Name:	
VIP ID:	

- Write your name and your VIP ID in the space provided above.
- The test has five (5) pages, including this one and the table of Laplace transforms at the end.
- Show sufficient work to justify all answers unless otherwise stated in the problem. Correct answers with inconsistent work may not be given credit.
- Credit for each problem is given at the right of each problem number.

Page	Max	Points
2	60	
3	20	
4	20	
Total	100	

**Problem 1** (60 pts—10 pts each). Find the Laplace transform of the following functions:

(a)  $f(x) = 3x^2 - 4x + 7$ 

 $F(s) = \tag{s > 1}$ 

(b)  $f(x) = x^3 - x^{3/2}$ 

 $F(s) = \boxed{ \qquad \qquad (s > )}$ 

(c)  $f(x) = 2e^{3x} - 8e^{-7x} + \cos(\pi x)$ 

 $F(s) = \begin{pmatrix} & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & \\ & & & \\$ 

 $(d) f(x) = 3x^2 \sin(5x)$ 

 $F(s) = \begin{pmatrix} s \\ s \end{pmatrix}$ 

(e)  $f(x) = 6xe^{-x}\sin x$ 

 $F(s) = \boxed{ (s > )}$ 

(f)  $f(x) = \sin x \cos x$ 

 **Problem 2** (20 pts—10 pts each). Find the inverse Laplace transform of the following functions in the given domains.

(a) 
$$F(s) = \frac{2s-3}{s^2-2s-15}$$
,  $(s > 5)$ 

$$f(x) =$$

(b) 
$$F(s) = \frac{s-3}{(s-3)^2+16}$$
,  $(s>3)$ 

$$f(x) =$$

**Problem 3** (20 pts). Use techniques based on the Laplace transform to solve the initial value problem y'' + 3y' + 2y = x that satisfies y(0) = 0, y'(0) = 2.

f(x)	$\mathcal{L}{f} = \int_0^\infty e^{-sx} f(x)  dx$				
1	$\frac{1}{s}$	s > 0	$cf(x)\pm g(x)$	$cF(s) \pm G(s)$	s > max(a, b)
$x^n$	$\frac{n!}{s^{n+1}}$	s > 0	$e^{\alpha x}f(x)$	$F(s-\alpha)$	$s > a + \alpha$
$x^p$	$\frac{p}{s}\mathcal{L}\{x^{p-1}\}$	s > 0	$x^n f(x)$	$(-1)^n F^{(n)}(s)$	s > a
$e^{\alpha x}$	$\frac{1}{s-\alpha}$	$s > \alpha$	f'(x)	sF(s) - f(0)	s > a
$\sin \beta x$	$\frac{\beta}{s^2 + \beta^2}$	s > 0			
$\cos \beta x$	$\frac{s}{s^2 + \beta^2}$	s > 0			

You may use this as scratch paper. Do not detach from the rest of the test