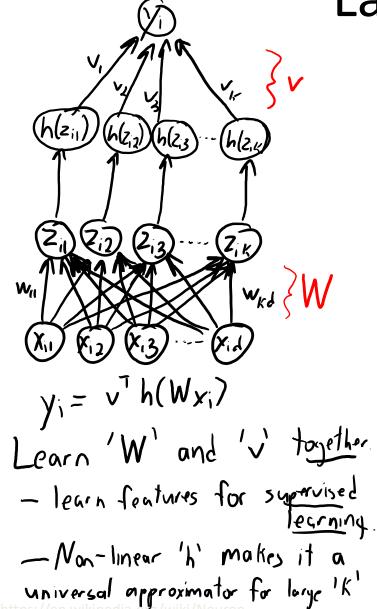
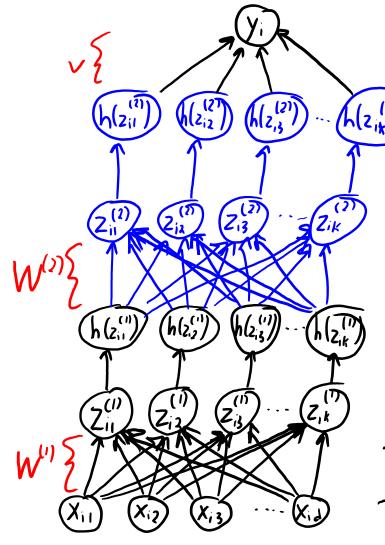
CPSC 340: Machine Learning and Data Mining

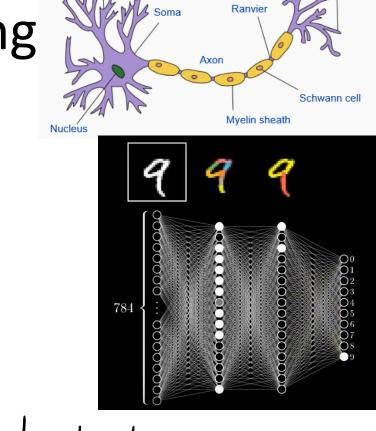
More Deep Learning Fall 2019

Neural network.

Last Time: Deep Learning





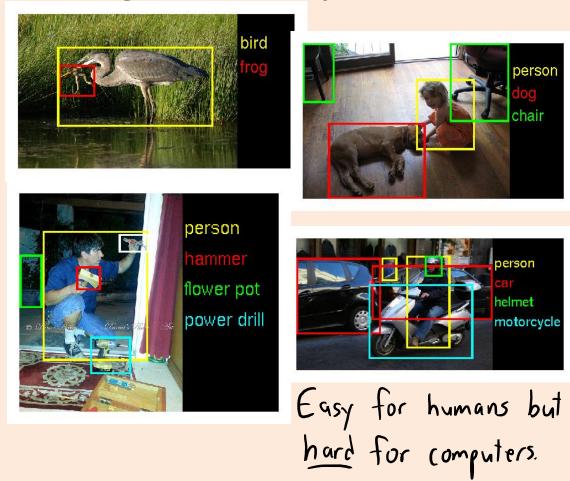


Deep neural networks: $y_i = \sqrt{h(W^{(2)}h(W^{(1)}x_i)}$

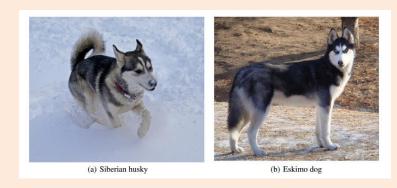
- Unprecedented performance on difficult problems.
- Each layer combines "parts" from previous layer

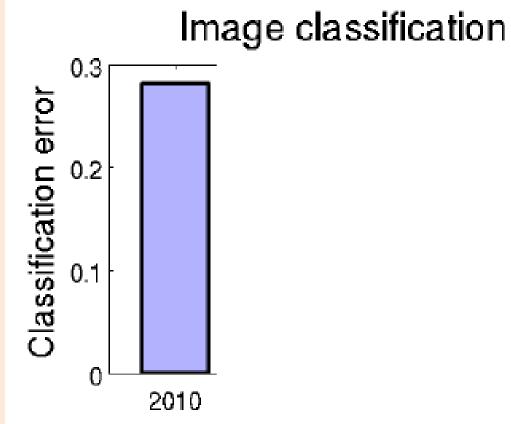
nttps://en.wikipedia.org/wiki/Neuron

Millions of labeled images, 1000 object classes.



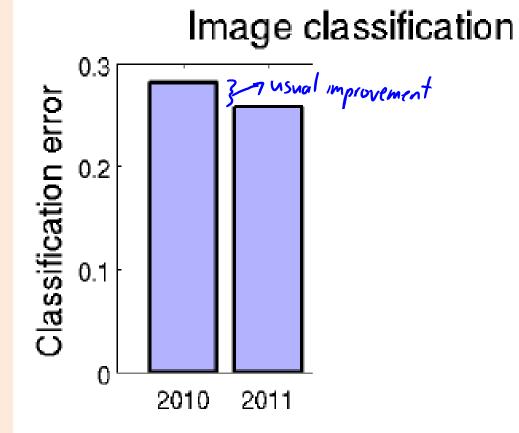
- Object detection task:
 - Single label per image.
 - Humans: ~5% error.





