CS 5/7320

with figures from the AIMA textbook





Types of uncertainty in the environment\*



#### **Nondeterministic Actions:**

Outcome of an action in a state is uncertain.



#### No observations:

Sensorless problem



Partially observable environments:

The agent does not know in what state the environment is.

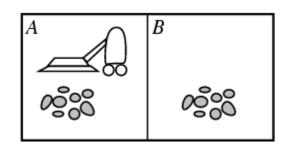


#### **Exploration:**

Unknown environments and Online search

\* we will quantify uncertainty with probabilities later.

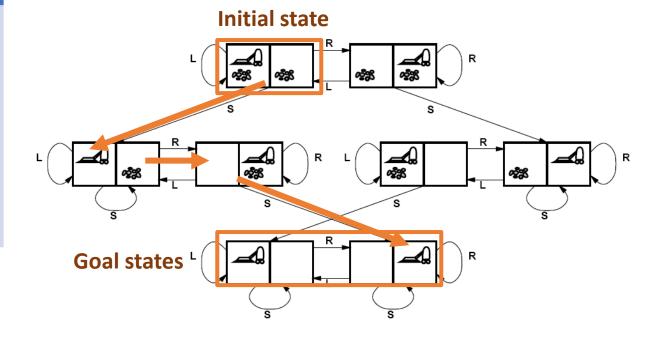
## **Remember**: Solving Search Problems under Certainty



### No Uncertainty

- Deterministic actions with known transition model  $Result(s_1, a) = s_4$
- Full observability (we know where everything is while planning)

**State space:** A state completely describes the environment and agent



**Solution** of the planning phase is a **sequence of actions** also called a **plan** that can be blindly followed: [Suck, Right, Suck]

### Consequence of Uncertainty

1. The agent may not know in what state it and the environment exactly is in.

It needs to keep track of all the states it could be in. This set is called the **believe state**.

2. The solution is typically not a fixed precomputed plan (sequence of actions), but a

conditional plan (also called strategy or policy)

that depends on percepts.



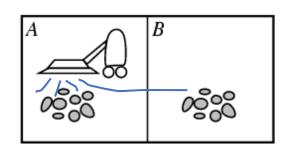
### Nondeterministic Actions

Outcome of actions in the environment is nondeterministic = transition model need to describe uncertainty.

Example transition:  $Results(s_1, a) = \{s_2, s_4, s_5\}$ 

i.e., action a in  $s_1$  can lead to one of several states.

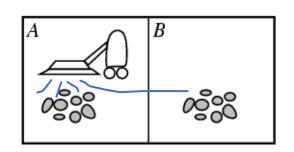
# Example: Erratic Vacuum World

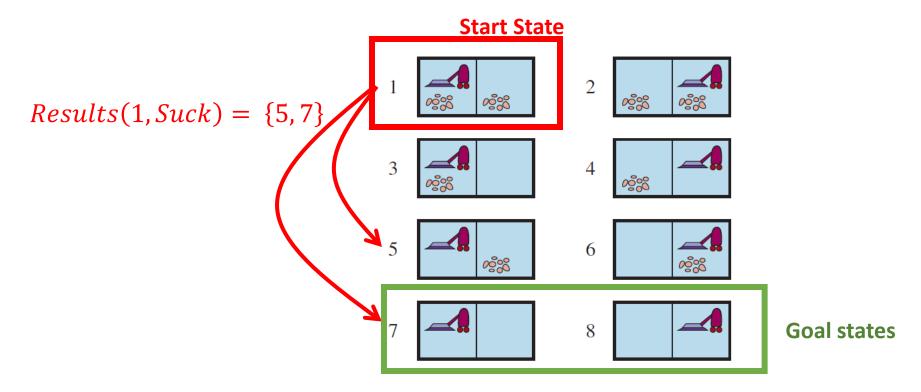


Regular deterministic vacuum world, but the action 'suck' is more powerful and nondeterministic:

- a) On a dirty square: cleans the square and sometimes cleans dirt on adjacent squares as well.
- **b)** On a clean square: sometimes deposits some dirt on the square.

