

Problem 1

(1) $n=8^3=512$

(2) Statistically, when $n=512$ Max k should be between 7 and 8

Maximum Collisions k Relative to Size N

k	$(e/k)^k$	$n=(k/e)^{k/4}$
6	8.65E-03	2.89E+01
7	1.33E-03	1.88E+02
8	1.78E-04	1.41E+03
9	2.09E-05	1.20E+04
10	2.20E-06	1.13E+05
11	2.10E-07	1.19E+06
12	1.83E-08	1.37E+07
13	1.46E-09	1.71E+08
14	1.08E-10	2.31E+09
15	7.47E-12	3.35E+10
16	4.82E-13	5.19E+11
17	2.92E-14	8.56E+12

(2) Simulation Result

	1st	2nd	3rd	Average	%
0	221	241	220	227.33	44%
1	153	124	143	140.00	27%
2	87	85	98	90.00	18%
3	28	40	36	34.67	7%
4	17	14	10	13.67	3%
5	3	6	5	4.67	1%
6	3	2	0	1.67	0%
7	0	0	0	0.00	0%
	512	512	512	512	100%

(3) Conclusion : Therefore, this simulation result is within the range of statistical probability.

<Attachment - Problem 1 - Simulation 1>

179, 120, 61, 272, 387, 394, 171, 212, 271, 234, 330,
28, 450, 279, 358, 447, 469, 146, 415, 298, 189, 300,
177, 177, 357, 244, 494, 227, 438, 366, 498, 39, 242,
206, 280, 378, 90, 112, 396, 148, 198, 157, 284, 476,
366, 312, 192, 185, 38, 45, 175, 339, 371, 317, 23,
449, 143, 455, 276, 425, 191, 464, 446, 328, 373, 178,
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4021032021
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2001111002
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0223101201
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0011022006
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0101110402
0100110110
1013000102
2101010100
1011124001
1304110203
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0024100210
2101000013
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0 0 0 0 2 0 2 1 0 0
2 1 2 0 0 2 2 1 0 0
3 0

#of conflict=0 : 221, 43.1641 %
#of conflict=1 : 153, 29.8828 %
#of conflict=2 : 87, 16.9922 %
#of conflict=3 : 28, 5.46875 %
#of conflict=4 : 17, 3.32031 %
#of conflict=5 : 3, 0.585938 %
#of conflict=6 : 3, 0.585938 %
#of conflict=7 : 0, 0 %
#of conflict=8 : 0, 0 %
#of conflict=9 : 0, 0 %
#of conflict=10 : 0, 0 %
#of conflict=11 : 0, 0 %
#of conflict=12 : 0, 0 %
#of conflict=13 : 0, 0 %

0 --> JCU

1

2

3

4 --> QGO --> QGN

5

6 --> MEH

7 --> OQX --> ORX

8

9 --> STK --> KNR --> KNS

10 --> BYV --> AZU

11 --> MPF

12 --> PEV

13

14

15

16 --> HCI --> GCI

17 --> SRP --> PSR

18

19

20 --> SDA --> QDA

21 --> INF

22 --> UDN --> UDN

23 --> EGY

24 --> DWN --> EZM

25 --> PMY

26 --> KCC

27

28 --> WHB

29 --> YVP --> HKK --> ZUR --> GLK --> ILJ

30

31 --> TRL --> USK

32

33 --> WPZ --> XSY --> ZRY --> WSZ

34

35 --> KLW

36 --> ZDG --> ZFG

37 --> HIQ

38

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40 --> KYU

41 --> WRF

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44 --> AUJ --> BVH --> BVG --> BTG

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51 --> QNF --> SNF --> QMF --> QND --> RNE --> RNE

