Engage3_Report

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This report proceeds in two parts. First, the data join and cross tabulation. See the attached .csv. Then, the exploratory analysis/model build. In short, there is definitely an issue with the quality of the data, but after removing the bad data, there are no suprises with the results of the model.

```
[1]: import numpy as np
[2]: import pandas as pd
[3]: auditors = pd.read_csv('data/auditors.csv');
[4]: prices = pd.read_csv('data/prices.csv');
[5]: stores = pd.read_json('data/stores.json')
```

Join Data

```
6.09
                                                                   5.19
Safeway 11873171
                        NaN
                                   NaN
         15052612
                      53.99
                                   NaN
                                                            {\tt NaN}
                                                                  54.49
         16482322
                      17.89
                                   NaN
                                                            NaN
                                                                  18.09
         16729338
                      7.99
                                   NaN
                                                           9.39
                                                                   8.09
         16829288
                       3.59
                                   NaN
                                                           4.19
                                                                   3.59
```

```
[12]: table.to_csv('data/table.csv')
```

Exploratory Analysis First of all, the Whole Foods in Kansas has a bunch of items that are \$1.99. I understand that this could be some kind of loss-leader situation, but this is unlikely.

```
[13]: table.tail()
[13]: Region
                             Kansas
                                     New York Northern California
     Banner
                 UPC
     Whole Foods 995798889
                               1.99
                                        62.39
                                                              70.39 60.59
                 996262978
                               1.99
                                        14.39
                                                              16.19
                                                                     13.89
                 996849471
                               1.99
                                        12.79
                                                                NaN
                                                                       NaN
                 998831540
                               1.99
                                        39.99
                                                                NaN 38.79
                                        58.09
                                                              65.49
                 999185078
                               1.99
                                                                       NaN
[14]: filtered_df = df[(df['Banner'] == 'Whole Foods') & (df['Region'] == 'Kansas')]
[15]: filtered_df['Auditor ID'].value_counts() #frequency table
[15]: 713
            913
     Name: Auditor ID, dtype: int64
[16]: filtered_df['Store ID'].value_counts() #frequency table
[16]: 39287
              913
     Name: Store ID, dtype: int64
```

It's either the auditor or the store. Either way, this data is no good. The data from this particular store will be removed from the model.

0.0.1 Running Model

I'll run a two-factor multi-level model using Stan. I'm excluding the UPC from the model, so that the linear model I'm using is more like $P_{ijk} = A_j + B_k$.

```
[17]: import pystan as pystan
[18]: stan_data = pystan.read_rdump('data/stan_data.r') #data needed to be converted_
      →to a stan data object in R, see issue here: https://github.com/stan-dev/
      →pystan/issues/437
[19]: | my_model_code = """
     data{
          int<lower=0> N_obs;
              int<lower=1> N regions;
          int<lower=1> N_banners;
              int banner_id[N_obs];
              int region_id[N_obs];
          real Price[N_obs];
      }
     parameters{
          vector[N_regions] a_r;
          vector[N_banners] a_s;
              real a;
```

```
real<lower=0> sigma_r;
         real<lower=0> sigma_s;
     real<lower=0> sigma;
}
model{
     vector[N_obs] mu;
     sigma \sim cauchy(0,1);
     a_r ~ normal(0,sigma_r);
         sigma_r \sim cauchy(0,1);
         a_s ~ normal(0, sigma_s);
         sigma_r ~ cauchy(0,1);
     mu = a + a_r[region_id] + a_s[banner_id];
     Price ~ normal(mu, sigma);
         }
0.00
```

[20]: sm = pystan.StanModel(model_code=my_model_code)

INFO:pystan:COMPILING THE C++ CODE FOR MODEL $\verb"anon_model_f173c5b356c0123acd48aa644ff2a541 NOW."$

```
[21]: fit = sm.sampling(data=stan_data, iter=1000, chains=4)
```

Banner(a_s): Walmart = 1; Whole Foods = 2; Wegmans = 3; Trader Joes = 4; Safeway = 5Region(a_r): Texas = 1; Kansas = 2; NY = 3; Northern CA = 4

```
[22]: print(fit)
```

