

***1 – Exercise (7 points)***

A IEEE 802.15.4 network is composed of a PAN Coordinator and two motes. Each mote is assigned 2 slots in the Collision Free Part for uplink traffic, and the PAN coordinator is assigned 4 slots in the CFP for downlink traffic (two slots dedicated to each one of the two motes). Each slot can carry packets of 128 [byte]. The nominal rate is  $R=125$  [kb/s] and the active part is composed of the beacon slot and the CFP only. The network is operated with a duty cycle  $\eta=10\%$ . The motes and the PAN coordinator have the following traffic pattern:

- Mote 1 generates packets towards the PAN coordinator according to a Poisson process with parameter  $\lambda_1=0.01$  [packets/s]
- Mote 2 generates packets towards the PAN coordinator according to a Poisson process with parameter  $\lambda_2 = 0.5$  [packet/s]
- The PAN coordinator generates packets toward each one of the two motes according to a Poisson process with parameter  $\lambda_3 = 0.1$  [packet/s]

Find (i) the duration of the Beacon Interval, (ii) the duration of a slot, (iii) the average energy consumed by the PAN coordinator Mote 1 assuming  $E_{rx} = 1$  [uJ],  $E_{tx}=3$  [uJ],  $E_{idle} = 0.5$  [uJ] and  $E_{sleep} = 1$  [nJ] to be respectively the energy for receiving, transmitting (circuitry + emitted power), being idle and sleeping in a slot.

**The slot duration is  $T_s=128[\text{byte}]/125$  [kb/s]= 8.192[ms].**

**The CFP is composed of  $N_{cfp} = 2 \times 2 + 4 = 8$  slots.**

**The active part is  $N_{active}=N_{cfp} + 1 = 9$  slots and its duration is  $T_{active}=N_{active} \times T_s = 73.728$  [ms].**

**The Beacon Interval is:  $BI= T_{active}/ \eta =737.28$  [ms].**

**The number of slots in the inactive part is  $N_{inactive}= (BI-T_{active})/T_s = 81$ .**

**The probability that Mote 1 are respectively:**

$$P_0= e^{-\lambda_1 BI}$$

$$P_1= -\lambda_1 BI e^{-\lambda_1 BI}$$

$$P_{>=2}=1 - P_0 - P_1$$

**The average energy consumed by the Mote 1 in a BI is:**

$$E = E_{rx} + 6E_{idle} + P_0 2 E_{idle} + P_1 (E_{tx} + E_{idle}) + P_{>=2} 2 E_{tx} + 81 E_{sleep}$$

A IEEE 802.15.4 network is composed of a PAN Coordinator and two motes. Each mote is assigned 2 slots in the Collision Free Part for uplink traffic, and the PAN coordinator is assigned 4 slots in the CFP for downlink traffic (two slots dedicated to each one of the two motes). Each slot can carry packets of 128 [byte]. The nominal rate is  $R=250$  [kb/s] and the active part is composed of the beacon slot and the CFP only. The network is operated with a duty cycle  $\eta=1\%$ . The motes and the PAN coordinator have the following traffic pattern:

- Mote 1 generates packets towards the PAN coordinator according to a Poisson process with parameter  $\lambda_1=0.01$  [packets/s]
- Mote 2 generates packets towards the PAN coordinator according to a Poisson process with parameter  $\lambda_2 = 0.5$  [packet/s]
- The PAN coordinator generates packets toward each one of the two motes according to a Poisson process with parameter  $\lambda_3 = 0.1$  [packet/s]

**The slot duration is  $T_s=128[\text{byte}]/250$  [kb/s]= 4.096[ms].**

**The CFP is composed of  $N_{cfp} = 2 \times 2 + 4 = 8$  slots.**

**The active part is  $N_{active}=N_{cfp} + 1 = 9$  slots and its duration is  $T_{active}=N_{active} \times T_s = 36.864$  [ms].**

