

# Informatics

## Algorithmic Thinking Part 2

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Elaboration on © Pearson – Fluency with Information Technology – Snyder  
– Ch.10

# Intersecting two Lists (I2L)

Write the friends of Mary and John in 2 pieces of paper  
and copy in a new piece of paper the *intersection*

| Friends of Mary | Friends of John | Intersection |
|-----------------|-----------------|--------------|
| Julie           | Susie           |              |
| Anne            | Charlie         |              |
| Frank           | Bob             |              |
| Susie           | Anne            |              |

# Intersecting 2 Lists

- put a marker in the first position of each list
- compare the elements pointed by the markers:  
equal or different?

| Friends of Mary | Friends of John | Intersection |
|-----------------|-----------------|--------------|
| Julie *         | Susie *         |              |
| Anne            | Charlie         |              |
| Frank           | Bob             |              |
| Susie           | Anne            |              |

# Intersecting 2 Lists

- different: advance the right marker
- compare the elements pointed by the markers:  
equal or different?

| Friends of Mary | Friends of John | Intersection |
|-----------------|-----------------|--------------|
| Julie *         | Susie           |              |
| Anne            | Charlie*        |              |
| Frank           | Bob             |              |
| Susie           | Anne            |              |

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| Anne            | Charlie         |              |
| Frank           | Bob *           |              |
| Susie           | Anne            |              |

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- different: advance the right marker
- compare the elements pointed by the markers:  
equal or different?

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|-----------------|-----------------|--------------|
| Julie *         | Susie           |              |
| Anne            | Charlie         |              |
| Frank           | Bob             |              |
| Susie           | Anne *          |              |

# Intersecting 2 Lists

- different, but the right marker is at the end:  
reset the right marker and advance the left marker
- compare the elements pointed by the markers:  
equal or different?

| Friends of Mary | Friends of John | Intersection |
|-----------------|-----------------|--------------|
| Julie           | Susie *         |              |
| Anne *          | Charlie         |              |
| Frank           | Bob             |              |
| Susie           | Anne            |              |

# Intersecting 2 Lists

- different: advance the right marker
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|-----------------|-----------------|--------------|
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| Anne *          | Charlie         |              |
| Frank           | Bob             |              |
| Susie           | Anne *          |              |

# Intersecting 2 Lists

- equal: copy the element at the end of the intersection
- **advance** left marker, and **reset** right marker
- compare the elements pointed by the markers:  
equal or different?

| Friends of Mary | Friends of John | Intersection |
|-----------------|-----------------|--------------|
| Julie           | Susie           | <b>Anne</b>  |
| Anne *          | Charlie         |              |
| Frank           | Bob             |              |
| Susie           | Anne *          |              |

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- different: advance the right marker
- compare the elements pointed by the markers:  
equal or different?

| Friends of Mary | Friends of John | Intersection |
|-----------------|-----------------|--------------|
| Julie           | Susie *         | <b>Anne</b>  |
| Anne            | Charlie         |              |
| Frank *         | Bob             |              |
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| Anne            | Charlie         |              |
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- different: advance the right marker
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equal or different?

| Friends of Mary | Friends of John | Intersection |
|-----------------|-----------------|--------------|
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| Anne            | Charlie         |              |
| Frank *         | Bob             |              |
| Susie           | Anne *          |              |

# Intersecting 2 Lists

- different: since the right marker is at the end, reset the right marker and advance the left marker
- compare the elements pointed by the markers:  
equal or different?

| Friends of Mary | Friends of John | Intersection |
|-----------------|-----------------|--------------|
| Julie           | Susie *         | <b>Anne</b>  |
| Anne            | Charlie         |              |
| Frank           | Bob             |              |
| Susie *         | Anne            |              |

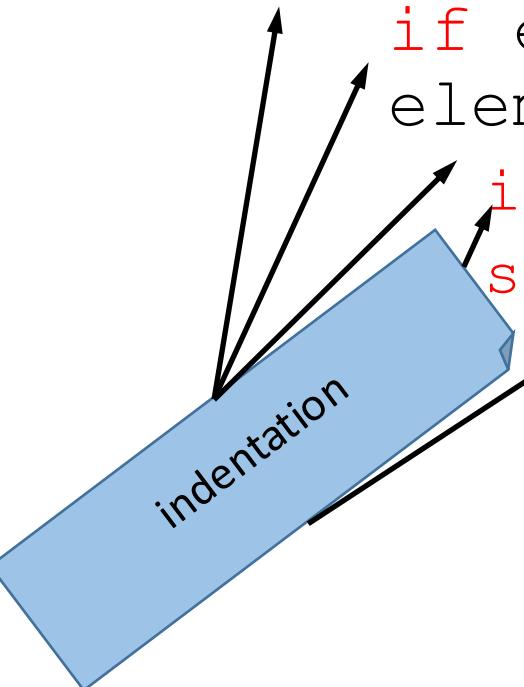
# Intersecting 2 Lists

- equal: copy the element to the Intersection
- since the left list is at the end stop, because all the elements of the left list have been compared with all the elements of the right list

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|-----------------|-----------------|--------------|
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| Anne            | Charlie         | <b>Susie</b> |
| Frank           | Bob             |              |
| Susie *         | Anne            |              |

# Intersecting two lists – algorithm in *pseudo-code*

```
prepare an empty variable intersection, set s to 0
repeat varying i from 1 to the length of list1
    repeat varying j from 1 to the length of list2
        if element in position i of list1 is equal to
            element in position j of list2
                increment s by 1
                store the element in position i of list1 into
                position s of intersection
```



# *Intersecting two Alphabetized Lists (IAL)*

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| Julie           | Charlie         |              |
| Susie           | Susie           |              |

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|-----------------|-----------------|--------------|
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| Frank           | Bob             | <b>Susie</b> |
| Julie           | Charlie         |              |
| Susie*          | Susie*          |              |

# Comparison

- IAL and IL are different algorithms
- IAL and IL accomplish the same thing, starting from the same data but in different order
- IL is much slower
- For two lists of 100 elements, worst case:
  - IAL:  $100+100 = 200$  comparisons
  - IL:  $100 \times 100 = 10,000$  comparisons
- *how many steps do we need to put lists in alphabetical order?*
  - *you will learn it by the end of the course*

# How Do We Know it Works?

- Algorithm solution is clear and simple and efficient
- Then, how do we know it works?
- If there is no loop, the program runs, gets to an end, and we can check the result
- What if there is a loop?
  - Programs with loops cannot be absolutely verified...there are too many possible cases

# Then, what?

- *The way to know that an algorithm works is to know why it works...*
- Strategy for knowing why it works:
  - Find one or more properties that ensure the algorithm works
  - Explain, using the program, why they make it work.

# Why IAL Works

- If a name appears in all lists, it forms a barrier
- Pointers that haven't reached the barrier move sooner than ones that have
- When they all reach the barrier, the name is recorded
- None can pass the next barrier until they all reach it
- Etc.

# Summary

- We use algorithms daily, and we continually create them as we instruct other people in how to do something
- Everyday algorithms can be sometimes be unclear because natural language is imprecise
- Algorithms have five fundamental properties

# Summary

- Algorithms can be given at different levels of detail depending on the abilities of the agent
- Problems can be solved by different algorithms in different ways
- Algorithms always finish—either they give the answer, or say no answer is possible—and they are evaluated on their use of resources such as space and time

**try to write the IAL algorithm in pseudo-code**