Name: _____

4-digit code: _____

- Write your name and the last 4 digits of your SSN in the space provided above.

- The test has five (5) pages, including this one.

- Enter your answer in the box(es) provided.

- You must show sufficient work to justify all answers unless otherwise stated in the problem. Correct answers with inconsistent work may not be given credit.

- Credit for each problem is given in parentheses at the right of the problem number.

- No books, notes or calculators may be used on this test.

Page	Max. points	Your points
2	20	
3	30	
4	20	
5	30	
Total	100	

Problem 1 (10 pts). Evaluate each limit:

$$\lim_{x \to 0} \cot 2x \sin 6x = \boxed{}$$

$$\lim_{x \to 0} \frac{\sin(4x^2)}{x^2} = \boxed{}$$

Problem 2 (10 pts). Find an equation of the tangent line to the curve $y = \ln(xe^{x^2})$ at the point $(1, 1)$.

Problem 3 (30 pts). Sketch the graph of the rational function $f(x) = \dfrac{6x^2}{3 - 3x^2}$.

Indicate clearly:

- Domain
- x- and y-intercepts.
- Vertical and horizontal asymptotes (any holes?).
- Intervals of increase, decrease and different concavity.
- Location of relative extrema and inflection points.

Problem 4 (10 pts). Find the absolute extrema of $f(x) = \frac{8}{3}x^{4/3} - \frac{4}{3}x^{1/3}$ on the interval $[-1, 1]$.

Absolute maxima at

Absolute minima at

Problem 5 (10 pts). Use logarithmic differentiation to find the derivative of the function

$$y = \frac{\tan^2 x \sin^4 x}{e^{3x}(x^2 + 1)}$$

$$\frac{dy}{dx} =$$

Problem 6 (10 pts)**.** The volume of a cube is increasing at a rate of 300 cm^3/min. How fast are the edges increasing when the length of an edge is 10 cm?

The edges are increasing at a speed of

Problem 7 (20 pts)**.** Find the area of the largest rectangle that can be inscribed in a right triangle with legs of lengths 3 cm and 4 cm if two sides of the rectangle lie along the legs.

Area of largest rectangle: