

3. (a) Bresenham's line algorithm uses the decision parameter  $P(k)$  for the  $k^{th}$  step of the method:

$$P(k) = 2\Delta y x(k) - 2\Delta x y(k) + K.$$

If the line goes between the end points  $(x_1, y_1)$  and  $(x_2, y_2)$ :

- i. Step-by-step, derive an expression for  $P(k+1)$ , and the constant  $K$ . [5]
  - ii. What two values can  $P(k+1)$  take and what does that mean for the algorithm? [3]
  - iii. What is the initial value of  $P(k)$ , and which values can be pre-calculated knowing only the endpoints of the line? [3]
  - iv. What conditions need to be imposed on the slope? How can arbitrary slopes be dealt with without sacrificing efficiency? [4]
- (b) How could antialiasing be incorporated into Bresenham's line algorithm? [5]
- (c) What are the winding-number values at locations A, B, C, D, E, and F for the following two polygons? (Vertices are numbered in the order they are drawn).

