

Exercise 3 [20%]

11011 | 11001010111011000000

- Given $G(x) = x^4 + x^3 + x + 1$ generator polynomial
- Calculate the 4-bit CRC for the input 1100 1010 1110 1100
- The message above will degrade during the transmission.
- The receiver's data link layer will receive 1100 1010 1101 1010 0100.
- Is the error detectable by the generator polynomial? If not, why?

$$G(x) = x^4 + x^3 + x + 1 \quad L = 5$$

4-bit CRC is used $L - 1 = 4$

$$G(x) = 11011$$

$$M(x) = 11001010111011000000$$

Handwritten long division of 11011 into 11001010111011000000. The division shows a series of subtractions (XORs) where the divisor 11011 is shifted and subtracted from the dividend. The final remainder is 0100.

The remainder is 0100

Check if the received data's error is detectable by $g(x)$

$$\begin{array}{r}
 11011 \) \ 1100 \ 1010 \ 1101 \ 1010 \ 0100 \ 0000 \\
 \underline{11011} \\
 10010 \\
 \underline{11011} \\
 10011 \\
 \underline{11011} \\
 10001 \\
 \underline{11011} \\
 10100 \\
 \underline{11011} \\
 11111 \\
 \underline{11011} \\
 10010 \\
 \underline{11011} \\
 10011 \\
 \underline{11011} \\
 10000 \\
 \underline{11011} \\
 10110 \\
 \underline{11011} \\
 11011 \\
 \underline{11011} \\
 00000
 \end{array}$$

#ANS# The error is detectable by the polynomial.