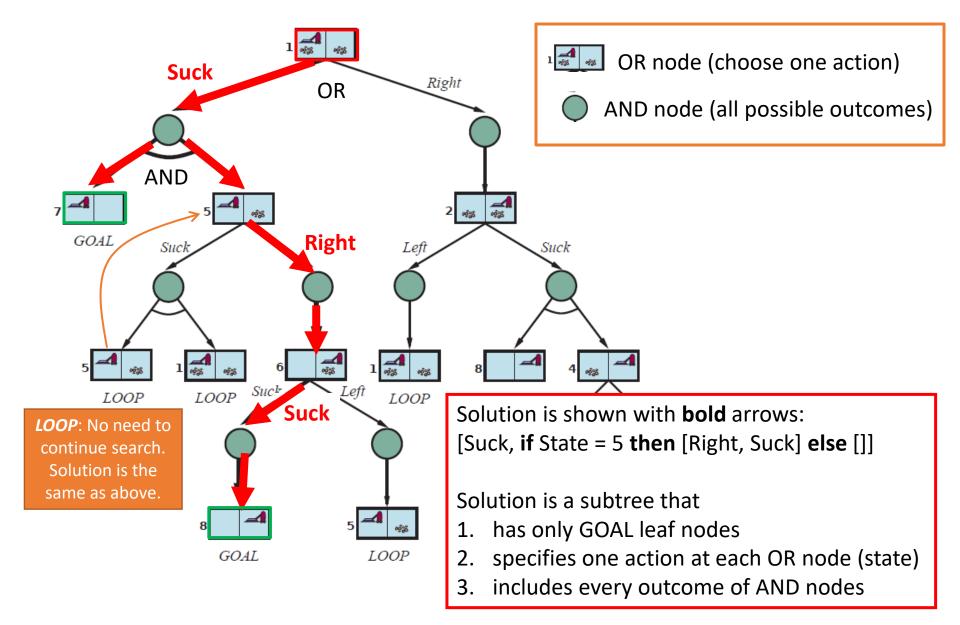
# Example: Erratic Vacuum World



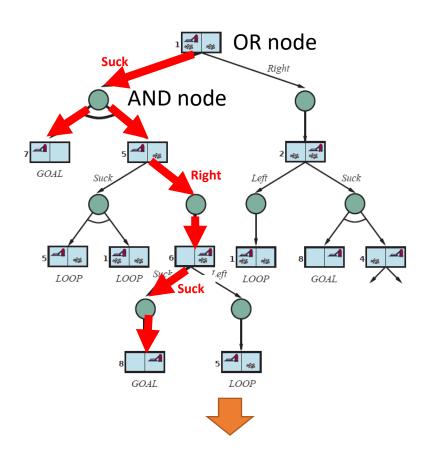


We need a conditional plan
[Suck, **if** State = 5 **then** [Right, Suck] **else** []]

### Finding a Cond. Plan: AND-OR Search Tree



### AND-OR Tree search: Idea



[Suck, if State = 5 then [Right, Suck] else []]

- Descend the tree by trying an action in each OR node and considering all resulting states of the AND nodes.
- Remove branches (actions) if we cannot find a subtree below that leads to only goal nodes. (see failure in the code on the next slide). Loop nodes can be ignored.
- Stop when we find a subtree that only has goal states in all leaf nodes.
- Construct the conditional plan that represents the subtree starting at the root node.

### AND-OR Recursive DFS Algorithm

= nested If-then-else statements

```
function AND-OR-SEARCH(problem) returns a conditional plan, or failure
  return OR-SEARCH(problem, problem.INITIAL, [])
                                                              path is only maintained for cycle checking!
function OR-SEARCH(problem, state, path) returns a conditional plan, or failure
  if problem.IS-GOAL(state) then return the empty plan
  if IS-CYCLE(path) then return failure
                                            // don't follow loops using path.
  for each action in problem. ACTIONS(state) do // try all possible actions
      plan \leftarrow AND\text{-SEARCH}(problem, RESULTS(state, action), [state] + path])
      if plan \neq failure then return [action] + plan
  return failure
                                               // fail means we found no action that leads to
                                               // a goal-only subtree
function AND-SEARCH(problem, states, path) returns a conditional plan, or failure
                                                  // try all possible outcomes, none can fail!
  for each s_i in states do
      plan_i \leftarrow \text{OR-SEARCH}(problem, s_i, path) // (= belief state)
                                                 // fail if we find any non-goal subtree
      if plan_i = failure then return failure
  return [if s_1 then plan_1 else if s_2 then plan_2 else ... if s_{n-1} then plan_{n-1} else plan_n]
```

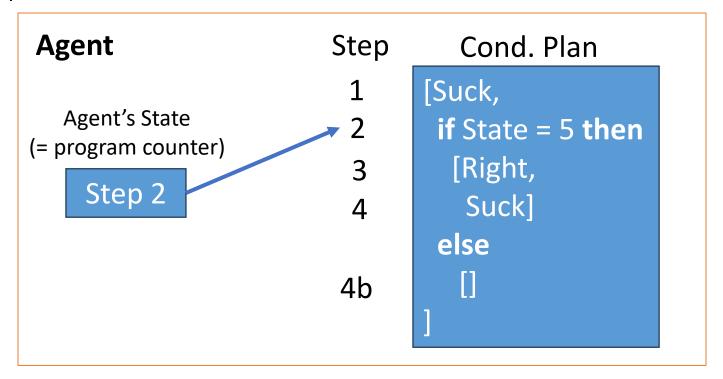
#### **Notes:**

- The DFS search tree is implicitly created using the call stack (recursive algorithm).
- DFS is **not optimal!** BFS and A\* search can be used to find better solutions (e.g., smallest subtree).

### Use of Conditional Plans

- Planning uses search to find a conditional plan that leads to a goal state.
- The conditional plan can be executed by a **model-based agent** that uses percepts for the if statements.

Example: After the initial action "suck"



# Search with no Observations

Using Actions to "Coerce" the World into Known States



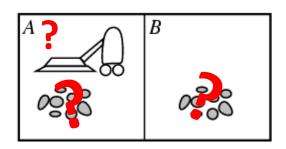
### No Observations

Sensorless problem = unobservable environment also called a conformant problem.

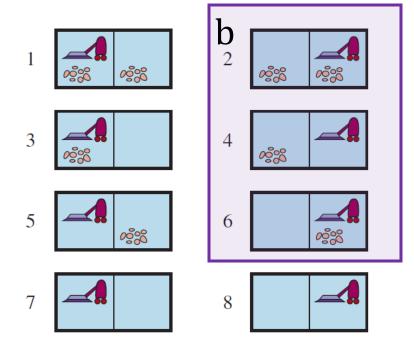
### Why is this useful?

- Example: Doctor prescribes a broad-band antibiotic instead of performing time-consuming blood work for a more specific antibiotic. This saves time and money.
- Basic idea: Find a solution (a sequence of actions) that works (reasonably well) from any state and then just blindly execute it (called in control theory: open loop system).

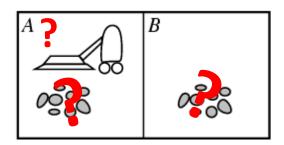
### **Belief State**



- The agent does not know in which state it is exactly in.
- However, it may know that it is in one of a set of possible states.
   This set is called a belief state of the agent.
- Example:  $b = \{s_2, s_4, s_6\}$

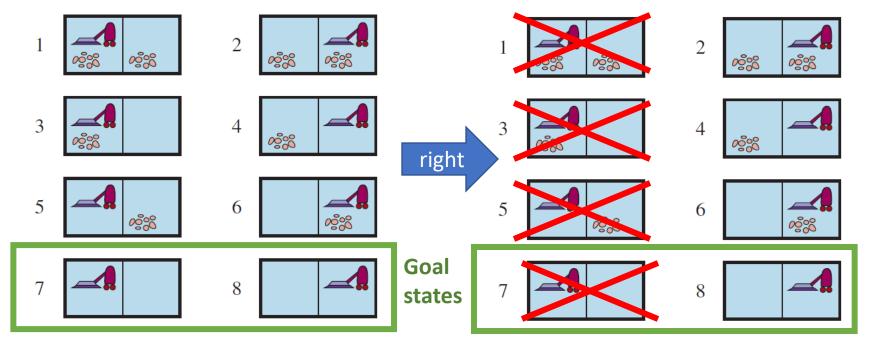


## Actions to Coerce the World into States

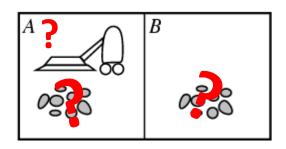


- Actions can reduce the number of possible states.
- **Example**: Deterministic vacuum world. Agent does not know its position and the dirt distribution.

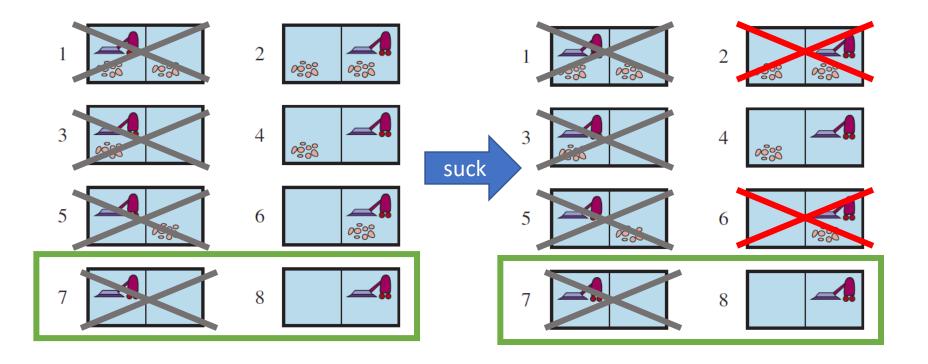
Initial belief state {1,2,3,4,5,6,7,8}



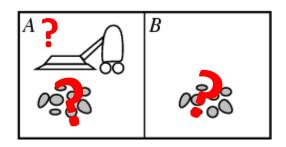
## Actions to Coerce the World into States



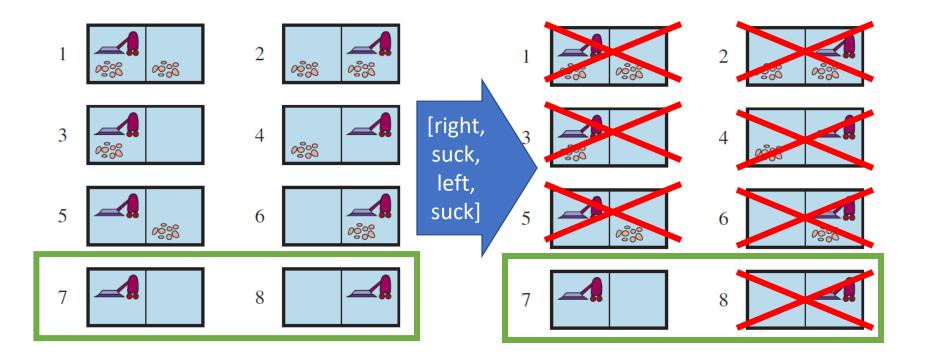
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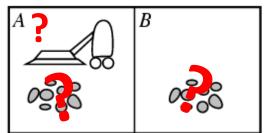
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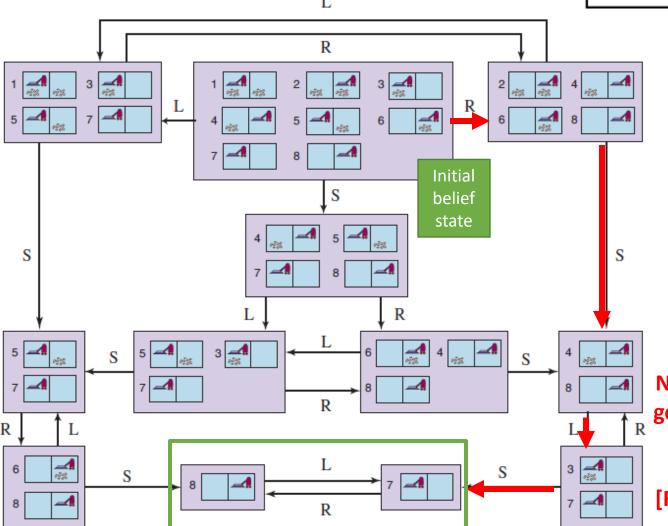


- The action sequence [right, suck, left, suck] coerces the world into the goal state 7. It works from any initial state!
- There are no observations so there is no need for a conditional plan.



