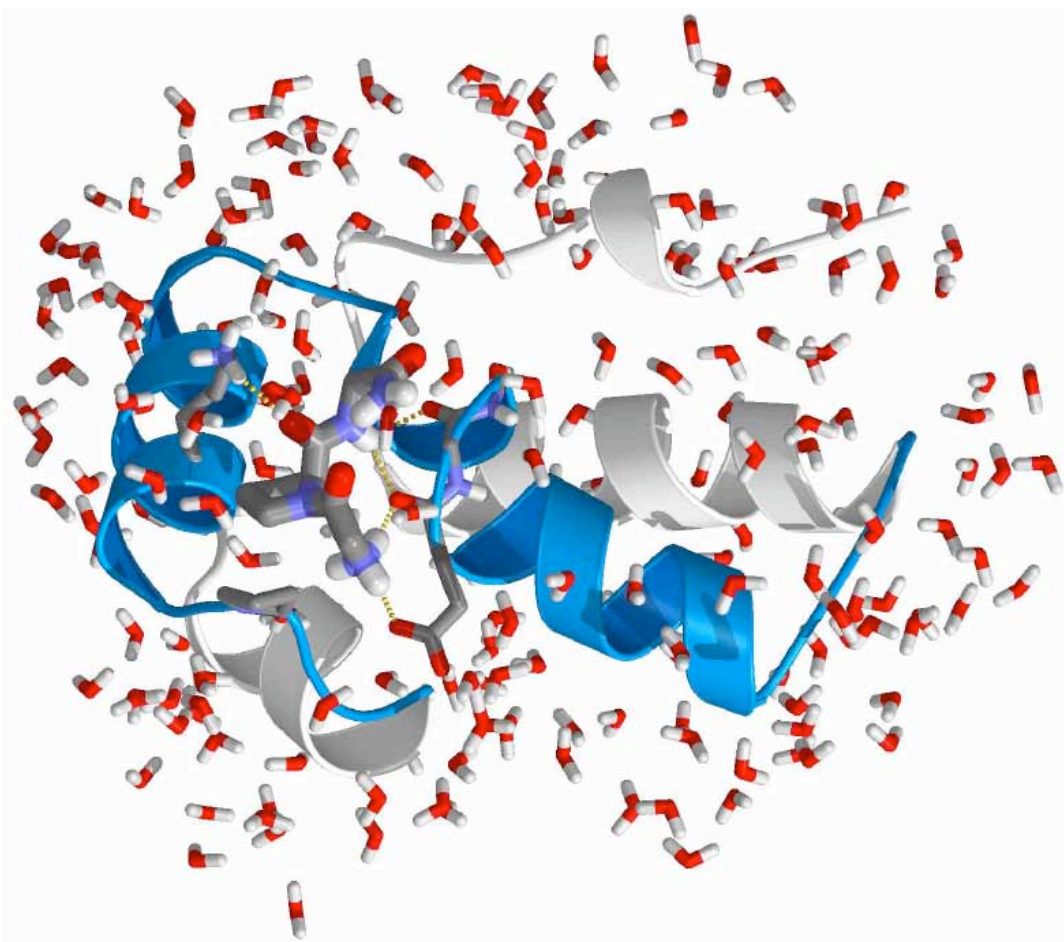


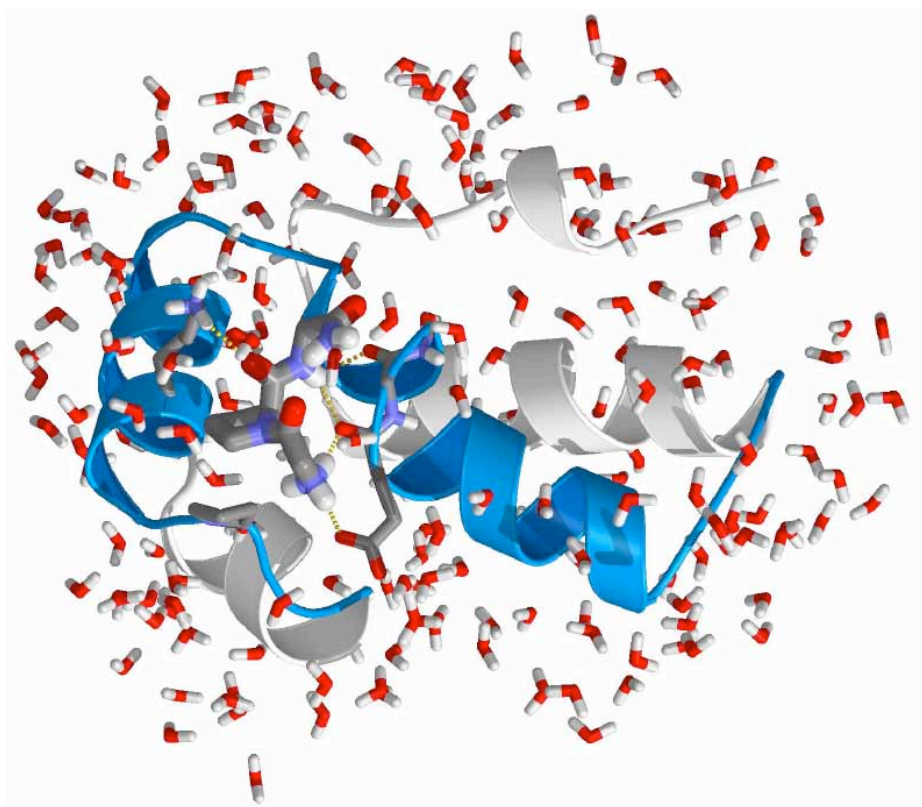
Molecular Dynamics Simulation

A Short Introduction



Michel Cuendet

Plan



- **Introduction**
- **The classical force field**
- **Setting up a simulation**
- **Connection to statistical mechanics**
- **Usage of MD simulation**

Why we do simulation

In some cases, experiment is :

1. impossible

Inside of stars

Weather forecast

2. too dangerous

Flight simulation

Explosion simulation

3. expensive

High pressure simulation

Windchannel simulation

4. blind

*Some properties cannot be
observed on very short time-scales
and very small space-scales*

Simulation is a useful complement, because it can :

⇒ replace experiment

⇒ provoke experiment

⇒ explain experiment

⇒ aid in establishing intellectual property



Molecular modeling

What is Molecular Modeling?

Molecular Modeling is concerned with the description of the atomic and molecular interactions that govern *microscopic* and *macroscopic* behaviors of physical systems

What is it good for?

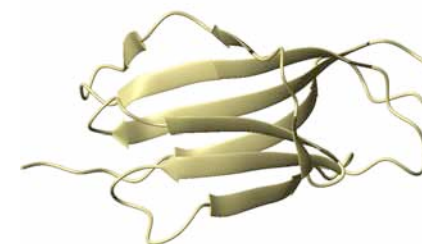
The essence of molecular modeling resides in the connection between the *macroscopic* world and the *microscopic* world provided by the theory of statistical mechanics



Macroscopic
observable
(Solvation energy,
affinity between two
proteins, H-H distance,
conformation, ...)



Average of observable
over selected microscopic
states



Computational tools

- **Quantum Mechanics (QM)**

Electronic structure (Schrödinger)

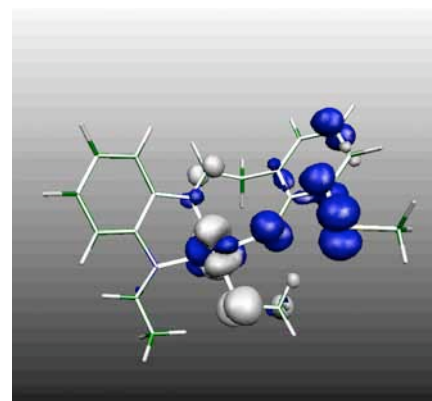
- ACCURATE
- EXPENSIVE \Rightarrow small system

- **Classical Molecular Mechanics (MM)**

Empirical forces (Newton)

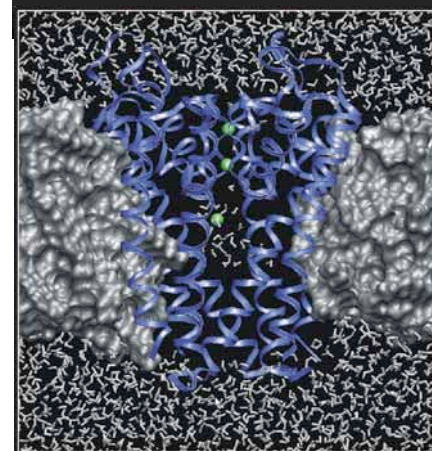
- LESS ACCURATE
- FAST

- **Mixed Quantum/Classical (QM/MM)**



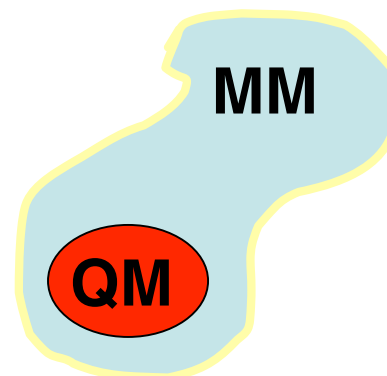
10-100 atoms

10-100 ps



10^4 - 10^5 atoms

10-100 ns



10^4 - 10^5 atoms

10-100 ps

Types of phenomena

Goal : simulate/predict *processes* such as

- | | | |
|---|---|--|
| 1. polypeptide folding | } | <i>thermodynamic equilibria
governed by weak
(non-bonded) forces</i> |
| 2. biomolecular association | | |
| 3. partitioning between solvents | | |
| 4. membrane/micelle formation | | |
| 5. chemical reactions, enzyme catalysis | } | <i>chemical transformations
governed by strong forces</i> |
| 6. enzyme catalysis | | |
| 7. photochemical reactions, electron transfer | | |

characteristics (1-4):

- | | | | |
|------------------------|---------------------------|---|--------------|
| - degrees of freedom: | atomic (solute + solvent) | → | classical MD |
| - equations of motion: | classical dynamics | | |
| - governing theory: | statistical mechanics | | |

characteristics (5-7):

- | | | | |
|------------------------|-------------------------------|---|------------|
| - degrees of freedom: | electronic, nuclear | → | quantum MD |
| - equations of motion: | quantum dynamics | | |
| - governing theory: | quantum statistical mechanics | | |

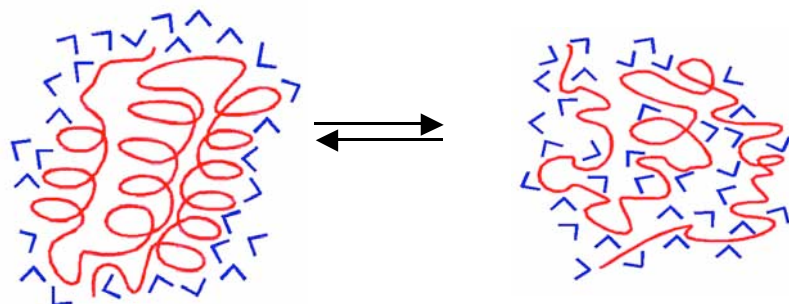
Processes: Thermodynamic Equilibria



Folding

folded/native

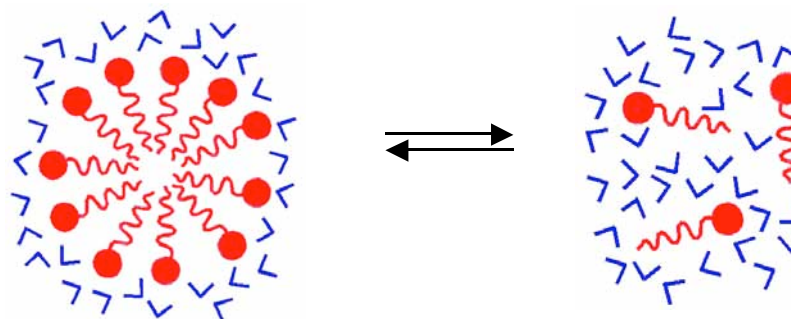
denatured



Micelle Formation

micelle

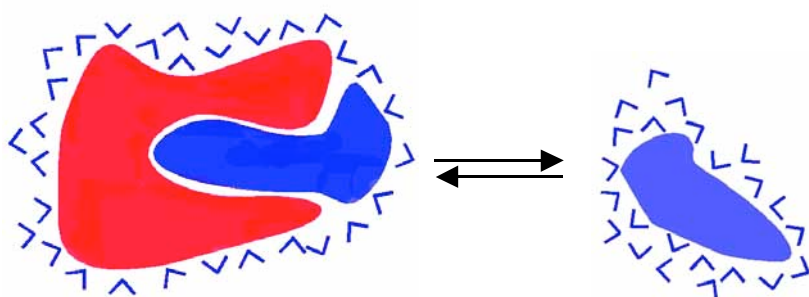
mixture



Complexation

bound

unbound

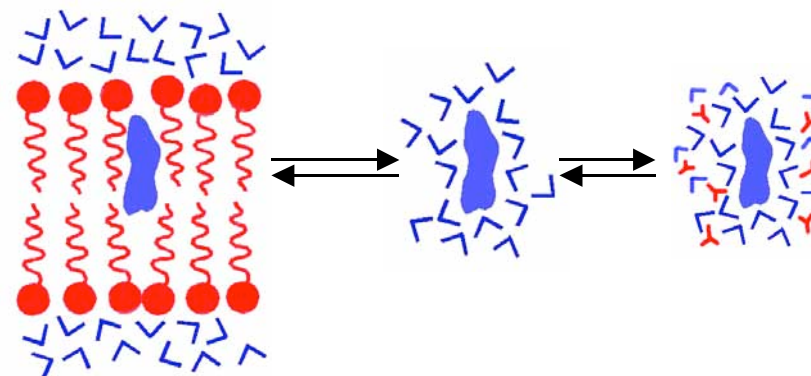


Partitioning

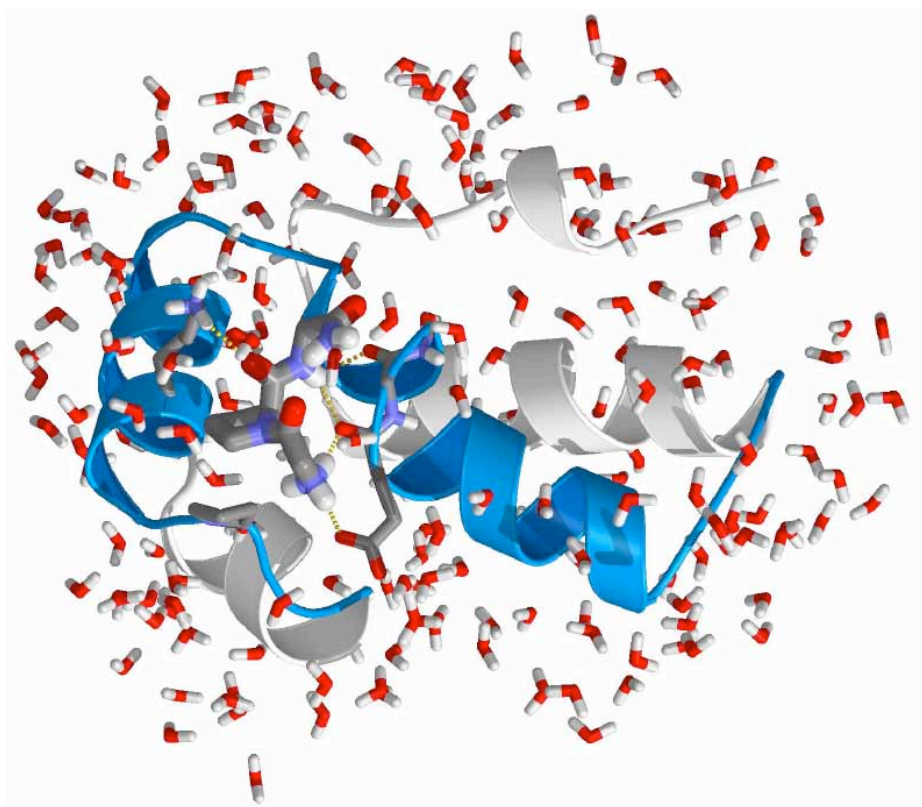
in membrane

in water

in mixtures



Plan

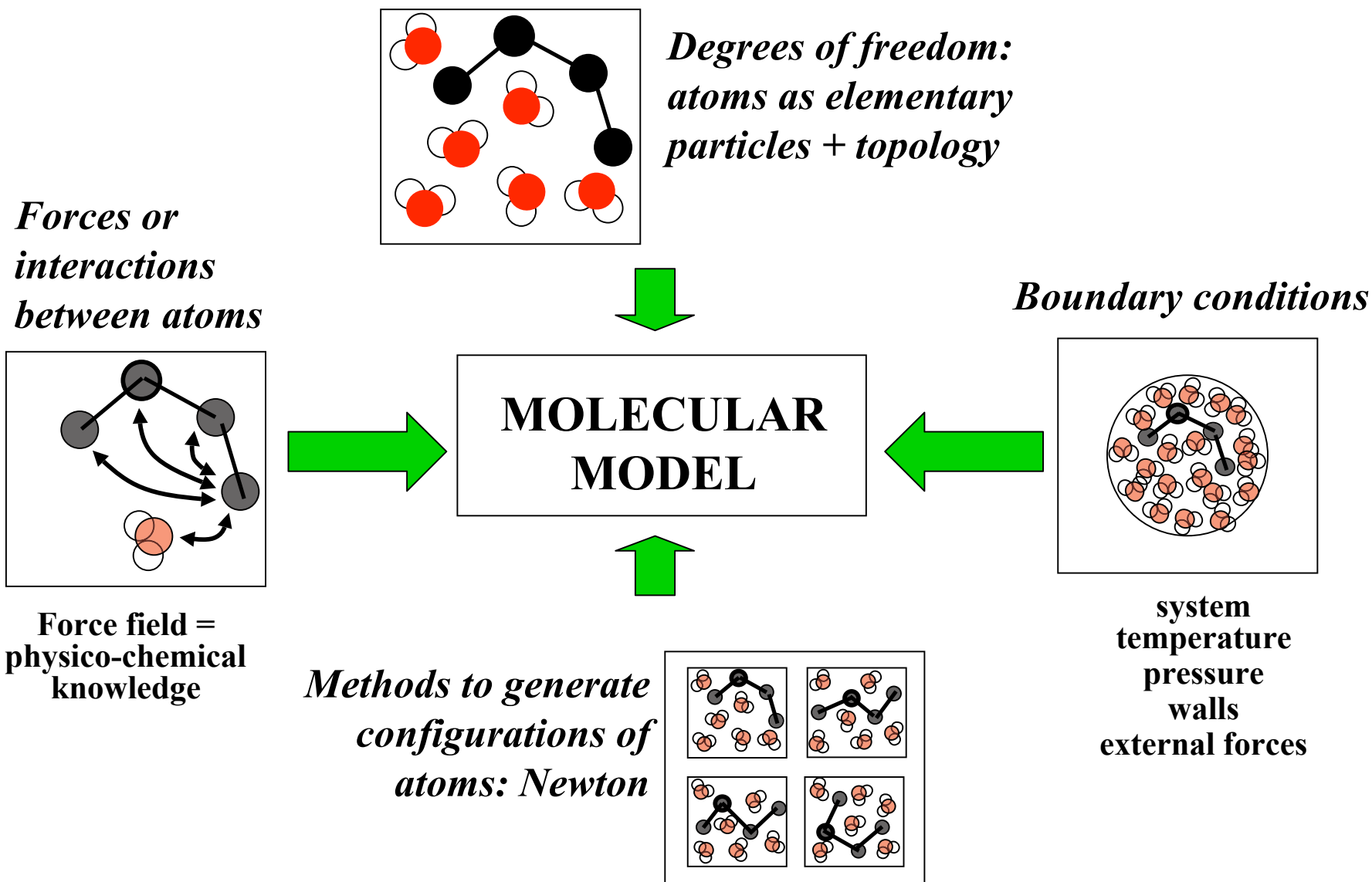


- Introduction
- **The classical force field**
- Setting up a simulation
- Connection to statistical mechanics
- Usage of MD simulation

Definition of a model for molecular simulation



Every molecule consists of atoms that are very strongly bound to each other





Classical force fields

Goals of classical (semi-empirical) force fields

- Definition of empirical potential energy functions $V(\mathbf{r})$ to model the molecular interactions
- These functions need to be differentiable in order to compute the forces acting on each atom: $\mathbf{F} = -\nabla V(\mathbf{r})$

Implementation of classical potential energy functions

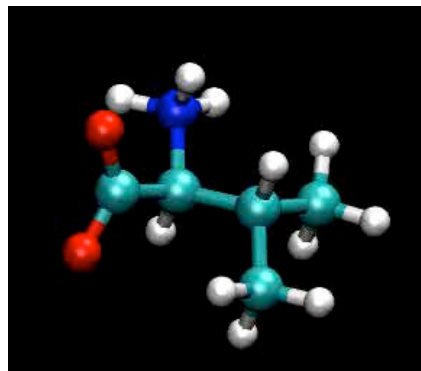
1. Theoretical functional forms are derived for the potential energy $V(\mathbf{r})$.
2. Definition of atom types that differ by their atomic number and chemical environment, e.g. the carbons in C=O or C-C are of different types.
3. Parameters are determined so as to reproduce the interactions between the various atom types by fitting procedures
 - experimental enthalpies (CHARMM)
 - experimental free energies (GROMOS, AMBER)

Parametrization available for [proteins](#), [lipids](#), [sugars](#), [ADN](#), ...