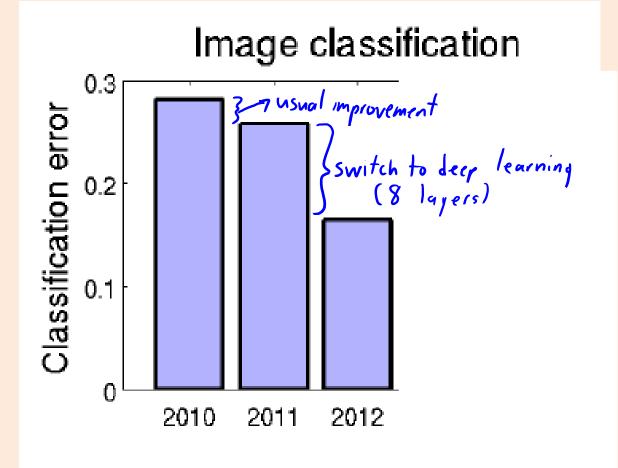
- Object detection task:
 - Single label per image.
 - Humans: ~5% error.





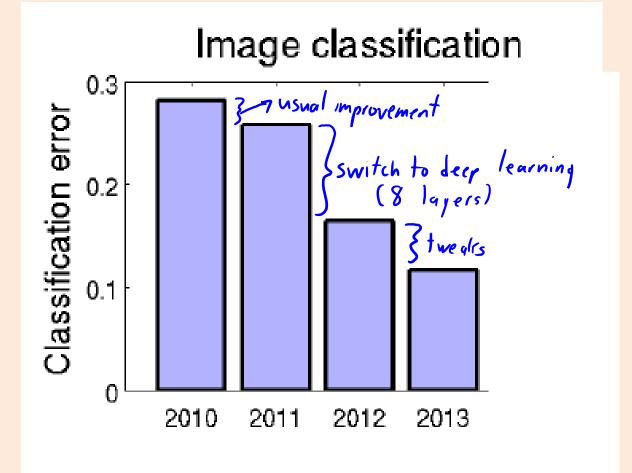
- Object detection task:
 - Single label per image.
 - Humans: ~5% error.





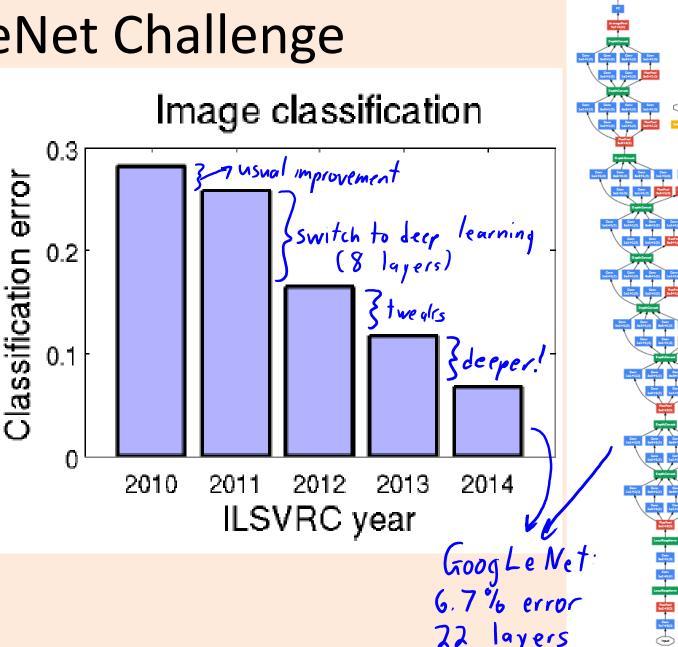
- Object detection task:
 - Single label per image.
 - Humans: ~5% error.



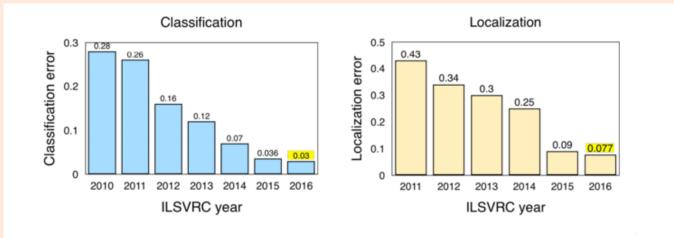


- Object detection task:
 - Single label per image.
 - Humans: ~5% error.





- Object detection task:
 - Single label per image.
 - Humans: ~5% error.
- 2015: Won by Microsoft Asia
 - 3.6% error.
 - 152 layers, "resnet" architecture.
 - Also won "localization" (finding location of objects in images).
- 2016: Chinese University of Hong Kong:
 - Ensembles of previous winners and other existing methods.
- 2017: fewer entries, organizers decided this would be last year.



