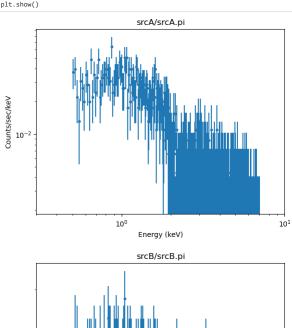
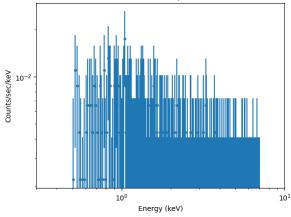
```
In [10]: from sherpa.astro.ui import * #import sherpa function
from ciao_contrib.runtool import * #import CIAO tools
             import matplotlib.pyplot as plt
 In [4]:
#we can define the source and bkg files to be used by specextract:
specextract.infile="../acisf09514_repro_evt2.fits[sky=region(srcA.reg)]"
specextract.bkgfile="../acisf09514_repro_evt2.fits[sky=region(bkg.reg)]"
# define the directory to load the outputs
specextract.outroot="srcA/srcA"
              #run the specextract function
             specextract()
 Out[4]: Running specextract
Version: 18 January 2023
             Aspect solution file ../pcadf09514_000N001_asol1.fits found.
             Bad pixel file ../acisf09514_repro_bpix1.fits found.
             Mask file ../acisf09514_000N003_msk1.fits found.
             Extracting bkg spectra
             Extracting src spectra
             Using mkacisrmf...
             Using mkacisrmf...
             Creating bkg RMF
             Creating bkg ARF
             Creating src RMF
             Creating src ARF
  In [5]: #we can define the source and bkg files to be used by specextract:
             specextract.infile="../acisf09514_repro_evt2.fits[sky=region(srcB.reg)]"
specextract.bkgfile="../acisf09514_repro_evt2.fits[sky=region(bkg.reg)]"
             # define the directory to Load the outputs
specextract.outroot="srcB/srcB"
              #run the specextract function
             specextract()
 Out[5]: Running specextract
Version: 18 January 2023
             Aspect solution file \dots/pcadf09514\_000N001\_asol1.fits found.
             Bad pixel file ../acisf09514_repro_bpix1.fits found.
             Mask file ../acisf09514_000N003_msk1.fits found.
             Extracting src spectra
             Extracting bkg spectra
             Using mkacisrmf...
             Using mkacisrmf...
             Creating src RMF
             Creating src ARF
             Creating bkg ARF
             Creating bkg RMF
 read ARF file srcA/srcA.arf
              read RMF file srcA/srcA.rmf
             read ARF (background) file srcA/srcA_bkg.arf
read RMF (background) file srcA/srcA_bkg.rmf
              read background file srcA/srcA_bkg.pi
             read ARF file srcB/srcB.arf
read RMF file srcB/srcB.rmf
             read ARF (background) file srcB/srcB_bkg.arf
read RMF (background) file srcB/srcB_bkg.rmf
read background file srcB/srcB_bkg.pi
  In [8]: #we constrain our energy range from 0.5-7 keV
             notice(0.5,7)
             dataset 1: 0.0073:14.9504 -> 0.4964:7.008 Energy (keV) dataset 2: 0.0073:14.9504 -> 0.4964:7.008 Energy (keV)
```

```
In [12]: #We plot the raw data of dataset 1
    plot_data(1,xlog=True,ylog=True)
    plt.xlim(0.3,10)
    plt.show()

#We plot the raw data of dataset 2
    plot_data(2,xlog=True,ylog=True)
    plt.xlim(0.3,10)
    plt.show()
```



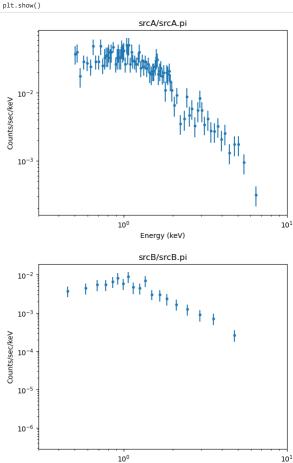


In [13]: #we group the data by 50 counts per group (default is 15)
group_counts(1,15)
group_counts(2,15)

#we subtract the background associated with each dataset
subtract(1)
subtract(2)

```
In [14]: #we now plot the regrouped, background subtracted spectrum of daset 1
plot_data(1,xlog=True,ylog=True)
plt.xlim(0.3,10)
plt.show()

#we do the same for dataset 2
plot_data(2,xlog=True,ylog=True)
plt.xlim(0.3,10)
plt.show()
```



we can now define our models. We will use

1 - xszpowerlw: redshifted power law photon spectrum. The default parameters are Pholndex, redshift, and norm.