52 --> BQM

53 --> OIY --> OHX --> NIW --> MHY --> OIW --> MGZ

54 --> NXO --> OXM

55 --> CCZ --> CAZ

56

57 --> UNS

58 --> FVC --> EVB

59

60 --> BMV

61

62 --> YCO

63 --> HEX

64 --> RYG --> SWH

65 --> VJY

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68 --> HRV

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70 --> VWU

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74 --> KUH --> JUG
75 --> YLS --> ZJS --> WKS
76 --> ISB --> IQC
77 --> KDP
78
79
80 --> OVV
81 --> KAY --> BBF --> LAX
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90 --> RVO
91 --> AZW --> BXW
92 --> MSG --> FOO
93 --> REX
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96
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98 --> QRT --> SST --> RRV --> PPU
99 --> CXD
100
101
102
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104 --> VTG --> TVH
105 --> EXR
106
107 --> KBD
108
109
110 --> HKN --> ZVU
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113 --> NCP
114
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116 --> LMB
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118 --> NON --> MNM
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121 --> JWW --> JYY --> KYZ --> KYZ
122
123
124 --> KLI --> PPC --> LLG --> JLH
125 --> CUJ
126 --> OJU
127 --> RCJ --> RCK
128
129 --> UAZ --> VAW
130
131
132 --> RMH
133 --> AQS
134
135 --> MXQ --> MWS --> OYP --> OZR
136 --> AEA
137 --> UAD
138
139
140 --> XQH
141 --> CNY --> GUP
142
143 --> ZAS
144
145 --> PXJ --> SZJ
146 --> VMB
147 --> FRL
148
149 --> GRW --> HRX --> ISX
150 --> KHN --> KIO
151 --> TYY --> TWY --> VYX --> UXY
152 --> NLC --> IEG --> MLC --> NKC
153
154
155 --> LVK
156 --> YJT
157 --> ISF
158 --> KDT --> JFV --> JDT
159
160 --> NGG --> OHH --> MGH --> NGH
161
162 --> BBG --> BCI
163 --> JQP
164
165 --> WYQ --> WZS --> YWS
166 --> RGU --> SHU
167

168 --> NEN --> MEO
169 --> MUD
170
171 --> PUS --> RVP --> PVQ
172 --> TJI
173 --> NQK --> DMP
174
175
176
177 --> EJW --> UYF --> EJZ
178 --> GAM --> HCN
179 --> SPW
180 --> BYI --> BWG --> CYH
181
182 --> XKA --> YKA --> YJC
183 --> INK --> INL
184
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186 --> EZV --> FZT
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188
189 --> LNZ
190 --> YIG
191 --> ILS
192
193
194 --> NBV
195 --> XTF
196
197 --> KNE
198
199 --> NNP --> MOS
200 --> QEH --> SDI
201
202 --> OCA --> NBB
203
204
205 --> KKL --> RSD --> LKJ --> RQF
206
207 --> OKZ
208 --> SAM
209
210 --> VFB
211 --> EIJ
212 --> FYA
213 --> RML --> SOJ
214 --> CQT

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217 --> ADD --> HGX --> BDE --> HGX
218 --> UBG
219 --> FEP
220
221 --> SLS --> XRL
222 --> IUUV --> GVV
223
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226
227 --> UMD --> VMF --> UOE
228 --> JZI --> EQN
229 --> ZOP --> ZMP
230 --> HTA
231 --> LGS
232 --> WAC --> YAA
233 --> NLE
234
235
236 --> JTN
237 --> WJW --> ZLW
238
239 --> KDX
240 --> BQB
241 --> NIK --> OGJ
242 --> OWB
243 --> CBK
244 --> KRU --> LQU --> JRT
245 --> DAY
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249 --> NDQ
250 --> OUI --> NTG
251
252
253 --> FAF
254 --> EOT
255 --> RGF
256 --> BLM
257
258
259 --> GCR --> GAR
260
261 --> TGQ --> VHR --> THQ

262
263 --> XJD --> XJE
264 --> XZT
265 --> TFX --> JED --> TDX
266
267 --> FZW
268
269
270 --> JSA --> LRB
271
272 --> ZYC
273
274
275 --> NAW --> NCW
276 --> MPM --> WTG --> NSO
277 --> IWP
278 --> LMI --> LOH
279
280
281 --> SDJ --> SFL
282 --> AHU --> CHV
283 --> MCF --> MCF --> NAE
284 --> FJI
285
286 --> RQG
287 --> AVR --> AVS
288
289 --> SBQ
290
291 --> UFD
292 --> VPV --> UPV --> UQU --> EGO
293
294 --> PON
295
296
297 --> NYY --> OXZ --> MYX --> XER --> YEP
298 --> IKA
299 --> UCK --> UAK
300
301
302 --> ZQO
303 --> GVV
304
305 --> WCY --> YBZ
306 --> III --> HII
307
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309 --> DSR --> DSS --> FPS --> DSP --> DRP --> JXK

310 --> ZNT

311 --> IVE --> IUE --> GUE

312

313 --> XCE --> WCD

314 --> OKH --> OKI

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316 --> AEG --> CDI

317 --> LTP

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319

320 --> JGA --> QJV

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322 --> MGM

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325 --> QXS

326 --> EDB

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328 --> PJC

329 --> AOL

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331 --> MUK

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333 --> RVX

334 --> EBI

335 --> FNW

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337 --> HSK --> HSJ --> GQK --> GQJ

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339 --> UZK --> FME

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341 --> SVD

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344 --> ZJH

345 --> ZWZ

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347 --> VTP

348 --> HAB

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350 --> LBN

351

352 --> ZIO

353 --> ZYE --> IKX --> YWD

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356
357 --> MQP
358
359 --> KOK --> KNL
360 --> BZO --> AWO
361 --> MNX
362
363 --> AGX
364
365 --> DKK
366
367 --> PQJ
368
369
370 --> RBV
371
372 --> UFI
373 --> VRW
374 --> EYH
375 --> PNQ --> QMQ
376 --> HXU --> ATC --> HYT --> AVC
377
378
379 --> IJD
380 --> UCN
381 --> UPE --> DDX --> TSF
382
383 --> WSQ --> WRP --> WSS --> XRR
384 --> GYC
385 --> LLP
386
387 --> IHK --> HIK
388
389 --> UMK --> TOJ --> TOK
390
391 --> WMX --> YNX --> WNW
392 --> HUG --> GTG
393 --> KIW --> LGW
394
395
396 --> RCA
397 --> CDK --> BEK
398
399
400
401 --> PJX
402

