

**Name:** \_\_\_\_\_

**VIP ID:** \_\_\_\_\_

- Write your name and VIP ID in the space provided above.
  - The test has four (4) pages, including this one.
  - Enter your answer in the box(es) provided.
  - You must show sufficient work to justify all answers unless otherwise stated in the problem. Correct answers with inconsistent work may not be given credit.
  - Credit for each problem is given in parentheses at the right of the problem number.
  - No books or notes may be used on this test.
  - An approved calculator may be used on this test.
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Page	Max. points	Your points
2	30	
3	49	
4	21	
<b>Total</b>	100	

**Problem 1.** (5 pts each) Find the derivative of the following functions:

(a)  $f(x) = 56$

$$f'(x) =$$

(b)  $y = t + \sqrt{t}$

$$y'(t) =$$

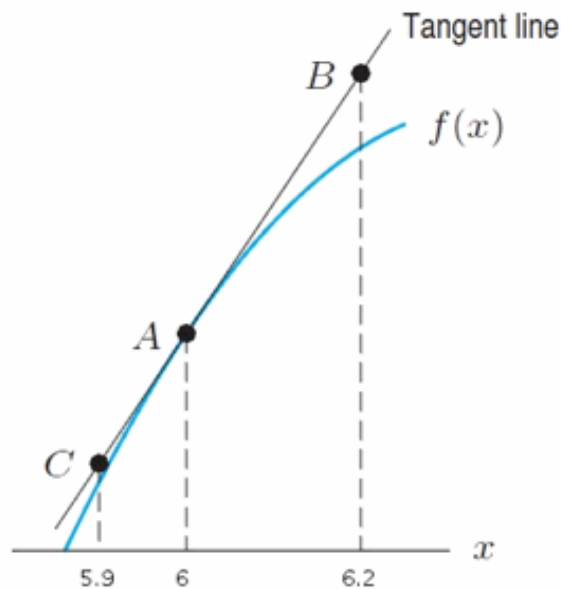
(c)  $f(x) = e^x + 2^x + 3 \cdot 3^x$

$$f'(x) =$$

(d)  $f(x) = \ln x - \ln \pi$

$$f'(x) =$$

**Problem 2** (10 pts). The function in the figure below has  $f(6) = 31$  and  $f'(6) = 2.1$ . Find the coordinates of the points  $A$ ,  $B$  and  $C$ .



$$A = ( \quad , \quad ), \quad B = ( \quad , \quad ), \quad C = ( \quad , \quad )$$

**Problem 3.** (7 pts each) Find the derivative of the following functions:

(a)  $f(x) = \sqrt{\frac{1}{x^{39}}}$

$f'(x) =$

(b)  $y = 6t^5 - 10\sqrt{t} + \frac{9}{t}$

$y'(t) =$

(c)  $f(x) = (2^x + x^5)(3 - \ln x)$

$f'(x) =$

(d)  $f(x) = \frac{x^8 + 2}{x}$

$f'(x) =$

(e)  $f(x) = \ln(8 - e^{-x})$

$f'(x) =$

(f)  $f(x) = (6 + \ln x)^{0.6}$

$f'(x) =$

(g)  $f(x) = 2e^{7x} + e^{-x^6}$

$f'(x) =$

**Problem 4** (7 pts). Find an equation for the tangent line to the graph of  $f(x) = 3x^2 - 5x + 6$  at  $x = 1$ .

 $y =$ 

**Problem 5** (7 pts). Find an equation for the tangent line to the graph of  $f(x) = (2x^2 - 1)(3x + 4)$  at  $x = 0$ .

 $y =$ 

**Problem 6** (7pts). The cost  $C$  (in dollars) to produce  $g$  gallons of a chemical can be expressed as  $C = f(g)$ . Using units, explain the meaning of the following statements in terms of the chemical.

(a)  $f(400) = 500$ .

The statement  $f(400) = 500$  means

(b)  $f'(400) = 6$

The statement  $f'(400) = 6$  means