Covalent bonds and angles

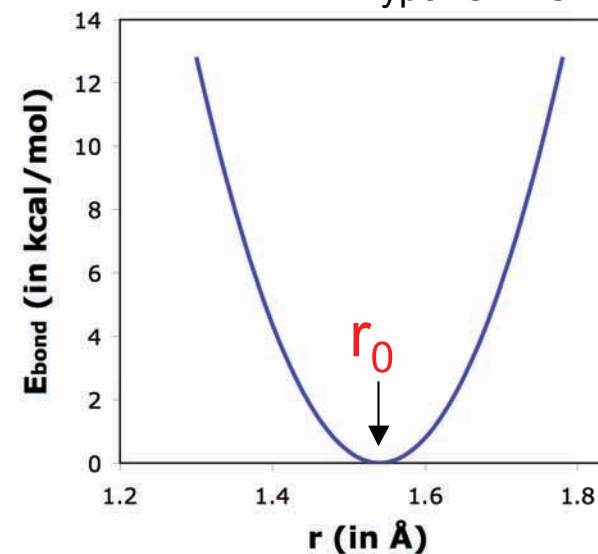


Bonds

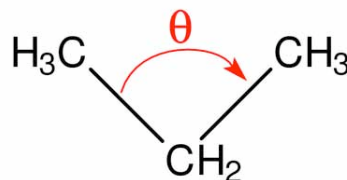
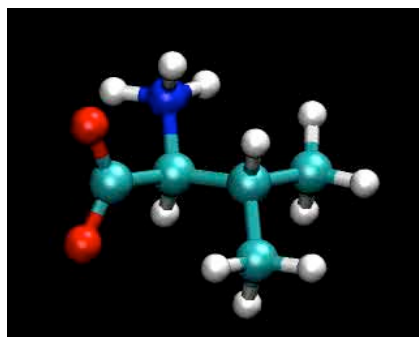


$$E_{\text{bond}} = K_b (r - r_0)^2$$

Type: CT1-CT1

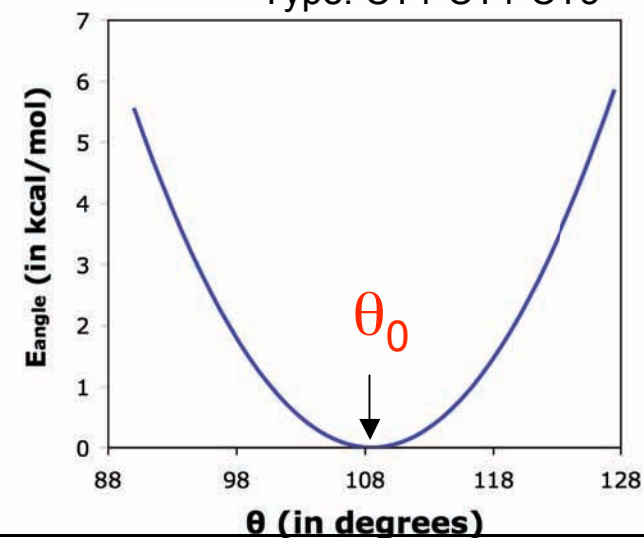


Angles



$$E_{\text{angle}} = K_{\theta} (\theta - \theta_0)^2$$

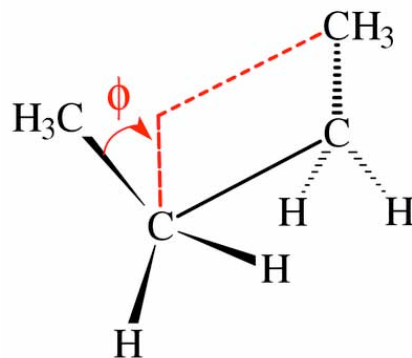
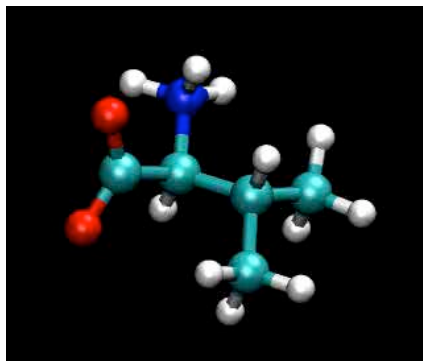
Type: CT1-CT1-CT3



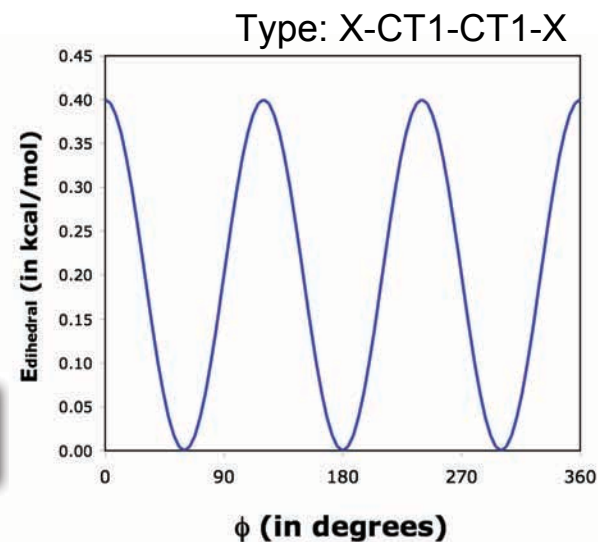
Dihedrals and Improper torsions



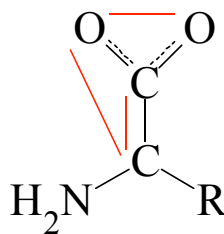
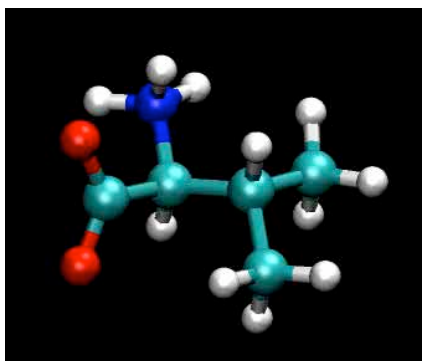
Dihedral angles



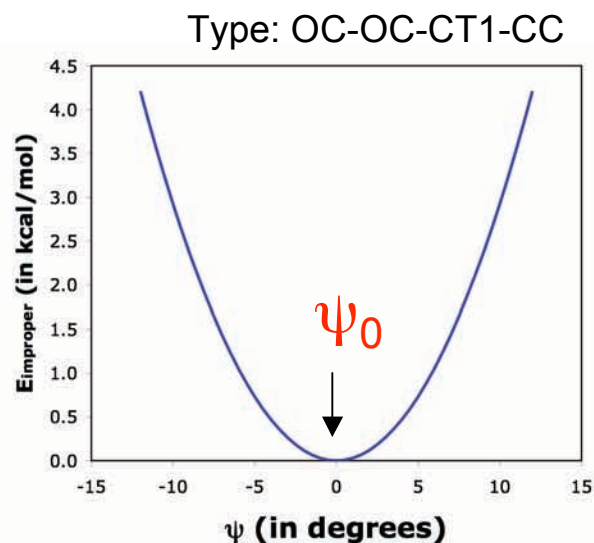
$$E_{\text{dihedral}} = K_{\phi} [1 + \cos(n\phi - \delta)]$$



Improper angles



$$E_{\text{improper}} = K_{\psi} (\psi - \psi_0)^2$$



Van der Waals interactions

Lennard -Jones potential :

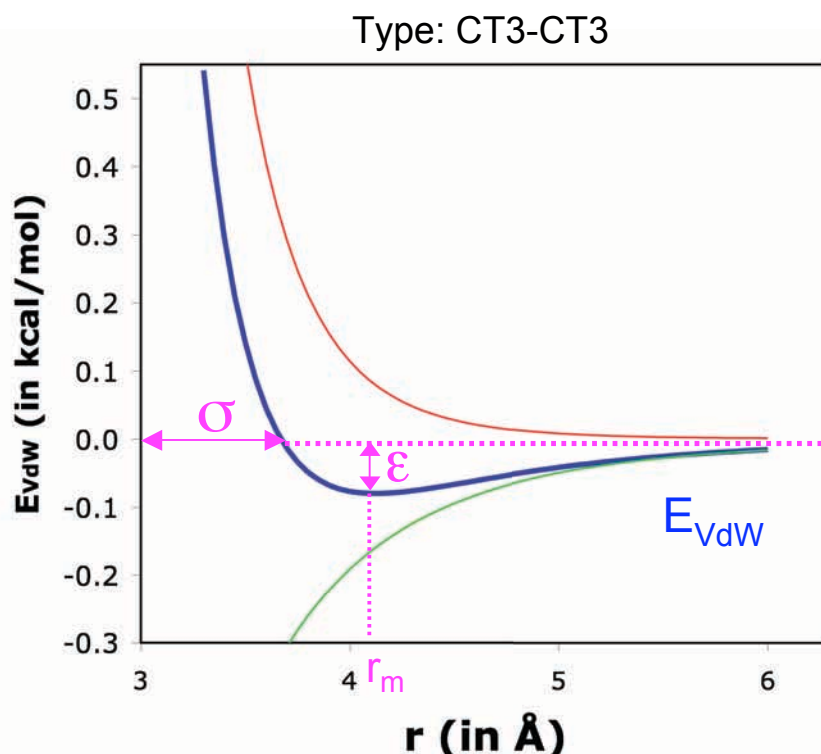
$$E_{\text{vdW}} = 4\epsilon \left[\left(\frac{\sigma}{r} \right)^{12} - \left(\frac{\sigma}{r} \right)^6 \right] = \epsilon \left[\left(\frac{r_m}{r} \right)^{12} - 2 \left(\frac{r_m}{r} \right)^6 \right]$$

σ : collision parameter

ϵ : well depth

r_m : distance at min $r_m = 2^{1/6} \sigma$

Combination rule for two different atoms i, j : $r_m = r_{m,i} + r_{m,j}$ $\epsilon = \sqrt{\epsilon_i \epsilon_j}$



Repulsive :
Pauli exclusion principle

$$\propto \frac{1}{r^{12}}$$

Attractive:
induced dipole / induced dipole

$$\propto -\frac{1}{r^6}$$

Electrostatic interactions

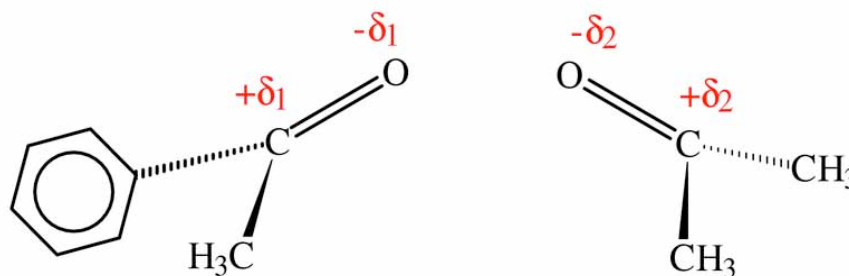


Coulomb law

$$E_{\text{elec}} = \frac{q_i q_j}{4\pi\epsilon_0\epsilon r_{ij}}$$

where ϵ is the dielectric constant :

1	for vacuum,
4-20	for protein core,
80	for water



The Coulomb energy decreases only as $1/r$

Despite dielectric shielding effects, it is a **long range interaction**

Special techniques to deal with this :

- PME : for systems with periodic boundary conditions
- Reaction Field : suppose homogeneous dielectric outside cutoff

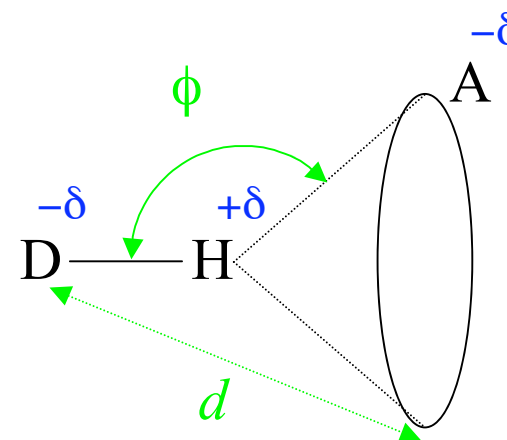
Derived Interactions



Some interactions are often referred to as particular interactions, but they result from the two interactions previously described, i.e. the electrostatic and the van der Waals interactions.

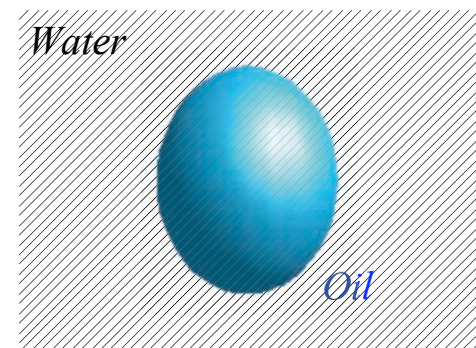
1) Hydrogen bonds (Hb)

- Interaction of the type $D-H \cdots A$
- The origin of this interaction is a dipole-dipole attraction
- Typical ranges for distance and angle:
 $2.4 < d < 4.5 \text{ \AA}$ and $180^\circ < \phi < 90^\circ$



2) Hydrophobic effect

- Collective effect resulting from the energetically unfavorable surface of contact between the water and an apolar medium (loss of water-water Hb)
- The apolar medium reorganizes to minimize the water exposed surface (compaction, association...)



The total potential energy function

$$E = \sum_{\text{bonds}} K_b (r - r_0)^2 + \sum_{\text{angles}} K_\theta (\theta - \theta_0)^2 + \sum_{\text{dihedrals}} K_\phi [1 + \cos(n\phi - \delta)] + \sum_{\text{impropers}} K_\psi (\psi - \psi_0)^2$$

$$+ \sum_{i>j} \epsilon \left[\left(\frac{r_m}{r} \right)^{12} - 2 \left(\frac{r_m}{r} \right)^6 \right] + \sum_{i>j} \frac{q_i q_j}{4\pi\epsilon_0 \epsilon r}$$

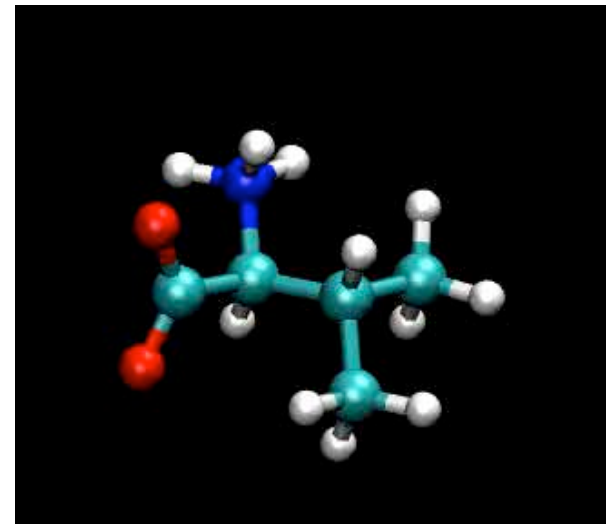
For a system with 1500 atoms



$\sim 10^6$ pairs of interacting atoms



Introduction of cutoff



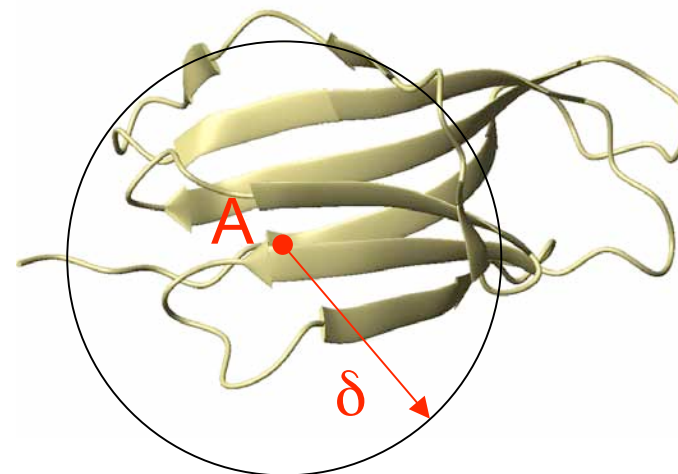
Cutoff for non-bonded interactions



For an atom A, only non-bonded interactions with atoms within δ Å are calculated

➡ Non-bonded neighbour lists

Generally, $\delta = 8$ to 14 Å

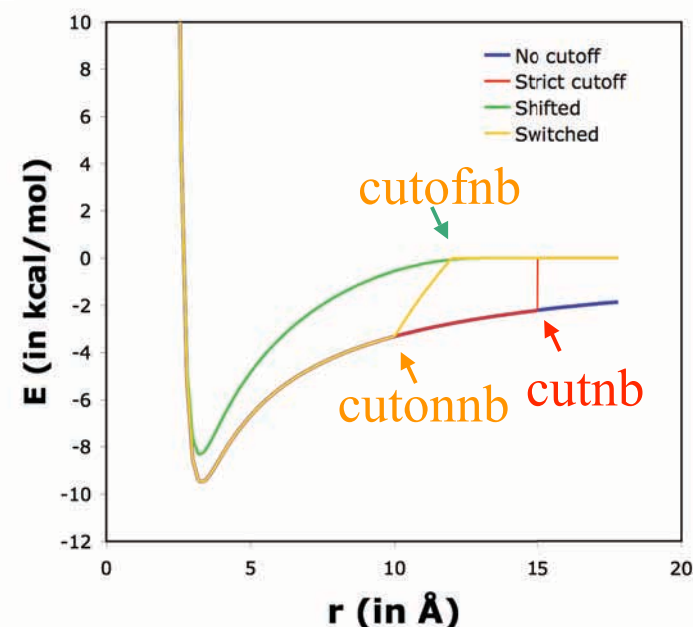


Three cutoff schemes: strict, shift, switch

Shift and switch:

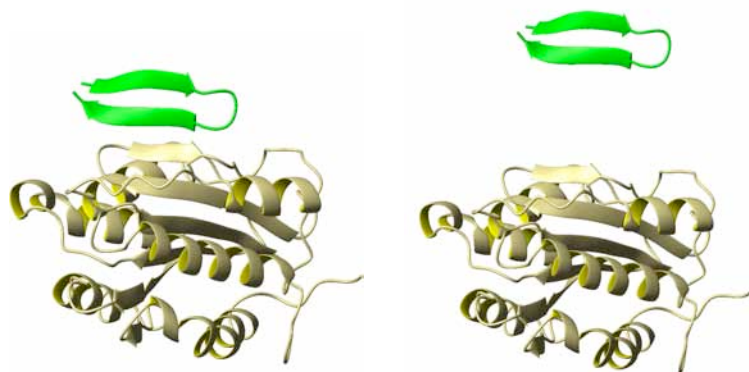
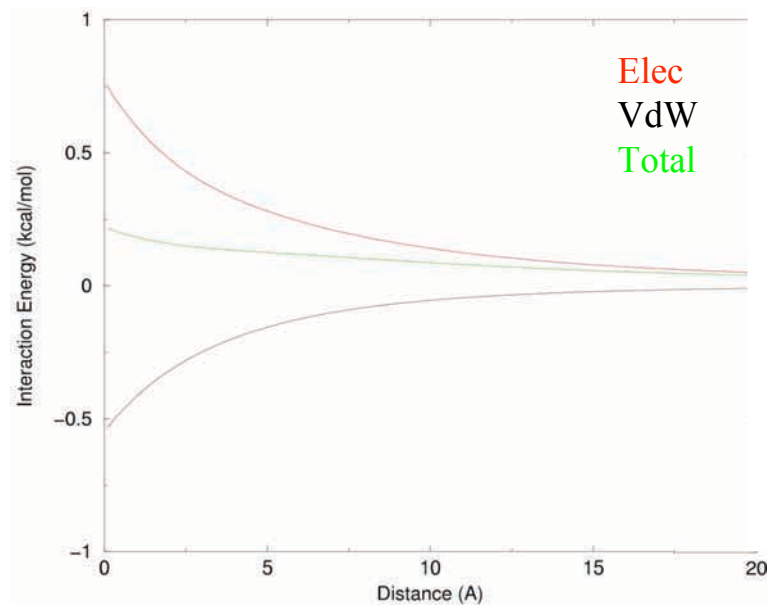
$$E'(r) = E(r) \times S(r)$$

$S(r)$ differentiable

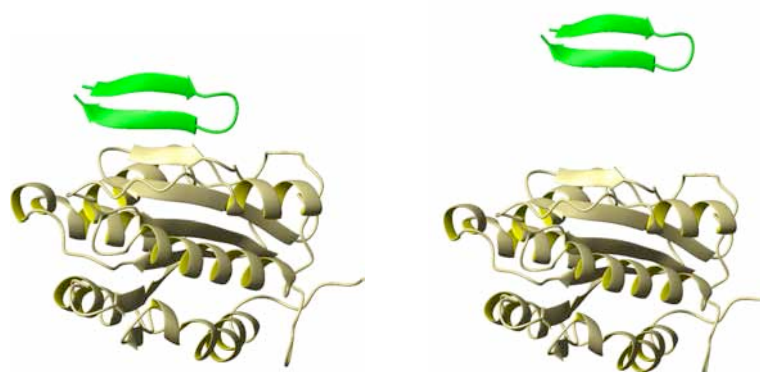
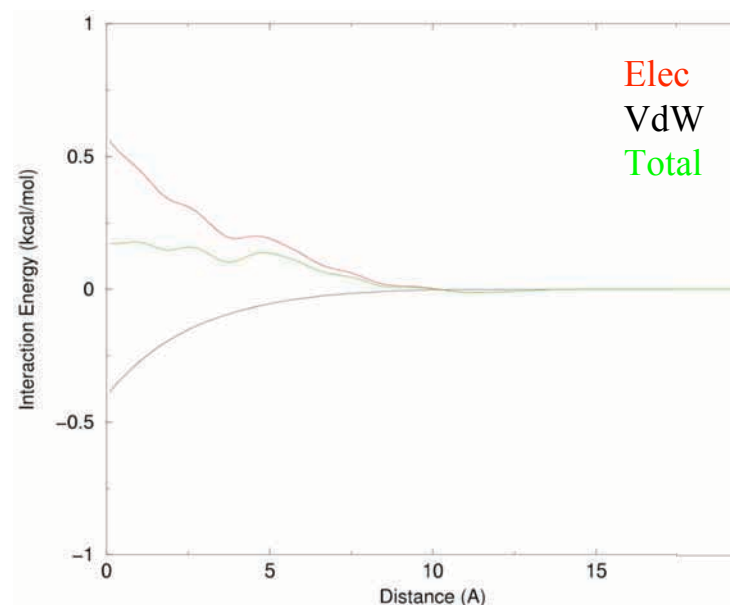


Effect of cutoff

No cutoff



8 Å cutoff



Force field parametrization



$$E = \sum_{\text{bonds}} K_b (r - r_0)^2 + \sum_{\text{angles}} K_\theta (\theta - \theta_0)^2 + \sum_{\text{dihedrals}} K_\phi [1 + \cos(n\phi - \delta)] + \sum_{\text{impropers}} K_\psi (\psi - \psi_0)^2 + \sum_{i>j} 4\epsilon \left[\left(\frac{\sigma}{r} \right)^{12} - \left(\frac{\sigma}{r} \right)^6 \right] + \sum_{i>j} \frac{q_i q_j}{4\pi\epsilon_0 \epsilon r}$$

Type of data	Type of system	Phase	Type of properties	Force field parameters
structural data (exp.)	small molecules	crystalline solid phase	molecular geometry: bond lengths, angles	r_0, θ_0, ψ_0
spectroscopic data (exp.)	small molecules	gas phase	intra-molecular vibrations: force constants	K_b, K_θ, K_ψ
quantum-chemical calculations : energy profiles (theor.)	small molecules	gas phase	torsional-angle rotational profiles	K_ϕ, δ, n
quantum-chemical calculations : electron densities (theor.)	small molecules	gas phase	atom charges	charges q_i (initial)
thermodynamic data (exp.)	molecules in solution, mixtures	condensed phase	heat of vaporisation, density, free energy of solvation	v. d. Waals : σ_i, ϵ_i charges q_i (final)
dielectric data (exp.)	small molecules	condensed phase	dielectric permittivity, relaxation	charges q_i
transport data (exp.)	small molecules	condensed phase	transport coefficients: diffusion, viscosity	v. d. Waals : σ_i, ϵ_i charges q_i

Solvation



Fundamental influence on the structure, dynamics and thermodynamics of biological molecules

Effect through:

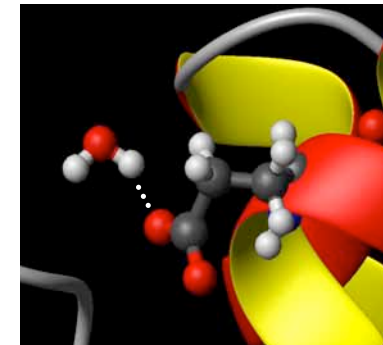
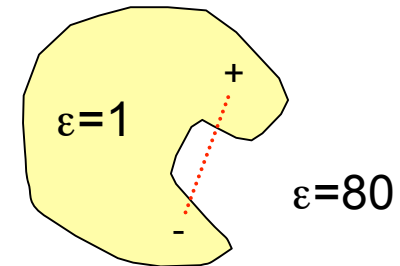
- Solvation of charge
- Screening of charge - charge interactions

$$E_{\text{elec}} = \frac{q_i q_j}{4\pi\epsilon_0\epsilon(r) r}$$

- Hydrogen bonds between water molecules and polar functions of the solute

Taken into account via:

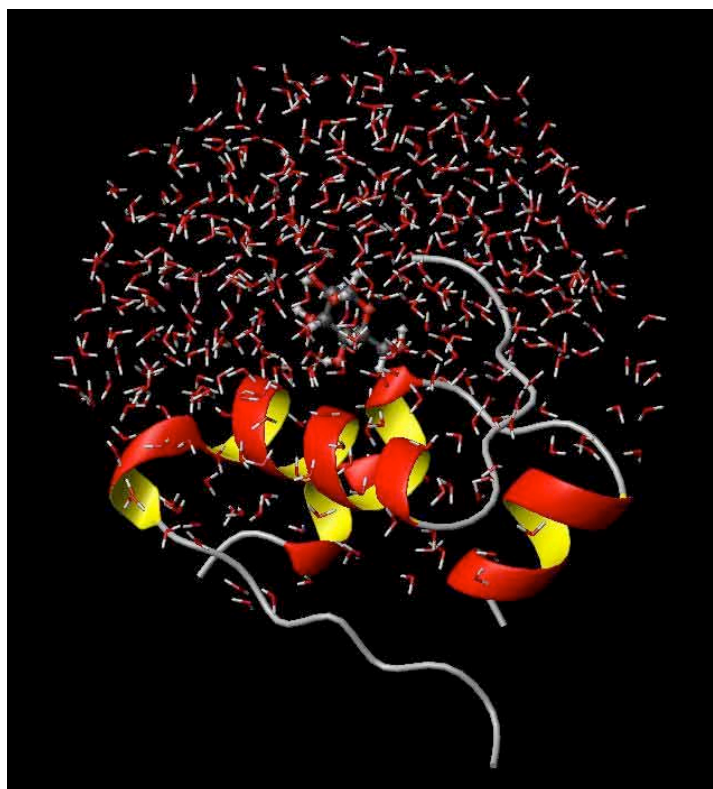
- ☐ Explicit solvation. Water molecules are included.
 - Stochastic boundary conditions
 - Periodic boundary conditions
- ☐ Implicit solvation. Water effect is modeled.
 - Screening constant
 - Implicit solvation models (Poisson Boltzmann, Generalized Born)



Explicit solvation schemes

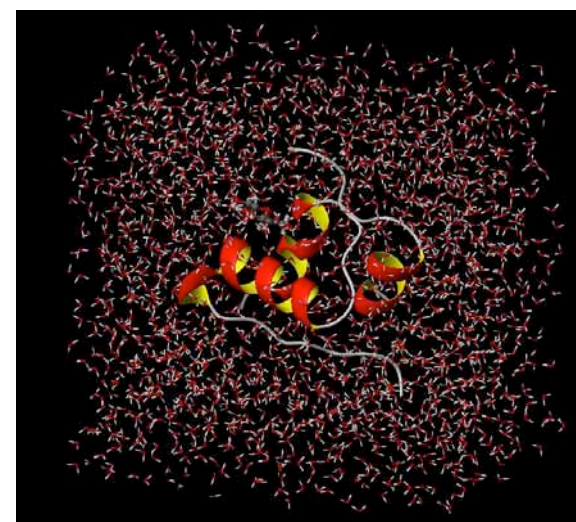
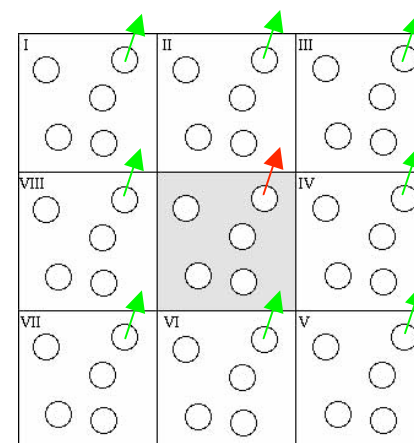
Stochastic boundary conditions

The region of interest is solvated in a water sphere at 1atm. The water molecules are submitted to an additional force field that restrain them in the sphere while maintaining a strong semblance to bulk water.



Periodic boundary conditions

The fully solvated central cell is simulated, in the environment produced by the repetition of this cell in all directions.



Implicit solvation



Screening constant

$$\epsilon = Nr$$

N=4,8. The dielectric constant is a function of atom distance.
Mimic screening effect of solvent. Simple, unphysical but efficient.

In CHARMM: `NBOND RDIE EPS 4.0`

Implicit solvent models

- Poisson Boltzmann (PB) equation.

$$\nabla \cdot \{ \epsilon(r) \nabla \phi(r) \} - \kappa' \sinh[\phi(r)] = -4\pi\rho(r)$$

$\phi(r)$: electrostatic potential,
 $\rho(r)$: charge density

Equation solved numerically. Very time consuming.
In CHARMM: PBEQ module.

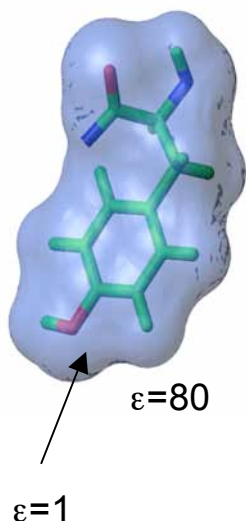
- Generalized born (GB) equation.

$$G_{elec} = \sum_{i>j} \frac{q_i q_j}{4\pi\epsilon_0 r} - \frac{1}{2} \left(1 - \frac{1}{\epsilon} \right) \sum_i \sum_j \frac{q_i q_j}{\sqrt{r^2 + a_i a_j} \exp(-r^2/4a_i a_j)}$$

a_i : Born radius

solvation energy

Others: EEF1, SASA, etc...



Explicit hydrogen bonds with water molecules are lost!

Introduction to molecular surfaces

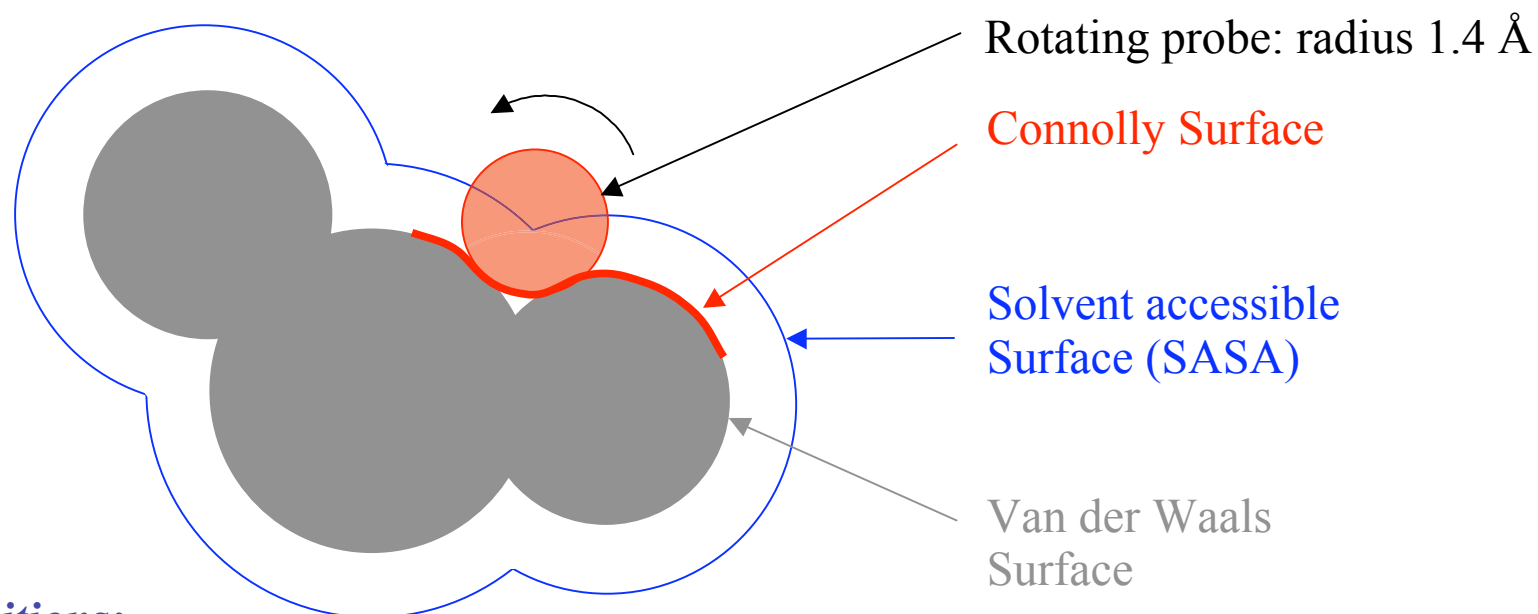
Hydrophobic effect :

Simply modelled by a non-polar solvation (free) energy term, proportional to the solvent accessible surface area (SASA) :

$$\Delta G_{np, solv} = \gamma SASA + b$$

$$\gamma = 0.00542 \text{ kcal mol}^{-1} \text{ \AA}^2$$

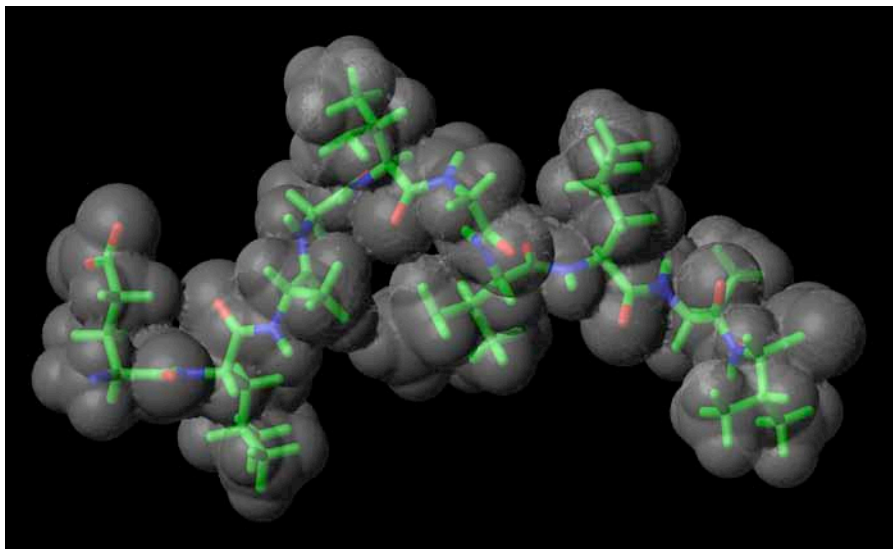
$$b = 0.92 \text{ kcal mol}^{-1}$$



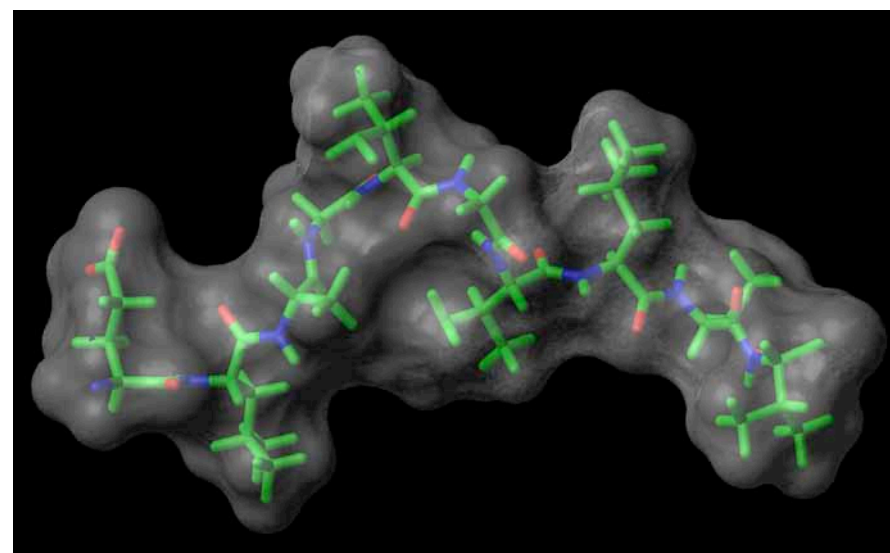
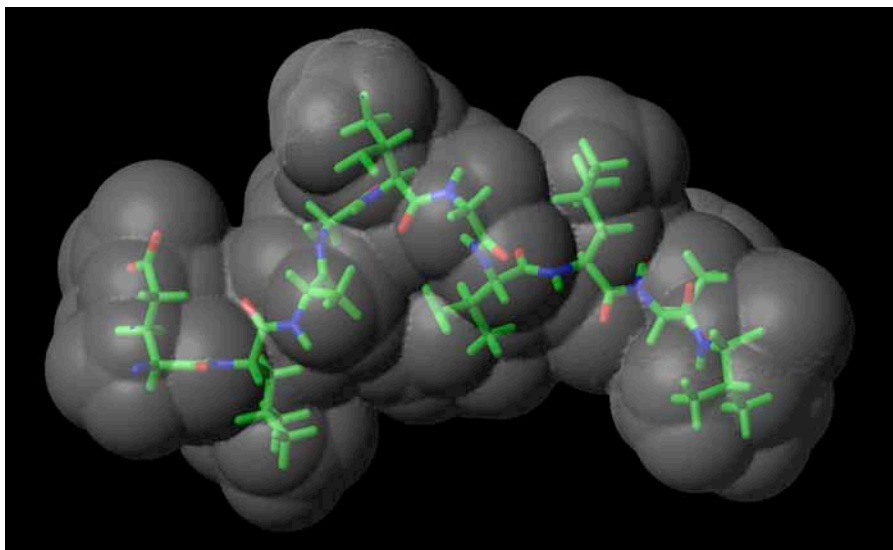
Definitions:

