

**Sample statistic:** a sample characteristic such as a sample mean  $\bar{x}$ , sample standard deviation  $s$ , sample proportion  $\bar{p}$ , etc. The value of the stat is used to estimate the value of the corresponding population parameter. **Sampling distribution:** a probability distribution consisting of all possible values of a sample statistic. **Point estimator:** The sample statistic that provides the point estimate of the population parameter. We refer to the sample mean as the point estimator of the population mean, the sample standard deviation  $s$  as the point estimator of the population standard deviation and the sample proportion as the point estimator of the population proportion  $p$ . The numerical value obtained is called the point estimate.  $\mu$  = population mean. **Central Limit Theorem:** in selecting random samples of size  $n$  from a population the sampling distribution of the sample mean  $\bar{x}$  or proportion  $\bar{p}$  can be approximated by a normal distribution as sample size become large (typically  $n \geq 30$ ). **Recall**  $\bar{p} = x/n$ ,  $x$ =# of elements of interest in the sample,  $n$ =sample size,  $N$ =population. **Sampling Distribution of  $\bar{p}$ :** the probability distribution of all the possible values of the sample proportion,  $\bar{p}$ .

Expected Value of $\bar{p}$	Standard Deviation of $\bar{x}$ (Standard Error)	Standard Deviation of $\bar{x}$ (Standard Error)	Standard Deviation of $\bar{p}$ (Standard Error)	Standard Deviation of $\bar{p}$ (Standard Error)
$E(\bar{p}) = p$	<i>Finite Population</i>	<i>Infinite Population</i>	<i>Finite Population</i>	<i>Infinite Population</i>
Expected Value of $\bar{x}$	$\sigma_{\bar{x}} = \sqrt{\frac{N-n}{N-1}} \left( \frac{\sigma}{\sqrt{n}} \right)$	$\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}}$	$\sigma_{\bar{p}} = \sqrt{\frac{N-n}{N-1}} \sqrt{\frac{p(1-p)}{n}}$	$\sigma_{\bar{p}} = \sqrt{\frac{p(1-p)}{n}}$
$E(\bar{x}) = \mu$	Use when $n/N > .05$		Use when $n/N > .05$	

**Interval Estimate (aka Confidence Interval):** an estimate of a population parameter that provides an interval believed to contain the value of the parameter. **Margin of Error:** the  $\pm$  value added and subtracted from a point estimate to develop an interval estimate.

**Interval Estimate, General Form: Point Estimate  $\pm$  Confidence Coeff. \* Std Error** [together = Margin of Error]. **Sigma  $\sigma$  Known:** historical data or other info provide a good value for the population standard deviation prior to sampling. **Confidence level:** if an interval estimation procedure provides intervals such that 95% of the intervals formed using the procedure will include the population parameter, the interval is said to be constructed with 95% confidence. **Confidence Coefficient:** the confidence level expressed as a decimal. **Level of Significance:** the probability that an interval estimate will generate an interval that does not contain the population parameter. **Alpha  $\alpha$  = 1 – Confidence Coeff.** **Sigma  $\sigma$  Unknown:** the more common case when no good basis exists for estimating the population standard deviation prior to taking the sample. **T-distribution:** a family of probability distributions that can be used to say things about a population mean whenever population standard deviation is unknown. **Degrees of Freedom:** a parameter of the t-distribution based on sample size  $n$ .  $df = n - 1$ . **Converting to Standard Normal Random Variable:**  $Z = (x - \text{Mean}) / \text{Std Dev}$   
 Lookup z score in Prob table. Resulting value is the probability.

Interval Estimate of a Population Mean: $\sigma$ Known		Values for Common Confidence Levels			
		Confidence Level	$\alpha$	$\alpha/2$	$z_{\alpha/2}$
$\bar{x} \pm z_{\alpha/2} \frac{\sigma}{\sqrt{n}}$		90%	.10	.05	1.645
		95%	.05	.025	1.960
		99%	.01	.005	2.576
Interval Estimate of a Population Proportion		Interval Estimate of a Population Mean: $\sigma$ Unknown			
$\bar{p} \pm z_{\alpha/2} \sqrt{\frac{\bar{p}(1-\bar{p})}{n}}$		$\bar{x} \pm t_{\alpha/2} \frac{s}{\sqrt{n}}$			

