

Position: Inference-Time Computations for LLM Reasoning and Planning: A Benchmark and Insights

Anonymous Authors¹

Abstract

We examine the reasoning and planning capabilities of large language models (LLMs) in solving complex tasks. Recent advances in inference-time techniques demonstrate the potential to enhance LLM reasoning without additional training by exploring intermediate steps during inference. Notably, OpenAI’s o1 model shows promising performance through its novel use of multi-step reasoning and verification. Here, we explore how scaling inference-time techniques can improve reasoning and planning, focusing on understanding the tradeoff between computational cost and performance. To this end, we construct a comprehensive benchmark, known as *Sys2Bench*, and perform extensive experiments evaluating existing inference-time techniques on eleven diverse tasks across five categories, including arithmetic reasoning, logical reasoning, common sense reasoning, algorithmic reasoning, and planning. Our findings indicate that simply scaling inference-time computation has limitations, as no single inference-time technique consistently performs well across all reasoning and planning tasks.

1. Introduction

Large language models (LLMs) (Brown et al., 2020) have demonstrated exceptional performance across a range of natural language processing (NLP) tasks, including question answering, machine translation, sentiment analysis, and text summarization (Devlin et al., 2019; Vaswani et al., 2017). Beyond NLP, LLMs have also been adapted for multimodal tasks involving vision (Parashar et al., 2024; Lin et al., 2025) and audio (Wu et al., 2024). Building on their success in these diverse domains, researchers are increasingly using LLMs as AI agents (Deng et al., 2024; Wang et al., 2024)

for complex tasks, such as robotics (Liu et al., 2023) and scientific discovery (Wang et al., 2024). These tasks require the reasoning and planning capabilities of LLMs, extending beyond simpler text comprehension.

Reasoning and planning in LLMs refer to their ability to solve complex problems by understanding, processing, and generating solutions across various domains (Hao et al., 2024). These capabilities can be analyzed from multiple perspectives; we propose a classification that organizes reasoning and planning tasks into five categories, namely arithmetic, logical, commonsense, algorithmic, and plan generation challenges. Recent advances in inference-time techniques demonstrate the potential to enhance LLM reasoning and planning without additional training. These techniques focus on decomposing complex problems into simpler intermediate steps during inference. For instance, Chain-of-Thought (Wei et al., 2022) encourages step-by-step reasoning, while Tree-of-Thought (Yao et al., 2024) chooses optimal reasoning paths using tree search. Notably, OpenAI’s O1 model, a large reasoning model (LRM) (Valmeekam et al., 2024), achieves state-of-the-art performance on various reasoning tasks, demonstrating the effectiveness of inference-time techniques. This success has inspired the research community to focus more on scaling inference-time techniques in the hope of similar performance improvements.

Although inference time techniques have improved LLM reasoning and planning, evaluation of these methods has been limited to specific tasks, models, and datasets. Moreover, these methods have additional computational costs, presenting a trade-off between computational overhead and performance gains. To overcome this limitation we introduce *Sys2Bench*, a comprehensive benchmark covering multiple tasks and models. Specifically, we perform experiments on eleven datasets and seven different LLMs, testing four widely used inference-time techniques. Based on our findings, **our position is that simply scaling inference-time computation has limitations. Instead, we need to explore diverse approaches to enhance the holistic reasoning capabilities of LLMs, as no single inference-time technique consistently outperforms others across all tasks.**

¹Anonymous Institution, Anonymous City, Anonymous Region, Anonymous Country. Correspondence to: Anonymous Author <anon.email@domain.com>.

Preliminary work. Under review by the International Conference on Machine Learning (ICML). Do not distribute.

2. Related Work

LLM Reasoning is the ability of LLMs to logically process information and draw coherent conclusions, enabling them to solve complex problems (Saparov & He, 2023). The success of LLMs in Natural Language Generation (Radford et al., 2018) and Natural Language Understanding (Vaswani et al., 2017; Devlin et al., 2019) has sparked interest in exploring reasoning capabilities. A range of datasets have been introduced to evaluate reasoning, covering tasks in arithmetic (Ling et al., 2017; Cobbe et al., 2021), logic (Chollet, 2019; Wang et al., 2022), common sense (Yang et al., 2018; Geva et al., 2021), and algorithmic reasoning (Yao et al., 2024). We introduce these tasks in more detail in Section 3, and report results across these tasks in Section 5.

LLM Planning involves constructing a sequence of actions to achieve defined goals (Valmeekam et al., 2023; Zheng et al., 2024). LLMs have been employed as planners or high-level controllers for robotic tasks (Liu et al., 2023; Huang et al., 2022) and as agents for web navigation (Deng et al., 2024), scientific discovery (Wang et al., 2024), and autonomous vehicles (Yang et al., 2023). Despite their broad adoption, studies reveal that LLMs often struggle to generate valid plans for complex tasks (Kambhampati et al., 2024; Xie et al., 2024). We provide details on evaluated planning problems in Section 3, with results and analyses in Section 5.

Inference Time Techniques for LLMs are methods applied during output generation to improve performance, and alignment with downstream tasks (Welleck et al., 2024). These techniques aid reasoning and planning by breaking complex tasks into smaller, manageable steps for systematic problem-solving. For instance, Chain-of-Thought prompting (CoT) (Wei et al., 2022) and its variants (Zhou et al., 2023; Kojima et al., 2022) decompose problems into sequential steps, while self-consistency (Wang et al., 2023) refines CoT by aggregating multiple responses through voting. Tree of Thought (Yao et al., 2024), Graph of Thought (Besta et al., 2024), and Monte Carlo Tree Search (Hao et al., 2023; Zhou et al., 2024) enhance problem-solving by systematically exploring reasoning paths. Details on inference-time methods are in Section 4, with results in Section 5.

3. Sys2Bench Problems and Datasets

In this section, we introduce our benchmark, Sys2Bench, designed to evaluate the reasoning and planning of LLMs across various tasks. We evaluate the reasoning and planning capabilities of LLMs and inference-time techniques using eleven datasets, classified into five primary types; namely, **Arithmetic Reasoning**, **Logical Reasoning**, **Common Sense Reasoning**, **Algorithmic Reasoning**, and **Planning**. We summarize the datasets in Table 1.

3.1. Arithmetic Reasoning

The ability of Large Language Models (LLMs) to solve multi-step arithmetic problems remains an active area of research (Snell et al., 2024; Kumar et al., 2024b; Hendrycks et al., 2021). Additionally, OpenAI’s o1 models (OpenAI, 2024) have prompted the research community to explore inference-time techniques to improve the arithmetic reasoning of LLMs (Zhao et al., 2024a). We evaluate the arithmetic reasoning of LLMs, on **GSM8K** (Cobbe et al., 2021) and **AQuA** (Ling et al., 2017) benchmark.

GSM8K is a popular dataset of high-quality, linguistically diverse elementary school math word problems, designed to evaluate multi-step arithmetic reasoning. The problems typically require 2 to 8 steps of arithmetic operations, testing the ability of LLMs to perform logical deduction and basic calculations.

AQuA is a dataset of around 100,000 algebraic word problems with multiple-choice answers and detailed rationales. It is designed to evaluate the arithmetic reasoning and problem-solving capabilities of models, making it a challenging benchmark for LLMs.

3.2. Logical Reasoning

Logical reasoning involves deriving conclusions based on a structured sequence of rules, or premises. The evaluation of the ability to reason logically by LLM helps assess their ability to solve structured and complex decision-making problems (Chollet, 2019). We use **ProntoQA** (Saparov & He, 2023) to evaluate the logical reasoning ability of LLMs.

