Name:	
4-digit code:	

- Write your name and the last 4 digits of your SSN in the space provided above.
- The test has six (6) pages, including this one.
- Enter your answer in the box(es) provided.
- You must show sufficient work to justify all answers unless otherwise stated in the problem. Correct answers with inconsistent work may not be given credit.
- Credit for each problem is given in parentheses at the right of the problem number.
- No books, notes or calculators may be used on this test.

Page	Max. points	Your points
2	20	
3	20	
4	25	
5	20	
6	15	
Total	100	

Problem 1 (10 pts). Find a formula for the general term of the following sequences:

(a) $\frac{1}{2}, \frac{3}{4}, \frac{5}{6}, \frac{7}{8}, \dots$

(b) $1 - \frac{1}{2}, \frac{1}{3} - \frac{1}{2}, \frac{1}{3} - \frac{1}{4}, \frac{1}{5} - \frac{1}{4}, \dots$

Problem 2 (10pts). Write out the first five terms of the sequence $\left\{\frac{(-1)^{n+1}}{n^2}\right\}_{n=1}^{\infty}$ Determine whether the sequence converges, and if so find its limit.

First five terms:

 $\lim_{n \to \infty} x_n =$

Problem 3 (20 pts). Determine whether the series converge, and if so find their sum:

(a)
$$\sum_{k=1}^{\infty} \left(-\frac{3}{4}\right)^{k-1}$$

$$\sum_{k=1}^{\infty} \left(-\frac{3}{4} \right)^{k-1} =$$

(b)
$$\sum_{k=1}^{\infty} \frac{1}{(k+2)(k+3)}$$

$$\sum_{k=1}^{\infty} \frac{1}{(k+2)(k+3)} = \boxed{}$$

Problem 4 (5 pts). Apply the divergence test and state what it tells you about the series.

$$\sum_{k=1}^{\infty} \frac{k^2 + k + 3}{2k^2 + 1}.$$

Problem 5 (10 pts). Use the **integral test** to determine whether the series $\sum_{k=1}^{\infty} \frac{1}{5k+2}$ converges.

Problem 6 (10 pts). Use the **ratio test** to determine whether the series $\sum_{k=1}^{\infty} \frac{4^k}{k^2}$ converges. If the test is inconclusive, then say so.

Problem 7 (10 pts). Use the **root test** to determine whether the series $\sum_{k=1}^{\infty} \left(\frac{3k+2}{2k-1}\right)^k$ converges. If the test is inconclusive, then say so.

Problem 8 (10 pts). Classify the series $\sum_{k=1}^{\infty} (-1)^k \frac{4k^2+1}{k^3+2}$ as absolutely convergent, convergent or divergent.

MATH 142 Exam#3. Fall 2011 Page 6/6

Problem 9 (15 pts). Find the MacLaurin series for $f(x) = \sin \pi x$. Find the associated radius of convergence.