### Steps of Hypothesis Testing:

- Step 1:** Develop the null and alternate hypothesis
- Step 2:** Specify the level of significance ( $\alpha$ )
- Step 3:** Collect the sample data and compute the value of the test statistic  
*p-Value Approach*
- Step 4:** Use the test statistic to compute the p-value
- Step 5:** Reject  $H_0$  if the p-value  $\leq \alpha$
- Step 6:** Interpret the statistical conclusion in the context of the application

**Hypothesis Test:** a statistical argument to show evidence of a theory about a population using sample data. Five parts:

1. **Hypotheses:**  $H_0$ : null hypothesis, opposite of the alternative.  $H_a$ : alternative hypothesis, what we are trying to prove.
2. **Test Statistic:** a formula that we plug our sample data into and get out one number.
3. **p Value:** a probability
4. **Rejection Rule:** Reject  $H_0$  if p value  $\leq \alpha$  (significance level)

5. **Conclusion:** Reject  $H_0$ , we can conclude  $H_a$ . **OR** Do not reject  $H_0$ , we cannot conclude  $H_a$ .

**Type I Error:** the error of rejecting  $H_0$  when it is true. **Type II Error:** the error of not rejecting  $H_0$  when it is false.

**Level of Significance:** tolerance for a Type I error. Often set at alpha  $\alpha = .05$

### Summary of Hypothesis test about a Mean: $\sigma$ Known

	Lower Tail Test	Upper Tail Test	Two Tailed Test
Hypothesis:	$H_0: \mu \geq \mu_0$ $H_a: \mu < \mu_0$	$H_0: \mu \leq \mu_0$ $H_a: \mu > \mu_0$	$H_0: \mu = \mu_0$ $H_a: \mu \neq \mu_0$
Test Statistic:	$z = \frac{\bar{x} - \mu_0}{\sigma/\sqrt{n}}$	$z = \frac{\bar{x} - \mu_0}{\sigma/\sqrt{n}}$	$z = \frac{\bar{x} - \mu_0}{\sigma/\sqrt{n}}$
<b>p-value Approach:</b> p-value	$P(Z < z)$	$1 - P(Z < z)$	$2P(Z < z)$ or $2(1 - P(Z < z))$ whichever is smaller
Rejection Rule	Reject $H_0$ if p-value $\leq \alpha$	Reject $H_0$ if p-value $\leq \alpha$	Reject $H_0$ if p-value $\leq \alpha$

### Summary of Hypothesis Tests about a Population Mean: **Sigma $\sigma$ Unknown**

	Lower Tail Test	Upper Tail Test	Two Tailed Test
Hypothesis:	$H_0: \mu \geq \mu_0$ $H_a: \mu < \mu_0$	$H_0: \mu \leq \mu_0$ $H_a: \mu > \mu_0$	$H_0: \mu = \mu_0$ $H_a: \mu \neq \mu_0$
Test Statistic:	$t = \frac{\bar{x} - \mu_0}{s/\sqrt{n}}$ With n-1 df	$t = \frac{\bar{x} - \mu_0}{s/\sqrt{n}}$ With n-1 df	$t = \frac{\bar{x} - \mu_0}{s/\sqrt{n}}$ With n-1 df
<b>p-value Approach:</b> p-value	$P(T > t)$	$P(T > t)$	$2P(T > t)$
Rejection Rule	Reject $H_0$ if p-value $\leq \alpha$	Reject $H_0$ if p-value $\leq \alpha$	Reject $H_0$ if p-value $\leq \alpha$

### Summary of Hypothesis Tests About a Population Proportion

	Lower Tail Test	Upper Tail Test	Two-Tailed Test
Hypotheses	$H_0: p \geq p_0$ $H_a: p < p_0$	$H_0: p \leq p_0$ $H_a: p > p_0$	$H_0: p = p_0$ $H_a: p \neq p_0$
Test Statistic	$z = \frac{\bar{p} - p_0}{\sqrt{\frac{p_0(1-p_0)}{n}}}$	$z = \frac{\bar{p} - p_0}{\sqrt{\frac{p_0(1-p_0)}{n}}}$	$z = \frac{\bar{p} - p_0}{\sqrt{\frac{p_0(1-p_0)}{n}}}$
Rejection Rule:	Reject $H_0$ if p-value $\leq \alpha$	Reject $H_0$ if p-value $\leq \alpha$	Reject $H_0$ if p-value $\leq \alpha$
p-Value Approach			