

1. (a) State formally what is meant by:

$f(n)$ is $\theta(g(n))$ [3 marks]

- (b) Determine whether each of the following statements is true or false, justifying your answers:

- i. $100n^3$ is $O(n^3)$
- ii. $n \log(n)$ is $\Omega(n)$
- iii. n^2 is $\theta(n^2 + n)$

[6 marks]

- (c) The following algorithm computes the determinant of a matrix of size 3. How many basic operations will be required to complete the calculation? State clearly any assumptions you make.

Algorithm *determinant*(X)

// Input array X of size 3

// Output an integer d which is the determinant of X

$d \leftarrow 0$

for $i \leftarrow 0$ to 2 do

$d \leftarrow d + X[i,0] * (X[i+1 \% 2, 1] * X[i+2 \% 2, 2] -$
 $X[i+2 \% 2, 1] * X[i+1 \% 2, 2])$

return d

[4 marks]