ProntoQA is a dataset developed to evaluate an LLM’s ability to reason and generate explicit reasoning chains for first-order logic-based queries (Barwise, 1977). It challenges models to not only produce correct answers but also provide detailed, step-by-step reasoning paths that justify their conclusions.

3.3. Common Sense Reasoning

Common Sense Reasoning is the process of drawing conclusions from implicit everyday knowledge. Evaluating this skill ensures that LLMs provide accurate and contextually appropriate responses. We evaluate this type of reasoning using the **StrategyQA** (Geva et al., 2021) and **HotPotQA** (Yang et al., 2018) datasets.

StrategyQA is a benchmark designed to assess a model’s ability to perform implicit multi-step reasoning using general knowledge or common sense facts. It consists of yes/no questions where the goal is to arrive at the correct answer by generating and verifying intermediate reasoning steps.

HotPotQA is a large-scale dataset designed to evaluate how

Table 1. Summary of the 11 datasets included in Sys2Bench.

	Algorithmic Reasoning		Planning			
	Game of 24	Binpacking	Blocksworld	Trip Plan	Calendar Plan	Rubik’s cube
Task	Propose an arithmetic expression to reach 24.	Pack items into the fewest bins.	Propose a plan that transforms initial state of blocks to a goal.	Plan a trip across cities for a set number of days.	Schedule a meeting considering time constraints of people.	Unscramble a scrambled 2X2 Rubik’s Cube.
Input	A list of 4 numbers.	List of item weights and bin capacity.	Initial state of blocks and goal state.	Cities, days per city, total days, and possible flights.	Calendars with meetings and time constraints.	A scrambled 2X2 Rubik’s Cube.
Output	An arithmetic expression.	Final list with items arranged in bins.	A sequence of actions as the plan.	A trip itinerary.	A meeting time fitting all schedules.	A sequence of rotations that unscramble the cube.
	Arithmetic Reasoning		Logical Reasoning	Common Sense Reasoning		
	GSM8K	AQuA	ProntoQA	StrategyQA	HotPotQA	
Task	Solve high school arithmetic problems.	Solve algebraic problems.	Draw a logical conclusion from a set of predicates.	Answer general knowledge questions.	Answer general knowledge questions using provided facts.	
Input	Arithmetic problem description.	Algebraic problem description.	A clause to verify as true or false using logical predicates.	A yes/no question.	General knowledge question with supporting facts.	
Output	A numerical value.	A multi choice option.	True or False, and reasoning.	Yes or No.	Short answer of 1 or 2 words.	

effectively models combine information from multiple documents to answer general knowledge questions. It features diverse question types and tests the use of sentence-level evidence for accurate and explainable multi-hop reasoning.

3.4. Algorithmic Reasoning

We focus on applying LLMs to solve complex NP-hard and NP-complete tasks, requiring them to evaluate constraints and propose optimized algorithms that achieve practical and effective solutions. Such problems assess the application of LLMs to combinatorial optimization and resource allocation tasks (Liu et al., 2024; Romera-Paredes et al., 2024). We use **Game of 24** (Yao et al., 2024), and a novel dataset, **Bin Packing**.

Game of 24 is a dataset where the goal is to form an arithmetic expression evaluating to 24 using '+', '-', '*', or '/' with a list of four numbers. As an NP-complete problem with multiple solutions, it challenges an LLM to efficiently generate expressions by focusing only on operations that can lead to the target value.

Bin Packing is a novel dataset introduced by us, inspired by the combinatorial optimization problems studied by Liu et al. (2024); Romera-Paredes et al. (2024). In this task, the goal is to find the least number of bins needed to pack a list of items. Specifically, a list of N items of weight $[W_1, W_2, \dots, W_n]$ is given, which must be divided into bins $B_1, B_2, B_3, \dots, B_m$. The sum of weights in each bin must not exceed the bin capacity C , and the objective is to minimize the total number of bins m . Formally, the task can be written as:

$$\min m \text{ subject to } \begin{cases} \bigcup_{j=1}^m B_j = \{1, \dots, n\}, & B_j \cap B_{j'} = \emptyset \quad (\forall j \neq j'), \\ \sum_{i \in B_j} W_i \leq C \quad (\forall j). \end{cases} \quad (1)$$

3.5. Planning

A planning problem is defined by (S_0, A, G) , where S_0 stands for an initial state, A is the set of actions needed to achieve the goal G . Planning problems require LLMs to demonstrate multistep reasoning, and sound decision making to arrive at correct solutions. These problems have broad applications in robotics and agent-based systems. Our evaluation focuses on four planning problems: **BlocksWorld** (Valmeekam et al., 2023), **Rubik’s Cube** (Ding et al., 2024), **TripPlan**, and **CalendarPlan** (Zheng et al., 2024).

BlocksWorld is a popular dataset to evaluate the planning capabilities of LLMs. Each task involves transitioning from an initial block configuration to a target configuration, which requires LLMs to generate a sequence of actions to achieve the goal.

Rubik’s Cube requires an LLM to solve a scrambled 2×2 cube by restoring each face to a uniform color. Starting from a scrambled cube, the LLM must generate a valid plan of cube rotations to achieve the goal.

Trip Plan challenges an LLM to plan a travel itinerary that satisfies constraints on cities, dates, and flight connectivity, ensuring that all cities are visited as specified.

Calendar Plan is a dataset designed to schedule a meeting by aligning the availability of a group of people. The goal is to find a feasible time slot that accommodates all the constraints of the participants.

4. Sys2Bench Baseline Methods

In Sys2Bench we evaluate popular inference-time techniques commonly used to enhance System 2 abilities of LLMs. While these techniques have typically been applied to specific tasks, we analyze their performance comprehensively in Sys2Bench. Sys2Bench allows us to uncover patterns and limitations that may not be previously evident.

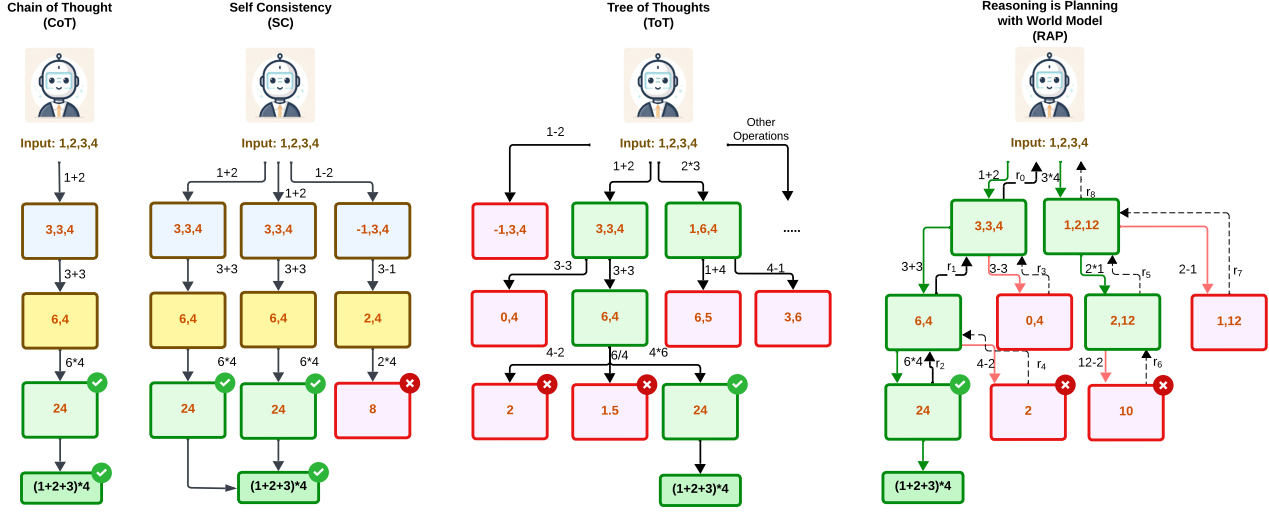


Figure 1. Overview of Inference-Time Techniques evaluated on the Game of 24 dataset. We evaluate four inference-time reasoning techniques. Chain of Thought (CoT) (Wei et al., 2022) solves problems through a linear sequence of reasoning steps. Self-Consistency (SC) (Wang et al., 2023) extends CoT by selecting answers through majority voting over multiple reasoning chains. Tree of Thoughts (ToT) (Yao et al., 2024) uses tree search to explore and expand reasoning paths. Reasoning as Planning (RAP) (Hao et al., 2023) combines Monte Carlo Tree Search (MCTS) with the LLM as a world model to reward reasoning steps and guide tree growth toward the answer.