# Example: The reachable belief-state space for the deterministic, sensorless vacuum world





Size of the belief state space depends on the number of states *N*:

$$P_S = 2^N = 2^8 = 256$$

Only a small fraction (12 states) are reachable.

No observations, so we get a solution sequence from an initial belief state:

[Right, Suck, Left, Suck]

### Finding a Solution Sequence

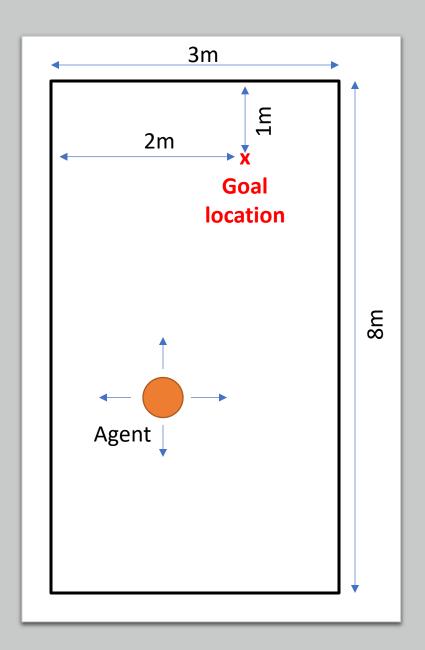
**Note**: State space size makes this impractical for larger problems!

Formulate as a regular search and solve with DFS, BFS or A\*:

- States: All belief states (=powerset  $\mathcal{P}_s$  of states of size  $2^N$  for N states)
- Initial state: Often the belief state consisting of all states.
- Actions: Actions of a belief state are the union of the possible actions for all the states it contains.
- Transition model:  $b' = Results(b, a) = \{s' : s' = Result(s, a) \text{ and } s \in b\}$
- Goal test: Are all states in the belief state goal states?
- **Simplifying property:** If a belief state (e.g.,  $b_1 = \{1,2,3,4,5\}$ ) is solvable (i.e., there is a sequence of actions that coerce all states to only goal states), then belief states that are subsets (e.g.,  $b_2 = \{2,5\}$ ) are also solved using the same action sequence. Used to prune the search tree.

#### Other approach:

Incremental belief-state search. Generate a solution that works for one state
and check if it also works for all other states. If it does not, then modify the
solution slightly. This is similar to local search.



## Case Study

The agent can move up, down right, left.

The agent has **no sensors** and does not know its current location.

1. Can you navigate to the goal location? How?

2. What would you need to know about the environment?

3. What type of agent can do this?



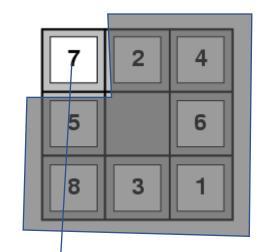
### Percepts and Observability

- Many problems cannot be solved efficiently without sensing (e.g., 8-puzzle).
- We need to see at least one square.

Percept function: Percept(s)

s is the state

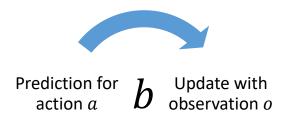
- Fully observable: Percept(s) = s
- Sensorless: Percept(s) = None
- Partially observable: Percept(s) = oo is called an observation and tells us something about s



Percept(s) = Tile7

Problem: Many states (different order of the hidden tiles) can produce the same observation!

## Use Observations to Learn About the State



Agents choose an action and then receive an observation. **Idea**: Observations can be used to learn about the agent's state.



Assume we have a current belief state b (i.e., the set of states we could be in).

**Prediction for action:** Choose an action a and compute a new belief state that results from the action.

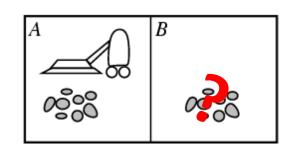
$$\hat{b} = Predict(b, a) = \bigcup_{s \in b} Result(s, a)$$

