CPSC 340: Machine Learning and Data Mining

Feature Engineering Fall 2019

Admin

- Assignment 3: grades posted.
- Assignment 4: due Friday of next week.
- Midterm: grades soon.
 - Can view exam my office hours this week or the week after.
- Projects: may get contacted by TA if there are concerns.
- We got a complaint about people entering classroom too early.
 - Please wait until 1:50pm before entering classroom.

Last Time: Multi-Class Linear Classifiers

- We discussed multi-class linear classification: y_i in {1,2,...,k}.
- One vs. all with +1/-1 binary classifier:
 - Train weights w_c to predict +1 for class 'c', -1 otherwise.

$$W = \begin{bmatrix} \begin{bmatrix} v_1^T \\ v_2 \end{bmatrix} \\ k \end{bmatrix}$$

- Predict by taking 'c' maximizing w_c^Tx_i.
- Multi-class SVMs:

- Trains the
$$w_c$$
 jointly to encourage maximum $w_c^T x_i$ to be correct $w_{y_i}^T x_i$.
$$\{ (w_{ij} w_{jj}, w_{jk}) = \sum_{i=1}^{n} \max_{k} \{0, 1 - w_{y_i}^T x_i + w_c^T x_i\} + \frac{1}{2} \sum_{k=1}^{k} \|w_k\|^2$$

Multi-Class Logistic Regression

- We derived binary logistic loss by smoothing a degenerate 'max'.
 - A degenerate constraint in the multi-class case can be written as:

$$W_{y_i}^{T}x_i \geqslant \max_{c} w_{c}^{T}x_i$$

or $0 \geqslant -W_{y_i}^{T}x_i + \max_{c} \{w_{c}^{T}x_i\}$

- We want the right side to be as small as possible.
- Let's smooth the max with the log-sum-exp:

$$-W_{y_i}^{7}x_i + \log(\xi \exp(w_c^{7}x_i))$$

- This is no longer degenerate: with W=0 this gives a loss of log(k).
- Called the softmax loss, the loss for multi-class logistic regression.

Multi-Class Logistic Regression

We sum the loss over examples and add regularization:

f(W) =
$$\sum_{i=1}^{K} - w_{y_i} x_i + \log(\sum_{i=1}^{K} \exp(w_{i} x_i))) + \frac{1}{2} \sum_{i=1}^{K} \frac{1}{2} w_{i}$$

Tries to

Approximates max $\{w_{i} x_{i}\}$

Whake $w_{i} x_{i}$ big for so tries to make $w_{i} x_{i}$ small on elements of 'w' the correct label for all labels.

- This objective is convex (should be clear for 1st and 3rd terms).
 - It's differentiable so you can use gradient descent.
- When k=2, equivalent to using binary logistic loss.
 - Not obvious at the moment.

Multi-Class Linear Prediction in Matrix Notation

In multi-class linear classifiers our weights are:

$$W = \begin{bmatrix} \begin{bmatrix} v_1 \\ v_2 \end{bmatrix} \\ k \end{bmatrix}$$

- To predict on all training examples, we first compute all $w_c^T x_i$.

So predictions are maximum column indices of XW^T (which is 'n' by 'k').

Digression: Frobenius Norm

• The Frobenius norm of a ('k' by 'd') matrix 'W' is defined by:

We can use this to write regularizer in matrix notation:

$$\frac{1}{3} \sum_{c=1}^{k} \sum_{j=1}^{k} w_{cj}^{2} = \frac{1}{3} \sum_{c=1}^{k} ||w_{c}||^{2} \quad ("L_{2} \text{ regularizer on each vector"})$$

$$= \frac{2}{3} ||W||_{F}^{2} \quad ("\text{Frobenius-regularizer on matrix"})$$

(pause)

Feature Engineering

- "...some machine learning projects succeed and some fail. What makes the difference? Easily the most important factor is the features used."
 - Pedro Domingos

- "Coming up with features is difficult, time-consuming, requires expert knowledge. "Applied machine learning" is basically feature engineering."
 - Andrew Ng

Feature Engineering

Better features usually help more than a better model.

- Good features would ideally:
 - Capture most important aspects of problem.
 - Reflects invariances (generalize to new scenarios).
 - Allow learning with few examples, be hard to overfit with many examples.

- There is a trade-off between simple and expressive features:
 - With simple features overfitting risk is low, but accuracy might be low.
 - With complicated features accuracy can be high, but so is overfitting risk.

Feature Engineering

The best features may be dependent on the model you use.

- For counting-based methods like naïve Bayes and decision trees:
 - Need to address coupon collecting, but separate relevant "groups".