**The Beacon Interval is:  $BI= T_{active}/ \eta =368.64$  [ms].**

**The number of slots in the inactive part is  $N_{inactive}= (BI-T_{active})/T_s = 891$ .**

**The probability that Mote 1 are respectively:**

$$P_0= e^{-\lambda_1 BI}$$

$$P_1= -\lambda_1 BI e^{-\lambda_1 BI}$$

$$P_{>=2}=1 - P_0 - P_1$$

**The average energy consumed by the Mote 1 in a BI is:**

$$E = E_{rx} + 6E_{idle} + P_0 2 E_{idle} + P_1 (E_{tx} + E_{idle}) + P_{>=2} 2 E_{tx} + 891 E_{sleep}$$

**2 – Exercise (4 points)**

Find the average efficiency of Dynamic Frame ALOHA collision resolution protocol with an initial population of  $n=3$  tags and an initial frame size  $r=2$ . Assume that the size of the frames after the first one is “optimally” set to the current backlog.

**Applying the recursive formula we get:**

$$L_3 = 2 + \sum_{i=0}^2 P(S=i) L_{3-i}$$

$$L_3 = 2 + P(S=0)L_3 + P(S=1)L_2 + P(S=2)L_1$$

**Knowing that,  $P(S=0) = 1/4$ ,  $P(S=2) = 0$ ,  $P(S=1) = 3/4$ , we obtain:**

$$L_3 = 2 + \frac{1}{4}L_3 + \frac{3}{4}L_2$$

**Iteratively**

$$L_2 = 2 + P(S=0)L_2 + P(S=1)L_1$$

**$P(S=0)=1/2$ ,  $P(S=1)=0$ , which leads to  $L_2=4$ .**

**Substituting the value of  $L_2$  in the first expression we get:**

**$L_3 = 2 + 1/4L_3 + 3/4 \times 4$ , that is  $L_3 = 20/3$**

**The efficiency is  $\eta = 9/20$ .**

Find the average efficiency of Dynamic Frame ALOHA collision resolution protocol with an initial population of  $n=4$  tags and an initial frame size  $r=2$ . Assume that the size of the frames after the first one is “optimally” set to the current backlog.

**Applying the recursive formula we get:**

$$L_4 = 2 + P(S=0)L_4 + P(S=1)L_3 + P(S=2)L_2 + P(S=3)L_1$$

**$P(S=3)=P(S=2)=0$**

**$P(S=1)=P(S=0)=1/2$**

$$L_4 = 2 + 1/2L_4 + 1/2L_3$$

**Iterating**

$$L_3 = 3 + P(S=0)L_3 + P(S=1)L_2 + P(S=2)L_1$$

**$P(S=2)=0$**

**$P(S=0)=(1/3)^3 = 1/27$**

**$P(S=1)=(1/3)^3 \times 3 = 6/27$**

$$L_3 = 3 + 1/27L_3 + 6/27L_2$$

**$L_2=4$**

**$L_3=3+1/27L_3+6/27 \times 4$**

**$L_3=9/8 (3+24/9)=51/8$**

**$L_4=2+1/2L_4 + 1/2 \times 51/8$**

**$L_4=2 (2+51/4)=59/2$**  83/8

**$\eta=8/59$**  32/83

**3 – Exercise (6 points)**

A MQTT client (Client 1) is subscribed to the topic /humidity. The MQTT broker is connected to 2 additional MQTT clients which publish messages on the topic /humidity according to the following traffic processes:

- Client 2 publishes one message on topic /humidity according to a Poisson process with parameter  $\lambda = 10$  message/minute
- Client 3 publishes one message on topic /humidity according to a Poisson process with parameter  $\lambda = 2$  message/minute

Find the average energy consumed by the MQTT Client 1 in a time period of 1 hour in the two cases where the all the publish messages require QoS level 0 and 1. Clearly describe the message exchange session between the MQTT broker and Client 1 in the three cases.