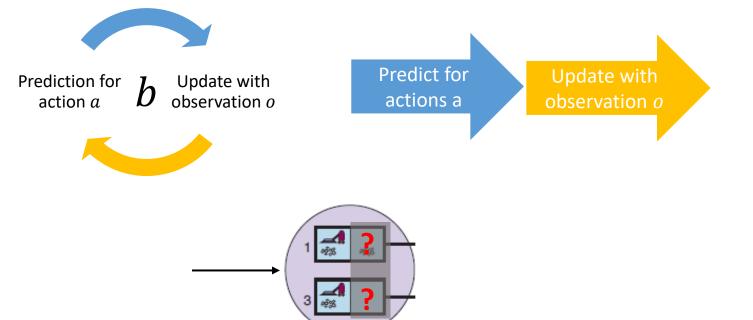
**Update with observation**: You receive an observation o and only keep states that are consistent with the new observation. The belief after observing o is:

$$b_o = Update(\hat{b}, o) = \{s : s \in \hat{b} \land Percept(s) = o\}$$

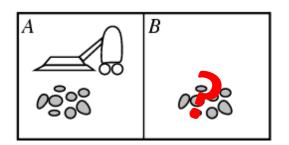
Both steps in one:  $b \leftarrow Update(Predict(b, a), o)$ 

## Example: Deterministic local sensing vacuum world

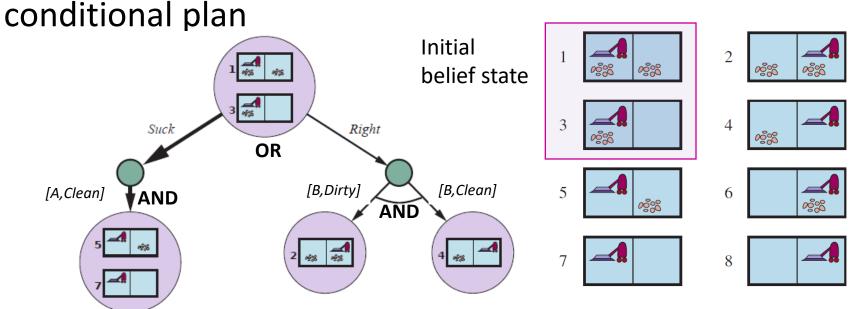




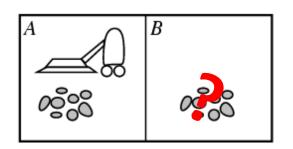
$$b \leftarrow Update(Predict(b, a), o)$$
  
 $Update(Predict(\{1,3\}, Right), [B, Dirty]) = \{2\}$ 



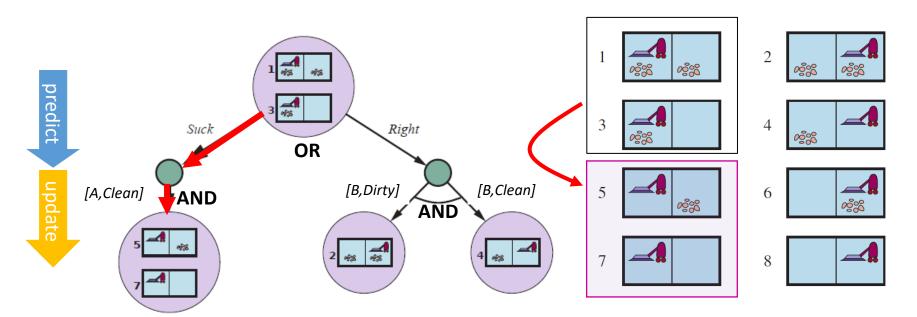
Use an AND-OR tree of belief states to create a



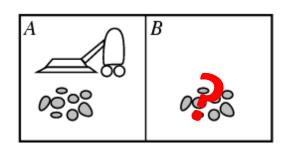
**Solution**: [Suck, Right, if  $b = \{6\}$  then Suck else []]



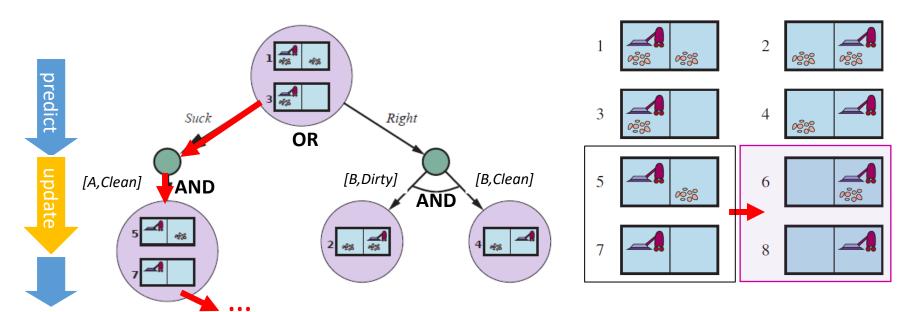
Use an AND-OR tree to create a conditional plan