- For distance-based methods like KNN:
 - Want different class labels to be "far".

- For regression-based methods like linear regression:
 - Want labels to have a linear dependency on features.

Discretization for Counting-Based Methods

- For counting-based methods:
 - Discretization: turn continuous into discrete.

| Age | | < 20 | >= 20, < 25 | >= 25 |
|-----|----------|------|-------------|-------|
| 23 | | 0 | 1 | 0 |
| 23 | → | 0 | 1 | 0 |
| 22 | | 0 | 1 | 0 |
| 25 | | 0 | 0 | 1 |
| 19 | | 1 | 0 | 0 |
| 22 | | 0 | 1 | 0 |

- Counting age "groups" could let us learn more quickly than exact ages.
 - But we wouldn't do this for a distance-based method.

Standardization for Distance-Based Methods

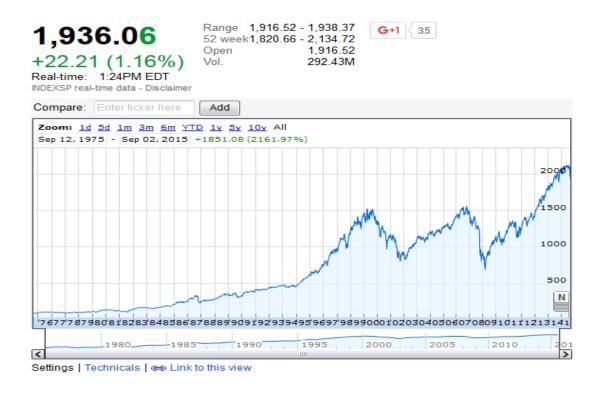
Consider features with different scales:

| Egg (#) | Milk (mL) | Fish (g) | Pasta (cups) |
|---------|-----------|----------|-----------------|
| 0 | 250 | 0 | 1 |
| 1 | 250 | 200 | 1 |
| 0 | 0 | 0 | 0.5 |
| 2 | 250 | 150 | 0 |

- Should we convert to some standard 'unit'?
 - It doesn't matter for counting-based methods.
- It matters for distance-based methods:
 - KNN will focus on large values more than small values.
 - Often we "standardize" scales of different variables (e.g., convert everything to grams).

Non-Linear Transformations for Regression-Based

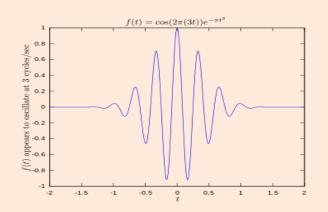
- Non-linear feature/label transforms can make things more linear:
 - Polynomial, exponential/logarithm, sines/cosines, RBFs.

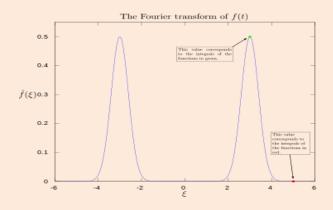


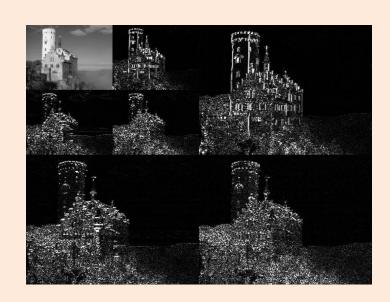


Domain-Specific Transformations

- In some domains there are natural transformations to do:
 - Fourier coefficients and spectrograms (sound data).
 - Wavelets (image data).
 - Convolutions (we'll talk about these soon).







https://en.wikipedia.org/wiki/Fourier_transform

https://en.wikipedia.org/wiki/Spectrogram

https://en.wikipedia.org/wiki/Discrete_wavelet_transform

Discussion of Feature Engineering

- The best feature transformations are application-dependent.
 - It's hard to give general advice.

- My advice: ask the domain experts.
 - Often have idea of right discretization/standardization/transformation.
- If no domain expert, cross-validation will help.
 - Or if you have lots of data, use deep learning methods from Part 5.
- Next: I'll give some features used for text/image applications.

(pause)

Text Example 1: Language Identification

Consider data that doesn't look like this:

$$X = \begin{bmatrix} 0.5377 & 0.3188 & 3.5784 \\ 1.8339 & -1.3077 & 2.7694 \\ -2.2588 & -0.4336 & -1.3499 \\ 0.8622 & 0.3426 & 3.0349 \end{bmatrix}, \quad y = \begin{bmatrix} +1 \\ -1 \\ -1 \\ +1 \end{bmatrix},$$

But instead looks like this:

$$X = \begin{bmatrix} \text{Do you want to go for a drink sometime?} \\ \text{J'achète du pain tous les jours.} \\ \text{Fais ce que tu veux.} \\ \text{There are inner products between sentences?} \end{bmatrix}, y = \begin{bmatrix} +1 \\ -1 \\ -1 \\ +1 \end{bmatrix}.$$

How should we represent sentences using features?