- Van der Waals: ensemble of van der Waals sphere centered at each atom
- Connolly: ensemble of contact points between probe and vdW spheres
- Solvent: ensemble of probe sphere centers

Examples of molecular surfaces



Van der Waals



Connolly
(Contact)

Solvent accessible

Limitations of classical MD

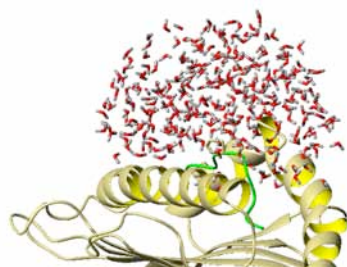


Problems

1) Fixed set of atom types

2) No electronic polarization:

- fixed partial charges allow for *conformational* polarization but not *electronic* polarization



3) Quadratic form of potentials:

- problematic far from equilibrium values
- no bond creation or deletion

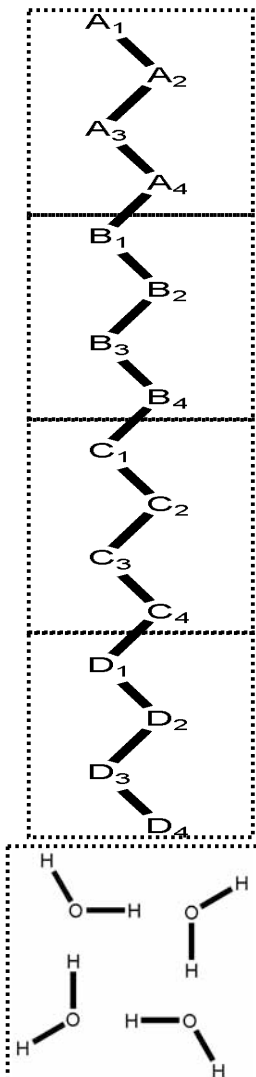


Solutions

- Fluctuating charges treated as dynamical parameters
- Charges on springs representing e⁻ clouds
- QM-MM
- Full QM simulations
- QM-MM
- Full QM simulations

Coarse grain models

All-atom model
16 (CH_2 or CH_3) atoms



Map
to all-atom
configurations

Centre of mass
 $A_1 - A_4$

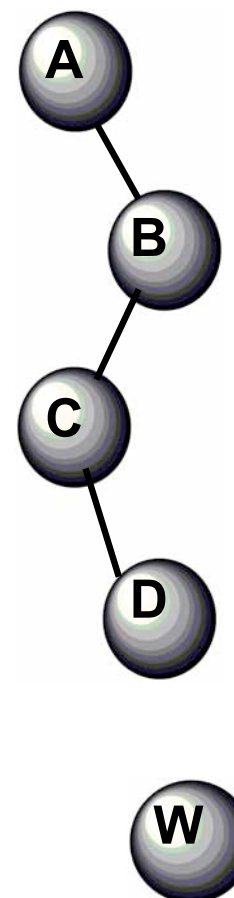
Centre of mass
 $B_1 - B_4$

Centre of mass
 $C_1 - C_4$

Centre of mass
 $D_1 - D_4$

Centre of mass
 $W_1 - W_4$

Coarse-grained model
4 atoms



Molecular dynamics software

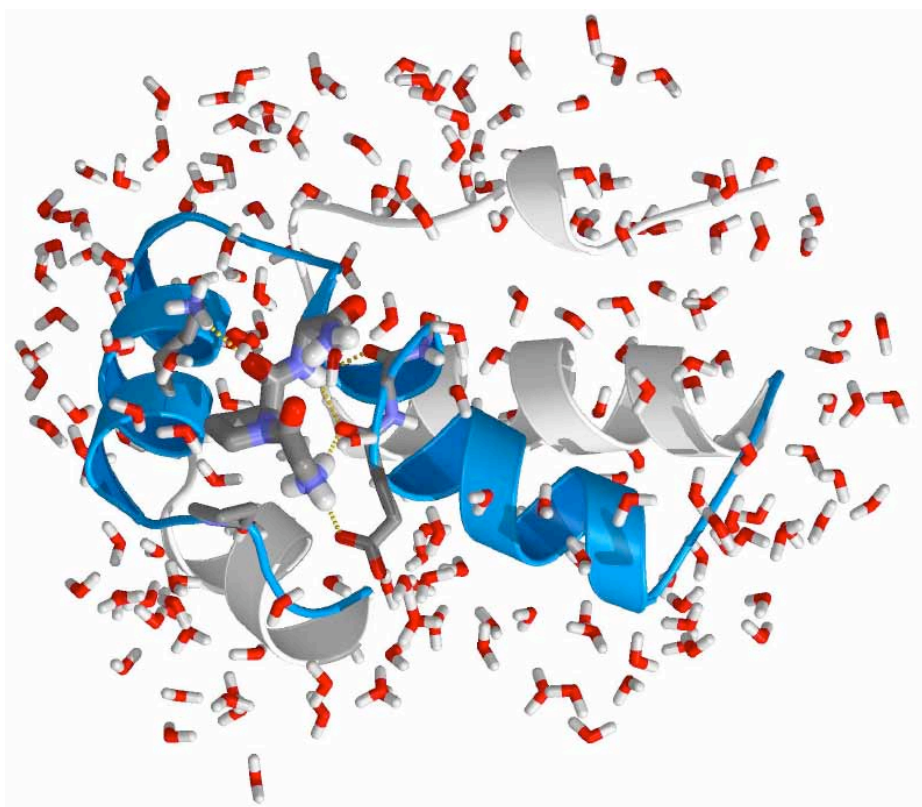


Package name	supported force fields
• CHARMM www.charmm.org	CHARMM (E / I; AA / UA), Amber
• Amber amber.scripps.edu	Amber (E / I ; AA)
• GROMOS www.igc.ethz.ch/GROMOS	Gromos (E / vacuum ; UA)
• Gromacs www.gromacs.org	Amber, Gromos, OPLS - (all E)
• NAMD www.ks.uiuc.edu/Research/namd	CHARMM, Amber, Gromos, ...

E = explicit solvent
I = implicit solvent

AA = all atom
UA = united atom (apolar H omitted)

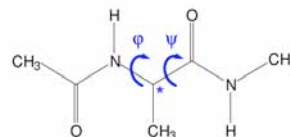
Plan



- Introduction
- The classical force field
- **Setting up a simulation**
- Connection to statistical mechanics
- Usage of MD simulation

Minimal input for MM

1) Topological properties:



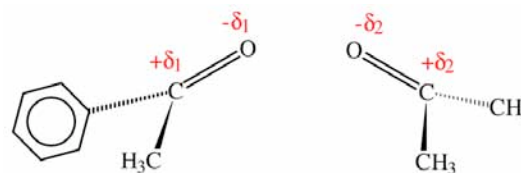
description of the covalent **connectivity** of the molecules to be modeled

2) Structural properties:



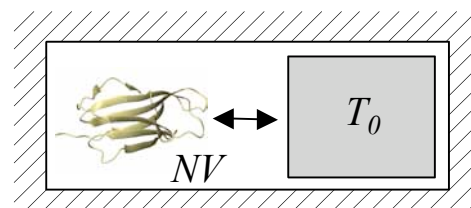
the starting **conformation** of the molecule, provided by an X-ray structure, NMR data or a theoretical model

3) Energetical properties:



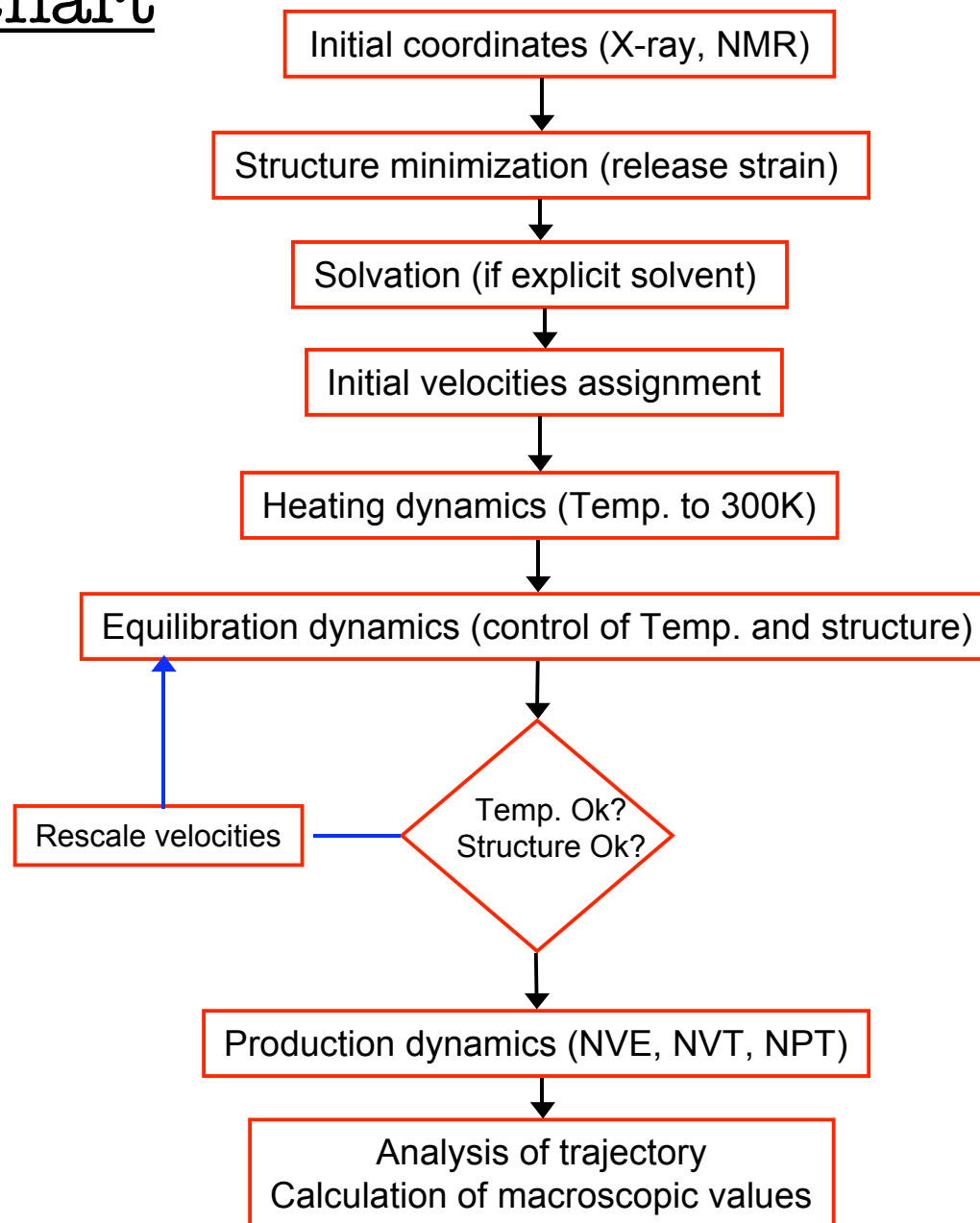
a **force field** describing the force acting on each atom of the molecules

4) Thermodynamical properties:



a sampling **algorithm** that generates the thermodynamical ensemble that matches experimental conditions for the system, e.g. N, V, T , N, P, T , ...

MD flowchart



Coordinate files

Cartesian coordinates

(x,y,z)

ATOM	1	N	VAL	1	-0.008	-0.022	-0.030	1.00	0.00	PEP
ATOM	2	HT1	VAL	1	-0.326	0.545	0.778	1.00	0.00	PEP
ATOM	3	HT2	VAL	1	-0.450	-0.956	-0.084	1.00	0.00	PEP
ATOM	4	HT3	VAL	1	-0.172	0.566	-0.876	1.00	0.00	PEP
ATOM	5	CA	VAL	1	1.477	-0.077	0.073	1.00	0.00	PEP
ATOM	6	HA	VAL	1	1.777	-0.598	0.971	1.00	0.00	PEP
ATOM	7	CB	VAL	1	2.038	-0.740	-1.193	1.00	0.00	PEP

Internal coordinates (IC)

Given 4 consecutive atoms A-B-C-D, the IC are:



R_{AB} , θ_{ABC} , ϕ_{ABCD} , θ_{BCD} , R_{CD}

1	1	N	1	C	1	*CA	1	CB	1.4896	105.11	117.88	111.68	1.5353
2	1	N	1	C	1	*CA	1	HA	1.4896	105.11	-118.25	108.30	1.0807
3	1	N	1	CA	1	CB	1	CG1	1.4896	108.86	176.05	110.92	1.5421
4	1	CG1	1	CA	1	*CB	1	CG2	1.5421	110.92	121.67	110.44	1.5454
5	1	CG1	1	CA	1	*CB	1	HB	1.5421	110.92	-118.15	109.36	1.1177
6	1	CA	1	CB	1	CG1	1	HG11	1.5353	110.92	56.96	111.11	1.1099
7	1	HG11	1	CB	1	*CG1	1	HG12	1.1099	111.11	-119.80	110.60	1.1134
8	1	HG11	1	CB	1	*CG1	1	HG13	1.1099	111.11	120.81	110.60	1.1103

It is possible to calculate missing cartesian coordinates
from the existing ones and the IC

Definition of atom types

The residue topology file (RTF) contains the **atom types** and the **standard topology** of residues.

Example: the CHARMM force field, version 22
file : [top_all22_prot.inp](#)

Atom types section :

```

MASS      1  H      1.00800 H ! polar H
MASS      2  HC      1.00800 H ! N-ter H
MASS      3  HA      1.00800 H ! nonpolar H
MASS      4  HT      1.00800 H ! TIPS3P WATER HYDROGEN
MASS      5  HP      1.00800 H ! aromatic H
MASS      6  HB      1.00800 H ! backbone H
[ ... ]
MASS     20  C      12.01100 C ! carbonyl C, peptide backbone
MASS     21  CA      12.01100 C ! aromatic C
MASS     22  CT1     12.01100 C ! aliphatic sp3 C for CH
MASS     23  CT2     12.01100 C ! aliphatic sp3 C for CH2
MASS     24  CT3     12.01100 C ! aliphatic sp3 C for CH3
MASS     25  CPH1    12.01100 C ! his CG and CD2 carbons
  
```

90 atom types

No. atom type mass atom
 ↗ ↗ ↗ ↗

Decomposition into residues

In CHARMM, **molecules are decomposed into residues**.

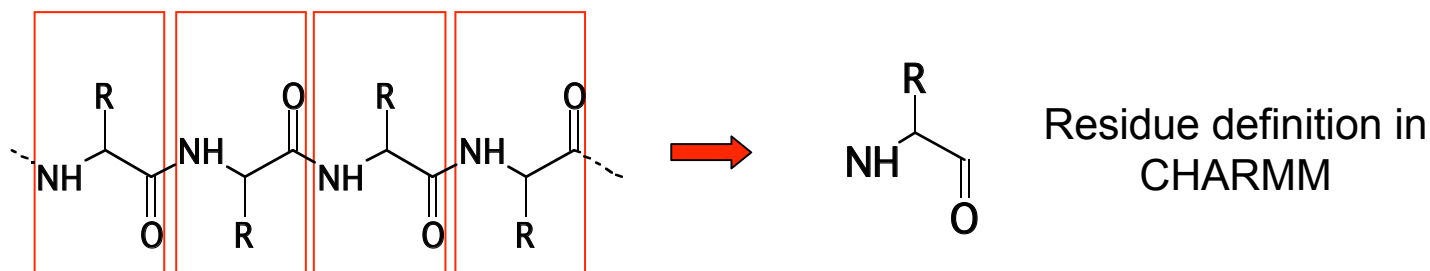
A molecule may be composed of one to several hundreds or thousands of residues.

Residues correspond to **amino acids** for proteins or to **nucleotides** for DNA.

Topologies for individual residues are **pre-defined** in CHARMM

➡ **Easy construction of the protein topology from the sequence.**

Only informations about 20 amino acids needed to construct the topology of all proteins.



Residue topology definition

file : [top_all22_prot.inp](#)



```

RESI ALA      0.00
GROUP
ATOM N        NH1  -0.47  !      |
ATOM HN       H    0.31  !      HN-N
ATOM CA       CT1  -0.07  !      |      HB1
ATOM HA       HB   0.09  !      |      /
GROUP        !      HA-CA--CB-HB2
ATOM CB       CT3  -0.27  !      |      \
ATOM HB1      HA   0.09  !      |      HB3
ATOM HB2      HA   0.09  !      O=C
ATOM HB3      HA   0.09  !      |
GROUP        !
ATOM C        C    0.51
ATOM O        O   -0.51
BOND CB CA N HN N CA
BOND C CA C +N CA HA CB HB1 CB HB2 CB HB3
DOUBLE O C
IMPR N -C CA HN C CA +N O
DONOR HN N
ACCEPTOR O C
IC -C CA *N HN 1.3551 126.4900 180.0000 115.4200 0.9996
IC -C N CA C 1.3551 126.4900 180.0000 114.4400 1.5390
IC N CA C +N 1.4592 114.4400 180.0000 116.8400 1.3558
IC +N CA *C O 1.3558 116.8400 180.0000 122.5200 1.2297
IC CA C +N +CA 1.5390 116.8400 180.0000 126.7700 1.4613
IC N C *CA CB 1.4592 114.4400 123.2300 111.0900 1.5461
IC N C *CA HA 1.4592 114.4400 -120.4500 106.3900 1.0840
IC C CA CB HB1 1.5390 111.0900 177.2500 109.6000 1.1109
IC HB1 CA *CB HB2 1.1109 109.6000 119.1300 111.0500 1.1119
IC HB1 CA *CB HB3 1.1109 109.6000 -119.5800 111.6100 1.1114
    
```

→ Total charge

→ Atom name

→ Atom type

→ Atom charge

→ Bond

→ Improper
angle

→ Previous residue

→ Next residue

IC

Angles and dihedrals can be generated automatically from this.