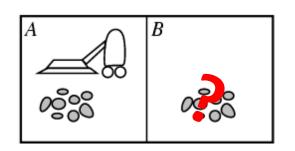
**Solution**: [Suck, Right, if  $b = \{6\}$  then Suck else []]



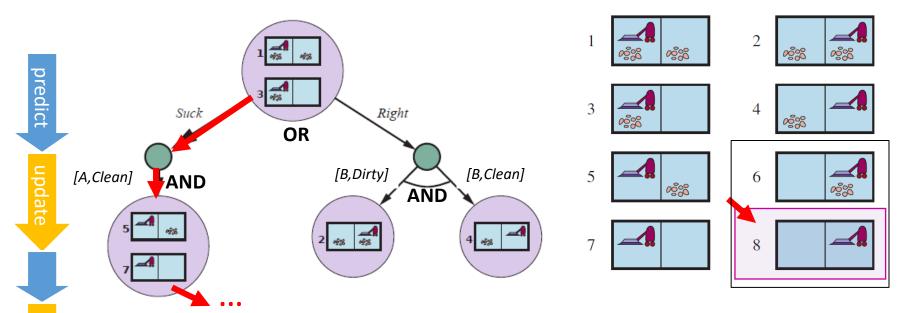
Use an AND-OR tree to create a conditional plan



**Solution**: [Suck, Right, if  $b = \{6\}$  then Suck else []]



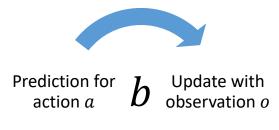
Use an AND-OR tree to create a conditional plan



Solution: [Suck, Right, if  $b = \{6\}$  then Suck else []]

b = {6} is the result of the update with o = [r, Dirty]

## State Estimation and Approximate Belief States

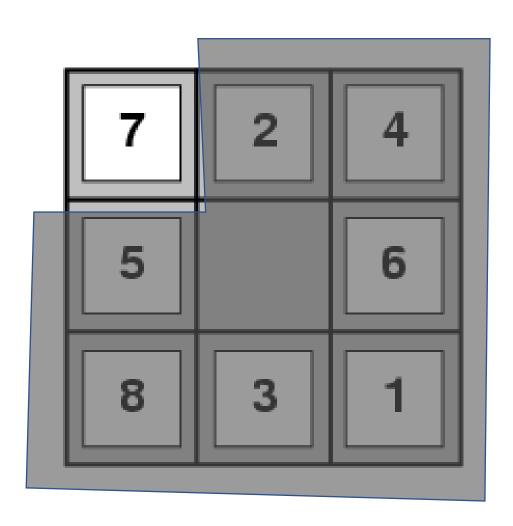




- Agents choose an action and then receive an observation from the environment.
- The agent keep track of its belief state using the following update:

$$b \leftarrow Update(Predict(b, a), o)$$

- This process is often called
  - · monitoring,
  - filtering, or
  - state estimation.
- The agent needs to be able to update its belief state following observations in real time! For many practical application, there is only time to compute an approximate belief state! These approximate methods are used in control theory and reinforcement learning.



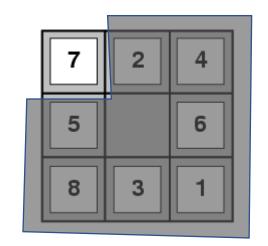
## Case Study

Partially Observable 8-Puzzle

## Partially Observable 8-Puzzle

- 1. Give a problem description for each step.
  - States:
  - Initial state:
  - Actions:
  - Transition model:
  - Goal test:
  - Percept function:
- 2. The problem can be solved using an AND-OR Tree, but is there an easier solution?

- a. What type of agent do we use?
- b. What algorithms can be used?





### Online Search

- Recall offline search: Create a plan using the state space as a model before taking any action. The plan can be a sequence of actions or a conditional plan to account for uncertainty.
- The agent uses the transition function to predict the consequence of actions. What if the **transition function is unknown**?
- Online search explores the real world one action at a time. Prediction is replaced by "act" and update by "observe."



