

流道原型STP/STL

设置目标函数:

1. 能量耗散目标: $T1 = \text{integral}[\text{grad}(u) * \text{grad}(u) * dx]$
2. 体积目标: $T2 = (\text{Integral}[dx] - \text{target_vol})^2$

选择CFD控制方程(Navier Stoke):

- C1: $v * \text{grad}(v) + \text{grad}(p) + \text{laplace}(v) = 0$
C2: $\text{divergence}(v) = 0$

组建拉格朗日方程:

$$J = T1 + T2 + \text{adjoint}_1 * C1 + \text{adjoint}_2 * C2$$

定义控制变量(control_variable): position即是x, y, z坐标

定义状态变量(state_variable): v(velocity)速度, p(pressure)压力

adjoint为拉格朗日乘子也作为TestFunction用于有限元求解

OpenFoam基于有限体积法(FVM)求解state_variable

对J进行变分:

$$\text{variation}_J = \text{variation}(J, \text{state_variable}) + \text{variation}(J, \text{control_variable})$$

使 $\text{variation}(J, \text{state_variable}) = 0$, 求取adjoint

根据Riesz Representation(Laplace smoothing) of shape gradient:

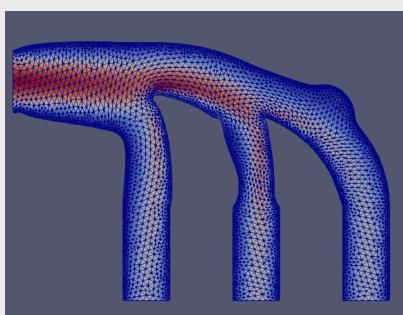
$$-\text{laplace}(\text{grad_position}) = dJ(\text{position}), \text{求得形状梯度shape_gradient}$$

更新geometry:

$$\text{new_shape} = \text{old_shape} - \text{stepSize} * \text{shape_gradient}$$

如果变形量很小

是



Exit

否