We summarize these methods in Fig. 1.

Chain of Thought (CoT) enables LLMs to solve complex problems by breaking them into intermediate reasoning steps, improving their logical coherence and accuracy (Wei et al., 2022). CoT enhances structured problem-solving of LLMs by providing in-context examples of step-by-step reasoning during inference.

Self Consistency (SC) extends CoT by generating multiple reasoning paths for a problem and selecting the most consistent answer through majority voting (Wang et al., 2023).

Tree of Thoughts (ToT) uses structured tree search to enhance reasoning in LLMs by systematically exploring multiple paths, with the LLM evaluating its own intermediate generations to decide which paths to expand (Yao et al., 2024). Evaluation can be performed by rating LLM generation on a scale of 1-10 or using logits for scoring.

ToT has three search strategies: depth-first search (DFS), breadth-first search (BFS), and beam search. In our experiments, we use beam search because it performs the best amongst all variants.

Reasoning as Planning with World Models (RAP) reformulates reasoning as a planning problem, where the LLM acts as both the reasoning agent and the world model (Hao et al., 2023). The reasoning agent generates potential reasoning paths, while the world model simulates and evalu-

ates these paths. Specifically, RAP uses Monte Carlo Tree Search (MCTS) (Coulom, 2006) to explore and refine reasoning paths.

Unlike ToT, which does exhaustive tree search, RAP dynamically prioritizes high-potential paths using MCTS, resulting in improved performance. RAP requires logits for MCTS, which is why it is exclusively implemented on LLaMA. Since RAP requires extensive prompt engineering to frame all tasks as planning problems, we evaluate it on a subset of tasks, including GSM8K, AQuA, ProntoQA, StrategyQA, Game of 24, Binpacking, Blocksworld, and Rubik’s Cube.

5. Experiments

In this section, we present the experiments conducted on various tasks in the Sys2Bench benchmark. We begin by outlining the experimental setup, detailing the models and implementation specifics of the inference-time methods. Next, the results for the different inference-time methods are shown in Table 2 and Table 3.

5.1. Setup

In this subsection, we provide details about the experimental setup used to evaluate the performance of various inference-time techniques in Sys2Bench. We describe the models, the implementation specifics of the inference-time methods,

and the metrics used for evaluation.

Models evaluated in Sys2Bench, consist of three LLaMa 3.1 models, two GPT-based models, and two large reasoning models (LRMs). The LLaMa 3.1 variants are 8B, 70B, and 405B, while the GPT-based models include GPT-4o and GPT-4o-mini. Additionally, the O1 and O1-mini models are tested as part of our LRM evaluation. By default, we use a temperature of 0.8 across all models for generation.

Chain of Thought (CoT) involves including in-context learning examples in the prompt. In our benchmark, we limit this to five examples per prompt. These examples are selected from the in-context examples provided by the dataset or the training set. If neither is available, we use a subset of test examples and evaluate the remaining test instances.

Self Consistency (SC) follows the same settings as CoT. We generate five CoT responses from the LLM and determine the final output through majority voting.

Tree of Thought (ToT) implementation in Sys2Bench uses beam search. The beam size is 5 for most tasks except planning tasks, where the number of possible actions at each state is larger, thus, the beam size is increased to 10. By default, beam ranking is performed by asking the LLM to rate outputs on a scale of 1 to 10, except for LLaMa 3.1 8B, where logits are used instead. Finally, the search depth is task-dependent, ranging from 4 for Game of 24 to 20 for Trip Plan.

Reasoning as Planning (RAP) uses Monte Carlo Tree Search (MCTS) with up to 10 rollouts during inference. Due to its reliance on a reward model that requires logits, RAP is implemented exclusively on LLaMa 3.1 8B. Similar to ToT, the search depth in RAP varies depending on the task.

Input Output Prompting (IO) is utilized with LRMs, as they generate their own reasoning steps and do not require in-context learning examples. Instead, we provide the necessary format and instruct the models to respond in the same format.

Metric used across all tasks is accuracy. Note that the context of accuracy differs depending each task. For arithmetic, commonsense, and algorithmic reasoning tasks, accuracy is measured on the correctness of the final answer. Logical reasoning tasks, namely, ProntoQA, accuracy measures the ability of an LLM to generate the correct reasoning chain. Finally, for planning tasks, accuracy measures the correctness of the proposed plan.

5.2. Results

In this subsection, we present the results of the Sys2Bench benchmark, organized by the types of reasoning outlined in

Section 3. This grouping allows for a clearer comparison of performance across tasks, demonstrating the strengths and limitations of different inference-time techniques.

Arithmetic Reasoning tasks in Table 2 have strong results with CoT. Performance further improves with SC, as it reduces the impact of randomness in the CoT answers. However, this strong performance does not transfer to tree search methods. ToT significantly underperforms on this task, as its approach of prompting the LLM to explore multiple reasoning paths relies on the LLM generating and selecting correct intermediate reasoning steps. Since LRMs struggle with self-verification (Huang et al., 2024), it selects incorrect intermediate arithmetic steps, leading to wrong answers. In contrast, RAP shows modest gains on the GSM8K dataset, benefiting from the LLM’s role as a world model to select better arithmetic steps. However, RAP still underperforms SC on AQuA, indicating that tree search methods are not well-suited for arithmetic reasoning tasks. Meanwhile, LRMs deliver exceptional arithmetic reasoning performance, as shown in Table 3, highlighting their strength in arithmetic.

Logical Reasoning results in Table 2 show interesting trends. For instance, SC improves performance over CoT on LLaMa 3.1 8B and 70B. However, for LLaMa 3.1 405B and GPT-based models, SC results in performance drops, as it increases the likelihood of generating multiple incorrect reasoning chains in the ProntoQA task, where evaluation focuses on the accuracy of these chains. Majority voting does not help when the LLM outputs multiple wrong reasoning chains. Consistent with arithmetic reasoning, tree search methods such as ToT and RAP also underperform in this task, indicating their limitations in logical reasoning. Finally, as shown in Table 3, LRMs do not consistently outperform LLMs on this task, with O1 performing worse than GPT-4o on this task.

Common Sense Reasoning performance of CoT and SC improves with increasing LLM size. However, tree search methods show unique trends. Specifically, both RAP and ToT generate supporting facts for each question, but their effectiveness varies by task. To be specific, in StrategyQA, the binary output (yes or no) enables LLaMA models to effectively utilize the generated facts, leading to improved performance. In contrast, for HotPotQA, tree search is not effective as the LLM needs to output short answers. Additional facts often cause LLM hallucinations and increased error rates. Furthermore, compared to other tasks, performance improvements seen with LRMs are limited (see Table 3).