403 --> MGR --> MHR
404 --> OZG
405 --> BBQ
406 --> QYV --> PXU
407
408
409 --> RJD
410
411
412 --> WCG --> NUO --> YBG --> WCG --> OVO
413 --> IEQ
414 --> QZA
415 --> FBK --> TLP
416 --> DQC
417 --> PIL
418 --> HQN
419
420 --> UXN
421 --> GBX
422
423
424
425
426
427
428 --> TUT --> UVU
429 --> OEZ --> NEW --> HAE
430
431
432 --> JSG --> KQH
433 --> YGR --> ZIP --> ZGS --> XHP
434 --> YYI
435
436
437 --> MED --> NEE
438 --> ORU
439
440 --> KNM --> QTI
441 --> BYQ
442
443 --> PDR
444
445
446
447
448 --> RRM
449 --> CVZ --> THF --> TGF

450
451
452
453 --> TEJ --> UDJ
454
455 --> FXK
456 --> SOU
457 --> IXW
458
459 --> WDW --> WDY
460 --> ILG --> HKI
461
462 --> URH --> TQH
463 --> FTS
464 --> WQT
465 --> GWD
466 --> JLT
467
468 --> GGM --> GIO --> IGN --> HHN
469
470
471
472 --> WQB --> WRB
473 --> ITJ
474 --> JKA
475
476 --> NLN --> OLM --> OLO
477 --> PBF --> PCF
478
479 --> LTY
480 --> EGB
481
482 --> SMB --> PMA --> SMB
483
484 --> NGT
485 --> NZJ
486 --> CBT
487 --> QYZ --> PWX --> PWW
488 --> DFI --> TNN --> VMO
489 --> DPX
490
491
492
493
494 --> GFV --> IEU
495
496 --> ECM --> UKU

497 --> FRF

498

499

500 --> LII --> LII

501 --> EMK

502 --> IEA --> GFB

503

504

505 --> KVE --> KVD

506 --> ZJO --> ZJN

507 --> HNZ

508

509

510 --> OHB --> NGA --> OGB

511

RUN SUCCESSFUL (total time: 1s)

<Attachment - Problem 1 - Simulation 2>

23, 101, 294, 145, 81, 131, 362, 18, 227, 91, 78,
239, 227, 317, 36, 475, 269, 473, 121, 286, 42, 37,
246, 463, 313, 333, 495, 387, 173, 367, 224, 277, 88,
491, 209, 56, 255, 1, 21, 197, 239, 472, 406, 421,
364, 102, 341, 6, 430, 125, 240, 416, 228, 509, 18,
236, 320, 369, 306, 324, 119, 317, 376, 446, 158, 503,
82, 333, 344, 492, 404, 237, 475, 405, 159, 122, 15,
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2211001023
0021001300
4011041010
0201202302
0310042210
2032001303
1031030011
1001212020
0024020002
0021003040
0211300031
2012311210
0200222231
0210100110
3204110032
0150202204

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0 1 1 0 0 0 0 1 3 2
0 0 2 0 2 0 1 0 2 0
0 2 0 3 0 2 1 0 0 4
1 0 0 0 0 0 1 1 0 0
1 0

#of conflict=0 : 241, 47.0703 %
#of conflict=1 : 124, 24.2188 %
#of conflict=2 : 85, 16.6016 %
#of conflict=3 : 40, 7.8125 %
#of conflict=4 : 14, 2.73438 %
#of conflict=5 : 6, 1.17188 %
#of conflict=6 : 2, 0.390625 %
#of conflict=7 : 0, 0 %
#of conflict=8 : 0, 0 %
#of conflict=9 : 0, 0 %
#of conflict=10 : 0, 0 %
#of conflict=11 : 0, 0 %
#of conflict=12 : 0, 0 %
#of conflict=13 : 0, 0 %

