

#### Group #4 Extra Credit

##### Jake Banner – Triple Spherical

1. Find the spherical limits for the integral that calculates the volume of the solid between the sphere  $\rho = \cos \Phi$  & the hemisphere  $\rho = 9, z \geq 0$ . Then evaluate the integral.
2. Evaluate the spherical coordinate integral:  $\iiint p^2 \sin \Phi \, dp \, d\Phi \, d\theta$ .  $2\pi \geq \theta \geq 0, \pi \geq \Phi \geq 0, 4 \sin \Phi \geq \rho \geq 0$ .

##### Nathan Howell – Triple Cylindrical

1. Evaluate the Cylindrical coordinate integral:  $\iiint z \, dz \, r \, dr \, d\theta$ .  $3\sqrt{9-r^2} \geq z \geq -\sqrt{9-r^2}, \theta/\pi \geq r \geq 0, \pi \geq \theta \geq 0$ .
2. Find the volume of the region bounded by  $z = 10e - ex^2 - ey^2$  above and  $z = ex^2 + ey^2$  below.

##### Dylan Myers – Double Polar & Conversion

1. Change the cartesian integral into an equivalent polar integral. Then evaluate the polar integral.  $\iint e^{\sqrt{x^2+y^2}} \cdot \sqrt{(\ln 3)^2 - y^2} \, dx \, dy$ .  $\ln 3 \geq y \geq 0$ .
2. Sketch the region of integration and convert the polar integral to a cartesian integral. Evaluate  $\iint r^5 \cos^2 \theta \, dr \, d\theta$ .  $4 \sec \theta \geq r \geq 0, \pi/4 \geq \theta \geq 0$ .
3. Find the area of the region cut from the first quadrant by the curve  $r = 2(2 - \sin 2\theta)^2$
4. Evaluate the Integral

$$\int_0^{\tan^{-1} \frac{4}{3}} \int_0^{3 \sec \theta} r^7 \, dr \, d\theta + \int_{\tan^{-1} \frac{4}{3}}^{\pi/2} \int_0^{4 \csc \theta} r^7 \, dr \, d\theta$$

##### Mark McMurtury – Double Type I and II.

1. Find the area of the region enclosed by  $2x+2$  and  $x^2+x$ .
2. Find the area of the region bound by the points  $(-1,0)$ ,  $(1,0)$ , and  $(0,3)$ .

##### Zachary Owens – Triple I, II & III

1. Describe the tetrahedron with vertices at  $(0,0,0)$ ,  $(1,0,0)$ ,  $(0,2,0)$  &  $(0,0,3)$  as a **TYPE III** solid.
2. Write an integral that represents the volume of the tetrahedron cut from the first octant by the plane  $2x + 3y + z = 6$ . Use **Type II** to help solve.
3. Evaluate  $\iiint_R 6xy \, dz \, dy \, dx$  where  $R$  lies under  $z = 1+x+y$  but above the region bounded by  $y = \sqrt{x}$ ,  $y = 0$  and  $x = 1$ . Use **Type I** to solve.

##### Robert Hansen – Spherical Conversion

1. Set up triple integrals for the volume of a sphere  $\rho = 10$  in
  - a. Spherical Coordinates
  - b. Cylindrical Coordinates
  - c. Rectangular Coordinates
2. Set up the triple Integral for the cylinder  $5 \geq z \geq 0, 7 \geq r \geq 0, \pi/2 \geq \theta \geq 0$  in
  - a. Cylindrical Coordinates
  - b. Spherical Coordinates
  - c. Rectangular Coordinates

Jeffrey Eberspecker – Cylindrical Conversion

1. Find the volume of the region enclosed by the cylinder  $x^2 + y^2 = 36$  and the planes  $z = 0$  &  $y + z = 12$
2. Find the volume of the region cut from the solid cylinder  $x^2 + y^2 \leq 9$  by the sphere  $x^2 + y^2 + z^2 = 16$

Ralph DeFilio – Change of Variables in Multiple Integrals

1. Evaluate  $\iint \sqrt{x+y} (y-2x)^2 \, dy \, dx$ .  $1-x \geq y \geq 0$ ,  $1 \geq x \geq 0$
2. Evaluate  $\iint_R (2x^2 - xy - y^2) \, dx \, dy$ . For the Region R in the first quadrant bounded by the lines  $y = -2x+4$ ,  $y = -2x+7$ ,  $y = x-2$  and  $y = x+1$ .