Algorithmic Reasoning tasks include the Game of 24 and Binpacking datasets, as described in Section 3. Table 2 shows that both CoT and SC underperform on these tasks. Due to the combinatorial optimization nature of these tasks,

that require extensive search, tree search methods perform well on all models, except LLaMa 3.1 8B. The smaller size of LLaMa 3.1 8B limits the model to accurately evaluate and determine the next steps toward a solution. When comparing LLMs to LRMs, results in Table 3 highlight the potential of O1-mini and O1 in solving NP-Hard and NP-Complete problems, with O1 slightly underperforming O1-mini on Game of 24.

Planning tasks are the most challenging in Sys2Bench. Generally, CoT and SC performance improves with larger model sizes, and SC consistently outperforming CoT.

Tree search methods show mixed results across tasks and models. On smaller models, such as LLaMa 3.1 8B and GPT-4o-mini, ToT shows improvements on tasks like Blocksworld and TripPlan. However for larger models and other tasks, ToT often decreases performance. This is because planning tasks require LLMs to generate actions to solve problems, and incorrect actions can lead to incorrect solutions. Although ToT is intended to help LLMs explore multiple reasoning paths, which in planning means considering different actions, LLMs often fail to generate accurate actions, ultimately reducing performance. The other tree search method, RAP, performs exceptionally well on Blocksworld by leveraging the LLM as a world model to predict future states and rewards.

Compared to LLMs, LRMs perform significantly better on planning tasks, with O1 achieving near-perfect results on Blocksworld. However, the Rubik’s Cube task remains challenging for all methods and models, as it requires advanced spatial reasoning and precise prediction of the consequences of each action. Both LLMs and LRMs currently lack the reasoning capabilities needed for this task, making it out-of-distribution (OOD) for current language models.

5.3. Insights

We extend our main experiments to provide additional insights and uncover important trends. As the research community shows increasing interest in inference-time techniques and improving LLM reasoning, these findings offer valuable contributions to ongoing discussions.

Inference-time compute scaling is limited by LLM bias.

These techniques aim to improve LLM reasoning by guiding them to generate intermediate steps, simplifying complex tasks into smaller, manageable parts. However, this premise is flawed as LLMs do not exhaustively search for all reasoning paths and remain biased toward certain ones. As inference-time compute scales, this bias persists, limiting exploration and leading to diminished performance. As task complexity increases, this issue becomes worse, exacerbating errors in reasoning and decision-making.

Our Sys2Bench experiments show this trend in arithmetic

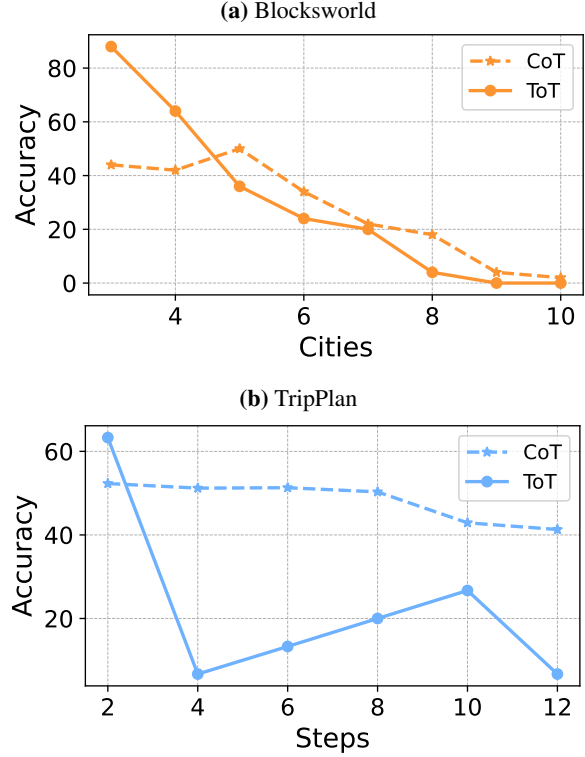


Figure 2. Tree of Thought (ToT) performance declines as task complexity increases. In (a) Blocksworld and (b) TripPlan, the number of steps or cities is the required tree depth for LLM inference-time search. While ToT performs well for smaller depths, performance deteriorates as problem complexity grows, eventually falling below CoT. Notably, CoT achieves better performance with significantly lower computational resources, as shown in Table 4. These results are on the LLaMa 405B model.

and logical reasoning. In these tasks, LLMs excel with CoT but struggle with tree search, failing to explore reasoning paths and select the correct one.

Tree search struggles with increasing complexity, performing significantly worse than CoT. As shown in Fig 2, its benefits diminish beyond a depth of 4 for the TripPlaning and Blocksworld tasks on LLaMa 3.1 405B. Note that, LLaMa 3.1 405B has a strong CoT performance in challenging planning tasks and ideally ToT should lead to further improvements. However, as complexity grows, generating the right intermediate steps becomes crucial, leading to worse performance of ToT compared to CoT. A potential explanation for this observation is the inherent bias of LLMs at each step of the reasoning process. These biases may propagate through successive steps, leading to cumulative errors that degrade ToT performance.

Language models rely on retrieval rather than true understanding. Despite advancements in reasoning abilities with LRMs such as O1 and O1-Mini, they still appear to be

Table 2. Results of Inference Time Techniques across diverse tasks show that as model size increases, performance of CoT (CoT) (Wei et al., 2022) and Self Consistency (SC) (Wang et al., 2023) improves. However, this trend doesn’t extend to tree search methods like Tree of Thought (ToT) (Yao et al., 2024), where performance does not improve with the bigger models. Furthermore, a comparison between ToT and Reasoning as Planning with World Models (RAP) (Hao et al., 2023) shows that RAP outperforms ToT in planning and arithmetic reasoning tasks but lags in commonsense reasoning while performing equally in algorithmic reasoning tasks. All methods and LLMs fail to solve the Rubik’s Cube planning task. This failure can be attributed to the spatial understanding capabilities required for the task, which are currently out of distribution (OOD) for existing LLMs.

Methods	Algorithmic Reasoning										Logical Reasoning					
	GSM8K					AQuA					ProntoQA					
	LLaMa 3.1					GPT					LLaMa 3.1					
	8B	70B	405B	4o mini	4o	8B	70B	405B	4o mini	4o	8B	70B	405B	4o mini	4o	
Chain of Thought Methods																
CoT	79.8	95.5	97.0	92.6	94.7	58.7	77.2	78.0	73.6	79.9	45.8	82.6	91.0	61.4	91.8	
SC @ 5	86.7	96.5	97.5	93.3	94.9	70.9	85.8	86.2	79.9	83.9	54.2	88.4	89.0	58.0	91.4	
Tree Search Methods																
ToT	60.0	91.5	96.0	91.5	93.5	44.8	78.0	85.8	81.1	78.0	13.5	24.2	62.6	42.0	32.8	
RAP	87.3	—	—	—	—	68.1	—	—	—	—	0.0	—	—	—	—	—
	Common Sense Reasoning										Algorithmic Reasoning					
	HotPotQA					StrategyQA					Game of 24					
	LLaMa 3.1					GPT					LLaMa 3.1					
	8B	70B	405B	4o mini	4o	8B	70B	405B	4o mini	4o	8B	70B	405B	4o mini	4o	
Chain of Thought Methods																
CoT	13.8	30.6	41.0	38.6	52.8	46.0	61.5	76.0	76.6	79.2	6.0	8.0	7.0	13.0	14.0	6.0
SC @ 5	20.6	36.6	45.6	40.6	52.6	53.5	66.0	78.5	76.0	79.8	6.0	8.0	6.0	15.0	18.0	6.0
Tree Search Methods																
ToT	23.0	30.0	31.5	31.4	38.2	68.0	82.0	79.5	67.5	73.5	1.0	59.0	69.0	42.0	62.0	1.0
RAP	—	—	—	—	—	58.5	—	—	—	—	1.0	—	—	—	—	1.0
	Planning										Rubik’s Cube					
	Blocksworld					Trip Plan					Calendar Plan					
	LLaMa 3.1					GPT					LLaMa 3.1					
	8B	70B	405B	4o mini	4o	8B	70B	405B	4o mini	4o	8B	70B	405B	4o mini	4o	
Chain of Thought Methods																
CoT	3.5	26.1	48.7	18.4	37.5	12.3	29.5	27.0	5.3	6.3	10.4	31.2	44.8	26.0	47.0	0.6
SC @ 5	4.5	30.7	52.1	21.2	41.5	12.0	32.3	34.3	5.0	5.8	11.6	38.0	45.6	29.6	47.4	0.6
Tree Search Methods																
ToT	13.9	4.6	19.9	23.1	12.4	2.0	32.5	29.5	7.8	19.5	16.8	32.0	40.0	29.0	41.4	0.6
RAP	46.8	—	—	—	—	—	—	—	—	—	—	—	—	—	—	0.6

pattern matching rather than genuine reasoning. This issue has been observed in prior studies for LLMs (Valmeekam et al., 2023), but we are the first to demonstrate it for LRMs, including O1 and O1-Mini. As shown in Fig. 3, we compare GPT-4o, O1-Mini, and O1 based on how frequently their generated moves in the Rubik’s Cube task align with known online algorithms. Our analysis shows that GPT-4o and O1-Mini repeat these popular moves in nearly all cases, with rates of 75% and 90%, respectively. While O1 performs better, it still follows common move sequences about 20% of the time.

There is a tradeoff between performance and the cost of inference-time methods. Table 4 includes results across Blocksworld, Game of 24, and GSM8K using LLaMa 3.1 8B, along with the number of tokens generated per task. We present more comparisons for other models in Table 13 and 14. Compared to CoT and SC, ToT and RAP have significantly higher computational costs. However, increased token usage does not mean better performance. Addition-

ally, solving 100 Game of 24 problems with GPT-4o and ToT costs around \$60 due to high token usage, with costs rising for larger models and harder tasks. This tradeoff highlights our position that increasing inference-time computation does not always yield proportional gains.

6. Alternate Views and Discussions

Contrary to our position, there is growing interest in scaling inference-time computation to enhance LLM performance (Snell et al., 2024). These methods have demonstrated strong results in arithmetic (Kumar et al., 2024a) and gameplay tasks (Schultz et al., 2024). However, these improvements rely on verifiers or external models to guide reasoning, and without them, performance gains disappear. Moreover, tasks like Common Sense Reasoning lack verifiers, highlighting the limitation of verifier-dependent inference-time scaling.

On the other hand, LRMs like O1 leverage reinforcement

Table 3. Results of large reasoning models (LRMs). We report the results of IO prompting on LRMs, including OpenAI O1-mini and O1, without providing any in-context learning examples, as recommended by OpenAI (OpenAI, 2024). Overall, LRMs achieve state-of-the-art performance, with O1 outperforming O1-mini on all tasks except the Game of 24. Similar to LLMs, LRMs also struggle with the Rubik’s Cube task, indicating a lack of spatial understanding.

	Arithmetic Reasoning		Logical Reasoning	Common Sense Reasoning		Algorithmic Reasoning	Planning				
	GSM8K	AQuA	ProntoQA	HotPotQA	StrategyQA	Game of 24	Binpacking	Blocksworld	Trip Plan	Calendar Plan	Rubik’s Cube
O1 Mini	98.0	92.0	64.0	35.0	74.0	77.0	90.0	48.3	24.0	88.2	0.0
O1	98.0	91.0	74.0	59.0	81.0	73.0	99.0	99.2	58.3	90.0	0.6

learning (RL) with inference-time search to improve reasoning (OpenAI, 2024; Zhao et al., 2024b). These models are trained to generate correct reasoning steps, enabling better performance (see Table 2). Despite significant gains, our experiments highlight limitations, particularly in planning and common sense reasoning tasks. With inference costs reaching $60\times$ that of standard LLMs, it is crucial to assess their limitations.

In contrast to alternative views, we argue that simply scaling inference-time computation is not the solution. Instead, improving LLM reasoning requires a more strategic approach, and combination of RL with inference-time methods has been promising (DeepSeek-AI et al., 2025). The recent release of DeepSeek-R1 hints at progress in this direction, offering a glimpse of what more refined models could achieve in the future.

7. Conclusion

This position paper examines the impact of scaling inference-time computation on improving the reasoning and planning abilities of LLMs. Our position is that scaling inference-time computation has limitations. Instead, we need to explore diverse approaches to enhance the holistic reasoning capabilities of LLMs. We explore this by introducing Sys2Bench, a new benchmark, and conduct extensive experiments evaluating inference-time techniques across eleven diverse tasks spanning five categories, namely, arithmetic reasoning, logical reasoning, common sense reasoning, algorithmic reasoning, and planning. Our findings provide important insights into the limitations of inference-time techniques. Finally, we discuss alternative perspectives from the literature, critically analyze their implications, and outline potential directions for future research.

Impact Statement

This paper presents work whose goal is to advance the field of Large Language Model reasoning and planning. There are many potential societal consequences of our work, none which we feel must be specifically highlighted here.

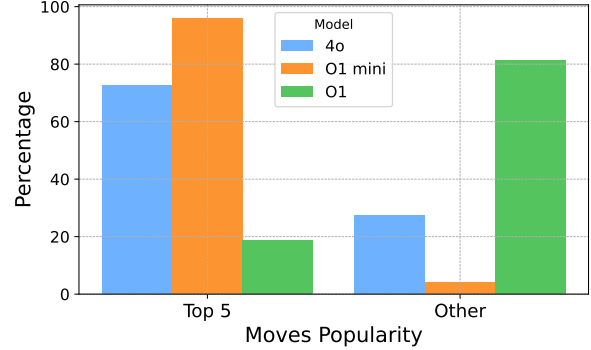


Figure 3. Moves are grouped based on their popularity in online Rubik’s Cube solutions. LLMs like GPT-4o frequently generate moves commonly found in online algorithms. This issue is even more pronounced in O1-mini, where nearly 90% of the moves are repeated! O1 exhibits this behavior less frequently, but it remains a notable pattern.

Table 4. Token count comparison of CoT, SC, ToT, and RAP on LLaMA 3.1 8B across Blocksworld, Game of 24, and GSM8K. The results highlight that scaling up inference-time techniques increases computational cost without proportionate performance gains, contrasting with the trends observed by Snell et al. (2024).