0

1 --> KRL --> LQL --> KPK

2

3

4

5 --> AJY --> ALX --> CKZ

6

7

8

9 --> JNS --> JNR --> SUL --> QTJ --> SUK --> QVK

10 --> CXU --> CWU

11 --> NSF --> MQE

12 --> SFU

13

14

15 --> FLS

16 --> IAI --> GAG

17 --> RPR --> PRS --> QPR

18 --> BYB --> CWC --> AXA --> AWA --> VIG

19

20

21 --> BHK

22 --> TFO

23

24 --> FXM --> FWO

25 --> RMZ --> PMY

26 --> JBC

27
28 --> ZHC
29
30
31 --> VQK
32 --> OAN --> DVV
33 --> ZSY
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36 --> XEG
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40 --> LYV
41 --> YQF
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43 --> KJE
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46 --> QAH
47 --> CEQ --> BDS --> AES
48 --> LZC --> LWA
49 --> FHE
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55 --> ACW --> AAX
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57 --> TMQ --> EEJ
58 --> DVB
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63 --> HEX
64 --> SWG --> PZG
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70 --> TWT
71 --> IFD --> IED
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74 --> LTH
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77 --> LES
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79 --> MHD
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81 --> ACD --> JCX
82 --> LQN --> JSN
83
84 --> YYO --> WYM --> XWN --> YZN --> ZWN
85 --> SGS --> SHP
86
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90 --> RUO --> SUN
91 --> AWW
92
93 --> PFW
94 --> AKI
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96 --> VZB --> TWB
97 --> GAJ --> IBJ
98
99 --> CYD --> AWD --> AXE
100
101 --> SFD --> YHX --> XHY --> RFE
102 --> HOI
103 --> VEQ
104 --> FJA --> VTI
105 --> FYP
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107 --> LAF --> JCD
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110 --> IJM
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112 --> VQN
113 --> EUW --> OCS --> MBQ --> MCS --> FVX
114
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116 --> JOA
117 --> YFL
118 --> ONM --> ONM --> NMN --> MNO
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120

121 --> KWZ --> LZW
122
123
124 --> PQA
125
126 --> NLU
127
128
129 --> JWD --> KYF --> UAZ --> LYD --> LWD
130 --> FHG
131
132
133 --> APS --> CQP --> BSR
134
135 --> MZR --> NZS --> NWP
136 --> CFC --> AFB --> GGU
137
138
139
140 --> QKN
141
142
143 --> YAQ --> XBQ
144
145 --> QZJ
146 --> VNC
147
148
149
150 --> JHM
151 --> VXX --> UYW
152
153
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155 --> LVK
156 --> YLV
157 --> IRD
158 --> JFU
159
160
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162 --> BBG --> CBG
163 --> JRP --> JSS
164
165 --> XWS --> XYR --> XXP
166
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168
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171
172 --> VKG --> DBA --> EBC --> DAA
173 --> EOR --> ENP
174 --> SIB
175 --> ALJ
176
177
178 --> HAO --> HCO
179 --> PQZ --> SRZ
180 --> TGM --> UIO
181
182 --> YJA
183 --> INL --> GNJ
184 --> UEV --> TFU
185 --> DJD
186
187
188
189 --> KNW --> KOW --> JNY --> LNZ
190 --> YHG
191 --> ZUX --> ZTZ --> GKR --> HLS --> ZTW --> HKQ
192
193 --> TRR --> TQP
194 --> NCT
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196 --> HZM --> HXM
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198
199
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201 --> AHS
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203
204
205 --> JKL
206
207 --> MKZ --> OKW --> NLX
208 --> RCO --> SCO --> RCO --> PAN
209 --> BFW --> BEW --> CEZ
210
211 --> EHJ
212 --> EYC
213
214

215
216
217 --> GIY --> HIY
218
219 --> VNX
220
221 --> ZSK --> PKS
222
223
224 --> XBV
225 --> GGD --> IHF
226
227 --> VNE
228 --> JXH
229 --> WNP --> XMP
230 --> IVB --> GTA
231
232 --> YAA --> YBB
233 --> MKF
234
235
236 --> LVM
237
238
239 --> LDW
240
241
242
243 --> BBJ
244 --> JQV --> KQT --> SXM
245
246
247 --> SGZ --> RGY --> PHZ --> RGZ
248 --> AMI
249 --> MES --> NER
250 --> OUH
251
252
253
254 --> EMU
255 --> SIF
256 --> ISG
257
258 --> FOA
259
260
261 --> TGQ --> UHP --> THS

262
263 --> YLF --> WJF
264 --> GMN --> XXU --> GON
265 --> VFY --> TEZ --> VEX
266
267 --> EYZ
268
269 --> LAK
270 --> KQB
271 --> WGL
272 --> IJV --> HLV --> XZB
273
274
275 --> MCW
276 --> MSN --> ZVG --> NQM
277 --> HYQ --> GYS
278 --> JMI
279
280 --> NOT --> NNT
281
282 --> AGV
283 --> NCF --> OAD --> MAE
284
285
286 --> PRI
287 --> BVR
288
289 --> QBR
290
291
292 --> VQV --> URV
293 --> EWF --> DWD
294
295 --> AQY --> ARW --> CQY
296
297 --> WES --> ZDR --> ZFR --> OXZ --> NYX
298 --> HLB
299 --> VBK --> VBJ
300 --> EET --> URB
301 --> EVL --> DTL
302 --> YPN
303 --> HUW
304
305
306 --> GGI
307
308 --> VOH --> UMG

