

Name: \_\_\_\_\_

4-digit code: \_\_\_\_\_

- Write your name and the last 4 digits of your SSN in the space provided above.
- The test has six (6) pages, including this one.
- Enter your answers in the boxes provided.
- You must show sufficient work to justify all answers unless otherwise stated in the problem. Correct answers with inconsistent work may not be given credit.
- Credit for each problem is given in parentheses at the right of the problem number.
- No books, or notes may be used on this test. Calculators are OK.

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Page	Max. points	Your points
2	20	
3	20	
4	20	
5	20	
6	20	
<b>Total</b>	100	

**Problem 1** (5 pts—all or nothing). Find the domain of  $f(x) = \sqrt{(1-x)(2-x)}$ .

domain =

**Problem 2** (5 pts—all or nothing). Let  $f(x) = x^2 + 4$ ,  $g(x) = \sqrt{x}$ . Find  $g \circ f$

$(g \circ f)(x) =$

**Problem 3** (5pts). Evaluate the following limit:

$$\lim_{n \rightarrow \infty} \sum_{k=1}^n \frac{5k}{n^2}$$

**Problem 4** (5 pts). Assume  $y$  is a function of  $x$  given implicitly by  $\sin(x+y) = x+y$ . Find  $y'$ .

**Problem 5** (10 pts). Use logarithmic differentiation to find the derivative of the function

$$y = \frac{\tan^2 x \sin^4 x}{e^{3x}(x^2 + 1)}$$

$y' =$

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**Problem 6** (10 pts). Find an equation of the tangent line to the curve  $y = \ln(xe^x)$  at the point  $(1, 1)$ .

**Problem 7** (20 pts). Sketch the graph of the rational function  $f(x) = \frac{x^2}{1 - x^2}$ .

Indicate clearly: Domain;  $x$ - and  $y$ -intercepts; vertical and horizontal asymptotes; intervals of increase, decrease and different concavity. Indicate also the location of relative extrema and inflection points, if any.

**Problem 8** (10 pts). The volume of a cube is increasing at a rate of  $300 \text{ cm}^3/\text{min}$ . How fast are the edges increasing when the length of an edge is 10 cm?

The edges are increasing at a speed of

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**Problem 9** (10 pts). A farmer wants to fence an area of 1.5 million square feet in a rectangular field and then divide it in half with a fence parallel to one of the sides of the rectangle. How can he do this so as to minimize the cost of the fence?

Dimensions of most economic fence:

**Problem 10** (1/2/3/4 pts). Compute the following limits:

(a)  $\lim_{x \rightarrow -\infty} \frac{x^2 - 2x - 8}{x^2 - 4} =$

(b)  $\lim_{x \rightarrow 2} \frac{x^2 + 2x - 8}{x^2 - 4} =$

(c)  $\lim_{x \rightarrow -2} \frac{x^2 - 2x - 8}{x^2 - 4} =$

(d)  $\lim_{x \rightarrow 0} x^{1/x} =$

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**Problem 11** (3/3/4 pts). Evaluate each integral:

(a)  $\int \left( \frac{1}{x} - 2^x \right) dx =$

(b)  $\int (3 \sin x - 2 \cos x) dx =$

(c)  $\int_1^2 \left( 5x + \frac{2}{3x^5} - \sqrt{2}e^x \right) dx =$