

7. (a) Work out the Bezier polynomials for a cubic spline. [5]
- (b) Derive a Bezier matrix,  $\mathbf{B}$ , for a cubic spline satisfying the blending formula:

$$\mathbf{q}(u) = \mathbf{U}\mathbf{B}\mathbf{b}$$

making the definitions of  $\mathbf{U}$  and  $\mathbf{b}$  clear. [7]

- (c) Derive the conditions under which 1st and 2nd order continuity can be achieved between successive knots of the spline designed above. [7]
- (d) Given the forward-differencing approximation:

$$\Delta x(u) = x(u + \delta) - x(u),$$

find an expression for  $\Delta x(u)$  if

$$x(u) = a_3x^3 + a_2x^2 + a_1x + a_0.$$

Explain why this result is helpful in reducing the calculations required to draw splines. How many operations are required to calculate one step,  $\delta$ , forward when drawing a 2D cubic spline using forward-differencing? [6]