309 --> JWL --> FPP --> EQQ
310
311
312 --> LGV --> JHT
313 --> XCF
314
315
316 --> BFG
317 --> KUR --> KVS --> KUQ
318
319
320 --> RLV --> QLU --> JHA --> RJU
321
322 --> OIN
323 --> OYD
324
325 --> KRX --> KQZ --> RYQ --> RXP
326 --> DFC
327
328 --> PLC
329
330
331 --> MVJ --> MTL
332
333 --> SVZ
334 --> DBI --> TLN
335
336 --> YNC --> YMC
337 --> AKQ --> ALP --> AKP
338
339 --> DME --> UZK
340
341 --> SVF --> RVF --> RTE
342 --> TIU
343
344
345 --> GOR --> YYZ --> YWY --> XYY
346 --> KFH --> JDH
347 --> VUQ --> TUR
348 --> MDT
349
350 --> JCN --> LAO
351
352 --> ZIN --> WIO --> XHO
353 --> GJX --> XXD
354
355

356 --> NFB
357 --> OPP --> WVJ --> XTJ
358
359 --> KOL --> KOK --> KMJ
360 --> CWO
361
362 --> QDO --> RFN --> SEN
363 --> AIZ
364
365 --> EKJ --> DJK --> DKK
366
367
368 --> AVV
369 --> OOE
370 --> RBV
371
372
373 --> UPZ
374 --> FWI --> EXG
375 --> SNQ
376 --> HZV --> CTB
377
378 --> XEU --> WET
379
380
381
382 --> DVM --> ETM
383 --> YRR --> XQQ --> ZPQ --> ZSR
384
385 --> LKQ --> LLS
386
387
388
389 --> TMK --> TMK
390
391
392 --> HUG --> HVG
393 --> JGX
394
395
396 --> QAB --> QCC --> RCA
397
398 --> KVT --> KVV --> KTT --> KUT
399
400
401 --> LIE --> KGD
402 --> BSI

403 --> NIQ
404 --> MXI --> MWG --> OXG
405
406
407
408 --> EQT --> DRU --> FRV
409 --> QKE
410 --> COO --> ANO
411
412 --> XAI
413 --> GFP --> IDP
414 --> PXA --> SYA --> PYB
415 --> TKQ
416 --> ESB
417 --> QHL --> WOD
418 --> IPM
419
420
421 --> IBZ --> GAX
422
423
424 --> JVC --> JVB
425 --> ZKL --> ZKK
426 --> GNV --> IOV
427 --> LDL --> JEK
428 --> VVU --> VVT --> TVV
429 --> OFW
430
431 --> JBP --> KAR
432 --> JSI
433
434 --> XWI
435
436
437 --> ODF
438 --> NQU
439
440 --> LNM --> PTI --> JON
441 --> AZS --> AXS
442
443 --> PFP --> RDQ --> RES --> REQ
444 --> CKA
445 --> OAJ
446
447
448 --> RSN --> QQM --> RSM
449 --> VHD --> ATZ

450
451 --> RCX
452 --> BIH --> CHG --> CHI --> AGG --> IOC
453
454 --> DGT --> DIV
455
456 --> SOT --> PMV
457 --> BVD --> AVE
458
459 --> XFZ --> ZFZ --> WFY --> XEX
460 --> IJG --> XTM --> YVN
461
462 --> TPG --> TPG --> VRH
463
464
465 --> GZE
466 --> KLU
467 --> YEF --> ZFE --> YEF
468 --> NNH
469
470
471 --> JWR
472 --> XPA
473
474
475
476
477 --> QAE
478 --> BDM --> BFN --> CFN
479 --> JVV --> KTY
480
481
482 --> RNB --> SNB
483
484 --> MIV --> MGU
485
486 --> BBT
487
488 --> DDH --> UOM
489
490
491 --> BNP --> BOS
492
493 --> NTP --> YAK --> YCL
494
495 --> SWE --> PWE
496 --> DBM

497

498

499 --> ISR --> ISR --> GPQ --> HSR

500 --> LIG

501

502

503

504

505

506 --> ZKN

507 --> GOY

508

509

510 --> MHC

511

RUN SUCCESSFUL (total time: 1s)

