Name:	
VIP ID:	

- Write your name and VIP ID in the space provided above.
- The test has five (5) pages, including this one.
- Enter your answer in the box(es) provided.
- Show sufficient work to justify all answers unless otherwise stated in the problem. Correct answers with inconsistent work may not be given credit.
- Credit for each problem is given at the right of each problem number.

Page	Max	Points
2	40	
3	20	
4	20	
5	20	
Total	100	

Skills tested on this page:

Terminology	Notation	Background Algebra
Derivatives	Integration	Management of constants

**Problem 1** (40 pts). Consider the following *first-order separable* differential equation:

$$y' = x(y+1)$$

(a) [10 pts] Find an implicit form of its general solution.

(b) [10 pts] Find a particular solution that solves the following initial value problem

$$y' = x(y+1), \quad y(0) = e-1$$

y =

(c) [10 pts] Are there any singular solutions? Find at least one.

y =

(d) [10 pts] Find an explicit particular solution that solves this other initial value problem

$$y' = x(y+1), \quad y(0) = -1$$

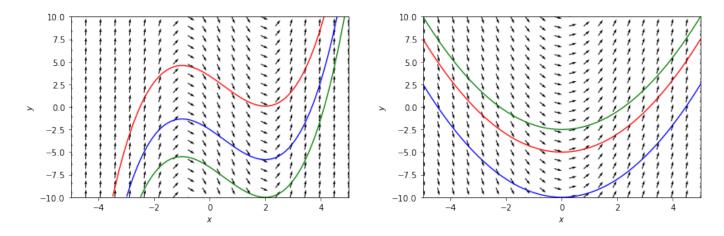
y =

## Skills on this page: Slope fields, Euler's Method

**Problem 2** (10 pts—all or nothing). Which of the following is the slope field of the following differential equation?

$$y' = x^2 - x - 2$$

(You do not need to show work)



**Problem 3** (10 pts). Use Euler's method with a step size h = 0.5 to obtain a numerical approximation of the following **initial value problem** 

$$y' = x^2 y, \quad y(0) = 1$$

n	$x_n$	$y_n$	$f(x_n, y_n)$
0			
1			
2			

## Skills on this page: Basic First-order differential equations

**Problem 4** (10 pts). Solve the following initial value problem:

$$9y' = \frac{1}{\sqrt{3x+4}} \qquad y(7) = -1$$



**Problem 5** (10 pts). Solve the following differential equation:

$$xy' = \sqrt{x^2 + y^2} + y$$

## Skills on this page: Basic First-order differential equations

**Problem 6** (20 pts). Solve the following differential equation:

$$y' + 2\frac{y}{x} = x - 1$$