Patching residues

Treat protein special features.

To make N- and C-termini:

```
PRES NTER      1.00 ! standard N-terminus
GROUP          ! use in generate statement
ATOM N   NH3   -0.30 !
ATOM HT1  HC    0.33 !      HT1
ATOM HT2  HC    0.33 !      (+)/
ATOM HT3  HC    0.33 !  --CA--N--HT2
ATOM CA   CT1   0.21 !      |  \
ATOM HA   HB    0.10 !      HA   HT3
DELETE ATOM HN
BOND HT1 N HT2 N HT3 N
DONOR HT1 N
DONOR HT2 N
DONOR HT3 N
IC HT1  N   CA   C   0.0000  0.0000  180.0000  0.0000  0.0000
IC HT2  CA  *N   HT1 0.0000  0.0000  120.0000  0.0000  0.0000
IC HT3  CA  *N   HT2 0.0000  0.0000  120.0000  0.0000  0.0000
```

To make disulfide bridges:

```
PRES DISU      -0.36 ! patch for disulfides. Patch must be 1-CYS and 2-CYS.
                  ! use in a patch statement
                  ! follow with AUTOgenerate ANGLeS DIHEdralS command
GROUP
ATOM 1CB  CT2   -0.10 !
ATOM 1SG  SM    -0.08 !      2SG--2CB--
GROUP          !      /
ATOM 2SG  SM    -0.08 !  -1CB--1SG
ATOM 2CB  CT2   -0.10 !
DELETE ATOM 1HG1
DELETE ATOM 2HG1
BOND 1SG 2SG
IC 1CA 1CB 1SG 2SG 0.0000 0.0000 180.0000 0.0000 0.0000
IC 1CB 1SG 2SG 2CB 0.0000 0.0000 90.0000 0.0000 0.0000
IC 1SG 2SG 2CB 2CA 0.0000 0.0000 180.0000 0.0000 0.0000
```

Etc...

The parameter file

Contains **force field** parameters. file : `par_all22_prot.inp`

Bonds:

```

BONDS
!
!V(bond) = Kb(b - b0)**2
!
!Kb: kcal/mole/A**2
!b0: A
!
!atom type Kb      b0
!
!Carbon Dioxide
CST  OST 937.96      1.1600 ! JES
!Heme to Sulfate (PSUL) link
SS  FE   250.0      2.2200 !force constant a guess
!equilibrium bond length optimized to reproduce
!CSD survey values of
!2.341pm0.01 (mean, standard error)
!adm jr., 7/01
C    C    600.000    1.3350 ! ALLOW ARO HEM
! Heme vinyl substituent (KK, from propene (JCS))
CA   CA   305.000    1.3750 ! ALLOW  ARO
! benzene, JES 8/25/89
CE1  CE1   440.000    1.3400  !
! for butene; from propene, yin/adm jr., 12/95
CE1  CE2   500.000    1.3420  !
! for propene, yin/adm jr., 12/95
CE1  CT2   365.000    1.5020  !
! for butene; from propene, yin/adm jr., 12/95
CE1  CT3   383.000    1.5040  !
! for butene, yin/adm jr., 12/95
CE2  CE2   510.000    1.3300  !
  
```

Diagram illustrating the bond energy formula and parameters:

$$V(\text{bond}) = K_b(b - b_0)^2$$

Where:

- K_b is the force constant (kcal/mole/A**2).
- b_0 is the equilibrium bond length (A).

Red arrows point from the text labels K_b and r_0 to the corresponding parameters in the input file. The value 937.96 is circled in red, and the value 2.2200 is also circled in red.

Idem for angles, dihedrals, impropers, ...



Setting up a system in CHARMM

```
$ charmm < input_file.inp > output_file.out
```

```
*  
  
!----- Standard Topology and Parameters  
OPEN UNIT 1 CARD READ NAME top_all22_prot.inp  
READ RTF CARD UNIT 1  
CLOSE UNIT 1  
  
OPEN UNIT 1 CARD READ NAME par_all22_prot.inp  
READ PARA CARD UNIT 1  
CLOSE UNIT 1  
  
! Generate actual topology  
OPEN UNIT 1 READ CARD NAME laho-xray.pdb  
READ SEQUENCE PDB UNIT 1  
GENE 1S SETUP FIRST NTER LAST CTER  
REWIND UNIT 1  
READ COOR PDB UNIT 1  
CLOSE UNIT 1  
  
! Make disulfide bridges  
PATCH DISU 1S 12 1S 63  
PATCH DISU 1S 16 1S 36  
PATCH DISU 1S 22 1S 46  
PATCH DISU 1S 26 1S 48  
AUTOgenerate ANGLeS DIHEdrals
```

```
! Fill IC table and build missing coordinates  
IC FILL  
IC PARA ALL  
IC BUILD  
  
! Build better coordinates for hydrogens  
HBUILD SELE TYPE H* END  
  
! Write coordinates in CHARMM format  
OPEN UNIT 1 WRITE CARD NAME laho.crd  
WRITE COOR CARD UNIT 1  
CLOSE UNIT 1  
  
! Write coordinates in PDB format  
OPEN UNIT 1 WRITE CARD NAME laho.pdb  
WRITE COOR PDB UNIT 1  
CLOSE UNIT 1  
  
! Write Protein Structure File for subsequent use  
OPEN UNIT 1 WRITE CARD NAME laho.psf  
WRITE PSF CARD UNIT 1  
CLOSE UNIT 1
```

```
PSFSUM> Summary of the structure file counters :  
Number of segments      =      1   Number of residues    =      64  
Number of atoms         =     962   Number of groups     =     298  
Number of bonds         =     980   Number of angles     =    1753  
Number of dihedrals     =    2591   Number of impropers  =     169  
Number of cross-terms   =      0  
Number of HB acceptors  =     98    Number of HB donors  =     118  
Number of NB exclusions =      0    Total charge =     1.00000
```



The protein structure file (PSF)

The PSF is **generated by CHARMM** from the sequence of the proteins, the ligands, the water molecules, etc..., using the information present in the residue topology file (RTF)

It contains **all the information needed for future simulations** :

- Residues and segments. How the system is divided into residues and segments.
- Atom information. Names, types, charges, masses.
- Bond, angle, dihedral and improper dihedral lists
- Electrostatic groupings. How some numbers of atoms are grouped for the purpose of calculating long range electrostatic

A **segment** is a group of molecules, for example:

- one single protein
- a collection of water molecules
- a collection of ions
- a ligand

Performing a calculation in CHARMM



Second step : perform calculation, e.g. energy evaluation

input

```
*
!----- Standard Topology and Parameters
OPEN UNIT 1 CARD READ NAME top_all22_prot.inp
READ RTF CARD UNIT 1
CLOSE UNIT 1

OPEN UNIT 1 CARD READ NAME par_all22_prot.inp
READ PARA CARD UNIT 1
CLOSE UNIT 1

!----- Actual topology
OPEN UNIT 1 READ CARD NAME laho.psf
READ PSF CARD UNIT 1
CLOSE UNIT 1

!----- Coordinates
OPEN UNIT 1 READ CARD NAME laho.pdb
READ COOR PDB UNIT 1
CLOSE UNIT 1

!----- Energy calculation
ENERGY

!----- End of input file
STOP
```

output

```
CHARMM> ENERGY

NONBOND OPTION FLAGS:
  ELEC   VDW   ATOMs   CDIElec  SHIFt   VATOm   VSWitch
  BYGrouP NOEXtnd NOEWald
CUTNB = 14.000 CTEXNB =999.000 CTONNB = 10.000 CTOFNB = 12.000
WMIN = 1.500 WRNMXD = 0.500 E14FAC = 1.000 EPS = 1.000
NBXMOD = 5
There are 0 atom pairs and 0 atom exclusions.
There are 0 group pairs and 0 group exclusions.
<MAKINB> with mode 5 found 2733 exclusions and 2534 interactions(1-4)
<MAKGRP> found 886 group exclusions.
Generating nonbond list with Exclusion mode = 5
== PRIMARY == SPACE FOR 276432 ATOM PAIRS AND 0 GROUP PAIRS

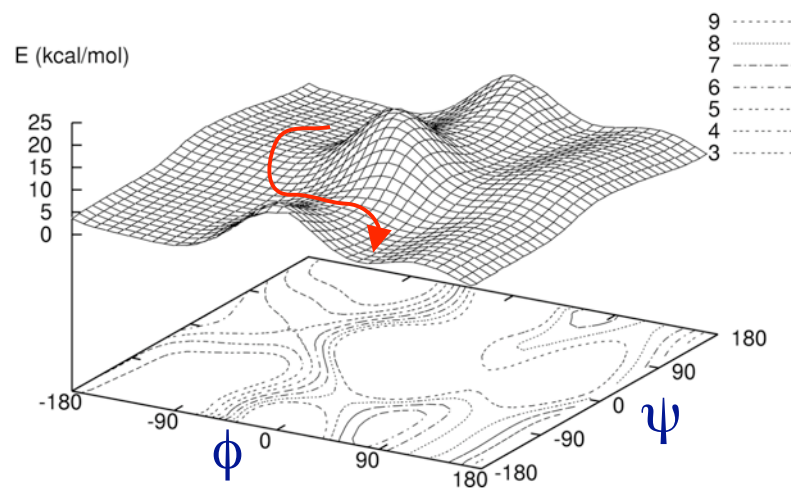
General atom nonbond list generation found:
224678 ATOM PAIRS WERE FOUND FOR ATOM LIST
9439 GROUP PAIRS REQUIRED ATOM SEARCHES

ENER ENR: Eval# ENERGY Delta-E GRMS
ENER INTERN: BONDS ANGLES UREY-b DIHEdrals IMPRopers
ENER EXTERN: VDwaals ELEC HBONds ASP USER
-----
ENER> 0 -1222.13834 0.00000 4.26768
ENER INTERN> 29.79474 88.24015 5.92868 239.13668 2.18868
ENER EXTERN> -302.00504 -1285.42224 0.00000 0.00000 0.00000
-----
```

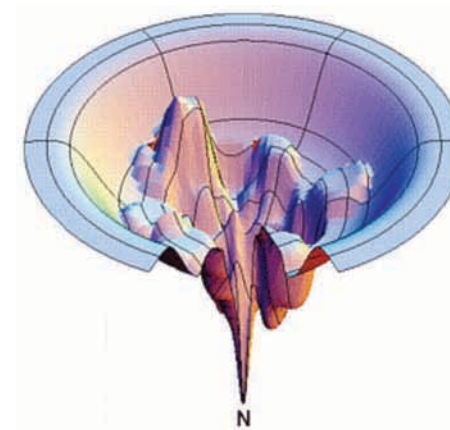
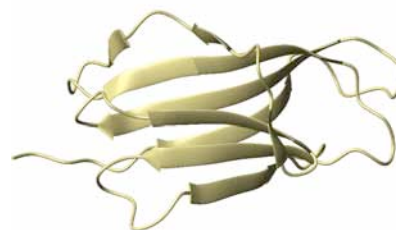
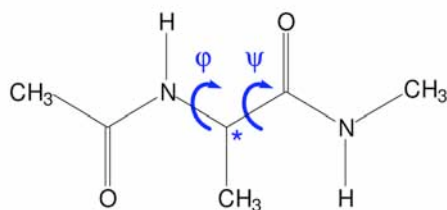
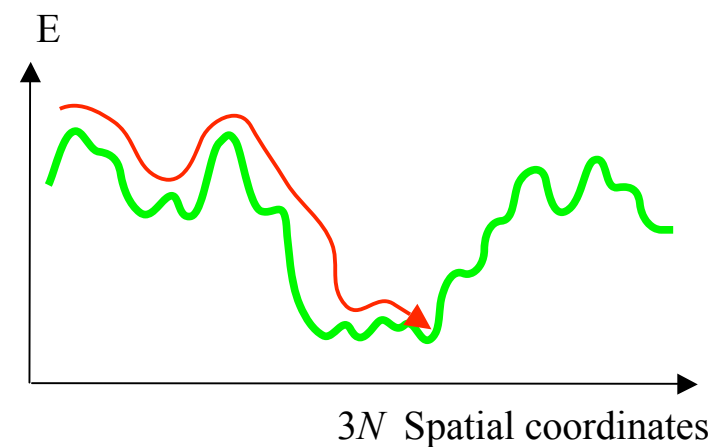
Energy landscape



Landscape for ϕ/ψ plane of dialanine



Complex landscape for a protein



Minimization

Finding **minimum energy conformations** given a potential energy function:

$$\frac{\partial E}{\partial x_i} = 0 \quad \text{and} \quad \frac{\partial^2 E}{\partial x_i^2} > 0$$

Used to:

- relieve strain in experimental conformations
- find (energetically) stable states

Huge number of degrees of freedom in macromolecular systems.



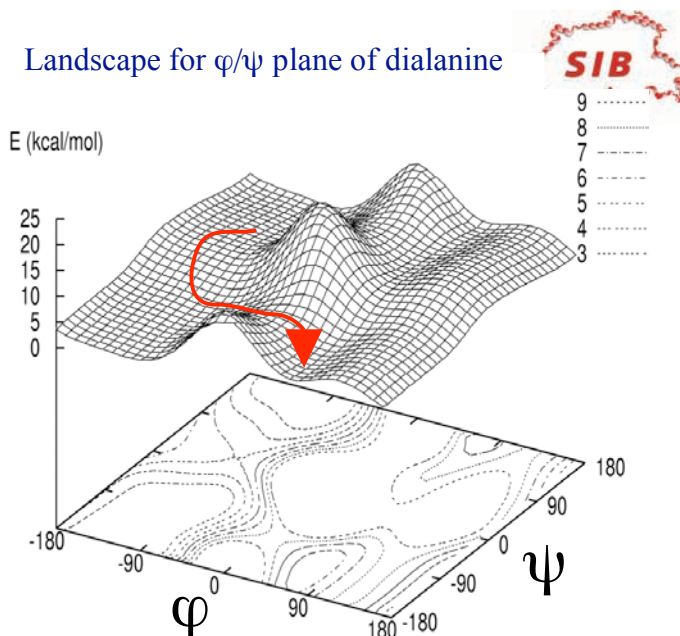
Huge amount of local minima

Impossible to find true global minimum

Different minimization methods available:

- **Steepest descent** (SD) → relieve strain, find close local minimum
- **Conjugated gradient** (CONJ)
- **Adopted Basis Newton Raphson** (ABNR)

} Find lower energy minima



CHARMM input for minimization



```

*

!----- Standard Topology and Parameters
OPEN UNIT 1 CARD READ NAME top_all22_prot.inp
READ RTF CARD UNIT 1
CLOSE UNIT 1

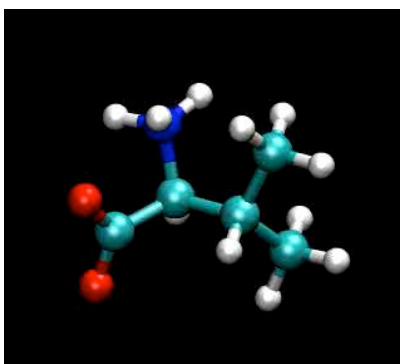
OPEN UNIT 1 CARD READ NAME par_all22_prot.inp
READ PARA CARD UNIT 1
CLOSE UNIT 1

!----- Actual topology
OPEN UNIT 1 READ CARD NAME val.psf
READ PSF CARD UNIT 1
CLOSE UNIT 1

!----- Coordinates
OPEN UNIT 1 READ CARD NAME val.pdb
READ COOR PDB UNIT 1
CLOSE UNIT 1

!----- ABNR minimization
MINI ABNR NSTEP 200

!----- End of input file
STOP
    
```



ABNR> An energy minimization has been requested.

```

EIGRNG = 0.0005000 MINDIM = 5
NPRINT = 50 NSTEP = 200
PSTRCT = 0.0000000 SDSTP = 0.0200000
STPLIM = 1.0000000 STRICT = 0.1000000
TOLFUN = 0.0000000 TOLGRD = 0.0000000
TOLITR = 100 TOLSTP = 0.0000000
FMEM = 0.0000000
    
```

MINI MIN: Cycle	ENERgy	Delta-E	GRMS	Step-size	IMPRopers
MINI INTERN:	BONDs	ANGLes	UREY-b	DIHEdral	USER
MINI EXTERN:	VDWaals	ELEC	HBONDs	ASP	
MINI> 0	-18.69945	0.00000	3.66846	0.00000	
MINI INTERN>	0.49721	2.67684	0.28823	6.34896	0.15433
MINI EXTERN>	7.68221	-36.34723	0.00000	0.00000	0.00000
MINI> 50	-26.40712	7.70767	0.60709	0.00545	
MINI INTERN>	0.65246	3.04259	0.34085	0.97825	0.05940
MINI EXTERN>	4.90369	-36.38436	0.00000	0.00000	0.00000
MINI> 100	-27.90707	1.49995	0.38850	0.00279	
MINI INTERN>	0.84536	3.91951	0.53225	1.87179	0.09659
MINI EXTERN>	6.11013	-41.28270	0.00000	0.00000	0.00000

UPDECI: Nonbond update at step 103

Generating nonbond list with Exclusion mode = 5

== PRIMARY == SPACE FOR 172 ATOM PAIRS AND 0 GROUP PAIRS

General atom nonbond list generation found:

120 ATOM PAIRS WERE FOUND FOR ATOM LIST

0 GROUP PAIRS REQUIRED ATOM SEARCHES

MINI> 150	-28.09742	0.19035	0.04299	0.00027	
MINI INTERN>	0.93508	3.79489	0.58387	2.19377	0.06973
MINI EXTERN>	6.18507	-41.85983	0.00000	0.00000	0.00000
MINI> 200	-28.09805	0.00062	0.00826	0.00005	
MINI INTERN>	0.92928	3.80437	0.58415	2.18679	0.06957
MINI EXTERN>	6.19000	-41.86221	0.00000	0.00000	0.00000

ABNR> Minimization exiting with number of steps limit (200) exceeded.

ABNR MIN: Cycle	ENERgy	Delta-E	GRMS	Step-size	IMPRopers
ABNR INTERN:	BONDs	ANGLes	UREY-b	DIHEdral	USER
ABNR EXTERN:	VDWaals	ELEC	HBONDs	ASP	
ABNR> 200	-28.09805	0.00062	0.00826	0.00005	
ABNR INTERN>	0.92928	3.80437	0.58415	2.18679	0.06957
ABNR EXTERN>	6.19000	-41.86221	0.00000	0.00000	0.00000

Simple Molecular dynamics



Newton's law of motion:

$$F_i = m_i a_i = - \frac{dE_i}{dr_i}$$

In discrete time : integration algorithm.