(pause)

Deep Learning Practicalities

- This lecture focus on deep learning practical issues:
 - Backpropagation to compute gradients.
 - Stochastic gradient training.
 - Regularization to avoid overfitting.

- Next lecture:
 - Special 'W' restrictions to further avoid overfitting.

But first: Adding Bias Variables

Recall fitting line regression with a bias:

$$\hat{y}_i = \sum_{j=1}^d w_j x_{ij} + \beta$$

- We avoided this by adding a column of ones to X.
- In neural networks we often want a bias on the output:

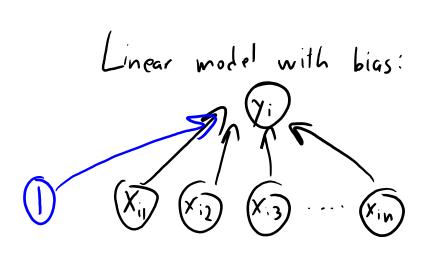
$$y_i = \sum_{i=1}^{k} v_c h(w_c^7 x_i) + \beta$$

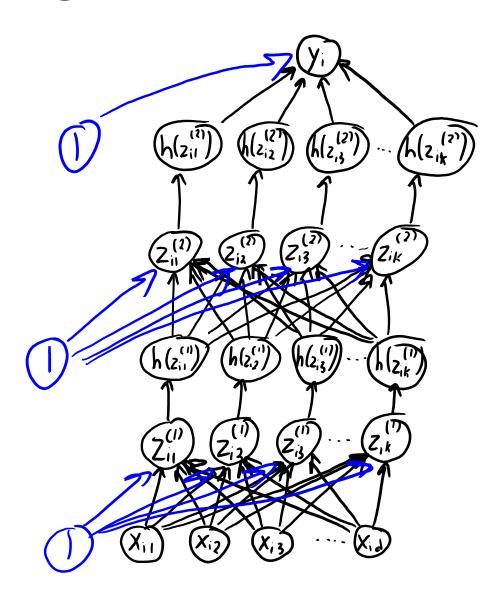
 $y_i = \sum_{c=1}^k v_c h(w_c^T x_i) + \beta$ • But we also often also include biases on each z_{ic} :

$$\hat{y}_i = \underbrace{\xi}_{c} v_c h(w_c x_i + \beta_c) + \beta$$

- A bias towards this $h(z_{ic})$ being either 0 or 1.
- Equivalent to adding to vector h(z_i) an extra value that is always 1.
 - For sigmoids, you could equivalently make one row of w_c be equal to 0.

But first: Adding Bias Variables





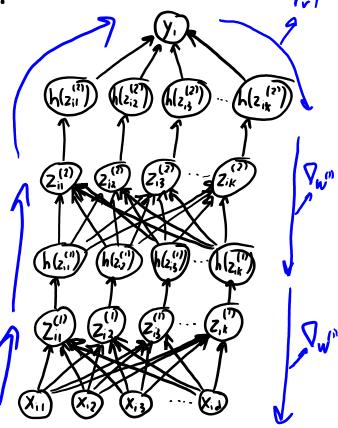
Artificial Neural Networks

With squared loss and 1 hidden layer, our objective function is:

$$f(u_{1}W) = \frac{1}{2} \sum_{i=1}^{n} (v_{1}h(Wx_{i}) - y_{i})^{2}$$

- Usual training procedure: stochastic gradient.
 - Compute gradient of random example 'i', update both 'v' and 'W'.
 - Highly non-convex and can be difficult to tune.
- Computing the gradient is known as "backpropagation".
 - Video giving motivation <u>here</u>.

- Overview of how we compute neural network gradient:
 - Forward propagation:
 - Compute $z_i^{(1)}$ from x_i .
 - Compute $z_i^{(2)}$ from $z_i^{(1)}$.
 - ...
 - Compute \hat{y}_i from $z_i^{(m)}$, and use this to compute error.
 - Backpropagation:
 - Compute gradient with respect to regression weights 'v'.
 - Compute gradient with respect to $z_i^{(m)}$ weights $W^{(m)}$.
 - Compute gradient with respect to $z_i^{(m-1)}$ weights $W^{(m-1)}$.
 - ...
 - Compute gradient with respect to $z_i^{(1)}$ weights $W^{(1)}$.
- "Backpropagation" is the chain rule plus some bookkeeping for speed.