A (Bad) Universal Representation

- Treat character in position 'j' of the sentence as a categorical feature.
 - "fais ce que tu veux" => x_i = [f a i s " c e " q u e " t u " v e u x .]
- "Pad" end of the sentence up to maximum #characters:
 - "fais ce que tu veux" => x_i = [fais "ce" que"tu" veux.γγγγγγγ...]
- Advantage:
 - No information is lost, KNN can eventually solve the problem.
- Disadvantage: throws out everything we know about language.
 - Needs to learn that "veux" starting from any position indicates "French".
 - Doesn't even use that sentences are made of words (this must be learned).
 - High overfitting risk, you will need a lot of examples for this easy task.

Bag of Words Representation

Bag of words represents sentences/documents by word counts:

The **International Conference on Machine Learning** (ICML) is the leading international <u>academic conference</u> in <u>machine learning</u>

| ICML | International | Conference | Machine | Learning | Leading | Academic |
|------|---------------|------------|---------|----------|---------|----------|
| 1 | 2 | 2 | 2 | 2 | 1 | 1 |

- Bag of words loses a ton of information/meaning:
 - But it easily solves language identification problem

Universal Representation vs. Bag of Words

Why is bag of words better than "string of characters" here?

- It needs less data because it captures invariances for the task:
 - Most features give strong indication of one language or the other.
 - It doesn't matter where the French words appear.
- It overfits less because it throws away irrelevant information.
 - Exact sequence of words isn't particularly relevant here.

Text Example 2: Word Sense Disambiguation

- Consider the following two sentences:
 - "The cat ran after the mouse."
 - "Move the mouse cursor to the File menu."
- Word sense disambiguation (WSD): classify "meaning" of a word:
 - A surprisingly difficult task.
- You can do ok with bag of words, but it will have problems:
 - "Her mouse clicked on one cat video after another."
 - "We saw the mouse run out from behind the computer."
 - "The mouse was gray." (ambiguous without more context)

Bigrams and Trigrams

- A bigram is an ordered set of two words:
 - Like "computer mouse" or "mouse ran".
- A trigram is an ordered set of three words:
 - Like "cat and mouse" or "clicked mouse on".

- These give more context/meaning than bag of words:
 - Includes neighbouring words as well as order of words.
 - Trigrams are widely-used for various language tasks.
- General case is called n-gram.
 - Unfortunately, coupon collecting becomes a problem with larger 'n'.

Text Example 3: Part of Speech (POS) Tagging

- Consider problem of finding the verb in a sentence:
 - "The 340 students jumped at the chance to hear about POS features."

- Part of speech (POS) tagging is the problem of labeling all words.
 - ->40 common syntactic POS tags.
 - Current systems have ~97% accuracy on standard ("clean") test sets.
 - You can achieve this by applying a "word-level" classifier to each word.
 - That independently classifies each word with one of the 40 tags.
- What features of a word should we use for POS tagging?

But first...

- How do we use categorical features in regression?
- Standard approach is to convert to a set of binary features:

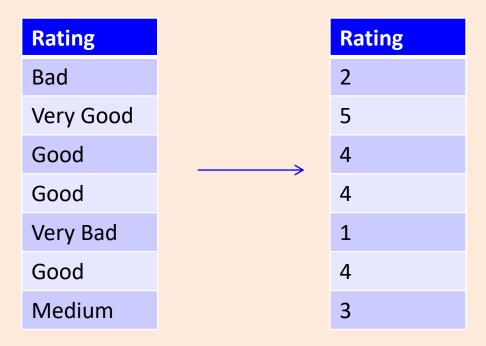
| Age | City | Income | Age | Van | Bur | Sur | Income |
|-----|------|-----------|--------|-----|-----|-----|-----------|
| 23 | Van | 22,000.00 | 23 | 1 | 0 | 0 | 22,000.0 |
| 23 | Bur | 21,000.00 | 23 | 0 | 1 | 0 | 21,000.00 |
| 22 | Van | 0.00 | 22 | 1 | 0 | 0 | 0.00 |
| 25 | Sur | 57,000.00 | 25 | 0 | 0 | 1 | 57,000.00 |
| 19 | Bur | 13,500.00 | 19 | 0 | 1 | 0 | 13,500.00 |
| 22 | Van | 20,000.00 | 22 | 1 | 0 | 0 | 20,000.00 |