Example: Verlet algorithm

$$r(t + \delta t) = r(t) + v(t) \times \delta t + \frac{1}{2} a(t) \times \delta t^2$$

$$r(t - \delta t) = r(t) - v(t) \times \delta t + \frac{1}{2} a(t) \times \delta t^2$$

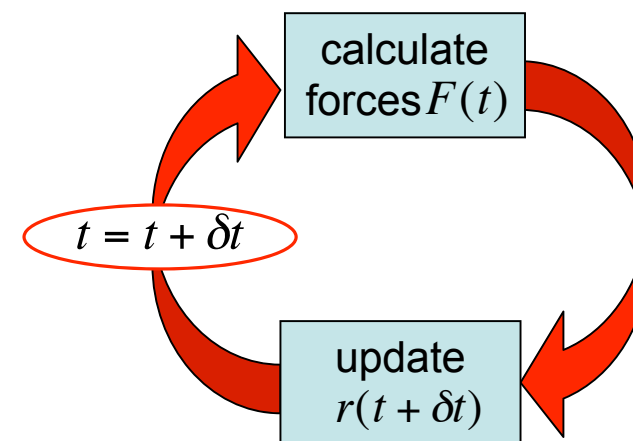


$$r(t + \delta t) = 2r(t) - r(t - \delta t) + \frac{F(t)}{m} \times \delta t^2$$

Propagation of time: position at time $t+\delta t$ is determined by position at time t and $t-\delta t$, and by the acceleration at time t (i.e., the forces at time t)

The equations of motion are deterministic, e.g., the positions and the velocities at time zero determine the positions and velocities at all other times, t .

MD algorithm



$$\delta t \sim 1 \text{ fs} = 10^{-15} \text{ s}$$

CHARMM input file for MD simulation

```

*

!----- Standard Topology and Parameters
OPEN UNIT 1 CARD READ NAME top_all22_prot.inp
READ RTF CARD UNIT 1
CLOSE UNIT 1

OPEN UNIT 1 CARD READ NAME par_all22_prot.inp
READ PARA CARD UNIT 1
CLOSE UNIT 1

!----- Actual topology
OPEN UNIT 1 READ CARD NAME val.psf
READ PSF CARD UNIT 1
CLOSE UNIT 1

!----- Coordinates
OPEN UNIT 1 READ CARD NAME val.pdb
READ COOR PDB UNIT 1
CLOSE UNIT 1

!----- MD simulation
OPEN WRITE UNIT 31 CARD NAME traj/dyna.rst ! Restart file
OPEN WRITE UNIT 32 FILE NAME traj/dyna.dcd ! Coordinates file
OPEN WRITE UNIT 33 CARD NAME traj/dyna.ene ! Energy file

DYNM VERLET START NSTEP 1000 TIMESTEP 0.001 -
IUNWRI 31 IUNCRD 32 KUNIT 33 -
IPRFRQ 100 NPRINT 100 NSAVC 100 NSAVV 100 ISVFRQ 2000 -
FIRSTT 300.0 FINALT 300.0 ICHEW 1 -
IEQFRQ 10 IASORS 0 ISCVEL 0 IASVEL 1 ISEED 8364127 -
INBFRQ 10

!----- End of input file
STOP

```

Generated files:

- Restart file (rst). To restart after crash or to continue MD sim.
- Collection of instantaneous coordinates along trajectory (dcd)

Control propagation of time.
Timestep in ps (i.e. 1fs here)

Control output

Control temperature

Control non bonded list update frequency

Output of MD simulation

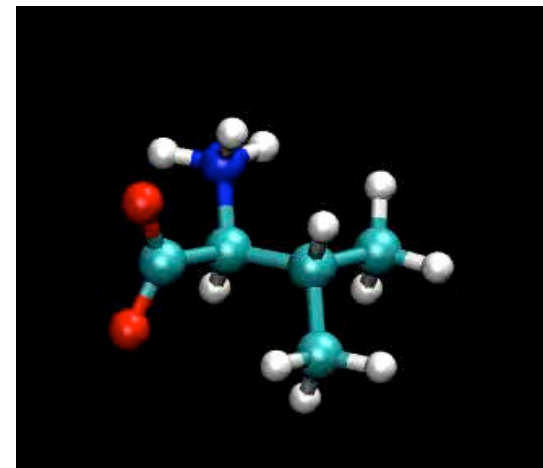


```

DYN> DYN: Step      Time      TOTEner      TOTKe      ENERgy      TEMPerature
DYN> PROP:          GRMS      HFCTote      HFCKe      EHFCor      VIRKe
DYN> INTERN:        BONds      ANGLEs      UREY-b      DIHEdrals    IMPRopers
DYN> EXTERN:        VDWaals      ELEC      HBONds      ASP      USER
DYN> PRESS:         VIRE      VIRI      PRESSE      PRESSI      VOLUme
-----
DYN> 0              0.00000      -6.35935      19.31479      -25.67414      381.16244
DYN> PROP>          1.79744      -6.35862      19.31700      0.00074      -3.31909
DYN> INTERN>         0.49721      2.67684      0.28823      3.69866      0.15433
DYN> EXTERN>         4.45183      -37.44124      0.00000      0.00000      0.00000
DYN> PRESS>         0.00000      2.21273      0.00000      0.00000      0.00000
-----
[...]
```

```

DYN> DYN: Step      Time      TOTEner      TOTKe      ENERgy      TEMPerature
DYN> PROP:          GRMS      HFCTote      HFCKe      EHFCor      VIRKe
DYN> INTERN:        BONds      ANGLEs      UREY-b      DIHEdrals    IMPRopers
DYN> EXTERN:        VDWaals      ELEC      HBONds      ASP      USER
DYN> PRESS:         VIRE      VIRI      PRESSE      PRESSI      VOLUme
-----
DYN> 10             0.01000      7.81721      16.21830      -8.40109      320.05568
DYN> PROP>          14.53782      7.92338      16.53681      0.10617      -73.15251
DYN> INTERN>         3.28801      14.20105      3.70007      3.31010      0.21480
DYN> EXTERN>         9.54825      -42.66337      0.00000      0.00000      0.00000
DYN> PRESS>         0.00000      48.76834      0.00000      0.00000      0.00000
-----
UPDECI: Nonbond update at step      10
[...]
```



Newtonian dynamics in practice

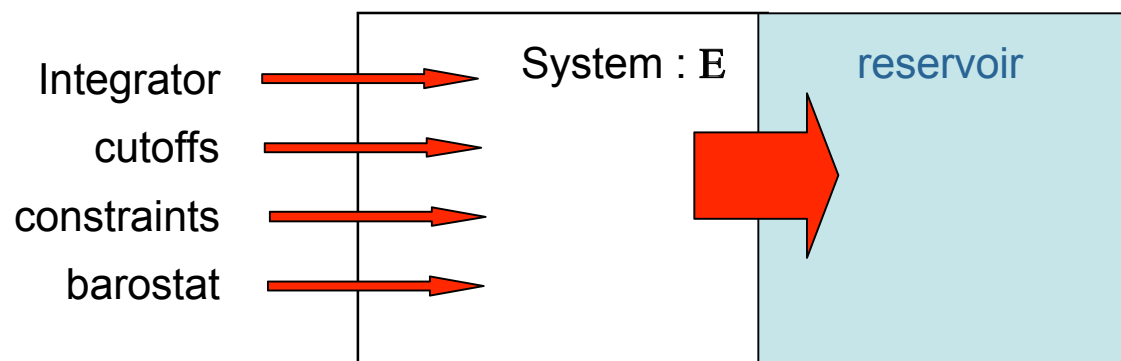
In theory, Newtonian dynamics **conserves the total energy** (isolated system) :

$$\begin{aligned} \dot{r} &= \frac{p}{m} \\ \dot{p} &= F(r) \end{aligned} \quad H(r, p) = \sum_i \frac{p_i^2}{2m_i} + V(r) = \text{cste}$$

In practice, constant energy dynamics is not often used for two reasons :

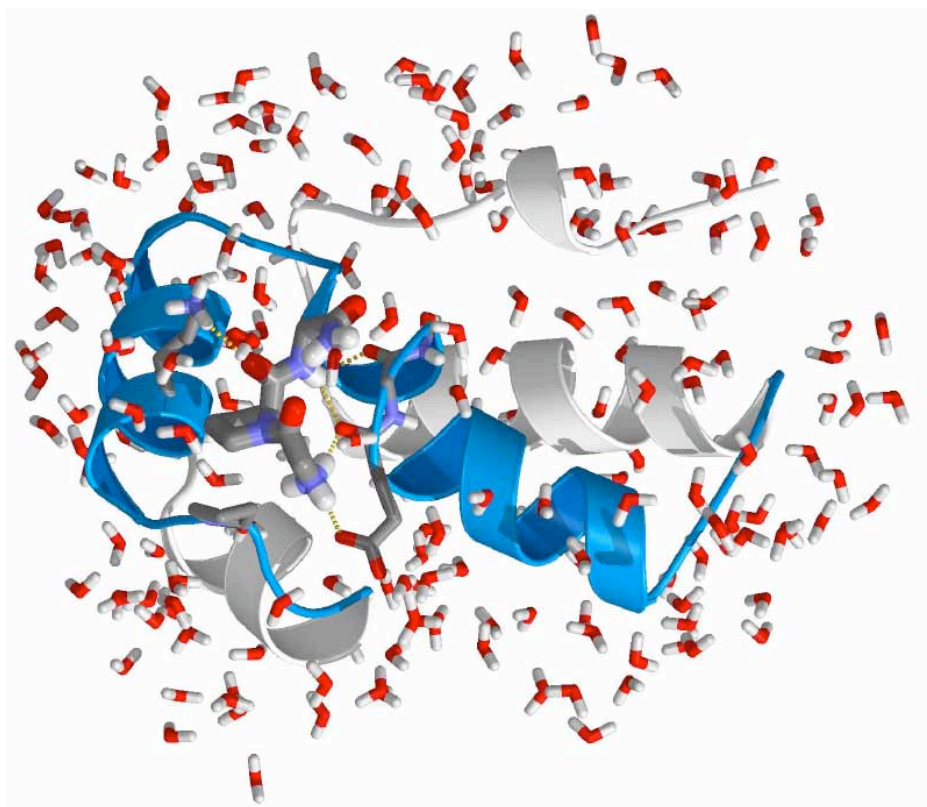
- 1) **Inaccuracies** of the MD algorithm tend to **heat up** the system

We can couple the system to a heat reservoir to absorb the excess heat



- 2) The constant energy dynamics (NVE) does **rearely represents the experimental conditions** for the system simulated.

Plan



- Introduction
- The classical force field
- Setting up a simulation
- **Connection to statistical mechanics**
- Usage of MD simulation



Thermodynamic ensembles

A **macroscopic state** is described by :

- | | | | |
|-------------------------|-----|------------------------|-------|
| - number of particles : | N | - chemical potential : | μ |
| - volume : | V | - pressure : | P |
| - energy : | E | - temperature : | T |

Definition: a *thermodynamical ensemble* is a collection of microscopic states that all realize an identical macroscopic state

A **microscopic state** of the system is given by a point (\mathbf{r}, \mathbf{p}) of the phase space of the system, where $\mathbf{r} = (\mathbf{r}_1, \dots, \mathbf{r}_N)$ and $\mathbf{p} = (\mathbf{p}_1, \dots, \mathbf{p}_N)$ are the positions and the momenta of the N atoms of the system.

Examples of thermodynamical ensembles:

- | | | |
|--------------------|-------------------|------------------|
| - Microcanonical: | fixed N, V, E | |
| - Canonical: | fixed N, V, T | often used in MD |
| - Constant P-T: | fixed N, P, T | often used in MD |
| - Grand Canonical: | fixed μ, P, T | |

Boltzmann (canonical) distribution

Boltzmann showed that the *canonical* probability of the microstate i is given by

$$P_i = \frac{1}{Z} e^{-\beta E_i}$$

$$\beta = 1/K_B T$$

K_B = Boltzmann constant

Z is the *partition function*,

$$Z = \sum_j e^{-\beta E_j}$$

such that : $\sum_i P_i = 1$

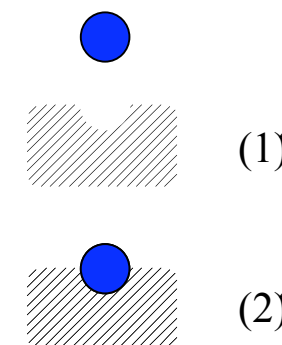
The *partition function* is a very complex function to compute, because it represents a measure of the whole space accessible to the system.

Illustration:

If a system can have two unique states, state (1) and state (2), then the ratio of systems in state (1) and (2) is

$$\frac{P_1}{P_2} = \frac{e^{-E_1}}{e^{-E_2}} = e^{-E_1 - E_2} = e^{-\Delta E}$$

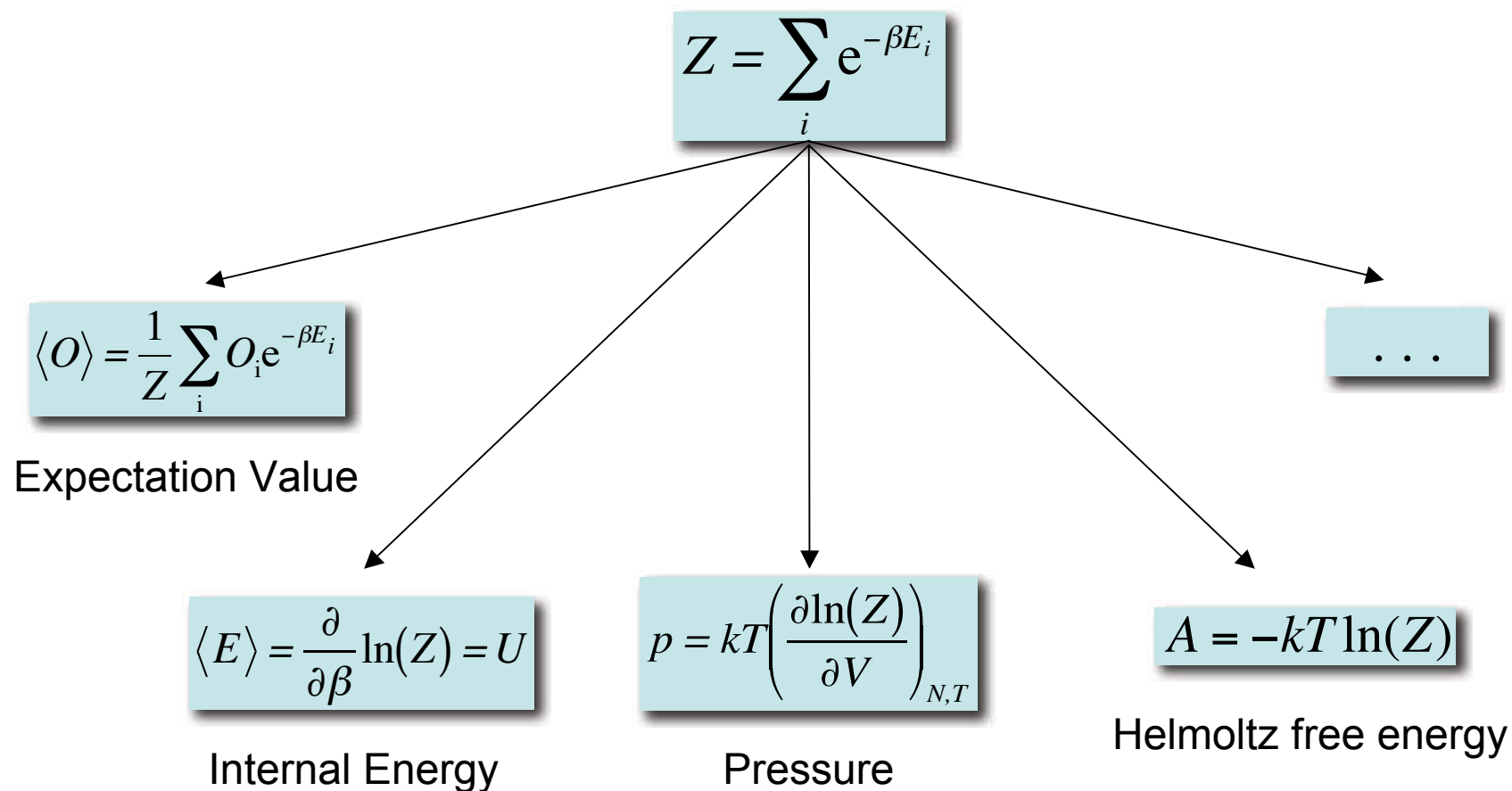
at 300K, a ΔE of 1.3 kcal/mol results in a P_1/P_2 of 1 log₁₀.



Cave: if state (1) and (2) are composed of several microscopic states, $\Delta E \neq \Delta G$

The partition function

The determination of the macroscopic behavior of a system from a thermodynamical point of view is tantamount to computing the **partition function**, Z , from which all the properties can be derived.