<Attachment - Problem 1 - Simulation 3>

248, 187, 377, 444, 31, 230, 26, 72, 374, 499, 105,
198, 378, 463, 258, 300, 490, 361, 369, 421, 467, 39,
2, 419, 31, 198, 299, 48, 31, 492, 177, 359, 298,
37, 13, 0, 494, 484, 300, 24, 24, 382, 115, 255,
418, 412, 120, 46, 484, 400, 366, 59, 243, 447, 57,
195, 453, 505, 185, 15, 45, 338, 355, 152, 46, 12,
485, 429, 471, 225, 132, 390, 363, 116, 294, 312, 434,
319, 204, 158, 172, 462, 397, 389, 475, 378, 264, 253,
469, 298, 85, 339, 473, 116, 131, 288, 37, 396, 476,
111, 419, 2, 277, 9, 367, 464, 275, 167, 250, 27,
438, 238, 67, 218, 327, 288, 237, 62, 382, 237, 301,
126, 102, 106, 88, 354, 114, 478, 502, 217, 131, 114,
37, 95, 385, 472, 166, 99, 437, 240, 125, 172, 444,
23, 50, 378, 242, 338, 164, 402, 22, 107, 155, 355,
155, 276, 38, 187, 349, 269, 19, 47, 410, 460, 44,
433, 43, 450, 6, 496, 367, 492, 141, 383, 442, 482,
476, 273, 483, 309, 389, 193, 239, 246, 95, 31, 452,
506, 412, 281, 115, 273, 338, 204, 356, 402, 58, 368,
136, 380, 375, 352, 92, 183, 383, 340, 224, 351, 408,
403, 295, 219, 248, 224, 40, 20, 63, 282, 461, 407,
177, 160, 167, 261, 7, 415, 341, 406, 404, 275, 4,
468, 455, 69, 339, 330, 244, 175, 104, 319, 232, 197,
361, 62, 306, 344, 87, 313, 324, 505, 221, 400, 191,
503, 339, 42, 56, 375, 120, 350, 364, 137, 502, 176,
436, 428, 474, 59, 385, 19, 149, 84, 345, 318, 191,
341, 29, 317, 496, 411, 218, 257, 396, 123, 327, 50,
427, 327, 122, 317, 189, 327, 263, 186, 206, 293, 47,
271, 469, 458, 428, 37, 493, 511, 142, 248, 447, 376,
75, 1, 37, 432, 315, 398, 396, 265, 41, 359, 25,
500, 58, 10, 258, 442, 94, 356, 348, 380, 247, 322,
10, 392, 244, 352, 244, 115, 255, 468, 49, 195, 346,
160, 420, 184, 225, 25, 503, 367, 205, 243, 293, 188,
482, 366, 53, 445, 175, 247, 504, 63, 321, 415, 273,
38, 485, 237, 157, 481, 13, 63, 383, 119, 390, 228,
191, 462, 156, 132, 362, 506, 221, 144, 498, 399, 363,
379, 117, 215, 419, 104, 488, 319, 244, 103, 348, 285,
456, 201, 98, 508, 320, 276, 36, 104, 182, 75, 25,
146, 453, 173, 301, 418, 199, 124, 507, 198, 146, 214,
217, 22, 388, 3, 175, 106, 173, 431, 413, 362, 388,
101, 488, 484, 61, 282, 349, 424, 373, 318, 236, 475,
448, 499, 498, 438, 481, 510, 509, 416, 410, 316, 108,
421, 16, 394, 82, 460, 146, 300, 147, 492, 440, 330,
405, 32, 105, 68, 21, 66, 472, 288, 480, 84, 89,
109, 34, 61, 414, 79, 310, 111, 320, 385, 318, 192,
4, 505, 411, 214, 66, 440, 19, 335, 218, 45, 129,
507, 416, 190, 290, 410, 193, 407, 47, 352, 110, 467,

453, 299, 278, 33, 386, 130,

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2010332100
0100100103
1210121000
0321103222
0101210210
3022222000
1200300000
1012020300
3103112133
0200021010
0023010100
0133010223
3020111000
0301001202
2100030011
1022205110
2210000022
1011004000
1211300011
1012100020
1301221002
1220015100
1021002130
1020230410
1331013021
0220202000
1121211010
0002414100
0110110100
0023001400
0101200220
0012102020
2121121103
0001002010
0111002011
1011123520
3002121022
0102200100
1200201010
0420110401

1 2 0 1 1 1 0 0 1 0
0 1 2 0 0 0 0 1 1 2
0 0 3 1 1 1 1 3 1 2
1 5 0 1 1 1 2 2 2 2
0 2 1 0 1 0 2 2 2 0
0 0

#of conflict=0 : 220, 42.9688 %
#of conflict=1 : 143, 27.9297 %
#of conflict=2 : 98, 19.1406 %
#of conflict=3 : 36, 7.03125 %
#of conflict=4 : 10, 1.95312 %
#of conflict=5 : 5, 0.976562 %
#of conflict=6 : 0, 0 %
#of conflict=7 : 0, 0 %
#of conflict=8 : 0, 0 %
#of conflict=9 : 0, 0 %
#of conflict=10 : 0, 0 %
#of conflict=11 : 0, 0 %
#of conflict=12 : 0, 0 %
#of conflict=13 : 0, 0 %

