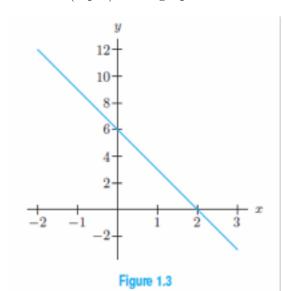
Name:	
VIP ID:	

- Write your name and VIP ID in the space provided above.
- The test has eight (8) pages, including this one, not counting the formula sheet attached at the end.
- You may remove the formula sheet as soon as the proctor instructs so.
- Credit for each problem is given in parentheses at the right of the problem number.
- You must show sufficient work to justify all answers except on multiple-choice questions. Correct answers with inconsistent or no work will not be given credit.
- No books or notes may be used on this test.
- No scratch paper is allowed. You may use the last page of this booklet for that purpose.
- An approved calculator may be used on this test.

Page	Max. points	Your points
2	16	
3	12	
4	28	
5	20	
6	12	
7	12	
Total	100	

**Problem 1** (4 pts). The graph below is a representation of which of the following functions?



$$\bigcirc y = 6x + 6$$

$$0 y = -3x + 6$$
$$0 y = -3x + 2$$

$$\bigcirc y = -3x + 2$$

$$\bigcirc y = 6x - 2$$

**Problem 2** (4 pts). You are to receive three equal payments of \$2000 each, paid once per year starting now. You can assume a 5% interest rate, compounded continuously. The future value of the payments, on the day you receive the final payment, is:

- $\bigcirc 6000e^{0.05\cdot3}$
- $\bigcirc 6000e^{0.05\cdot 2}$
- $\bigcirc 2000e^{0.05\cdot3} + 2000e^{0.05\cdot2} + 2000e^{0.05\cdot1}$
- $\bigcirc 2000e^{0.05\cdot 2} + 2000e^{0.05\cdot 1} + 2000$

**Problem 3** (4 pts each). Evaluate the following integrals.

(a) 
$$\int_0^4 \ln(y^2 + 1) \, dy =$$

(b) 
$$\int_{10}^{103} 9xe^{30x^2} dx =$$

**Problem 4** (4 pts). If the graph below is that of f'(x), which of the following statements is true concerning the function f(x)?

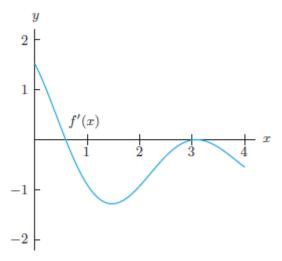


Figure 4.2

- $\bigcirc$  The derivative is zero at two values of x, both being local maxima.
- $\bigcirc$  The derivative is zero at two values of x, one is a local maximum, while the other is a local minimum.
- $\bigcirc$  The derivative is zero at two values of x, one is a local maximum on the interval, while the other is neither a local maximum nor a minimum.
- $\bigcirc$  The derivative is zero at two values of x, one is a local minimum on the interval, while the other is neither a local maximum nor a minimum.
- $\bigcirc$  The derivative is zero only at one value of x, where it is a local minimum.

**Problem 5** (4 pts). Find all local max, min, and inflection points of  $f(x) = 2x^3 + 3x^2 - 180x + 9$ .

**Problem 6** (4 pts). Find the global maximum and the global minimum of  $f(x) = 2x^3 - 9x^2$  over the interval  $-1 \le x \le 6$ .

**Problem 7** (4 pts each). Find the derivative of the following functions:

(a) 
$$f(x) = \sqrt{\frac{1}{x^{39}}}$$

$$f'(x) =$$

(b) 
$$y = 6t^5 - 10\sqrt{t} + \frac{9}{t}$$

$$y'(t) =$$

(c) 
$$f(x) = (2^x + x^5)(3 - \ln x)$$

$$f'(x) =$$

(d) 
$$f(x) = \frac{x^8 + 2}{x}$$

$$f'(x) =$$

(e) 
$$f(x) = \ln(8 - e^{-x})$$

$$f'(x) =$$

(f) 
$$f(x) = (6 + \ln x)^{0.6}$$

$$f'(x) =$$

(g) 
$$f(x) = 2e^{7x} + e^{-x^6}$$

$$f'(x) =$$

**Problem 8** (4 pts each). Compute the antiderivative of the following functions:

$$\int x^5 (5 - 3x^6)^{12} \, dx =$$

$$\int 6xe^{x^2} dx =$$

$$\int \frac{3x^2}{(8x^3 - 5)^3} dx =$$

$$\int 3x^2 4^{5x^3} dx =$$

$$\int \frac{(\ln x)^4}{x} dx =$$

**Problem 9** (4 pts). The number of acres in a region cleared for farming follows the formula  $A = f(t) = 2t^2$ , where t is the number of months since the region started to be farmed, and t ranges from t = 0 to t = 10. Find the **average rate of change** in the number of acres cleared for farming between t = 1 and t = 4.

- 10 acres/month
- $\bigcirc$  30 acres
- 10 months/acre
- O 30 months
- 0.10 months/acre

**Problem 10** (4 pts). What is the average value of  $f(x) = \sqrt{9-x^2}$  over the interval  $0 \le x \le 3$ ?

**Problem 11** (4 pts). For a product, the demand curve is  $p = 53 - q^2$  and the supply curve is  $p = 3 + q^2$ , where q is quantity and p is price in dollars per unit. Find the **producer surplus** when the market is in equilibrium (round your anwer to the nearest dollar).

**Problem 12** (4 pts). Find the value of constants a and b so that the minimum of the parabola  $f(x) = ax^2 - bx + 3$  is at (1, -1).

**Problem 13** (4 pts). At a price of \$80 for a half-day trip, a white-water rafting company attracts 300 customers. Every \$5 decrease in price attracts an additional 30 customers. What price should the company charge per trip to maximize revenue?

**Problem 14** (4 pts). The marginal cost of drilling an oil well depends on the depth at which you are drilling; drilling becomes more expensive, per meter, as you dig deeper into the earth. The fixed costs are one million dollars and, if x is the depth in meters, the marginal costs are MC(x) = 500 + 12x dollars per meter. Find the **total cost** of drilling a 400-meter well.

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