	Blocksworld		Game of 24		GSM8K	
	Accuracy ↑	Tokens ↓	Accuracy ↑	Tokens ↓	Accuracy ↑	Tokens ↓
CoT	3.5	3.2×10^4	6.0	8.0×10^3	79.8	1.9×10^4
SC	4.5	1.7×10^5	6.0	4.0×10^4	86.7	2.4×10^5
ToT	13.9	1.1×10^6	1.0	3.6×10^7	60.0	4.4×10^6
RAP	46.8	4.9×10^5	1.0	1.5×10^7	87.3	9.9×10^6

References

- Barwise, J. An introduction to first-order logic. In *Studies in Logic and the Foundations of Mathematics*, volume 90, pp. 5–46. Elsevier, 1977.
- Besta, M., Blach, N., Kubicek, A., Gerstenberger, R., Podstawski, M., Gianinazzi, L., Gajda, J., Lehmann, T., Niewiadomski, H., Nyczyk, P., et al. Graph of thoughts: Solving elaborate problems with large language models. In *Proceedings of the AAAI Conference on Artificial Intelligence*, volume 38, pp. 17682–17690, 2024.
- Brown, T., Mann, B., Ryder, N., Subbiah, M., Kaplan, J.,

- Dhariwal, P., Neelakantan, A., Shyam, P., Sastry, G., Askell, A., et al. Language models are few-shot learners. In *Advances in Neural Information Processing Systems (NeurIPS)*, volume 33, pp. 1877–1901, 2020.
- Chollet, F. On the measure of intelligence. *arXiv preprint arXiv:1911.01547*, 2019.
- Cobbe, K., Kosaraju, V., Bavarian, M., Chen, M., Jun, H., Kaiser, L., Plappert, M., Tworek, J., Hilton, J., Nakano, R., Hesse, C., and Schulman, J. Training verifiers to solve math word problems. *arXiv preprint arXiv:2110.14168*, 2021.
- Coulom, R. Efficient selectivity and backup operators in monte-carlo tree search. In *International conference on computers and games*, pp. 72–83. Springer, 2006.
- DeepSeek-AI, Guo, D., Yang, D., Zhang, H., Song, J., Zhang, R., Xu, R., Zhu, Q., Ma, S., Wang, P., Bi, X., Zhang, X., Yu, X., Wu, Y., Wu, Z. F., Gou, Z., Shao, Z., Li, Z., Gao, Z., Liu, A., Xue, B., Wang, B., Wu, B., Feng, B., Lu, C., Zhao, C., Deng, C., Zhang, C., Ruan, C., Dai, D., Chen, D., Ji, D., Li, E., Lin, F., Dai, F., Luo, F., Hao, G., Chen, G., Li, G., Zhang, H., Bao, H., Xu, H., Wang, H., Ding, H., Xin, H., Gao, H., Qu, H., Li, H., Guo, J., Li, J., Wang, J., Chen, J., Yuan, J., Qiu, J., Li, J., Cai, J. L., Ni, J., Liang, J., Chen, J., Dong, K., Hu, K., Gao, K., Guan, K., Huang, K., Yu, K., Wang, L., Zhang, L., Zhao, L., Wang, L., Zhang, L., Xu, L., Xia, L., Zhang, M., Zhang, M., Tang, M., Li, M., Wang, M., Li, M., Tian, N., Huang, P., Zhang, P., Wang, Q., Chen, Q., Du, Q., Ge, R., Zhang, R., Pan, R., Wang, R., Chen, R. J., Jin, R. L., Chen, R., Lu, S., Zhou, S., Chen, S., Ye, S., Wang, S., Yu, S., Zhou, S., Pan, S., Li, S. S., Zhou, S., Wu, S., Ye, S., Yun, T., Pei, T., Sun, T., Wang, T., Zeng, W., Zhao, W., Liu, W., Liang, W., Gao, W., Yu, W., Zhang, W., Xiao, W. L., An, W., Liu, X., Wang, X., Chen, X., Nie, X., Cheng, X., Liu, X., Xie, X., Liu, X., Yang, X., Li, X., Su, X., Lin, X., Li, X. Q., Jin, X., Shen, X., Chen, X., Sun, X., Wang, X., Song, X., Zhou, X., Wang, X., Shan, X., Li, Y. K., Wang, Y. Q., Wei, Y. X., Zhang, Y., Xu, Y., Li, Y., Zhao, Y., Sun, Y., Wang, Y., Yu, Y., Zhang, Y., Shi, Y., Xiong, Y., He, Y., Piao, Y., Wang, Y., Tan, Y., Ma, Y., Liu, Y., Guo, Y., Ou, Y., Wang, Y., Gong, Y., Zou, Y., He, Y., Xiong, Y., Luo, Y., You, Y., Liu, Y., Zhou, Y., Zhu, Y. X., Xu, Y., Huang, Y., Li, Y., Zheng, Y., Zhu, Y., Ma, Y., Tang, Y., Zha, Y., Yan, Y., Ren, Z. Z., Ren, Z., Sha, Z., Fu, Z., Xu, Z., Xie, Z., Zhang, Z., Hao, Z., Ma, Z., Yan, Z., Wu, Z., Gu, Z., Zhu, Z., Liu, Z., Li, Z., Xie, Z., Song, Z., Pan, Z., Huang, Z., Xu, Z., Zhang, Z., and Zhang, Z. Deepseek-r1: Incentivizing reasoning capability in llms via reinforcement learning, 2025. URL <https://arxiv.org/abs/2501.12948>.
- Deng, X., Gu, Y., Zheng, B., Chen, S., Stevens, S., Wang, B., Sun, H., and Su, Y. Mind2web: Towards a generalist agent for the web. *Advances in Neural Information Processing Systems*, 36, 2024.
- Devlin, J., Chang, M.-W., Lee, K., and Toutanova, K. BERT: Pre-training of deep bidirectional transformers for language understanding. In *Proceedings of the 2019 Conference of the North American Chapter of the Association for Computational Linguistics: Human Language Technologies*, pp. 4171–4186, 2019. URL <https://arxiv.org/abs/1810.04805>.
- Ding, R., Zhang, C., Wang, L., Xu, Y., Ma, M., Zhang, W., Qin, S., Rajmohan, S., Lin, Q., and Zhang, D. Everything of thoughts: Defying the law of penrose triangle for thought generation. In Ku, L.-W., Martins, A., and Srikumar, V. (eds.), *Findings of the Association for Computational Linguistics: ACL 2024*, pp. 1638–1662, Bangkok, Thailand, August 2024. Association for Computational Linguistics. doi: 10.18653/v1/2024.findings-acl.95. URL <https://aclanthology.org/2024.findings-acl.95/>.
- Geva, M., Khashabi, D., Segal, E., Khot, T., Roth, D., and Berant, J. Did aristotle use a laptop? a question answering benchmark with implicit reasoning strategies. *Transactions of the Association for Computational Linguistics*, 9: 346–361, 2021.
- Hao, S., Gu, Y., Ma, H., Hong, J. J., Wang, Z., Wang, D. Z., and Hu, Z. Reasoning with language model is planning with world model. In *The 2023 Conference on Empirical Methods in Natural Language Processing*, 2023. URL <https://openreview.net/forum?id=VTWWvYtFlR>.
- Hao, S., Gu, Y., Luo, H., Liu, T., Shao, X., Wang, X., Xie, S., Ma, H., Samavedhi, A., Gao, Q., et al. Llm reasoners: New evaluation, library, and analysis of step-by-step reasoning with large language models. *arXiv preprint arXiv:2404.05221*, 2024.
- Hendrycks, D., Burns, C., Kadavath, S., Arora, A., Basart, S., Tang, E., Song, D., and Steinhardt, J. Measuring mathematical problem solving with the math dataset. *arXiv preprint arXiv:2103.03874*, 2021.
- Huang, J., Chen, X., Mishra, S., Zheng, H. S., Yu, A. W., Song, X., and Zhou, D. Large language models cannot self-correct reasoning yet. In *The Twelfth International Conference on Learning Representations*, 2024. URL <https://openreview.net/forum?id=Ikmd3fKBPQ>.
- Huang, W., Abbeel, P., Pathak, D., and Mordatch, I. Language models as zero-shot planners: Extracting actionable knowledge for embodied agents. In *International*