POS Features

- Regularized multi-class logistic regression with these 19 features gives ~97% accuracy:
 - Categorical features whose domain is all words ("lexical" features):
 - The word (e.g., "jumped" is usually a verb).
 - The previous word (e.g., "he" hit vs. "a" hit).
 - The previous previous word.
 - The next word.
 - The next next word.
 - Categorical features whose domain is combinations of letters ("stem" features):
 - Prefix of length 1 ("what letter does the word start with?")
 - Prefix of length 2.
 - Prefix of length 3.
 - Prefix of length 4 ("does it start with JUMP?")
 - Suffix of length 1.
 - Suffix of length 2.
 - Suffix of length 3 ("does it end in ING?")
 - Suffix of length 4.
 - Binary features ("shape" features):
 - Does word contain a number?
 - Does word contain a capital?
 - Does word contain a hyphen?

Ordinal Features

Categorical features with an ordering are called ordinal features.



- If using decision trees, makes sense to replace with numbers.
 - Captures ordering between the ratings.
 - A rule like (rating ≥ 3) means (rating ≥ Good), which make sense.

Ordinal Features

- With linear models, "convert to number" assumes ratings are equally spaced.
 - "Bad" and "Medium" distance is similar to "Good" and "Very Good" distance.
- One alternative that preserves ordering with binary features:

| Rating | | ≥ Bad | ≥ Medium | ≥ Good | Very Goo |
|-----------|-------------|-------|----------|--------|----------|
| Bad | | 1 | 0 | 0 | 0 |
| Very Good | | 1 | 1 | 1 | 1 |
| Good | | 1 | 1 | 1 | 0 |
| Good | | 1 | 1 | 1 | 0 |
| Very Bad | | 0 | 0 | 0 | 0 |
| Good | | 1 | 1 | 1 | 0 |
| Medium | | 1 | 1 | 0 | 0 |

- Regression weight w_{medium} represents:
 - "How much medium changes prediction over bad".

(pause)

Motivation: Identifying Important E-mails

Recall that we discussed identifying 'important' e-mails.



- We have a big collection of e-mails:
 - Mark as 'important' if user takes some action based on them.

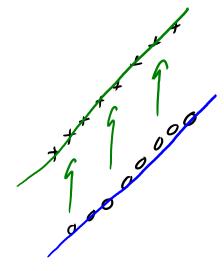
Feature Representation for E-mails

- How do we make label 'y_i' of an individual e-mail?
 - $-(y_i = 1)$ means "important", $(y_i = -1)$ means "not important".
- How do we construct features 'x_i' for an e-mail?
 - Use bag of words:
 - "hello", "vicodin", "\$".
 - Could add trigrams or phrases:
 - "be your own boss", "you're a winner", "MDS 573".
 - Could add regular expressions:
 - <recipient>, <sender domain == "mail.com">

Digression: Linear Models with Binary Features

- What is the effect of a binary features on linear regression?
- Suppose we use a bag of words:
 - With 3 words {"hello", "Vicodin", "340"} our model would be:

- If e-mail only has "hello" and "340" our prediction is:



- So having the binary feature 'j' increases \hat{y}_i by the fixed amount w_i .
 - Predictions are a bit like naïve Bayes where we combine features independently.
 - But now we're learning all w_i together so this tends to work better.

Motivation: "Personalized" Important E-mails



- There might be some "globally" important messages:
 - "This is your mother, something terrible happened, give me a call ASAP."
- But your "important" message may be unimportant to others.
 - Similar for spam: "spam" for one user could be "not spam" for another.

"Global" and "Local" Features

Consider the following weird feature transformation:

| "340" | | "340" (any user) | "340" (user?) |
|-------|----------|------------------|--------------------|
| 1 | | 1 | User 1 |
| 1 | <u> </u> | 1 | User 1 |
| 1 | | 1 | User 2 |
| 0 | | 0 | <no "340"=""></no> |
| 1 | | 1 | User 3 |

- First feature: did "340" appear in this e-mail?
- Second feature: if "340" appeared in this e-mail, who was it addressed to?
- First feature will increase/decrease importance of "340" for every user (including new users).
- Second (categorical feature) increases/decreases important of "340" for specific users.
 - Lets us learn more about specific users where we have a lot of data