Use the following parameters: energy for sending/receiving MQTT publish messages,  $E_{rx}=10[uJ]$ , energy for sending/receiving MQTT signaling messages (various ACK messages),  $E_{tx}= 3 [uJ]$ , energy for being idle  $E_{idle}=0[uJ]$ .

**Client 2 and Client 3 generate the following average number of messages per hour:**

**$M2= 10 [\text{message/minute}] \times 60 [\text{minutes}] = 600 \text{ messages}$**

**$M3 = 2 [\text{message/minute}] \times 60 [\text{minutes}] = 120 \text{ messages}$**

**The energy consumed by client 1 in the cases of QoS 0 and 1 are respectively:**

**$E0 = (M2+M3) E_{rx}$**

**$E1 = (M2+M3) (E_{rx}+ E_{tx})$**

A MQTT client (Client 1) is subscribed to the topic /humidity. The MQTT broker is connected to 2 additional MQTT clients which publish messages on the topic /humidity according to the following traffic processes:

- Client 2 publishes one message on topic /humidity according to a Poisson process with parameter  $\lambda = 10$  message/minute
- Client 3 publishes one message on topic /humidity according to a Poisson process with parameter  $\lambda = 2$  message/minute

Find the average energy consumed by the MQTT Client 1 in a time period of 1 hour in the two cases where the all the publish messages require QoS level 1 and 2. Clearly describe the message exchange session between the MQTT broker and Client 1 in the three cases.

Use the following parameters: energy for sending/receiving MQTT publish messages,  $E_{rx}=10[uJ]$ , energy for sending/receiving MQTT signaling messages (various ACK messages),  $E_{tx}= 3 [uJ]$ , energy for being idle  $E_{idle}=0[uJ]$ .

**Client 2 and Client 3 generate the following average number of messages per hour:**

**$M2= 10 [\text{message/minute}] \times 60 [\text{minutes}] = 600 \text{ messages}$**

**$M3 = 2 [\text{message/minute}] \times 60 [\text{minutes}] = 120 \text{ messages}$**

**The energy consumed by client 1 in the cases of QoS 1 and 2 are respectively:**

**$E1 = (M2+M3) (E_{rx}+ E_{tx})$**

**$E1 = (M2+M3) (E_{rx}+ 3E_{tx})$**

### 3 – Questions (9 points)

1. Tell if the following statements are true or false. **MOTIVATE THE ANSWER. UNMOTIVATED ANSWER WILL NOT BE CONSIDERED**

- The IEEE 802.15.4 MAC layer is based only on random access procedures. **FALSE**
- The Schoute's estimate provides an estimate of the total number of already resolved tags. **FALSE**
- RPL uses a reactive approach. **FALSE**

A wireless link is characterized by the following parameters: packet error rate in both directions,  $p = 0.01$ , packets size,  $L=100[\text{byte}]$ , acknowledgment size=  $10[\text{byte}]$ , data rate,  $R=100[\text{kb/s}]$ , propagation delay,  $t=5[\mu s]$ . Find the Expected Transmission Time (ETT) for the link.

2 alternatives considered correct

$ETX=1/(1-p)$

$ETX=1/(1-p)^2$

$$RTT = L/R + l_{ack}/R + 2t$$
$$ETT = ETX \times RTT$$

A wireless link is characterized by the following parameters: packet error rate in both directions,  $p = 0.05$ , packets size,  $L = 100$ [byte], acknowledgment size = 5[byte], data rate,  $R = 200$ [kb/s], propagation delay,  $t = 5$ [us]. Find the Expected Transmission Time (ETT) for the link.

2 alternatives considered correct

$$ETX = 1/(1-p)$$

$$ETX = 1/(1-p)^2$$

$$RTT = L/R + l_{ack}/R + 2t$$

$$ETT = ETX \times RTT$$