- Useful for
  - Real-time problems: When offline computation takes too long and there is a penalty for sitting around and thinking.
  - Nondeterministic domain: Only focus on what actually happens instead of planning for everything!
  - **Unknown environment**: The agent has no complete model of how the environment works. It needs to explore an unknown state space and/or what actions do. I.e., it needs to **learn** the transition function  $f: S \times A \to S$

# Design Considerations for Online Search

- Knowledge: What does the agent already know about the outcome of actions? E.g.,
  - Does go north and then south lead to the same location?
  - Where are the walls in the maze?

Often a part or all of the transition function is unknown!

- We need a safely explorable state space/world: There are no irreversible actions (e.g., traps, cliffs) or the agent needs to be able to avoid these actions using percepts.
- Exploration order is important: Expanding nodes in local order is more efficient if you must execute the actions to get observations: Depth-first search with backtracking instead of BFS or A\* Search.

### Online Search: Model-based Agent Program for Unknown Transition model

Environment is deterministic and fully observable (the percept is the full state) but

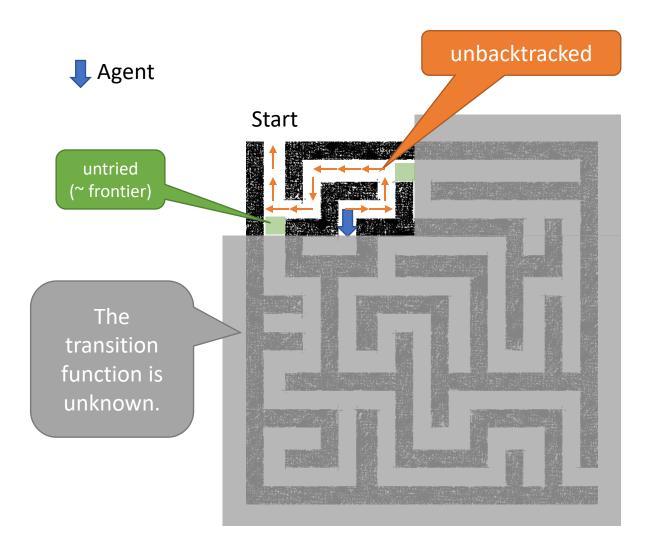
• unknown transition model (function *result*).

**Approach**: The agent builds the map  $result(s, a) \rightarrow s'$  by trying all actions and backtracks when all actions in a state have been explored.

```
Learns results function
                                                                                (= transition function)
function ONLINE-DFS-AGENT(problem, s') returns an action
               s, a, the previous state and action, initially null
  persistent: result, a table mapping (s, a) to s', initially empty
                                                                                 Untried is the "frontier"
               untried, a table mapping s to a list of untried actions _
               unbacktracked, a table mapping s to a list of states never backtracked to
                                                                     unbacktracked stores the current path
  if problem.IS-GOAL(s') then return stop
  if s' is a new state (not in untried) then untried [s'] \leftarrow problem.ACTIONS(s')
  if s is not null then
                                                                      Record the found transition
      result[s, a] \leftarrow s'
      add s to the front of unbacktracked[s']
                                                                       Keep breadcrumbs to go back
  if untried[s'] is empty then
      if unbacktracked[s'] is empty then return stop
      else a \leftarrow an action b such that result[s', b] = POP(unbacktracked[s'])
  else a \leftarrow POP(untried[s'])
  s \leftarrow s'
  return a
```

# Case Study: DFS with Backtracking for an unknown Maze

- We can only see adjacent squares and don't know the location of the goal!
- We cannot plan but we must explore by walking around!
- We only know what we have already explored.
- A simple method is to store the path for backtracking to get back to untied paths when we run into a dead end (i.e., use breadcrumbs).
- This is DFS without a reached data structure.





Important concepts that you should be able to explain and use now...

- Difference between solution types:
  - a. a fixed actions sequence,
  - b. a conditional plan (also called a strategy or policy), and
  - c. exploration.
- What are belief states?
- How actions can be used to coerce the world into known states.
- How observations can be used to learn about the state: State estimation with repeated predict and update steps.
- The use of AND-OR trees to solve small problems.