"Global" and "Local" Features

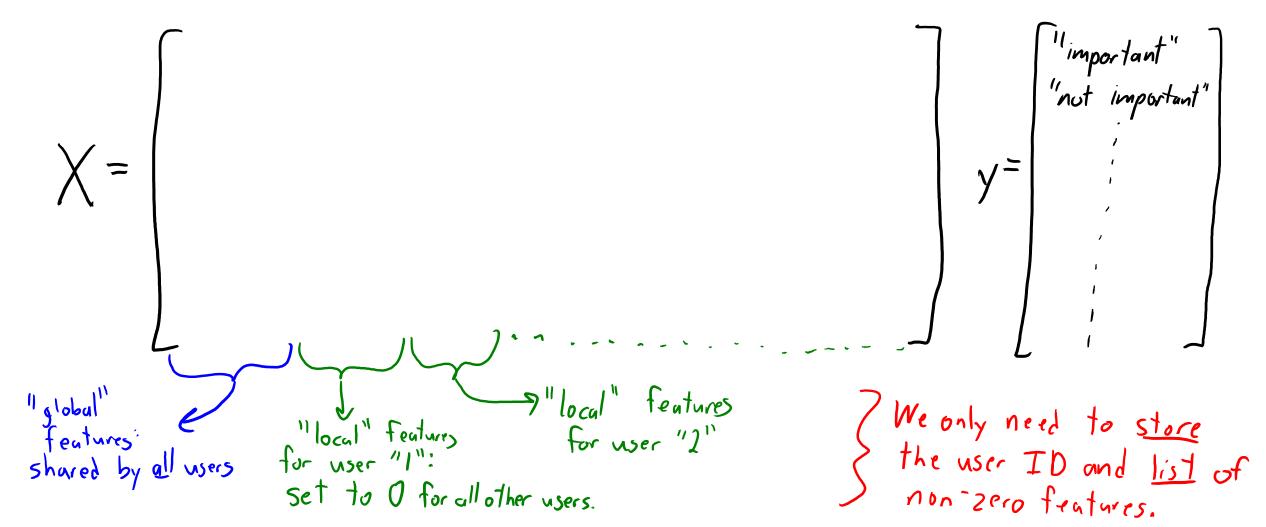
Recall we usually represent categorical features using "1 of k" binaries:

| "340" | "340" (any user) | "340" (user = 1) | "340" (user = 2) |
|-------|------------------|------------------|------------------|
| 1 | 1 | 1 | 0 |
| 1 | 1 | 1 | 0 |
| 1 | 1 | 0 | 1 |
| 0 | 0 | 0 | 0 |
| 1 | 1 | 0 | 0 |

- First feature "moves the line up" for all users.
- Second feature "moves the line up" when the e-mail is to user 1.
- Third feature "moves the line up" when the e-mail is to user 2.

The Big Global/Local Feature Table for E-mails

• Each row is one e-mail (there are lots of rows):



Predicting Importance of E-mail For New User

- Consider a new user:
 - We start out with no information about them.
 - So we use global features to predict what is important to a generic user.

$$\hat{y}_i = Sign(w_g^T x_{ig})$$
 $= features/weights shared across users.$

- Local features are initialized to zero.
- With more data, update global features and user's local features:
 - Local features make prediction personalized.

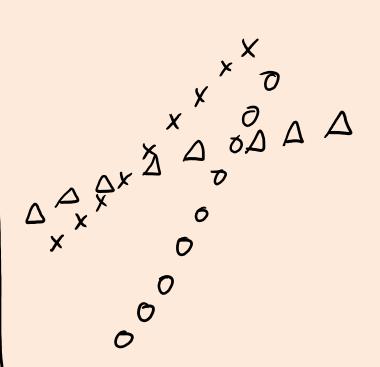
- What is important to this user?
- G-mail system: classification with logistic regression.
 - Trained with a variant of stochastic gradient descent (later).

