

**Time allowed: 3 hours.**

Answer **FOUR** questions.

Read carefully the instructions on the answer book and make sure that the particulars required are entered on each answer book.

Use of approved calculators is permitted in this examination.

---

1. (a) Distinguish between real-time and off-line computer graphics. How does computer graphics exploit human visual capabilities to achieve visual realism? [4]
- (b) What are the principal elements of a graphics system and what are the roles of an application model and a graphics kernel? [4]
- (c) What is meant by rasterization? Explain why standard frame-buffers store colour, transparency and depth information. [7]
- (d)
  - i. Specify the 3D rotation matrix that rotates points about the z-axis by  $\theta$  degrees.
  - ii. Specify the rotation matrix that takes the negative z-axis onto the positive z-axis.
  - iii. Give the set of rotations required to rotate a point about an arbitrary axis  $(a, b, c)^T$  which passes through the origin.
  - iv. What further homogeneous transformations would be required if the arbitrary axis in (iii) passed through a point  $(e, f, g)$  instead of the origin?

Give a set of OpenGL transformation statements which implements a rotation of  $\theta$  degrees, about axis  $(a, b, c)^T$  which passes through point  $(e, f, g)$ .

[10]

---

- 
2. (a) Write down the parametric equation of a line between points  $(x_0, y_0)$  and  $(x_1, y_1)$ . [4]
- (b) What inequalities need to be satisfied for this line to be clipped against a box with opposite corners at  $(x_{min}, y_{min}), (x_{max}, y_{max})$ ? [4]
- (c) Using your answer to (b), explain the Liang-Barsky Clipping method for a line which crosses one or more clipping boundaries. [11]
- (d) In what ways is the Liang-Barsky method more efficient than the Sutherland-Cohen method? [6]
- 

3. (a) Distinguish between diffuse and specular reflectors. What is meant by global illumination? State briefly how it can be approximated. [6]
- (b) Describe and illustrate the Phong lighting model for a single point light source. Explain carefully the purpose of the parameters of the model. [6]
- (c) With appropriate diagrams and equations, explain how interpolated shading is achieved. What is meant by per-pixel shading and why is it expensive to calculate? Give an expression for the per-pixel shading value at the origin,  $(0, 0)$ , for a triangle:

$$\{(-1, -1), (1, -1), (0, 1)\},$$

if the vertices have the illumination and normal attributes,

$$\{I_0, \mathbf{n}_0\}, \{I_1, \mathbf{n}_1\}, \{I_2, \mathbf{n}_2\}.$$

[6]

- (d) Explain how texture mapping works in terms of the necessary coordinate transformations required. [7]
-

---

4. A piece-wise polynomial, Bezier approximation curve of order  $n = 2$  needs to be designed to fit a set of points  $\{\mathbf{p}_k\}$ .

- (a) What set of blending functions need to be specified and, hence, what is the parametric form of the curve  $Q(u)$ ? [4]
- (b) Using your previous answer, or otherwise, derive a *matrix* form of  $Q(u)$ . [6]
- (c) Write down the first derivative of the curve,  $Q'(u)$ , and state the boundary condition which will ensure  $C_1$  continuity for successive piecewise approximations. [4]
- (d) Given  $\Delta Q(u) = Q(u + \delta) - Q(u)$  and  $\Delta^2 Q(u) = \Delta Q(u + \delta) - \Delta Q(u)$ , what are the constant terms,

$$\{\Delta^2 Q(0), \Delta Q(0), Q(0)\}$$

needed to accelerate the drawing of  $Q(u)$ ? [8]

- (e) How many multiplies and adds would be needed to trace part of a quadratic Bezier patch over one  $u + \delta u$  or  $v + \delta$  step? [3]
- 

5. (a) What are the main components of a GPU-based framebuffer graphics system? [4]

- (b) Detail the 3D Viewing Pipeline, carefully explaining where texture-mapping, blending and atmospheric effects, like fog, can be combined with vertex operations. [4]

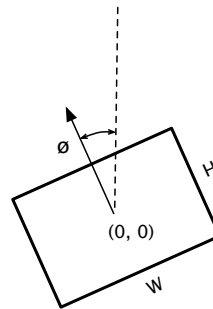
- (c) Derive Bresenham's decision parameter  $P_{k+1}$  for the  $k + 1$  step of a line, given that  $P_k = 2\Delta y x_k - 2\Delta x y_k + K$ , where  $(x_k, y_k)$  is the currently set pixel, the slope is  $\frac{\Delta y}{\Delta x}$  and  $K$  is a constant term. What are the two values that  $P_{k+1}$  can take? [8]

- (d) Outline how the Mid-point method works in efficiently scan converting implicit curves. Derive the starting decision parameter value,  $P_0$ , for a drawing a circle centred at the origin, with radius  $r$ . [9]
-

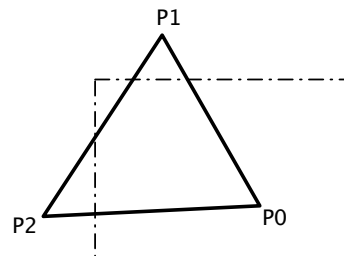
6. (a) What is meant by orthographic and perspective projection? What is the screen  $y$  coordinate of  $(p_x, p_y, p_z)$  if the centre of projection is at  $(0, 0, 0)$  and the view-plane is at a distance  $d$  from the viewer? [6]
- (b) A viewing system is defined with the eye at  $(0, 0, 1)$ , an up-vector  $(0, -1, 0)^T$  and a view plane given by

$$\begin{pmatrix} 0 & 0 & -1 \end{pmatrix} \begin{pmatrix} x \\ y \\ z \end{pmatrix} = 0.$$

- i. What are the view coordinates  $(v_x, v_y)$  of world coordinates  $(w_x, w_y, w_z)$ ? [4]
- ii. What are the screen coordinates of the same points on a viewport of size  $H \times W$  which is centred on the view axis and has an up-vector which is at  $\phi$  degrees to the vertical axis? [4]



- (c) Describe carefully the Sutherland-Hodgman polygon clipping algorithm. Illustrate your answer with the following example. Show when it can fail to work correctly.



[6]

- (d) What are winding numbers and how do they work?

[5]