Inference for Stan model: anon model f173c5b356c0123acd48aa644ff2a541. 4 chains, each with iter=1000; warmup=500; thin=1; post-warmup draws per chain=500, total post-warmup draws=2000.

```
2.5%
                                          25%
                                                  50%
                                                         75% 97.5%
                                                                     n_eff
                                                                               Rhat
          mean se_mean
                            sd
a_r[1]
         -1.18
                   0.04
                          0.94
                                -3.11
                                        -1.74
                                               -1.16
                                                        -0.6
                                                                0.72
                                                                        653
                                                                                1.0
                                -2.95
a_r[2]
         -1.06
                   0.04
                          0.95
                                        -1.63
                                               -1.04
                                                       -0.49
                                                                0.82
                                                                        627
                                                                                1.0
                                -2.46
         -0.53
                   0.04
                          0.95
                                       -1.12 -0.51
                                                                1.39
                                                                        674
a_r[3]
                                                        0.05
                                                                                1.0
a_r[4]
          2.92
                   0.04
                          0.95
                                   1.1
                                         2.31
                                                  2.9
                                                        3.49
                                                                4.91
                                                                        641
                                                                                1.0
         -2.15
                   0.09
                          1.44
                                -4.97
                                        -2.89
                                                 -2.2
                                                                1.22
                                                                        280
                                                                               1.01
a_s[1]
                                                       -1.49
a_s[2]
          3.16
                   0.09
                          1.45
                                  0.39
                                         2.39
                                                 3.09
                                                         3.8
                                                                6.56
                                                                        283
                                                                               1.01
          0.03
                   0.09
                          1.45 - 2.68
                                        -0.71
                                               -0.05
                                                        0.68
                                                                3.51
                                                                        282
                                                                               1.01
a_s[3]
                          1.44 -3.38
                                                                2.87
                                                                               1.01
a_s[4]
         -0.56
                   0.09
                                        -1.33
                                               -0.63
                                                        0.07
                                                                        287
a_s[5] -2.6e-3
                   0.09
                          1.42 - 2.78
                                        -0.74
                                               -0.09
                                                        0.64
                                                                3.41
                                                                        276
                                                                               1.01
         31.32
                   0.09
                          1.66 27.81
                                        30.41
                                               31.39
                                                       32.28
                                                              34.52
                                                                               1.01
                                                                        313
                   0.02
                          0.66
                                         1.32
sigma_r
          1.76
                                  0.93
                                                 1.62
                                                        2.02
                                                                3.51
                                                                       1052
                                                                                1.0
sigma_s
          2.94
                   0.07
                          1.72
                                  1.23
                                         1.89
                                                 2.49
                                                        3.43
                                                                7.53
                                                                        576
                                                                                1.0
                                17.05
                                         17.2
                                               17.27
                                                       17.35
                                                                       1990
sigma
         17.27
                 2.5e-3
                          0.11
                                                               17.49
                                                                                1.0
        -3.8e4
                    0.1
                          2.59 -3.8e4 -3.8e4 -3.8e4 -3.8e4 -3.8e4
                                                                        664
                                                                                1.0
lp__
```

Samples were drawn using NUTS at Sat Jan 11 01:25:19 2020.

For each parameter, n_eff is a crude measure of effective sample size, and Rhat is the potential scale reduction factor on split chains (at convergence, Rhat=1).

I'm not too surprised at the results. Looking at the posterior means...

For the regions (a_r), Northern CA(4) is the most expensive, New York(3) is relatively cheap (this is a surprise), and Texas and Kansas are the cheapest (no surprise).

For the banners (a_s), Walmart(1) is the cheapest, Whole Foods(2) in the most expensive, Wegmans, TJ's and Safeway are the least pricey. I'm a bit surprised TJ's is less expensive than Safeway.

The variance around the banners is large enough that we should take the differences with a grain of salt. Still, the gap between Walmart and Whole Foods is large.

The variance around the regions is large enough that CA really stands out among the other 3. The model converged well so the estimates are accurate within the model framework.