Foundations of Linear Programming Contents of His Course Models Jor Processing by mathematical algorithms techniques for solving models · Algorithms engines for executing a cyorithms · Software

History of Linear Programming Finding a Minimum Solution of a Function Newton 1788 Lagrangian Multipliers Lagrange 1823 Solution of a Set of Inequalities Founer 1826 Solution of a Set of Linear Equations Gauss 1896 Solution of a Set of Linear Equations
as a Combination of Extreme Points Minkowski 1936 Transposition Theorem and Linear Inequalities Motelin 1 before Lineas Programming

1939 Mathematical Methods of Organization and Production Kantoro vich (Nobel Prize 1975) Transportation Problem 1941 Hitchcock Linear Programming Model 1947 Vantzia 1951 Simplex Method Dantzig 1 Origins of Linear Programming Integer Programming 1958 Gomory, Johnson, Balas Ellipsoid Method Khachiyan 1979 1984 Interior Point Method Karmarkar

Optimization and Calculus Let J: Rn -7 1R, g: 112 n -7 1Rm, L: 112 n -7 1R be twice continuously differentiable general optimization problem $min \left\{ \left(x_{1}, \dots, x_{n} \right) \right\}$ subject to $g_i(x_i, x_n) \ge 0$ $\forall i = 1,..., m$ h (x,..,x,) = 0 + j = 1,..,k

Let y = 0 ER and ZER free and consider the Lagrangian Junction: $(x, y, z) = ((x) - \sum_{i=1}^{n} y_i \cdot g_i(x) - \sum_{i=1}^{n} z_i \cdot \lambda$ -> instead of min ((x) s.t. constraints search for a Local/global minimum of with respect to max min L(x, y, z

Optimization and linear Algebra (and Notation Lineas systems of equations equations in n variables m IR mxn matrix with rows a ER for i=1,..., m 912 ... ain

bER XER : column vectors right-Land sides variables When does Ax = 6 become interesting for optimization?