

Problem 1. Write out the form of the partial fraction decomposition. (Do not find the numerical values of the coefficients.)

(a) $\frac{3x - 1}{(x - 3)(x + 4)}$

(b) $\frac{2x - 3}{x^3 - x^2}$

(c) $\frac{5}{x(x^2 - 4)}$

(d) $\frac{x^2}{(x + 2)^3}$

Problem 2. Evaluate the integral.

(a) $\int \frac{dx}{x^2 - 3x - 4}$

(b) $\int \frac{dx}{x^2 - 6x - 7}$

(c) $\int \frac{11x + 17}{2x^2 + 7x - 4} dx$

(d) $\int \frac{dx}{x(x^2 - 1)}$

(e) $\int \frac{x^2 - 8}{x + 3} dx$

(f) $\int \frac{x^2 + 1}{x - 1} dx$

(g) $\int \frac{3x^2 - 10}{x^2 - 4x + 4} dx$

(h) $\int \frac{x^2}{x^2 - 3x + 2} dx$

Problem 3. Evaluate the integral by making a substitution that converts the integrand to a rational function.

(a) $\int \frac{\cos \theta}{\sin^2 \theta + 4 \sin \theta - 5} d\theta$

(b) $\int \frac{e^t}{e^{2t} - 4} dt$