- Let's illustrate backpropagation in a simple setting:
 - 1 training example, 3 hidden layers, 1 hidden "unit" in layer.

h (z,(31) $Z_i^{(3)}$ $h(z_i^{(2)})$ $h(z_i^{(1)})$

- Let's illustrate backpropagation in a simple setting:
 - 1 training example, 3 hidden layers, 1 hidden "unit" in layer.

$$f(W_{i}^{(i)},W_{i}^{(i)},W_{j}^{(i)},V) = \frac{1}{2} \left((y_{i}^{i} - y_{j}^{i})^{2} \right) wh_{tre} \qquad y_{i}^{i} = vh(w_{i}^{(i)}h(w_{i}^{(i)}x_{i}))$$

$$\frac{2f}{2v} = rh(W_{i}^{(i)}h(W_{i}^{(i)}h(W_{i}^{(i)}x_{i}))) = rh(z_{i}^{(3)})$$

$$\frac{2f}{2w_{i}^{(2)}} = rvh'(W_{i}^{(3)}h(W_{i}^{(2)}h(W_{i}^{(i)}x_{i}))) h(W_{i}^{(2)}h(W_{i}^{(i)}x_{i})) = rvh'(z_{i}^{(3)}) h(z_{i}^{(2)})$$

$$\frac{2f}{2w_{i}^{(2)}} = rvh'(W_{i}^{(3)}h(W_{i}^{(2)}h(W_{i}^{(i)}x_{i}))) h(W_{i}^{(2)}h(W_{i}^{(i)}x_{i})) h(W_{i}^{(2)}h(W_{i}^{(2)}x_{i})) h(W_{i}^{(2)}h(W_{i}^{(2)}x_{i})) h(Z_{i}^{(2)}) h(Z_{i}^{(2$$

- Let's illustrate backpropagation in a simple setting:
 - 1 training example, 3 hidden layers, 1 hidden "unit" in layer.

$$\frac{2f}{2v} = rh(z_{i}^{(3)})$$

$$\frac{2f}{2w^{(3)}} = rvh'(z_{i}^{(3)})h(z_{i}^{(2)})$$

$$\frac{2f}{2w^{(2)}} = r^{(3)}W^{(3)}h'(z_{i}^{(2)})h(z_{i}^{(0)})$$

$$\frac{2f}{2w^{(1)}} = r^{(2)}W^{(2)}h'(z_{i}^{(0)})x_{i}$$

$$\frac{2f}{2v_{c}} = \int h(z_{ic}^{(3)}) dz_{ic}^{(3)} dz_{ic}$$

- Only the first 'r' changes if you use a different loss.
- With multiple hidden units, you get extra sums.
 - Efficient if you store the sums rather than computing from scratch.

- I've marked those backprop math slides as bonus.
- Do you need to know how to do this?
 - Exact details are probably not vital (there are many implementations).
 - "Automatic differentiation" is becoming standard and has same cost.
 - But understanding basic idea helps you know what can go wrong.
 - Or give hints about what to do when you run out of memory.
 - See discussion <u>here</u> by a neural network expert.
- You should know cost of backpropagation:
 - Forward pass dominated by matrix multiplications by W⁽¹⁾, W⁽²⁾, W⁽³⁾, and 'v'.
 - If have 'm' layers and all z_i have 'k' elements, cost would be $O(dk + mk^2)$.
 - Backward pass has same cost as forward pass.
- For multi-class or multi-label classification, you replace 'v' by a matrix:
 - Softmax loss is often called "cross entropy" in neural network papers.

Deep Learning Vocabulary

- "Deep learning": Models with many hidden layers.
 - Usually neural networks.
- "Neuron": node in the neural network graph.
 - "Visible unit": feature.
 - "Hidden unit": latent factor z_{ic} or $h(z_{ic})$.
- "Activation function": non-linear transform.
- "Activation": h(z_i).
- "Backpropagation": compute gradient of neural network.
 - Sometimes "backpropagation" means "training with SGD".
- "Weight decay": L2-regularization.
- "Cross entropy": softmax loss.
- "Learning rate": SGD step-size.
- "Learning rate decay": using decreasing step-sizes.
- "Vanishing gradient": underflow/overflow during gradient calculation.

(pause)

ImageNet Challenge and Optimization

- ImageNet challenge:
 - Use millions of images to recognize 1000 objects.
- ImageNet organizer visited UBC summer 2015.
- "Besides huge dataset/model/cluster, what is the most important?"
 - 1. Image transformations (translation, rotation, scaling, lighting, etc.).
 - 2. Optimization.
- Why would optimization be so important?
 - Neural network objectives are highly non-convex (and worse with depth).
 - Optimization has huge influence on quality of model.

Stochastic Gradient Training

- Standard training method is stochastic gradient (SG):
 - Choose a random example 'i'.
 - Use backpropagation to get gradient with respect to all parameters.
 - Take a small step in the negative gradient direction.
- Challenging to make SG work:
 - Often doesn't work as a "black box" learning algorithm.
 - But people have developed a lot of tricks/modifications to make it work.
- Highly non-convex, so are the problem local mimina?
 - Some empirical/theoretical evidence that local minima are not the problem.
 - If the network is "deep" and "wide" enough, we think all local minima are good.
 - But it can be hard to get SG to close to a local minimum in reasonable time.

