

## Todo list

Summarize the paper in a paragraph of two. It should contain at least 70 and at most 150 words. You should motivate the research done, give some details about the experiments run and briefly mention the most important findings. ....	1
Perform a literature review: What has been done before in this field? What is the main technique/s used in the paper, and what has it/they been used for in the literature before? Give references to the most relevant work published. Example: [2]. ....	1
any picture? .....	3
[maybe picture from his paper and pseudocode] .....	4
write the rest. ....	4
Detail the experimental setup used to test the different algorithms. Present the results in an understandable manner (graphics, tables, etc.). Draw conclusions about what things worked (and why) and which didn't (and why). ...	11
combinations really failed. explain it. ....	11
why we use this parameters??? something is missing...why not an exhaustive search for finding the best parameter..no time? to less computational power...	11
Explain the main contributions of this work: what are the most important findings. Finally, explain how could this work be extended. What would be the next steps? .....	15



# Computational Intelligence in Games

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**Abstract.**

## 1 Introduction

Due to the fact that the game industry was growing over the past years [4] constructing good game artificial intelligences Artificial Intelligence (AI) comes more and more important. Normally a game AI is created for one specific game. Often if humans play against enemies there are different levels of difficulties that could adjusted for example easy, middle and hard. Our aim of the course "Computational Intelligence in Games"<sup>1</sup> at the Otto-von-Guericke-University Magdeburg in Germany<sup>2</sup> was to evaluate three different approaches on the General Video Game AI Competition<sup>3</sup>. The game AI should play unknown games as effectively as possible. The agent can observe the whole grid with game objects that are moving. Besides he gets information of all the collision that happened. Moreover the agent has 40 ms for each game step to act. All actions - depending on the game - are LEFT, UP, RIGHT, DOWN, USE and NIL. To find the best action the agent could simulate steps and so predict the next state. But there is uncertainty because the game objects move randomly.

All this facts form a complex problem to solve. The agent should play tight in order to win most of the games as fast as possible. Before each of the games is starting the aim of the controller is unknown. Therefore he should dynamically find out what is the target of the current game.

In this paper we introduce three general approaches for a game AI. Therefore we first outline our literature review and explain after that the background. The theory could not always be implemented like it was proposed because it has to fit the requirements of the games. For this reason we explain at the chapter 4 the details of our implementations. Then we evaluate first the best parameters of each approach and thereafter find out which agent is our winner.

## 2 Literature Review

<sup>1</sup> <http://is.cs.ovgu.de/Courses/Team+Projects/Computational+Intelligence+in+Games.html>

<sup>2</sup> <http://www.ovgu.de/>

<sup>3</sup> <http://www.vgcai.net/>

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Perform a literature review: What has been done before in this field? What is the main technique/s used in the paper, and what has it/they been used for in the literature before? Give references to the most relevant work published. Example: [2].

### 3 Background

In this project we were forced to investigate different ideas at three different research areas: heuristic based search, reinforcement learning and nature inspired algorithm. Of course there is an overlap between these approaches. All of them try to find the next best step for the agent by iterating through a search tree. This is build in base of all possible game steps that could done by the agent. One naive approach of iterating through the whole search tree is not possible cause of the time limitation. Generally this leads to find the trade-off between iterating similar to a breadth-first or depth-first search. First of all we introduce an depth-first approach that uses an estimation function for looking many steps ahead.

#### 3.1 Heuristic Based Search

A Heuristic (HR) is used to evaluate a game state by putting several facts into one number. When we have to decide which current active branch of a search tree should be iterated this score might help us. One common idea to estimate the distance to the target is the manhattan distance [1].

In a two dimensional space the manhattan distance is calculated by

$$dist(u, v) = |x_1 - x_2| + |y_1 - y_2| \quad (1)$$

adding the absolute value of the difference for the  $x$  and the  $y$  axis. The input consists always of the points that have one value for each dimension. This could be extended for a  $n$ -dimensional space as well. When thinking of a way at a grid this is always a path with one rectangle waypoint (cf. fig. 1).