The ensemble average

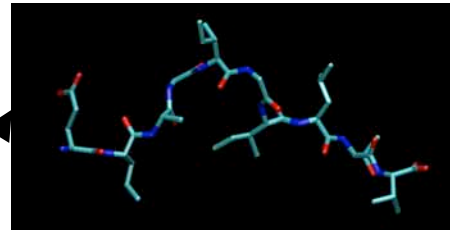


Macroscopic

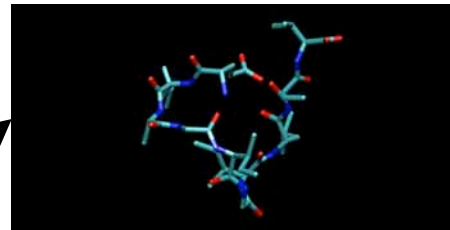
Expectation value

$$\langle O \rangle = \frac{1}{Z} \sum O_i e^{-\beta E_i}$$

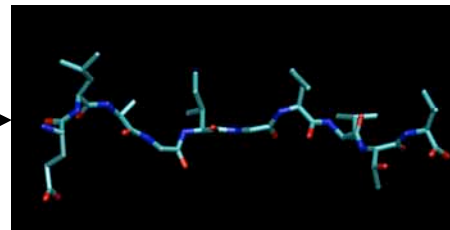
Where $Z = \sum e^{-\beta E_i}$
is the partition function



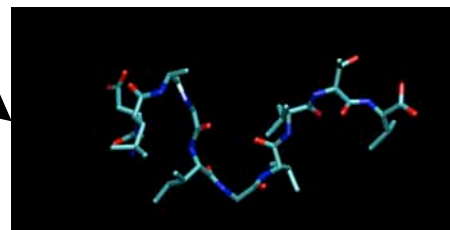
Microscopic
 $E_1, P_1 \sim e^{-\beta E_1}$



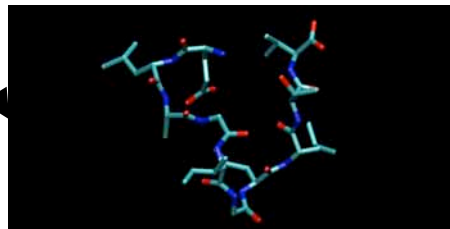
$E_2, P_2 \sim e^{-\beta E_2}$



$E_3, P_3 \sim e^{-\beta E_3}$



$E_4, P_4 \sim e^{-\beta E_4}$



$E_5, P_5 \sim e^{-\beta E_5}$

Ergodic Hypothesis

The *ergodic hypothesis* is that the **ensemble averages** used to compute expectation values can be **replaced by time averages** over the simulation.

$$\begin{aligned} \langle O \rangle_{ensemble} &\stackrel{\text{Ergodicity}}{=} \langle O \rangle_{time} \\ \frac{1}{Z} \int O(r, p) e^{-\beta E(r, p)} dr dp &= \frac{1}{\tau} \int_0^{\tau} O(t) dt \end{aligned}$$

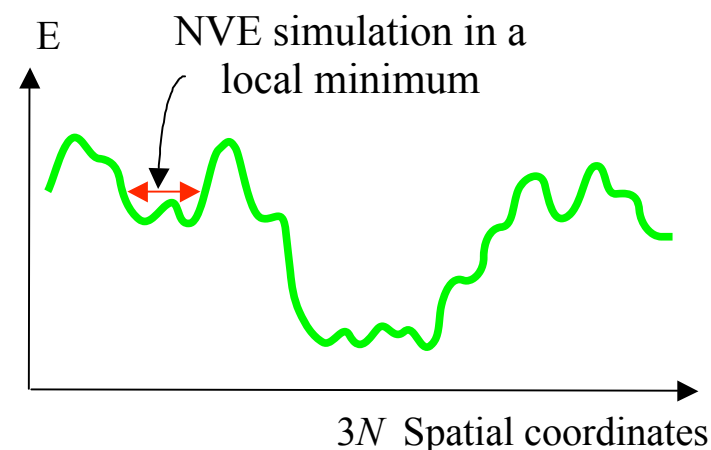
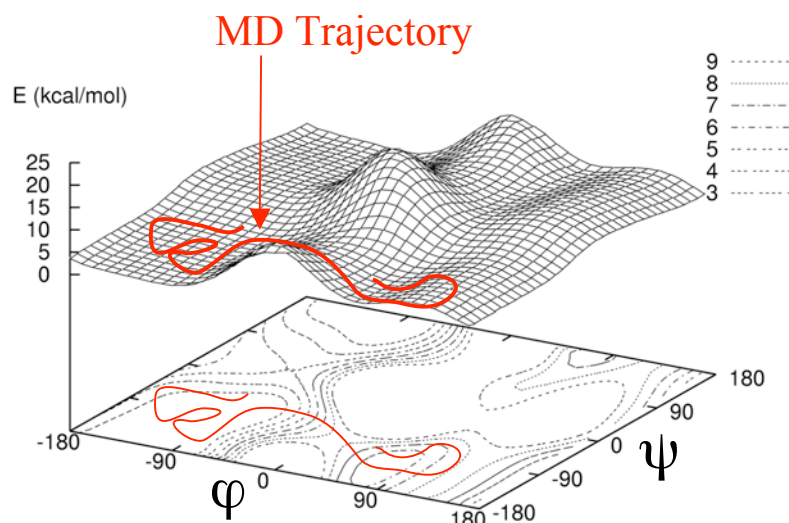
The microstates sampled by molecular dynamics are usually a small subset of the entire thermodynamical ensemble.

The validity of this hypothesis depends on the quality of the sampling produced by the molecular modelling technique. The sampling should reach all important minima and explore them with the correct probability,

- <i>NVE</i> simulations	⇔	Microcanonic ensemble	⇔ $P = cst.$
- <i>NVT</i> simulations	⇔	Canonical ensemble	⇔ $P(E) = e^{-\beta E}$
- <i>NPT</i> simulations	⇔	Isothermic-isobaric ensemble	⇔ $P(E) = e^{-\beta(E+PV)}$

Note that the Boltzmann weight $e^{-\beta E}$ is not present in the time average because it is assumed that conformations are sampled from the right probability.

Ergodic hypothesis : intuitive view



$$\langle O \rangle_{ensemble} = \frac{1}{Z} \int O(r,p) e^{-\beta E(r,p)} dr dp \quad ? \quad = \quad \frac{1}{\tau} \int_0^{\tau} O(t) dt = \langle O \rangle_{time}$$

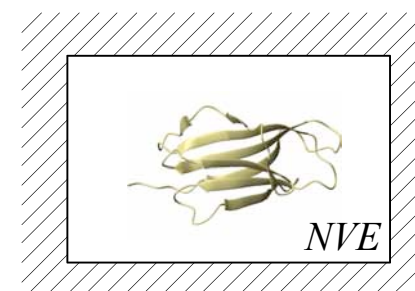
Two main requirements for MD simulation :

- 1) Accurate **energy function** $E(r,p)$
- 2) Appropriate **algorithm**, which
 - generates the right ensemble
 - samples efficiently

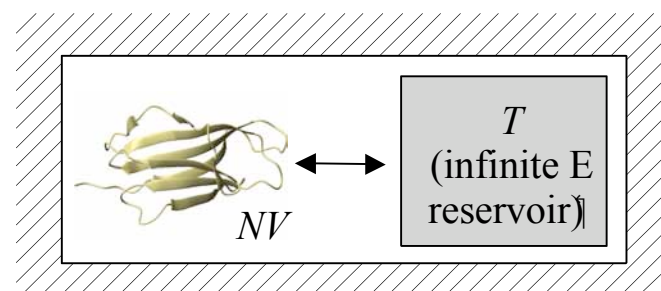
Sampling of the various ensembles



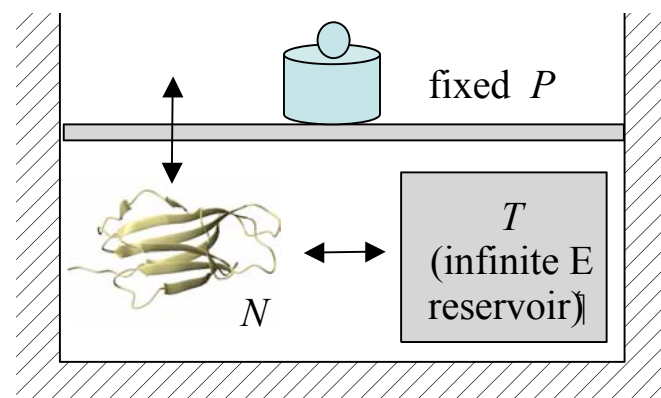
- 1) **Microcanonical ensemble** (constant N, V, E)
sampling is obtained by simple integration
of the Newtonian dynamics:
- Verlet, Leap-Frog, Velocity Verlet, Gear



- 2) **Canonical ensemble** (constant N, V, T)
sampling is obtained using thermostats :
- 1) **Berendsen**: scaling of velocities to obtain an exponential relaxation of the temperature to T
 - 2) **Nose-Hoover**: additional degree of freedom coupled to the physical system acts as heat bath.



- 3) **Isothermic-isobaric ensemble** (constant N, P, T)
In addition to the thermostat, the volume of the system is allowed to fluctuate, and is regulated by barostat algorithms.



The Nosé-Hoover thermostat

Phase space extended by two extra variables :

$$(\underbrace{r, p}_{\text{physical variables}}, \eta, p_\eta)$$

$$\begin{aligned} \dot{r}_i &= \frac{p_i}{m_i} && \leftarrow \text{Newton} \\ \dot{p}_i &= -\frac{\partial \Phi}{\partial r_i}(r, t) - \frac{p_\eta}{Q} p_i && \leftarrow \text{friction term} \\ \dot{\eta} &= \frac{p_\eta}{Q} \\ \dot{p}_\eta &= \sum_i \frac{p_i^2}{m_i} - N_{df} k_B T && \leftarrow \text{temperature regulation} \end{aligned}$$

- One can demonstrate that the **canonical distribution is reproduced** for the physical variables

$$Z(N, V, T) = \int dr dp e^{-\beta H(r, p)}$$

- Conserved quantity :

$$H'(\Gamma, t) = \sum_{i=1}^N \frac{p_i^2}{2m_i} + \Phi(r) + \frac{p_\eta^2}{2Q} + k_B T \bar{\eta}$$

- **Non-Hamiltonian** dynamics...

Other sampling methods I

Langevin Dynamics (LD)

In Langevin Dynamics, two additional forces are added to the standard force field:

- a *friction* force: $-\gamma_i \mathbf{p}_i$
whose direction is opposed to the velocity of atom i
- a *stochastic* (random) force: $\zeta(t)$ such that $\langle \zeta(t) \rangle = 0$.

This leads to the following equation for the motion of atom i :

$$\dot{\mathbf{r}}_i = \frac{\mathbf{p}_i}{m_i} \quad \dot{\mathbf{p}}_i = \mathbf{F}_i(\mathbf{r}) + \gamma \mathbf{p}_i + \zeta(t)$$

This equation can for example simulate the friction and stochastic effect of the solvent in implicit solvent simulations. The temperature is adjusted via γ and ζ , using the *dissipation-fluctuation* theorem.

The stochastic term can improve barrier crossing and hence sampling.

LD does *not* reproduce dynamical properties

Other sampling methods II



Monte Carlo Simulations and the Metropolis criterion

In this sampling method, instead of computing the forces on each atom to solve its time evolution, random movements are assigned to the system and the potential energy of the resulting conformer is evaluated.

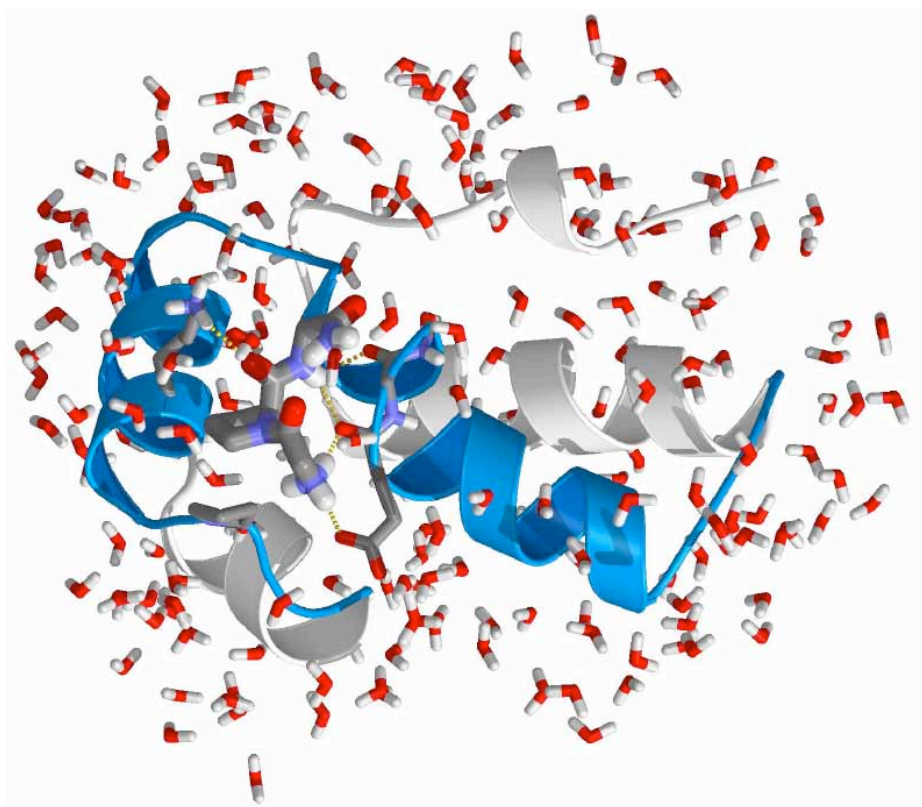
To insure Boltzmann sampling, additional criteria need to be applied on the new conformer. Let C be the initial conformer and C' the randomly modified:

- if $V(C') < V(C)$, the new conformer is kept and C' becomes C for next step
- if $V(C') > V(C)$, a random number, ρ , in the $[0,1]$ interval is generated and
if $e^{-\beta(V'-V)} > \rho$, the new conformer is kept and C' becomes C for next step

Using this algorithm, one insures Boltzmann statistics,

$$\frac{P(C')}{P(C)} = e^{-\beta(V'-V)}$$

Plan



- Introduction
- The classical force field
- Setting up a simulation
- Connection to statistical mechanics
- **Usage of MD simulation**

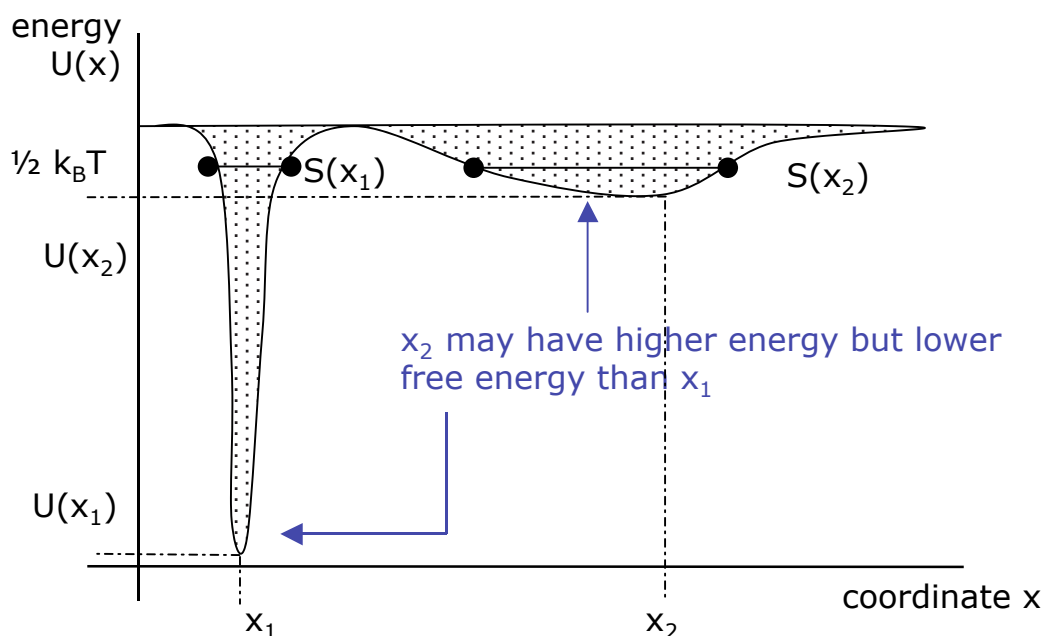
The importance of entropy

Mechanics: A state is characterised by **one minimum energy structure** (global minimum)

Statistical mechanics: A state is characterised by **an ensemble of structures**

Very small energy differences between states ($\sim k_B T = 2.5$ kJ/mol)
resulting from summation over very many contributions

Entropic effects : Not only energy minima are of importance but whole range of x -values with energies $\sim k_B T$



The free energy (F) governs the system

$$F = U - TS$$



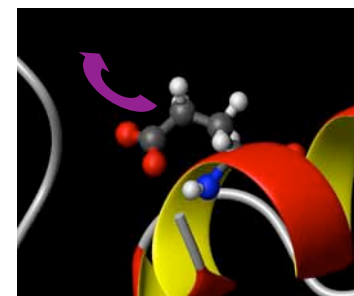
Energy (U) – entropy (S) compensation at finite temperature T

Dynamical behavior of proteins

Biological molecules exhibit a wide range of time scales over which specific processes occur; for example:

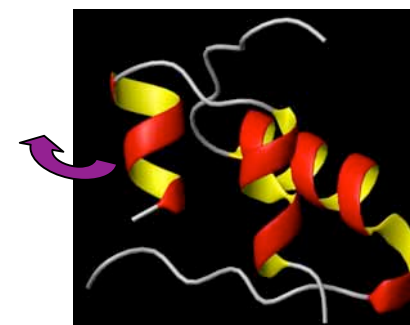
❑ Local Motions (0.01 to 5 Å, 10^{-15} to 10^{-1} s)

- Atomic fluctuations
- Sidechain Motions
- Loop Motions



❑ Rigid Body Motions (1 to 10 Å, 10^{-9} to 1 s)

- Helix Motions
- Domain Motions
- Subunit motions



❑ Large-Scale Motions (> 5 Å, 10^{-7} to 10^4 s)

- Helix coil transitions
- Dissociation/Association
- Folding and Unfolding

Types of problems



Molecular dynamics simulations permit the study of complex, dynamic processes that occur in biological systems. These include, for example:

- Protein stability
- Conformational changes
- Protein folding
- Molecular recognition: proteins, DNA, membranes, complexes
- Ion transport in biological systems

and provide the mean to carry out the following studies,

- Drug Design
- Structure determination: X-ray and NMR

Historical perspective



Theoretical milestones:

Newton (1643-1727):	Classical equations of motion: $F(t)=m a(t)$
Boltzmann(1844-1906):	Foundations of statistical mechanics
Schrödinger (1887-1961):	Quantum mechanical eq. of motion: $-i\hbar \partial_t \Psi(t)=H(t) \Psi(t)$

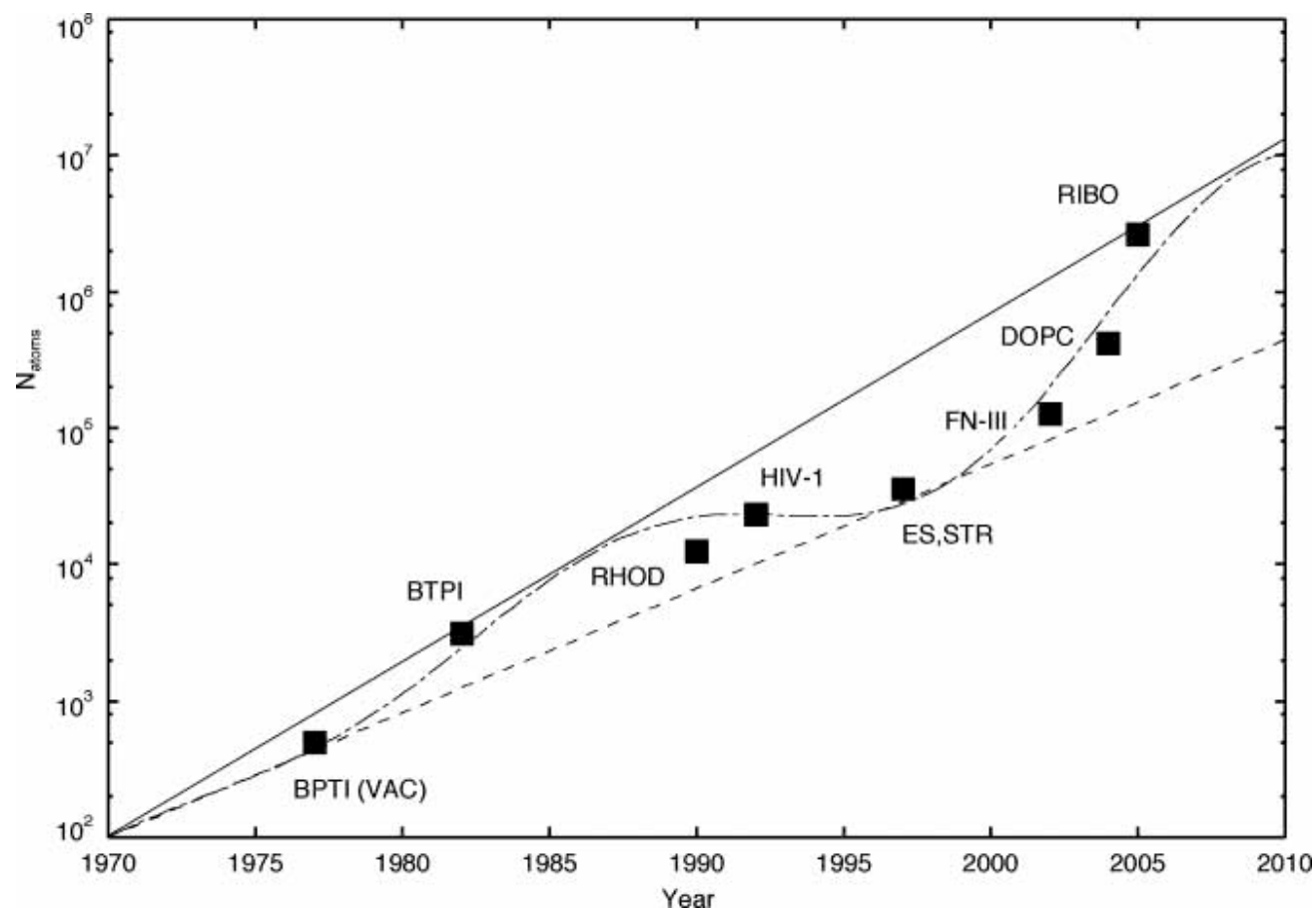
Molecular mechanics milestones:

Metropolis (1953):	First Monte Carlo (MC) simulation of a liquid (hard spheres)	<i>Liquids</i>
Wood (1957):	First MC simulation with Lennard-Jones potential	
Alder (1957):	First Molecular Dynamics (MD) simulation of a liquid (hard spheres)	
Rahman (1964):	First MD simulation with Lennard-Jones potential	
Karplus (1977) & McCammon (1977)	First MD simulation of proteins	<i>Proteins</i>
Karplus (1983):	The CHARMM general purpose FF & MD program	
Kollman(1984):	The AMBER general purpose FF & MD program	
Car-Parrinello(1985):	First full QM simulations	
Kollmann(1986):	First QM-MM simulations	

System sizes



Simulations in explicit solvent



BPTI (VAC), bovine pancreatic trypsin inhibitor without solvent

BPTI, bovine pancreatic trypsin inhibitor with solvent

RHOD, photosynthetic reaction center of *Rhodopseudomonas viridis*

HIV-1, HIV-1 protease

ES, estrogen–DNA

STR, streptavidin

DOPC, DOPC lipid bilayer

RIBO, ribosome

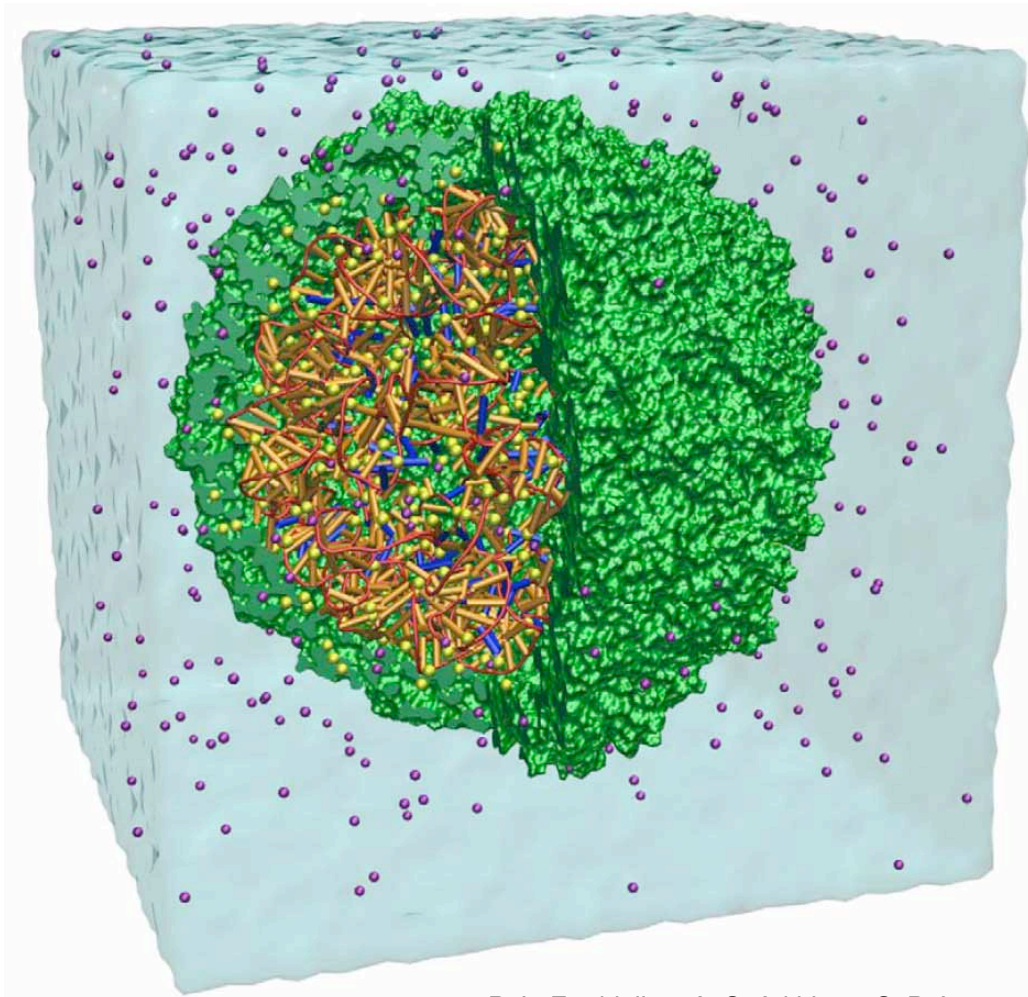
Solid curve, Moore's law doubling every 28.2 months.

Dashed curve, Moore's law doubling every 39.6 months.

Largest system 2006



satellite tobacco mosaic virus



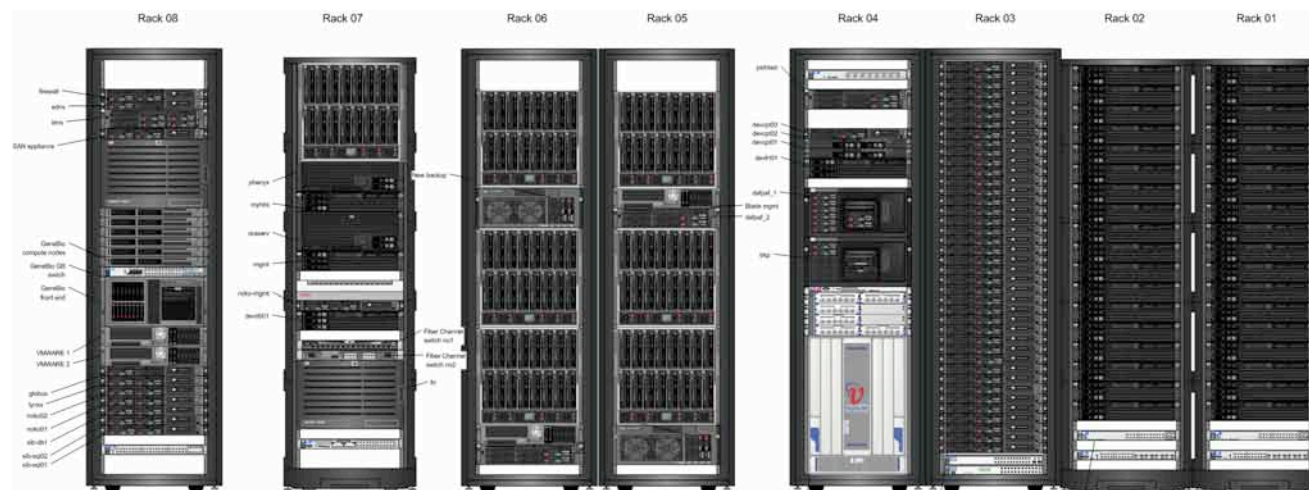
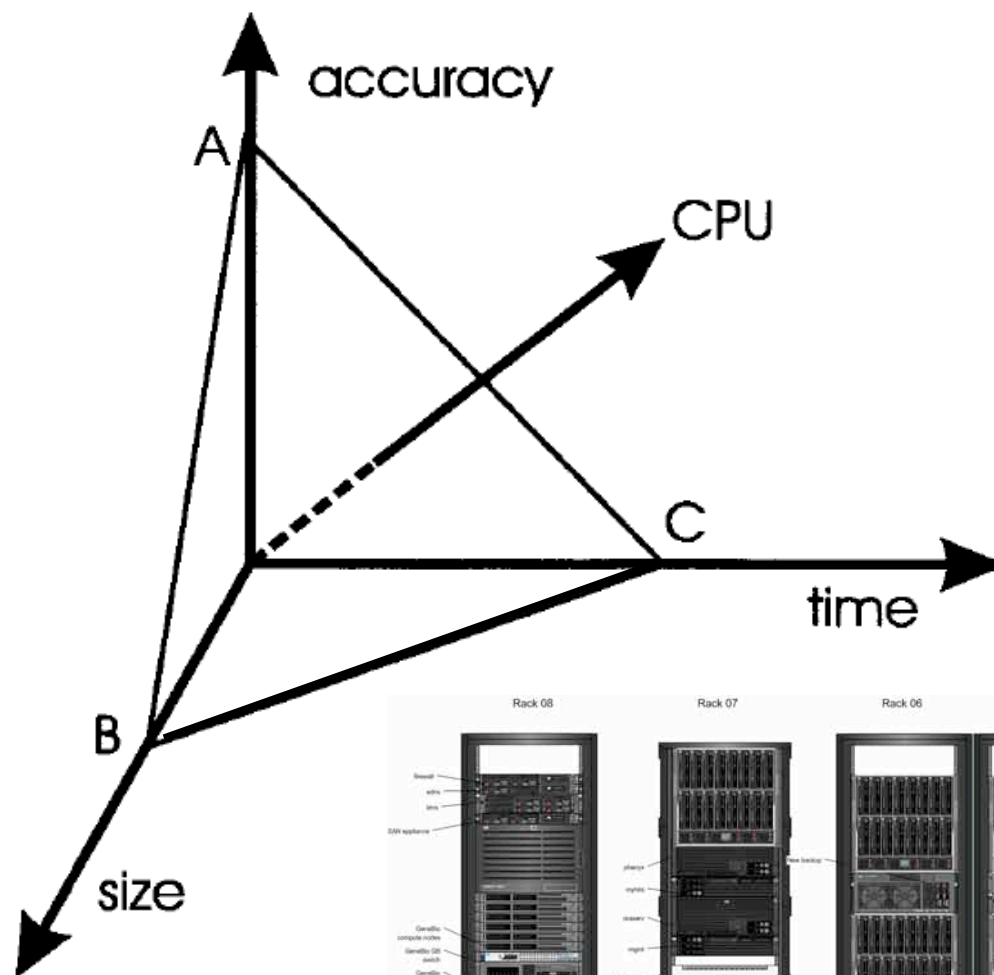
1 million atoms

Simulation time : 50 ns

system size : 220 Å

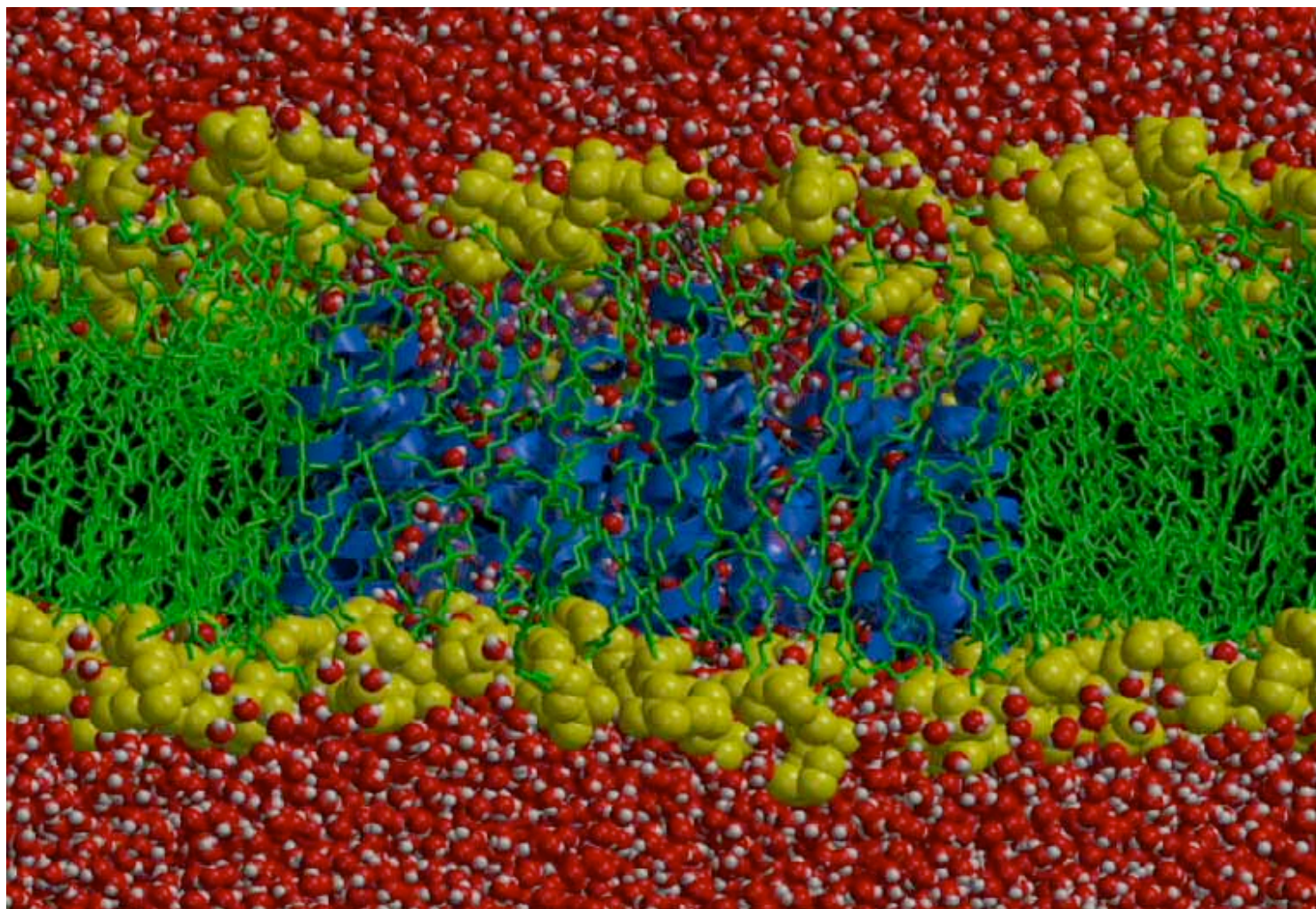
P. L. Freddolino, A. S. Arkhipov, S. B. Larson, A. McPherson, and K. Schulten, Molecular dynamics simulations of the complete satellite tobacco mosaic virus, *Structure* 14 (2006), 437.

The tradeoff we can afford



Exemple : Aquaporin

Selective translocation of water across a membrane

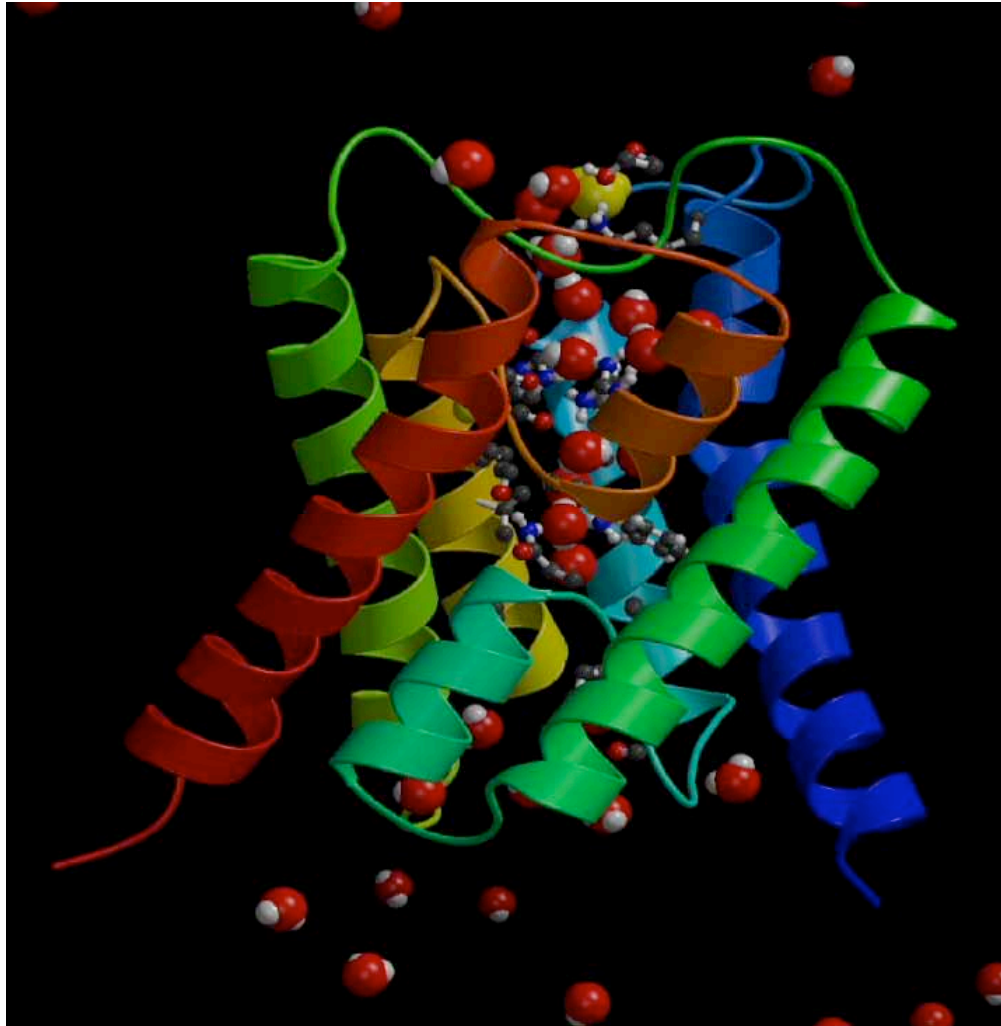


S. Hub and Bert L. de Groot. Mechanism of selectivity in aquaporins and aquaglyceroporins PNAS. 105:1198-1203 (2008)

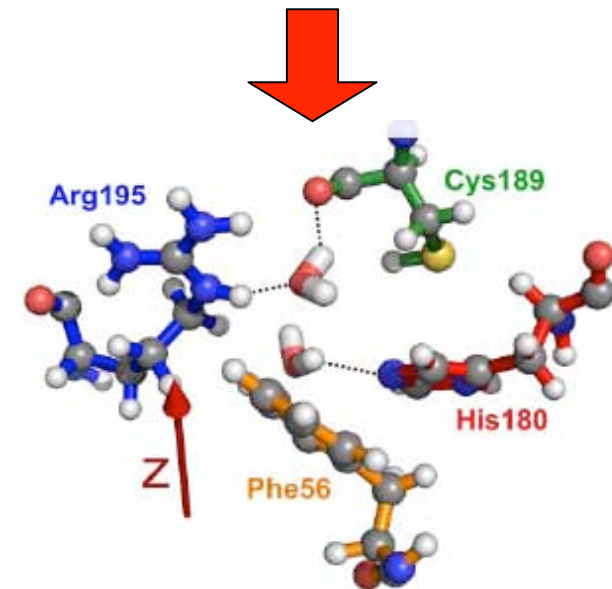
Exemple : Aquaporin



Selective translocation of water across a membrane



Propose a model for selectivity at the atomic level



S. Hub and Bert L. de Groot. Mechanism of selectivity in aquaporins and aquaglyceroporins, PNAS 105:1198-1203 (2008)