- conference on machine learning, pp. 9118–9147. PMLR, 2022.
- Kambhampati, S., Valmeekam, K., Guan, L., Verma, M., Stechly, K., Bhambri, S., Saldyt, L. P., and Murthy, A. B. Position: Llms can’t plan, but can help planning in llm-modulo frameworks. In *Forty-first International Conference on Machine Learning*, 2024.
- Kojima, T., Gu, S. S., Reid, M., Matsuo, Y., and Iwasawa, Y. Large language models are zero-shot reasoners. *Advances in neural information processing systems*, 35: 22199–22213, 2022.
- Kumar, A., Zhuang, V., Agarwal, R., Su, Y., Co-Reyes, J. D., Singh, A., Baumli, K., Iqbal, S., Bishop, C., Roelofs, R., Zhang, L. M., McKinney, K., Shrivastava, D., Paduraru, C., Tucker, G., Precup, D., Behbahani, F., and Faust, A. Training language models to self-correct via reinforcement learning, 2024a. URL <https://arxiv.org/abs/2409.12917>.
- Kumar, A., Zhuang, V., Agarwal, R., Su, Y., Co-Reyes, J. D., Singh, A., Baumli, K., Iqbal, S., Bishop, C., Roelofs, R., et al. Training language models to self-correct via reinforcement learning. *arXiv preprint arXiv:2409.12917*, 2024b.
- Lin, Z., Pathak, D., Li, B., Li, J., Xia, X., Neubig, G., Zhang, P., and Ramanan, D. Evaluating text-to-visual generation with image-to-text generation. In *European Conference on Computer Vision*, pp. 366–384. Springer, 2025.
- Ling, W., Yogatama, D., Dyer, C., and Blunsom, P. Program induction by rationale generation: Learning to solve and explain algebraic word problems. In Barzilay, R. and Kan, M.-Y. (eds.), *Proceedings of the 55th Annual Meeting of the Association for Computational Linguistics (Volume 1: Long Papers)*, pp. 158–167, Vancouver, Canada, July 2017. Association for Computational Linguistics. doi: 10.18653/v1/P17-1015. URL <https://aclanthology.org/P17-1015/>.
- Liu, B., Jiang, Y., Zhang, X., Liu, Q., Zhang, S., Biswas, J., and Stone, P. Llm+p: Empowering large language models with optimal planning proficiency. *arXiv preprint arXiv:2304.11477*, 2023.
- Liu, F., Xialiang, T., Yuan, M., Lin, X., Luo, F., Wang, Z., Lu, Z., and Zhang, Q. Evolution of heuristics: Towards efficient automatic algorithm design using large language model. In *Forty-first International Conference on Machine Learning*, 2024.
- OpenAI. Openai o1 system card, 2024. URL <https://openai.com/index/openai-o1-system-card/>.
- Parashar, S., Lin, Z., Liu, T., Dong, X., Li, Y., Ramanan, D., Caverlee, J., and Kong, S. The neglected tails in vision-language models. In *Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition*, pp. 12988–12997, 2024.
- Radford, A., Narasimhan, K., Salimans, T., and Sutskever, I. Improving language understanding by generative pre-training. *OpenAI*, 2018. URL https://cdn.openai.com/research-covers/language-unsupervised/language_understanding_paper.pdf.
- Romera-Paredes, B., Barekatin, M., Novikov, A., Balog, M., Kumar, M. P., Dupont, E., Ruiz, F. J., Ellenberg, J. S., Wang, P., Fawzi, O., et al. Mathematical discoveries from program search with large language models. *Nature*, 625 (7995):468–475, 2024.
- Saparov, A. and He, H. Language models are greedy reasoners: A systematic formal analysis of chain-of-thought. In *The Eleventh International Conference on Learning Representations*, 2023. URL <https://openreview.net/forum?id=qFVVBzXxR2V>.
- Schultz, J., Adamek, J., Jusup, M., Lanctot, M., Kaisers, M., Perrin, S., Hennes, D., Shar, J., Lewis, C., Ruoss, A., Zahavy, T., Veličković, P., Prince, L., Singh, S., Malmi, E., and Tomašev, N. Mastering board games by external and internal planning with language models, 2024. URL <https://arxiv.org/abs/2412.12119>.
- Snell, C., Lee, J., Xu, K., and Kumar, A. Scaling llm test-time compute optimally can be more effective than scaling model parameters. *arXiv preprint arXiv:2408.03314*, 2024.
- Valmeekam, K., Marquez, M., Sreedharan, S., and Kambhampati, S. On the planning abilities of large language models—a critical investigation. *Advances in Neural Information Processing Systems*, 36:75993–76005, 2023.
- Valmeekam, K., Stechly, K., and Kambhampati, S. Llms still can’t plan; can llms? a preliminary evaluation of openai’s o1 on planbench. *arXiv preprint arXiv:2409.13373*, 2024.
- Vaswani, A., Shazeer, N., Parmar, N., Uszkoreit, J., Jones, L., Gomez, A. N., Kaiser, , and Polosukhin, I. Attention is all you need. In *Advances in Neural Information Processing Systems*, volume 30, 2017. URL <https://arxiv.org/abs/1706.03762>.
- Wang, L., Ma, C., Feng, X., Zhang, Z., Yang, H., Zhang, J., Chen, Z., Tang, J., Chen, X., Lin, Y., et al. A survey on large language model based autonomous agents. *Frontiers of Computer Science*, 18(6):186345, 2024.

- Wang, S., Liu, Z., Zhong, W., Zhou, M., Wei, Z., Chen, Z., and Duan, N. From lsat: The progress and challenges of complex reasoning. *IEEE/ACM Transactions on Audio, Speech, and Language Processing*, 2022.
- Wang, X., Wei, J., Schuurmans, D., Le, Q. V., Chi, E. H., Narang, S., Chowdhery, A., and Zhou, D. Self-consistency improves chain of thought reasoning in language models. In *The Eleventh International Conference on Learning Representations*, 2023. URL <https://openreview.net/forum?id=1PLlNIMMrw>.
- Wei, J., Wang, X., Schuurmans, D., Bosma, M., Xia, F., Chi, E., Le, Q. V., Zhou, D., et al. Chain-of-thought prompting elicits reasoning in large language models. *Advances in neural information processing systems*, 35:24824–24837, 2022.
- Welleck, S., Bertsch, A., Finlayson, M., Schoelkopf, H., Xie, A., Neubig, G., Kulikov, I., and Harchaoui, Z. From decoding to meta-generation: Inference-time algorithms for large language models. *Transactions on Machine Learning Research*, 2024. ISSN 2835-8856. URL <https://openreview.net/forum?id=eskQMcIbMS>. Survey Certification.
- Wu, H., Chen, X., Lin, Y.-C., Chang, K.-w., Chung, H.-L., Liu, A. H., and Lee, H.-y. Towards audio language modeling—an overview. *arXiv preprint arXiv:2402.13236*, 2024.
- Xie, J., Zhang, K., Chen, J., Zhu, T., Lou, R., Tian, Y., Xiao, Y., and Su, Y. Travelplanner: A benchmark for real-world planning with language agents. In *Forty-first International Conference on Machine Learning*, 2024.
- Yang, Z., Qi, P., Zhang, S., Bengio, Y., Cohen, W. W., Salakhutdinov, R., and Manning, C. D. Hotpotqa: A dataset for diverse, explainable multi-hop question answering. *arXiv preprint arXiv:1809.09600*, 2018.
- Yang, Z., Jia, X., Li, H., and Yan, J. Llm4drive: A survey of large language models for autonomous driving. In *NeurIPS 2024 Workshop on Open-World Agents*, 2023.
- Yao, S., Yu, D., Zhao, J., Shafran, I., Griffiths, T., Cao, Y., and Narasimhan, K. Tree of thoughts: Deliberate problem solving with large language models. *Advances in Neural Information Processing Systems*, 36, 2024.
- Zhao, Y., Yin, H., Zeng, B., Wang, H., Shi, T., Lyu, C., Wang, L., Luo, W., and Zhang, K. Marco-o1: Towards open reasoning models for open-ended solutions. *arXiv preprint arXiv:2411.14405*, 2024a.
- Zhao, Y., Yin, H., Zeng, B., Wang, H., Shi, T., Lyu, C., Wang, L., Luo, W., and Zhang, K. Marco-o1: Towards open reasoning models for open-ended solutions, 2024b. URL <https://arxiv.org/abs/2411.14405>.
- Zheng, H. S., Mishra, S., Zhang, H., Chen, X., Chen, M., Nova, A., Hou, L., Cheng, H.-T., Le, Q. V., Chi, E. H., et al. Natural plan: Benchmarking llms on natural language planning. *arXiv preprint arXiv:2406.04520*, 2024.
- Zhou, A., Yan, K., Shlapentokh-Rothman, M., Wang, H., and Wang, Y.-X. Language agent tree search unifies reasoning, acting, and planning in language models. In *ICML*, 2024. URL <https://openreview.net/forum?id=njwv9BsGHF>.
- Zhou, D., Schärli, N., Hou, L., Wei, J., Scales, N., Wang, X., Schuurmans, D., Cui, C., Bousquet, O., Le, Q. V., and Chi, E. H. Least-to-most prompting enables complex reasoning in large language models. In *The Eleventh International Conference on Learning Representations*, 2023. URL <https://openreview.net/forum?id=WZH7099tgfM>.