Energy (keV)

- 2 xszphabs : photoelectric absorption of lens. Paramaters are nH and redshift.
- 3 xsphabs : photoelectric absorption from line of sight of observer. Parameters are nH.

 $models\ from\ \underline{https://cxc.cfa.harvard.edu/sherpa/models/}\ \underline{(https://cxc.cfa.harvard.edu/sherpa/models/)}$

structure for defining model is set_source(index,model name.variable model 2.variable 2 etc).

By passing the same variable name to multiple sources, we are linking the model (they will be the same value for all).

```
In [15]: set_source(1,xszpowerlw.p1*xszphabs.labs1*xsphabs.gabs)
set_source(2,xszpowerlw.p2*xszphabs.labs2*gabs)
```

we can now redefine some of the parameters to their known/observed value. The redshift of the source and the lens is found in the CASTLES survey (https://lweb.cfa.harvard.edu/castles/).

 $\label{thm:local_problem} The \ HI \ column \ density \ is \ found \ using \ \underline{HEASARC\ (\underline{https://heasarc.gsfc.nasa.gov/cgi-bin/Tools/w3nh/w3nh.pl)}.$

```
In [16]: #we fix the redshift of the source since it is known.
#we link it for all models since it is same z for all.
p1.redshift = 1.37
             link(p2.redshift,p1.redshift)
             #similarly, the redshift of the lens is known.
            #we fix it and link it to all the models. labs1.redshift = 0.48
             link(labs2.redshift,labs1.redshift)
             #We fix the aalactic nH value.
             #Again, it will be the same for all models.
            # 5.25 x 10^20 so
gabs.nh = 0.0525 #unit: 10^22 atoms / cm^2
             freeze(gabs.nH)
             #the photon index is expected to be the same for all sources:
             link(p2.PhoIndex, p1.PhoIndex)
             #we can look at our models:
             show model()
            Model: 1
             apply_rmf(apply_arf((31188.838169386 * ((xszpowerlw.p1 * xszphabs.labs1) * xsphabs.gabs))))
                                                                                      Max
                Param
                                 Type
                                                   Value
                                                                      Min
                                                                                                  Units
                                                                     ---
                p1.PhoIndex thawed
                                                                       -3
                                                                                        10
                p1.redshift frozen
                                                   1.37
                                                                  -0.999
                p1.norm
                                thawed
                                                  1
1
                                                                        0
                                                                                    1e+24
                 labs1.nH
                                 thawed
                                                                                   1e+06 10^22 atoms / cm^2
                labs1.redshift frozen
                                                      0.48
                                                                    -0.999
                                                                                   1e+06 10^22 atoms / cm^2
                gabs.nH
                                frozen
                                                 0.0525
             apply_rmf(apply_arf((31188.838169386 * ((xszpowerlw.p2 * xszphabs.labs2) * xsphabs.gabs))))
                                 Type
                                                                  Min Max
                Param
                                                  Value
                                                                                                  Units
                p2.PhoIndex linked
                                                                    expr: p1.PhoIndex
                p2.redshift linked
                                                   1.37
                                                                   expr: p1.redshift
                p2.norm
labs2.nH
                                                                   0
                                                  1
1
                                                                                    1e+06 10^22 atoms / cm^2
                                 thawed
                 labs2.redshift linked
                                                                  expr: labs1.redshift