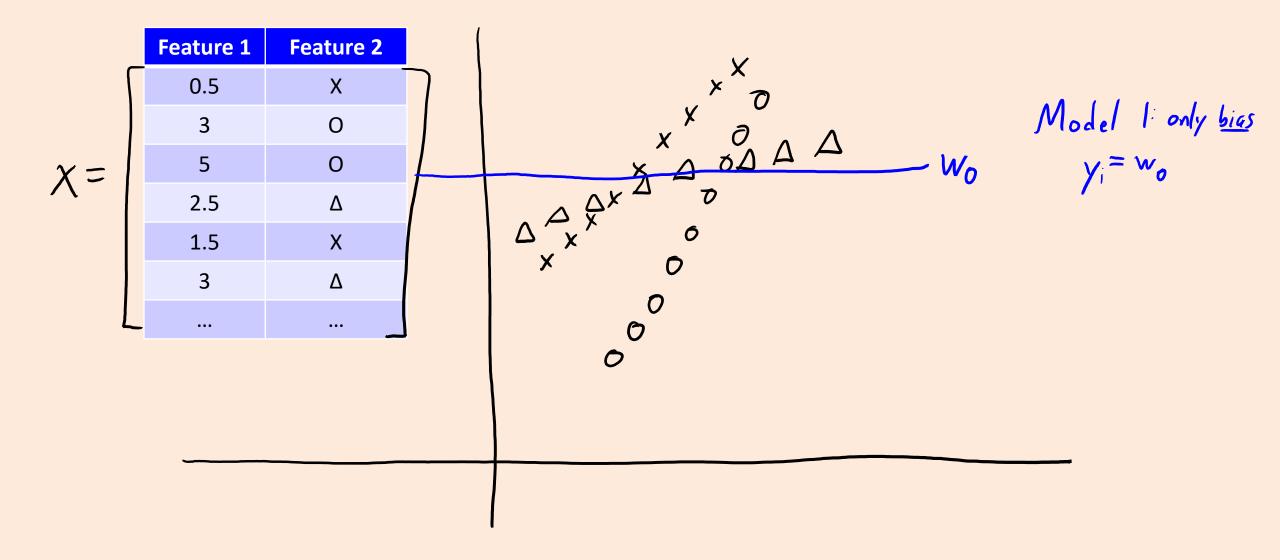
Summary

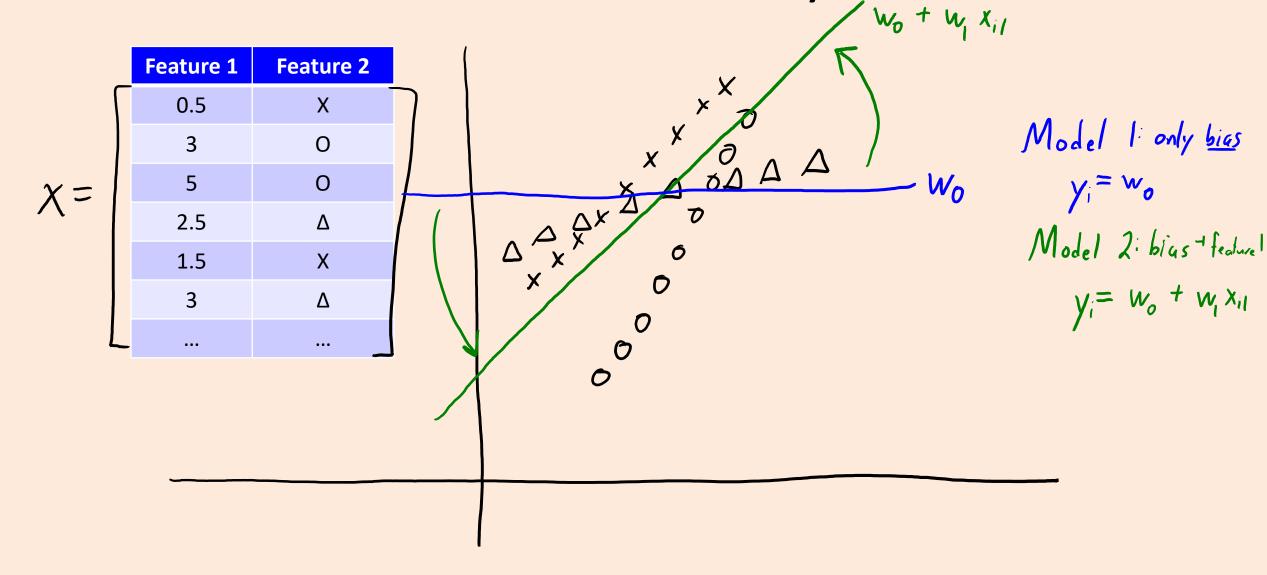
- Softmax loss is a multi-class version of logistic loss.
- Feature engineering can be a key factor affecting performance.
 - Good features depend on the task and the model.
- Bag of words: not a good representation in general.
 - But good features if word order isn't needed to solve problem.
- Text features (beyond bag of words): trigrams, lexical, stem, shape.
 - Try to capture important invariances in text data.
- Global vs. local features allow "personalized" predictions.