Position: Inference-Time Computations for LLM Reasoning and Planning: A Benchmark and Insights

Appendix

Outline

This document supplements the main paper with additional experiments and results. Below outlines the document.

- **Section A.** We provide a breakdown of results on Blocksworld, Bin packing, CalendarPlan and TripPlan highlighting performance with increasing complexity.
- **Section B.** We analyze the tradeoff between inference-time techniques, token usage, and performance for GPT-4o and LLaMa 405B.

A. Results Breakdown

This section presents a detailed breakdown of results for Blocksworld, Bin Packing, CalendarPlan, and TripPlan. These tasks vary in complexity, and the results indicate that performance declines as problem size increases. We present results on GPT 4o-mini, GPT 4o, LLaMa 3.1 8B, and OpenAI O1.

Table 5. 4o-mini results breakdown on Blocksworld and Binpacking

Methods	Blocksworld						Bin packing				
	Steps						Items				
	2	4	6	8	10	12	5	6	7	8	9
CoT	38.3	26.7	26.5	13.1	8.0	0.0	50.0	40.0	30.0	15.0	20.0
CoT - SC	55.3	36.1	30.3	12.4	4.4	0.0	55.0	40.0	40.0	35.0	35.0
ToT	71.1	10.0	26.3	16.6	20.5	17.4	60.0	70.0	50.0	55.0	30.0

Table 6. 4o-mini results breakdown on Calendar Plan and Trip Plan.

Methods	CalendarPlan					TripPlan							
	Days					Cities							
	1	2	3	4	5	3	4	5	6	7	8	9	10
CoT	31.0	33.0	28.0	23.0	15.0	26.0	10.0	0.0	6.0	0.0	0.0	0.0	0.0
CoT - SC	28.0	42.0	36.0	22.0	20.0	24.0	14.0	0.0	2.0	0.0	0.0	0.0	0.0
ToT	40.0	36.0	35.0	19.0	15.0	36.0	18.0	6.0	2.0	0.0	0.0	0.0	0.0

Table 7. 4o results breakdown on Blocksworld and Binpacking

Methods	Blocksworld						Bin packing				
	Steps						Bins				
	2	4	6	8	10	12	5	6	7	8	9
CoT	68.1	45.4	52.3	28.1	19.5	19.6	85.0	90.0	70.0	75.0	55.0
CoT - SC	63.8	39.5	57.4	35.3	26.5	28.2	100.0	90.0	90.0	80.0	70.0
ToT	75.5	21.4	10	1.3	2.7	2.2	100.0	85.0	75.0	65.0	60.0

Table 8. 4o results breakdown on Calendar Plan and TripPlan

Methods	CalendarPlan					TripPlan							
	Days					Cities							
	1	2	3	4	5	3	4	5	6	7	8	9	10
CoT	49.0	52.0	46.0	47.0	41.0	28.0	18.0	4.0	0.0	0.0	0.0	0.0	0.0
CoT - SC	48.0	56.0	46.0	45.0	42.0	16.0	22.0	6.0	0.0	0.0	0.0	2.0	0.0
ToT	42.0	40.0	39.0	44.0	42.0	64.0	36.0	30.0	14.0	2.0	6.0	2.0	2.0

Table 9. 8B results breakdown on Blocksworld and Bin Packing

Methods	Blocksworld						Bin packing				
	Steps						Bins				
	2	4	6	8	10	12	5	6	7	8	9
CoT	14.9	10.5	2.6	0.0	0.9	0.0	25.0	5.0	0.0	0.0	0.0
CoT - SC	19.2	11.6	3.2	2.0	0.0	0.0	15.0	10.0	5.0	0.0	0.0
ToT	33.3	25	15.1	11.3	4.5	2.2	0.0	0.0	5.0	0.0	0.0

B. Inference-time Methods Tradeoff on big LLMs

This section examines the tradeoff between scaling inference-time compute and performance in reasoning and planning tasks for LLaMa 405B and GPT-4o.

Table 10. 8B results breakdown on Calendar Plan and TripPlan

Methods	CalendarPlan					TripPlan							
	Days					Cities							
	1	2	3	4	5	3	4	5	6	7	8	9	10
CoT	6.0	12.0	14.0	16.0	4.0	44.0	22.0	18.0	12.0	2.0	0.0	0.0	0.0
CoT - SC	12.0	16.0	10.0	18.0	2.0	42.0	26.0	16.0	8.0	4.0	0.0	0.0	0.0
ToT	27.3	18.0	17.6	11.0	10.0	14.0	2.0	0.0	0.0	0.0	0.0	0.0	0.0

Table 11. O1 results breakdown on Blocksworld and Bin packing

Methods	Blocksworld						Bin packing				
	Steps						Bins				
	2	4	6	8	10	12	5	6	7	8	9
IO	100.0	100.0	100.0	100.0	95.0	100.0	100.0	100.0	95.0	100.0	100.0

Table 12. O1 results breakdown on CalendarPlan and TripPlan

Methods	CalendarPlan					TripPlan							
	Days					Cities							
	1	2	3	4	5	3	4	5	6	7	8	9	10
IO	95.0	80.0	90.0	85.0	100.0	80.0	93.0	73.3	60.0	66.7	40.0	26.7	26.7

Table 13. 405B tokens generated and accuracy achieved for Blocksworld, Game of 24, and GSM8K

	Blocksworld		Game of 24		GSM8K	
	Accuracy	Tokens	Accuracy	Tokens	Accuracy	Tokens
CoT	48.7	48456	7.0	8500	97.0	225000
SC	52.1	268727	6.0	41500	97.5	1176000
ToT	19.9	3437455	69.0	3817600	96.0	2067500

Table 14. 4o tokens generated and accuracy achieved for Blocksworld, Game of 24, and GSM8K

	Blocksworld		Game of 24		GSM8K	
	Accuracy	Tokens	Accuracy	Tokens	Accuracy	Tokens
CoT	37.5	40996	14.0	8400	94.7	312500
SC	41.5	214806	18.0	42000	94.9	1810500
ToT	12.4	2821108	62.0	3528500	93.5	1840500