

12. (a) Given that  $x(1 + t^2) = 1$  and  $y(1 + t^2) = t$ , prove that

$$\frac{dy}{dx} = \frac{1}{2} \left( t - \frac{1}{t} \right).$$

[5]

- (b) Given that  $y = \log(1 + x) - x/(1 + x)$ , find  $dy/dx$  and show that  $y$  is positive for all positive values of  $x$ .

[5]