                                                                                   1e+06 10^22 atoms / cm^2
                gabs.nH
                                frozen
                                                 0.0525
In [17]: #once our parameters are adjusted, we can simultaneously fit all 4 models.
             #we fit three times so the fit converges.
             fit(1,2)
             fit(1,2)
             fit(1,2)
                                     = 1, 2
= levmar
            Datasets
             Method
            Statistic = chi2gehrels
Initial fit statistic = 4.15646e+11
            Trinal fit statistic = 66.650 at function evaluation 322
Data points = 104
Pegrees of freedom = 99
Probability [Q-value] = 0.995587
            Reduced statistic = 0.667174
Change in statistic = 4.15646e+11
                                   1.90249 +/- 0.0860248
0.000407501 +/- 5.61505e-05
                p1.PhoIndex 1.90249
                labs1.nH
                                   0.00202197 +/- 0.0545696
7.71039e-05 +/- 1.13953e-05
                p2.norm
                                  0.0076188 +/- 0.0710819
= 1, 2
= levmar
                labs2.nH
            Datasets
            Method
                                      = chi2gehrels
            Initial fit statistic = 66.0503

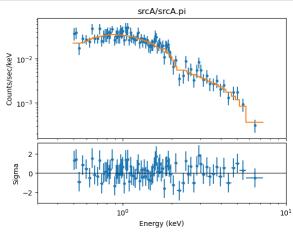
Final fit statistic = 65.5828 at function evaluation 291

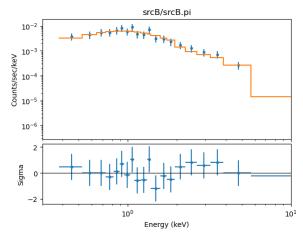
Data points = 104

Degrees of freedom = 99
            Probability [Q-value] = 0.996122
Reduced statistic = 0.662453
Change in statistic = 0.467438
                                  1. 90204 +/- 0.0884685
0.0004040742 +/- 5.96491e-05
0 +/- 0.0541931
7.30239e-05 +/- 1.20793e-05
                p1.PhoIndex 1.90204
                p1.norm
labs1.nH
                p2.norm
            p2.norm 7.30239e-05 +/- 1.20793e-05
labs2.nH 0 +/- 0.0698041
WARNING: parameter value labs1.nH is at its minimum boundary 0.0
WARNING: parameter value labs2.nH is at its minimum boundary 0.0
                                      = 1, 2
            Datasets
                                     = levmar
            Method
             Statistic
                                       = chi2gehrels
             Initial fit statistic = 65.5828
            Final fit statistic = 65.5665 at function evaluation 278
Data points = 104
Degrees of freedom = 99
             Probability [Q-value] = 0.996139
            Reduced statistic = 0.662288
Change in statistic = 0.0162759
                p1.PhoIndex 1.90221
p1.norm 0.0004053
                                   1.90221 +/- 0.0883648
0.00040539 +/- 5.96707e-05
                                  0 +/- 0.0541152
7.30838e-05 +/- 1.20771e-05
A +/- 0.0697446
                labs1.nH
                p2.norm
                labs2.nH
             WARNING: parameter value labs1.nH is at its minimum boundary 0.0
            WARNING: parameter value labs2.nH is at its minimum boundary 0.0
```

```
In [18]: #we can plot our fit for dataset 1 and include residuals
    set_xlog()
    set_ylog()
    plot_fit_delchi(1)
    plt.xlim(0.3,10)
    plt.show()

#we can plot our fit for dataset 1 and include residuals
    set_xlog()
    set_ylog()
    plot_fit_delchi(2)
    plt.xlim(0.3,10)
    plt.show()
```





In [19]: #we estimate the parameter confidence intervals conf(1,2)

```
labs1.nH lower bound:
labs2.nH lower bound:
p1.norm lower bound:
labs2.nH upper bound:
p1.norm upper bound:
                                        -2.00181e-05
                                       0.049471
4.90178e-05
pl.PhoIndex lower bound:
pl.PhoIndex lower bound:
pl.PhoIndex upper bound:
pl.PhoIndex upper bound:
                                      0.0301181
l: -0.0379315
l: 0.0766384
-5.74022e-06
p2.norm upper bound:
                                      1.08565e-05
                                   1.08565e-05
= 1, 2
= confidence
= None
= levmar
= chi2gehrels
Datasets
Confidence Method
Iterative Fit Method
Fitting Method
Statistic
confidence 1-sigma (68.2689%) bounds:
Param Best-Fit Lower Bound Upper Bound
     p1.PhoIndex
                                  1.90221
                                                   -0.0379315
                                                                         0.0766384
                             0.00040539 -2.00181e-05
     p1.norm
labs1.nH
                                                                      4.90178e-05
                                                                         0.0301181
                            7.30838e-05 -5.74022e-06
0 -----
     p2.norm
                                                                     1.08565e-05
     labs2.nH
                                                                           0.049471
```