Parameter Initialization

- Parameter initialization is crucial:
 - Can't initialize weights in same layer to same value, or they will stay same.
 - Can't initialize weights too large, it will take too long to learn.
- A traditional random initialization:
 - Initialize bias variables to 0.
 - Sample from standard normal, divided by 10⁵ (0.00001*randn).
 - w = .00001*randn(k,1)
 - Performing multiple initializations does not seem to be important.
- Popular approach from 10 years ago:
 - Initialize with deep unsupervised model (like "autoencoders" see bonus).

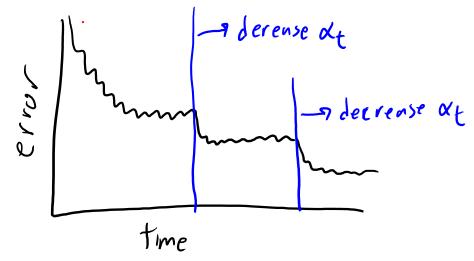
Parameter Initialization

- Parameter initialization is crucial:
 - Can't initialize weights in same layer to same value, or they will stay same.
 - Can't initialize weights too large, it will take too long to learn.
- Also common to transform data in various ways:
 - Subtract mean, divide by standard deviation, "whitten", standardize y_i.
- More recent initializations try to standardize initial z_i:
 - Use different initialization in each layer.
 - Try to make variance of z_i the same across layers.
 - Popular approach is to sample from standard normal, divide by sqrt(2*nInputs).
 - Use samples from uniform distribution on [-b,b], where

$$b = \frac{\sqrt{6}}{\sqrt{k^{(m)} + k^{(m)}}}$$

Setting the Step-Size

- Stochastic gradient is very sensitive to the step size in deep models.
- Common approach: manual "babysitting" of the step-size.
 - Run SG for a while with a fixed step-size.
 - Occasionally measure error and plot progress:



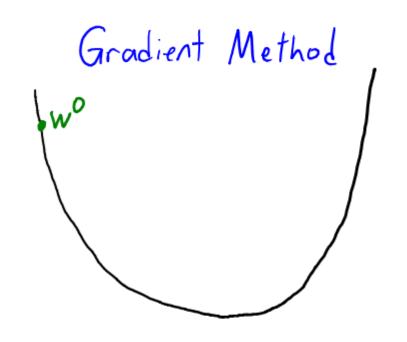
If error is not decreasing, decrease step-size.

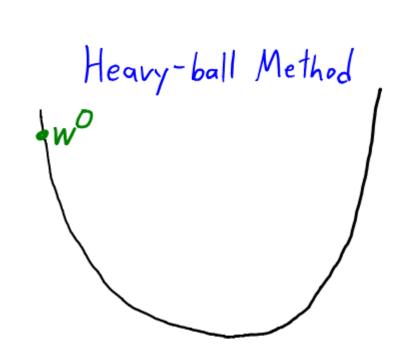
Setting the Step-Size

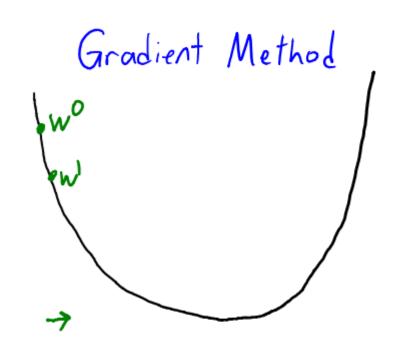
- Stochastic gradient is very sensitive to the step size in deep models.
- Bias step-size multiplier: use bigger step-size for the bias variables.
- Momentum (stochastic version of "heavy-ball" algorithm):
 - Add term that moves in previous direction:

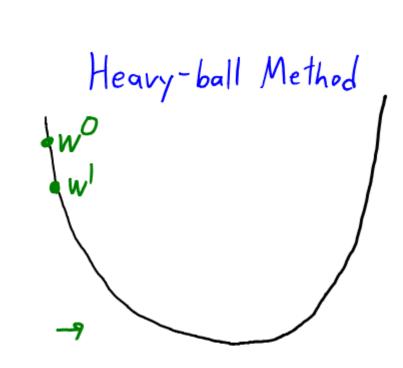
$$W^{t+1} = w^{t} - \alpha^{t} \nabla f_{i}(w^{t}) + \beta^{t}(w^{t} - w^{t-1})$$
skeep going in the old direction

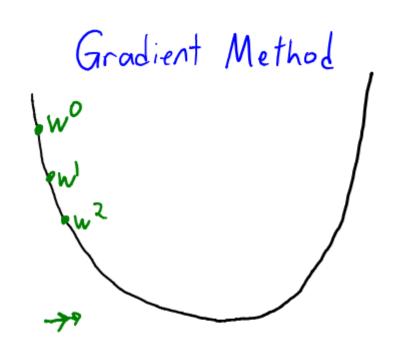
– Usually $\beta^t = 0.9$.

