

**Writing Skills 1**  
**Basic L<sup>A</sup>T<sub>E</sub>X Commands**

1. If  $s_n = a + ar + ar^2 + \cdots + ar^{n-1}$ , then

$$s_n = \sum_{k=1}^n ar^{k-1} = \frac{a(1-r^n)}{1-r}.$$

2. Here are some useful facts from Calculus:

(a)  $\frac{d}{dx}(\ln x) = \frac{1}{x}$

- (b) Double angle formulas

- $\sin(2x) = 2 \sin x \cos x$
- $\cos(2x) = \cos^2 x - \sin^2 x$

(c) If  $n \neq -1$ , then  $\int x^n dx = \frac{x^{n+1}}{n+1} + c$

3. If  $(x_1, y_1)$  and  $(x_2, y_2)$  are two points in the plane with  $x_1 \neq x_2$ , then the slope of the line through these points is

$$\frac{y_2 - y_1}{x_2 - x_1}. \tag{1}$$

We sometimes denote the slope given in Equation (1) by  $m$ .

4. If

$$x_n = \frac{n}{n+1} \text{ and } i_k = 2k+1,$$

then

$$x_{i_{12}} = \frac{i_{12}}{i_{12}+1} = \frac{25}{26}.$$

5. Completing the square, we see that if  $y = 2x^2 + 8x + 7$ , then

$$\begin{aligned} y &= 2(x^2 + 4x) + 7 \\ &= 2(x^2 + 4x + 4) + 7 - 2(4) \\ &= 2(x+2)^2 - 1. \end{aligned}$$