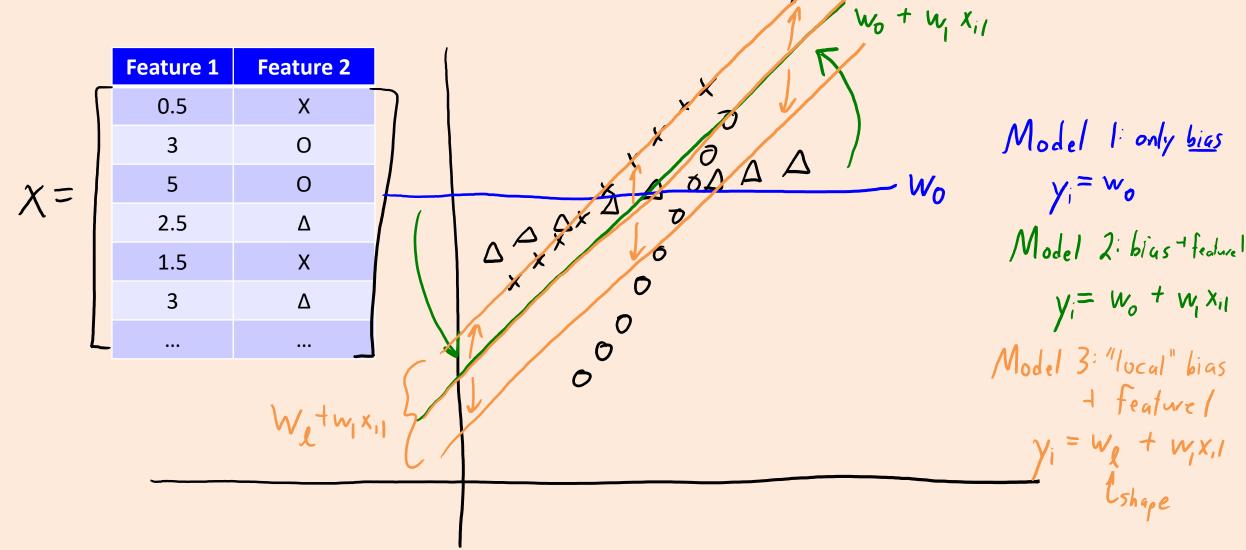
Next time: feature engineering for image and sound data.

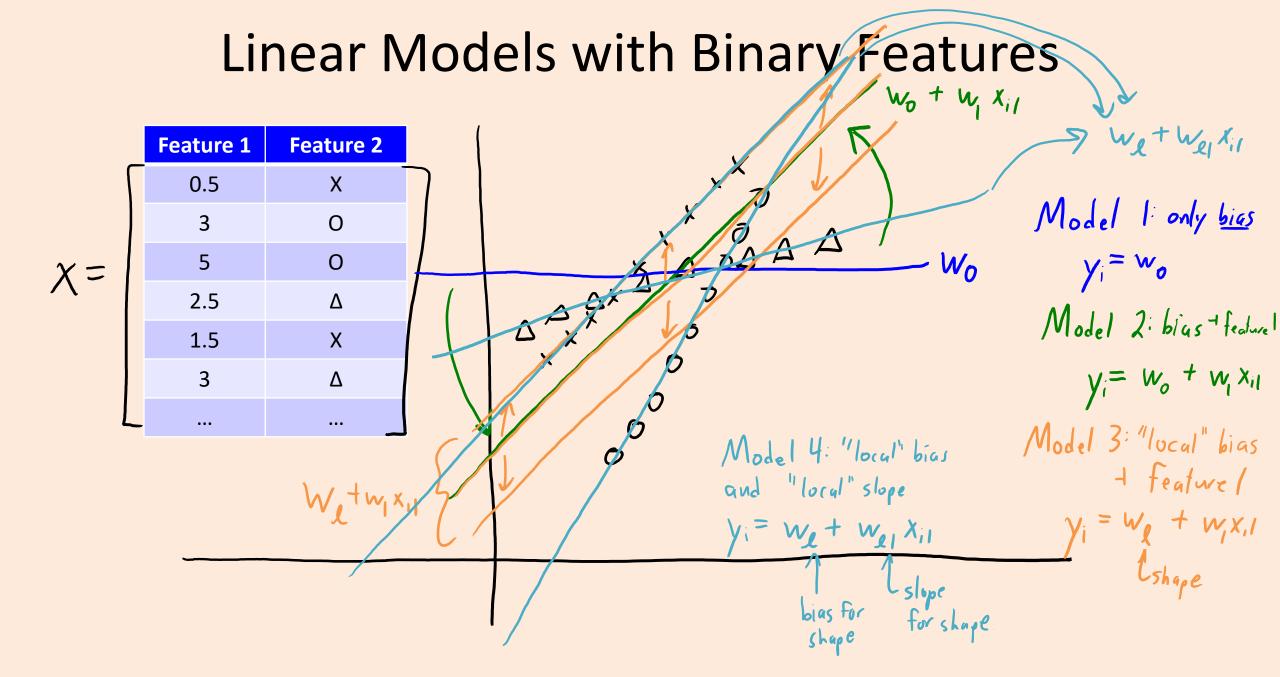
| _ | Feature 1 | Feature 2 | |
|------------|-----------|-----------|--|
| ſ | 0.5 | X | |
| | 3 | 0 | |
| $\chi = $ | 5 | 0 | |
| | 2.5 | Δ | |
| | 1.5 | X | |
| | 3 | Δ | |
| L | | | |