0 --> KAT --> LBU --> AAA --> KAV

1

2

3 --> YYK --> YZK

4 --> PHN

5 --> CLZ --> BJZ --> ALY --> CLW

6

7

8

9

10 --> AWU --> BYV

11

12

13 --> BLF --> BJD --> BKD

14

15

16 --> IAH

17

18 --> TGH --> THI --> BYB

19

20

21 --> AGJ --> BGJ --> CGJ

22 --> UEO --> TEM --> UDM

23 --> VTE --> EGZ

24 --> FYM

25 --> RNX --> SNY

26 --> LAA

27
28 --> XHC
29 --> IKJ --> HLJ
30
31 --> VRK
32
33
34 --> HZH
35
36 --> XFG
37 --> IHP
38
39
40
41
42
43 --> KLF --> LJD
44 --> AUH --> BVH
45 --> NKS
46 --> PBG
47 --> AEP --> CES
48 --> LXA --> TCT --> JZA --> JWC --> VAV
49
50
51
52 --> CRO
53
54 --> NXO
55 --> CCY
56
57 --> VNQ --> FDK --> EDK --> UNS
58
59
60 --> CNU --> CNV
61
62 --> XAM
63
64 --> SYI --> PYI --> QXH
65 --> VLW --> FCS --> UJY
66 --> DPG --> FSH
67 --> WOK
68
69
70
71 --> HDF
72
73

74 --> KVG
75
76
77 --> KDQ
78
79 --> MGF --> NGD --> NGE
80 --> NUV
81 --> BCF --> JAW
82 --> JQO
83
84 --> ZYO
85 --> QGQ --> SIP
86 --> CNB
87
88
89
90
91 --> BYW --> BYW --> CWY
92 --> NQG --> NRH
93 --> SEX
94 --> ALG
95
96 --> DKU --> TZC --> TWC
97 --> HCK --> IAK
98 --> SRV --> RQV
99 --> CWD --> TIK
100
101 --> XHY
102
103 --> TDQ
104 --> TVG --> DLC
105 --> EZS
106
107 --> KCD --> LAD
108 --> KOT
109
110 --> XUW --> WTU --> IKM
111
112 --> UPM --> VRO
113 --> MAQ --> DTY
114 --> XTB --> WTC
115 --> GXJ --> IYL
116 --> KOB --> JOB
117
118
119
120 --> CHM

121 --> KXW --> LXW
122
123
124 --> LJH --> LJI --> KKI
125
126
127
128
129
130 --> DHG
131
132 --> PMG
133 --> BPQ --> ARR
134
135 --> MWQ --> MWQ
136
137 --> VBD --> UBD --> VAE
138
139
140 --> WSI --> RJN --> SLN
141 --> BMX
142
143 --> YCR --> ZAP --> YBR
144 --> HHB
145 --> QYK
146 --> VNA --> TNA
147 --> DQK
148 --> ZON --> YNN --> WMN
149 --> ISX --> HPW --> GSZ
150
151 --> VWX --> TYZ
152
153
154
155 --> LVL --> JVL
156 --> WJV
157
158 --> JFV
159
160
161
162 --> BCH --> CCG
163 --> LQQ --> LRR --> JRP
164
165 --> XXQ
166
167 --> AOD

168
169
170
171 --> SUP
172 --> TJI --> UJI --> UJH
173 --> NPJ --> DNQ --> OSL
174
175 --> CJK
176
177 --> FJX --> DKZ
178 --> IAN --> IAO
179 --> PQZ --> PQZ --> SPY
180 --> AZH --> UIO --> CXH
181
182 --> ZJC --> YLA
183
184 --> TDV
185 --> DKD
186 --> FXU
187
188
189
190
191 --> WTW --> XUW --> HJQ
192
193 --> TPP
194
195
196 --> GZO
197 --> JNF --> JNE
198
199 --> OOQ --> NOQ
200 --> SEI --> QEG
201 --> CGS
202
203
204
205 --> SSE --> KJJ --> RQD
206
207
208 --> PAM
209 --> CDW
210 --> UFC
211
212 --> EYC --> DWB
213 --> ROK --> POL
214 --> CPV --> BPV

215
216 --> WEM --> OYU --> MYU --> WFO --> OYV
217 --> BEF
218 --> UAG
219
220 --> EUI --> FTI
221 --> RJP --> SLR
222 --> GTT
223
224
225
226
227
228 --> LZG --> EPN
229 --> WMR --> WMS
230 --> HVC
231
232 --> WCB
233 --> MKE
234
235
236 --> JVN --> LTO --> LUO --> LVM
237
238
239
240 --> APC
241 --> NGK --> MGL
242 --> NYA
243 --> CAK
244 --> JRV --> QZM --> QXM
245
246
247
248 --> BNI
249 --> MDP
250 --> MTI
251
252 --> PUT
253 --> ULJ --> UJL
254 --> EOV
255
256
257
258 --> VWG --> TYG
259
260 --> STA
261 --> AXK --> BZL --> VIR