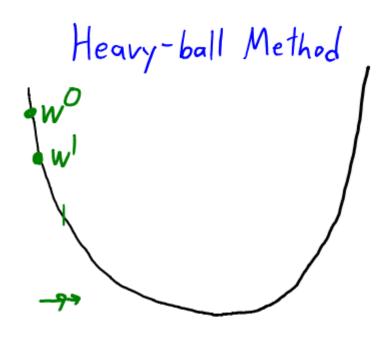


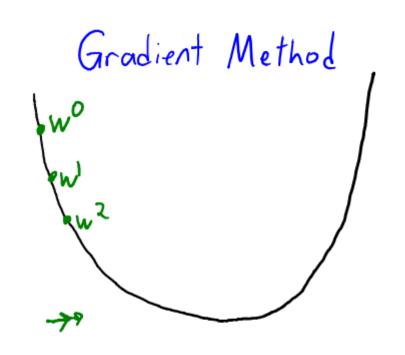


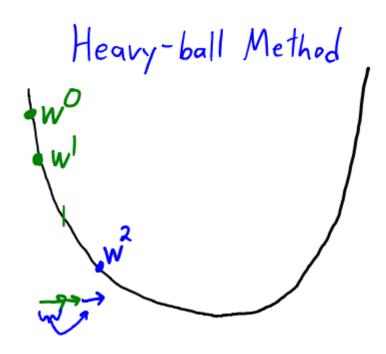


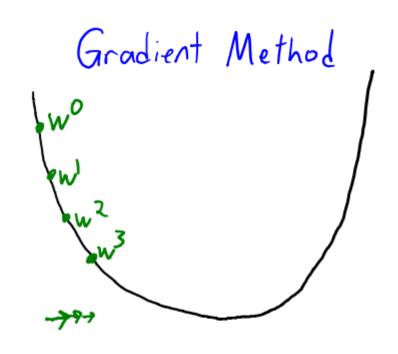


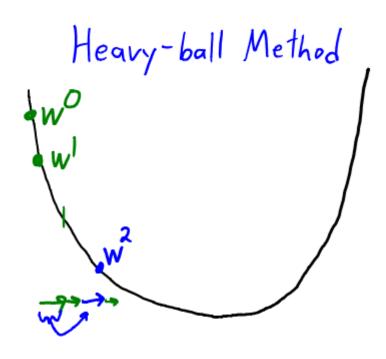


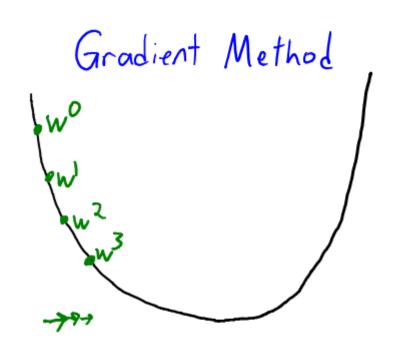


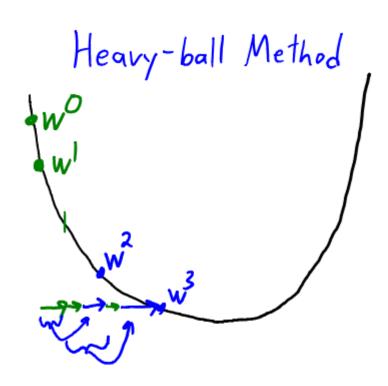


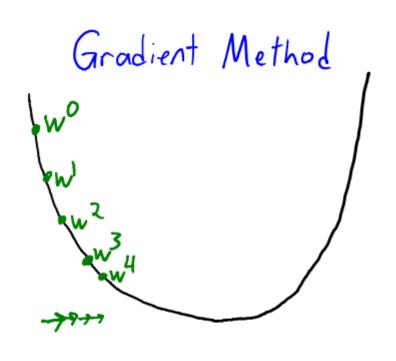


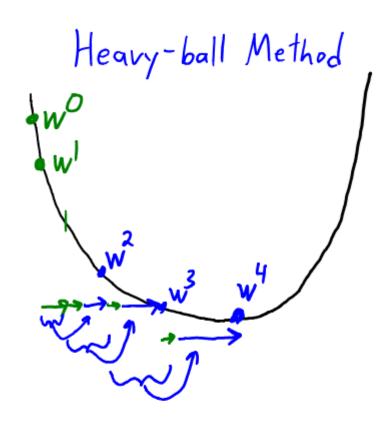


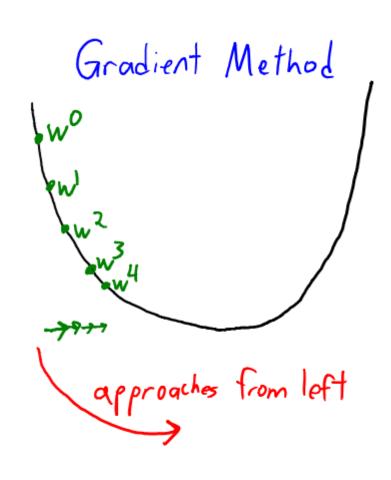


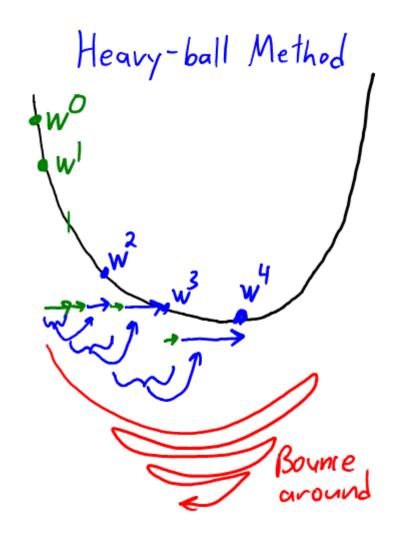












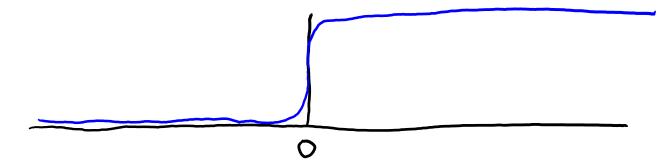
Setting the Step-Size

- Automatic method to set step size is Bottou trick:
 - 1. Grab a small set of training examples (maybe 5% of total).
 - 2. Do a binary search for a step size that works well on them.
 - 3. Use this step size for a long time (or slowly decrease it from there).
- Several recent methods using a step size for each variable:
 - AdaGrad, RMSprop, Adam (often work better "out of the box").
 - Seem to be losing popularity to stochastic gradient (often with momentum).
 - SGD often yields lower test error even though it takes longer and requires more tuning of step-size.
- Batch size (number of random examples) also influences results.
 - Bigger batch sizes often give faster convergence but maybe to worse solutions?
- Another recent trick is batch normalization:
 - Try to "standardize" the hidden units within the random samples as we go.
 - Held as example of deep learning "alchemy" (blog post here about deep learning claims).
 - Sounds science-ey and often works but little theoretical justification/understanding.

