

# Pythagorean Triples

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**Proposition 1.**

$$\begin{aligned}a_{k+1} &= a_k + 4 \\b_{k+1} &= \frac{1}{2}a_k + b_k + 1 \\c_{k+1} &= \frac{1}{2}a_k + c_k + 1\end{aligned}$$

*Generates Pythagorean Triples of Height 8 with  $a_0 = 20, b_0 = 21, c_0 = 29$*

*Proof.* We will prove by induction that Proposition 1 holds for all  $k \geq 0$ .

**Base Case:** Our base case is when  $k = 0$ . So when  $k = 0$ , by definition our formula gives us a Pythagorean Triple of height 8. So our proposition is true in this case.

**Induction Step:** Let  $k \geq 0$  be given and suppose our proposition is true for  $n = k$ . Then  $\square$