

to compare exchange of ion I and Ca in $\text{CaMgSi}_2\text{O}_6$

$$\Delta G_I = \Delta G_{\text{Ca}} + \cancel{\Delta G_{\text{strain}}^{\text{melt} \rightarrow 0}} - \Delta G_{\text{strain}}^{\text{cpx}}$$

What about the strain in the melt?

- Assume much smaller than crystal

$$\Delta G_{\text{strain}}^{\text{cpx}} = \Delta G_{\text{Ca}} - \Delta G_I$$

$$\Delta G_{\text{strain}}^{\text{cpx}} = -RT \ln D_{\text{Ca}} + RT \ln D_I$$

$$\ln x - \ln y = \ln \frac{x}{y}$$

$$\Delta G_{\text{strain}}^{\text{cpx}} = -RT \left(\ln \frac{D_I}{D_{\text{Ca}}} \right)$$

$$\frac{-\Delta G_{\text{strain}}^{\text{cpx}}}{RT} = \ln \frac{D_I}{D_{\text{Ca}}}$$

$$e^{\left(\frac{-\Delta G_{\text{strain}}^{\text{cpx}}}{RT} \right)} = \frac{D_I}{D_{\text{Ca}}}$$

$$D_{\text{Ca}} e^{\left(\frac{-\Delta G_{\text{strain}}^{\text{cpx}}}{RT} \right)} = D_I$$

$$W = E 4\pi \left(\frac{1}{3} (r_i - r_0)^3 - \frac{r_0}{2} (r_i - r_0)^2 \right) = \Delta G_{\text{strain}}^{\text{cpx}}$$

What about charge?



$$E \sim \frac{3K}{1-2\nu}$$

Bulk modulus

poisson's ratio