Vanishing Gradient Problem

Consider the sigmoid function:

- Away from the origin, the gradient is nearly zero.
- The problem gets worse when you take the sigmoid of a sigmoid:



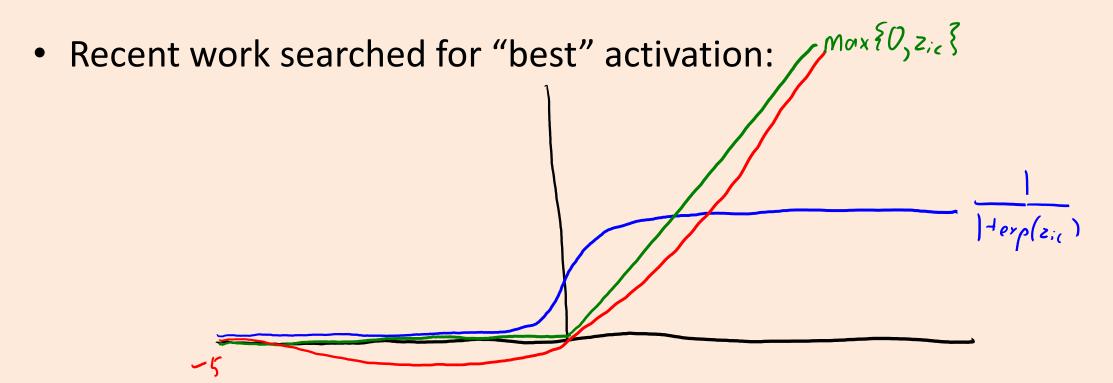
In deep networks, many gradients can be nearly zero everywhere.

Rectified Linear Units (ReLU)

• Replace sigmoid with perceptron loss (ReLU): Morx {0, z;c}

- Just sets negative values z_{ic} to zero.
 - Fixes vanishing gradient problem.
 - Gives sparser activations.
 - Not really simulating binary signal, but could be simulating "rate coding".

"Swish" Activiation



- Found that $z_{ic}/(1+exp(-z_{ic}))$ worked best ("swish" function).
 - A bit weird because it allows negative values and is non-monotonic.
 - But basically the same as ReLU when not close to 0.

"Residual" Networks (ResNets)

Impactful recent idea is residual networks (ResNets):

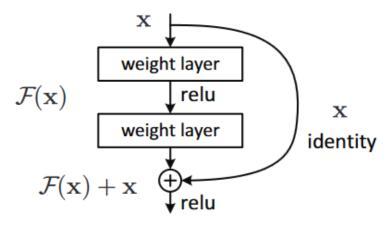


Figure 2. Residual learning: a building block.

- You can take previous (non-transformed) layer as input to current layer.
 - Also called "skip connections" or "highway networks".
- Non-linear part of the network only needs to model residuals.
 - Non-linear parts are just "pushing up or down" relevant parts of a linear model.
- This was a key idea behind first methods that used 100+ layers.
 - Evidence that biological networks have skip connections like this.

DenseNet

- More recent variation is "DenseNets":
 - Each layer can see all the values from many previous layers.
 - Gets rid of vanishing gradients.
 - May get same performance with fewer parameters.

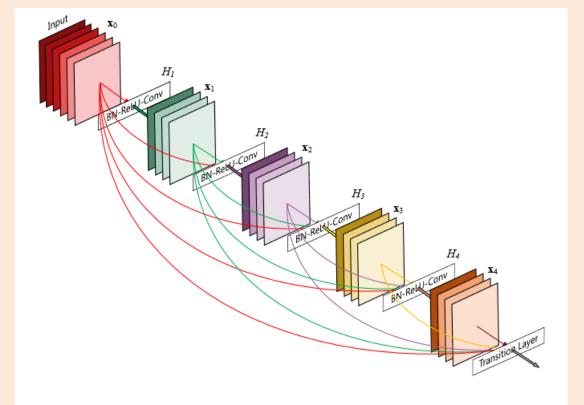


Figure 1: A 5-layer dense block with a growth rate of k=4. Each layer takes all preceding feature-maps as input.

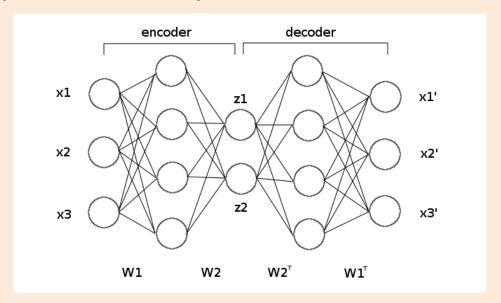
Summary

- Unprecedented performance on difficult pattern recognition tasks.
- Backpropagation computes neural network gradient via chain rule.
- Parameter initialization is crucial to neural net performance.
- Optimization and step size are crucial to neural net performance.
 - "Babysitting", momentum.
- ReLU and ResNets avoid "vanishing gradients".

- Next time:
 - Regularization, and getting these working for vision problems.

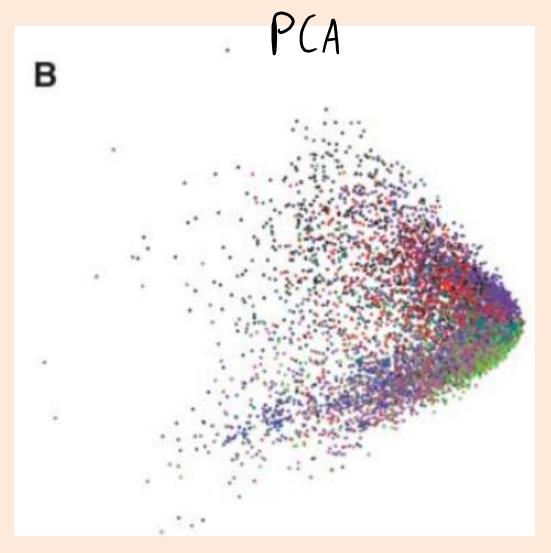
Autoencoders

- Autoencoders are an unsupervised deep learning model:
 - Use the inputs as the output of the neural network.

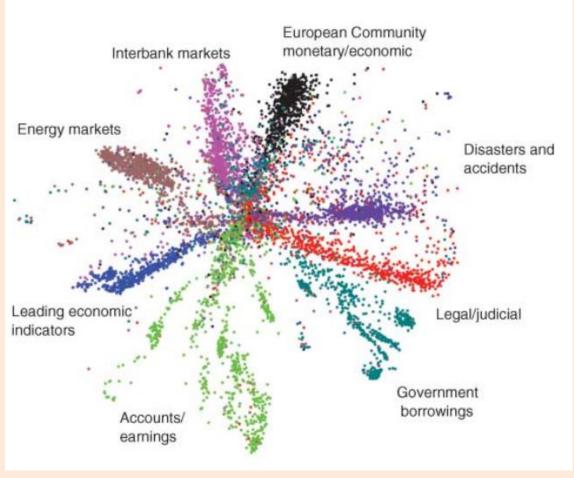


- Middle layer could be latent features in non-linear latent-factor model.
 - Can do outlier detection, data compression, visualization, etc.
- A non-linear generalization of PCA.
 - Equivalent to PCA if you don't have non-linearities.

Autoencoders

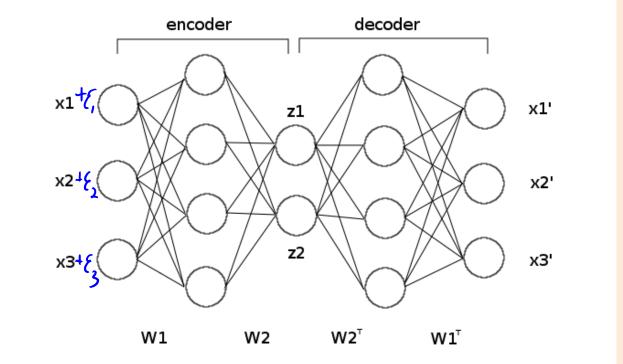






Denoising Autoencoder

Denoising autoencoders add noise to the input:



Learns a model that can remove the noise.