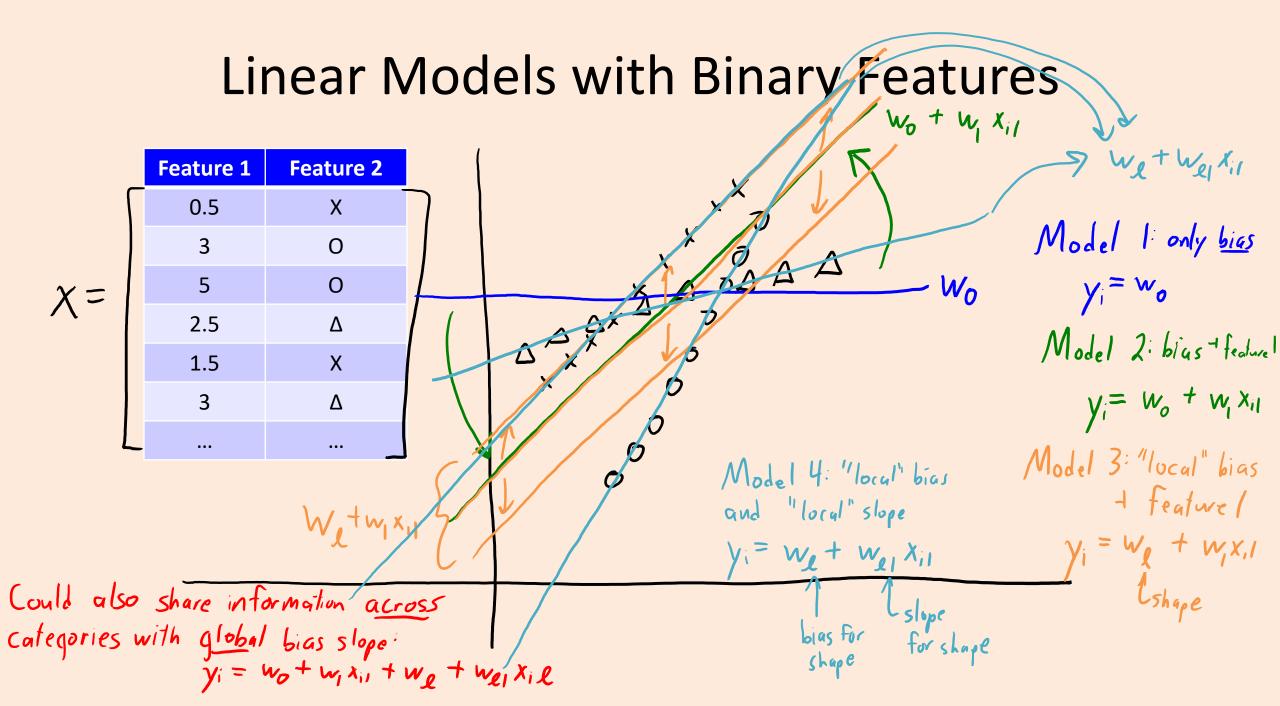












Global and Local Features for Domain Adaptation

- Suppose you want to solve a classification task,
 where you have very little labeled data from your domain.
- But you have access to a huge dataset with the same labels, from a different domain.
- Example:
 - You want to label POS tags in medical articles, and pay a few \$\$\$ to label some.
 - You have access the thousands of examples of Wall Street Journal POS labels.
- Domain adaptation: using data from different domain to help.

Global and Local Features for Domain Adaptation

- "Frustratingly easy domain adaptation":
 - Use "global" features across the domains, and "local" features for each domain.
 - "Global" features let you learn patterns that occur across domains.
 - Leads to sensible predictions for new domains without any data.
 - "Local" features let you learn patterns specific to each domain.
 - For linear classifiers this would look like: