

**Name:** \_\_\_\_\_

**4-digit code:** \_\_\_\_\_

- Write your name and the last 4 digits of your SSN in the space provided above.
- The test has five (5) pages, including this one.
- Enter your answer in the box(es) provided.
- You must show sufficient work to justify all answers unless otherwise stated in the problem. Correct answers with inconsistent work may not be given credit.
- Credit for each problem is given in parentheses at the right of the problem number.
- No books, notes or calculators may be used on this test.

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Page	Max. points	Your points
2	30	
3	30	
4	20	
5	20	
<b>Total</b>	100	

**Problem 1** (30 pts). Evaluate each integral:

(a)  $\int (3 \sin x - 2 \sec^2 x) dx$

(b)  $\int \frac{5x^4}{(x^5 + 1)^2} dx$

(c)  $\int_0^1 (5x - 3) dx$

**Problem 2** (20 pts). Express the following functions of  $n$  in closed form and then find the limit.

(a)  $\lim_{n \rightarrow \infty} \frac{1^2 + 2^2 + 3^2 + \cdots + n^2}{n^3}$

(b)  $\lim_{n \rightarrow \infty} \sum_{k=1}^n \frac{5k}{n^2}$

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**Problem 3** (10 pts). Use the definition of **definite integral** to express  $\int_{-\pi/2}^{\pi/2} (1 + \cos x) dx$  as a limit.

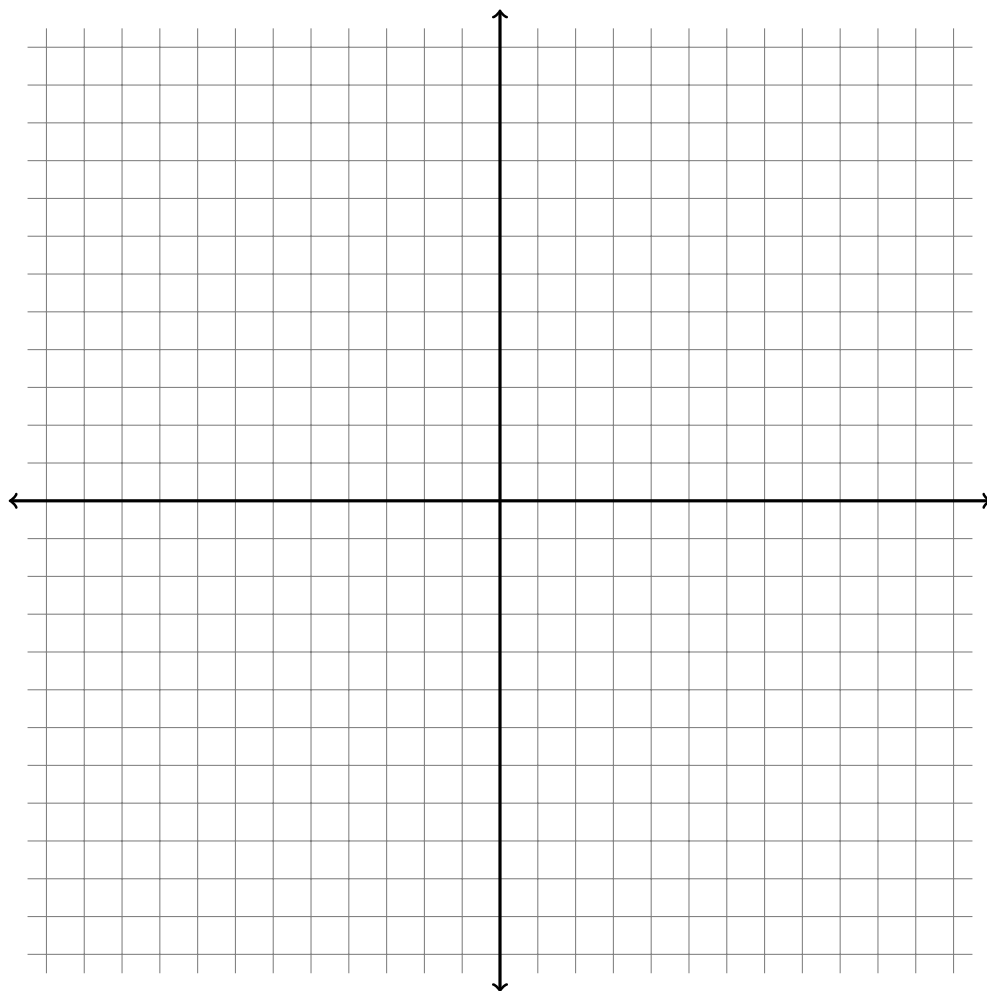
**Problem 4** (20 pts). Sketch the graph of the rational function  $f(x) = \frac{2x^2 - 8}{x^2 - 16}$ .

Use the back of this page for computations and sign-charts. Indicate clearly:

- Domain
- $x$ - and  $y$ -intercepts.
- Vertical and horizontal asymptotes (any holes?).
- Intervals of increase, decrease and different concavity.
- Location of relative extrema and inflection points.

**HINT:** The first and second derivatives are, respectively

$$f'(x) = \frac{-48x}{(x^2 - 16)^2}, \quad f''(x) = 48 \frac{3x^2 + 16}{(x^2 - 16)^3}$$



**Problem 5** (10 pts). Use the Fundamental Theorem of Calculus to find the derivative of the following functions.

(a)  $g(x) = \int_1^x \frac{1}{t^3 + 1} dt$

$g'(x) =$

(b)  $g(y) = \int_x^\pi \sqrt{1 + \sec t} dt$

$g'(y) =$

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**Problem 6** (10 pts). Find the antiderivative  $F$  of  $f(x) = 4 - 3(1 + x^2)^{-1}$  that satisfies  $F(1) = 0$ .

**HINT:** You need to use the constant of integration.

$F(x) =$