262
263 --> ZLD
264 --> HMN --> ZZT
265 --> UDZ --> KDF
266 --> TUN
267
268
269 --> JBL --> LAL
270 --> JQB
271 --> ZHJ --> ZGL
272 --> GJU --> YXA
273
274
275 --> MBZ
276 --> NPM --> ORM --> WVH --> XVG --> ORO
277 --> HWS
278
279
280 --> NNU
281
282 --> BGU --> CGU
283 --> NAE
284
285
286 --> QSI --> PRG
287 --> AVR
288 --> NMC --> MMA --> MMC
289
290 --> BGC
291
292 --> FHO --> EGN
293
294 --> SNM --> SNM
295 --> BQZ --> ARZ --> CRX
296
297 --> MWX --> WDP --> NXX --> MXW
298 --> IKA
299
300 --> UQA
301 --> FUK --> FTJ --> DVK
302 --> YPN --> ZPO --> WQO
303 --> GUZ
304
305 --> ZAY
306 --> HHH --> IGI --> GII
307
308 --> UNI --> UMG

309 --> EPS
310
311 --> ITE --> HVE
312 --> KGV --> KHU
313
314 --> NJH --> OKH
315
316 --> ADG --> BDH
317
318
319
320 --> SKU
321 --> BQF
322 --> NIN --> OIO
323 --> OYD
324 --> ABM --> BBN
325 --> JQZ
326 --> DDB
327
328 --> PJB
329
330
331
332
333 --> PTX --> SVZ
334 --> VLN --> UJO --> ECH --> DAG
335 --> FOW
336 --> QIG --> RHI --> RHH --> ZOC
337 --> BJS
338
339
340
341 --> SVD
342 --> VGU
343
344 --> ZJH
345 --> XZW
346
347 --> VVQ
348
349
350
351
352 --> XGO --> ZGO
353 --> XXF --> YZD --> WZD
354
355

356 --> MEB
357 --> WVK --> OQR --> NRR --> XVK
358
359
360
361 --> MMW
362
363 --> BHY
364 --> MAI --> MAH
365
366
367 --> PQJ --> RRK
368 --> TGC --> THB
369
370
371
372 --> UFH
373 --> FHR --> UQW
374 --> DWH
375
376 --> CTA --> GXV
377
378 --> ZDV --> XFU
379
380 --> VAO --> TAO
381 --> EFW
382 --> FTM --> DUO
383 --> XPR
384 --> IXB
385 --> JJS --> LKR
386 --> ZEA
387 --> IGL
388
389 --> UOL --> UOL --> VML
390
391
392
393 --> LGW
394
395
396 --> QAA --> QBA
397
398 --> LUT
399
400
401 --> QKZ
402 --> CPG

403 --> OIP
404
405
406 --> SZT --> RZT
407
408 --> EQT
409 --> RJF
410 --> BON
411
412 --> YCH
413 --> IFS
414 --> SZC
415 --> FCL --> VJQ
416 --> FRC --> ESA --> FRA
417 --> QGL --> RGJ --> PGK --> WOF --> WME
418 --> ISN --> GQM
419
420 --> UXM --> TZN --> DNG
421
422
423 --> TGX --> UHY
424 --> JVA
425 --> XJJ --> YLK
426 --> GNT
427
428 --> VUV --> UTV
429 --> MEY --> HCE
430
431 --> KBP
432
433 --> WGS --> WHP
434 --> ZWG --> XWH
435
436
437 --> OEE
438
439
440 --> KMM
441 --> CWQ --> AWQ
442
443
444 --> BJC --> BJC
445
446 --> DJO
447
448 --> RQO
449

450
451 --> RAW --> SAX --> SAZ --> SBW
452 --> HNA --> HOB
453
454 --> UTA
455 --> DZL
456
457 --> GWX --> HXZ --> BVE --> GXW
458
459 --> XDW
460 --> YUM
461 --> TBQ --> TAQ
462
463 --> DVR
464 --> ZQV
465 --> IZF
466
467
468 --> MMG
469
470
471 --> LWP
472 --> XPC --> WQA
473
474
475
476
477 --> PCD
478 --> ADO
479 --> KUY --> KTW
480
481
482 --> SOB --> POA --> SNC
483 --> APL
484 --> MGW
485 --> MXK
486 --> BCU
487 --> RXX --> RWX --> QYW
488 --> TNM
489 --> FQW --> FRZ
490 --> QKG
491 --> AOR --> AMP --> ANS --> AMQ --> COR
492
493 --> MVS
494 --> GFT
495 --> SYF
496 --> EAN --> VKV

497 --> FRD --> DSD
498 --> XNI --> WMH
499 --> GSP --> GPS
500
501 --> ENL --> TZS
502 --> GDA
503
504 --> TKB
505
506 --> ZLN --> XJO
507 --> HMY --> IMY
508 --> KEM --> KDO
509
510
511

RUN SUCCESSFUL (total time: 1s)