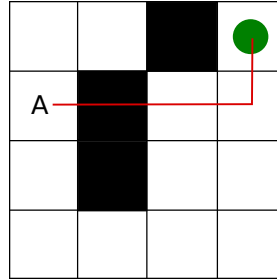


Fig. 1: Manhattan distance

**3.1.1 Greedy** Greedy-algorithms are a whole class of algorithms and strategies. All of them follow a specific scheme/rule. They are iterative and choose in every step the state with the best reward. The state is in most cases a node which represents the state of the algorithm. The advantage of greedy algorithms is that they are very fast but on the other hand they are not optimal they often only find a local optima and not the global one. The advantage and disadvantage is caused by the greedy approach.

**3.1.2 One Step Lookahead** One step lookahead is a very simple tree search algorithm which follows the greedy approach. The actual state is the root node. From this node we only look one step ahead to all nodes which are connected by one edge and compute a heuristic value or another kind of reward value for these nodes (cf. fig. 2).

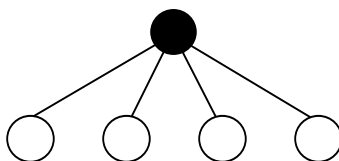


Fig. 2: Search tree for One Step Lookahead

After that the algorithm terminates and we pick the node with the best heuristic value. This algorithm is a special greedy approach that is limited by the first level at the search tree.

**3.1.3 AStar** The A\* tree search algorithm is a modification of the dijkstra algorithm and also belongs to the class of greedy algorithms. The Algorithm finds the shortest path between two nodes. In difference to normal greedy algorithms A\* is an optimal algorithm, it finds a solution when a solution exists (in this case the shortest path). The algorithm uses a heuristic to estimate the shortest path. The value  $f(x)$  of a node N is the sum of its heuristic value  $h(x)$  and the costs from the start-node to N  $g(x)$ .

$$f(x) = h(x) + g(x) \quad (2)$$

any picture?

A\* contains two sets of nodes, the openlist and the closedlist. In every step of the algorithm the Node N with the lowest  $f(x)$  value in the openlist is put on the closedlist and all its connected nodes, which are not in the closedlist, are put in the openlist (with reference to their father N). If a connected node is already in the closedlist but the new generated value  $f'(x)$  is lower than  $f(x)$  then  $f(x)$  will be replaced by  $f'(x)$  and the new father-reference is N. The openlist contains all the nodes to which the path is already known and which can be checked in the next step, the closedlist contains every visited and checked node. When the actual node is the goal-node, the algorithm terminates. To generate the path, the algorithm goes back from the goal-node to the start node (guided by the father-references).

## 3.2 Reinforcement learning

Reinforcement Learning (RL) is a field in Machine learning which is a section of Artificial Intelligence. RL methods are mostly used by agents in an environment called Markov Decision Process (MDP). MDP is a mathematical description of decision processes. They have different states S and some actions A which are available in the actual

state. Every timestep the agent chooses an action  $a$  and the process switches from state  $s_a$  to  $s_n$ . The probability to go over from a state  $S$  to another state  $S'$  by any action  $A$  can be described as

$$G : S * S * A \rightarrow [0, 1] \quad (3)$$

and the reward given to the agent can be described by this:

$$R : S * S * A \rightarrow \mathbb{R} \quad (4)$$

So that

$$(s_a, s_n, a) \rightarrow p(s_n | s_a, a) \quad (5)$$

would describe the probability  $p$  to go over in the state  $s_n$ , given the actual state  $s_a$  and the chosen action  $a$  and

$$(s_a, s_n, a) \rightarrow r \quad (6)$$

shows its corresponding reward.

In differ to other learn methods and approaches like the (semi)supervised learning, RL algorithms never use information which they do not figured out themselves, so no correct samples were given to the algorithm. The only information is the reward given to the agent and some additional information like heuristic values, depending of the specific algorithm. A big problem problem in **RL** is the conflict between exploration of new and unvisited areas of the solution room and exploitation which is the improvement of already found solutions. ...

**3.2.1 Monte Carlo Tree Search** Monte Carlo Tree Search (**MCTS**) is a class of **RL** algorithms. It is the most important concept in this paper. **MCTS** needs a tree of nodes which represent the different states, the edges represent the actions used by the agent to get to this node. The **MCTS** algorithm traverses to this tree and expands it. To find the global optimum a good balancing ratio between exploration and exploitation is required.

[maybe picture from his paper and pseudocode]

The general **MCTS** algorithm has four steps, selection, expansion, simulation and backpropagation. In the selection the algorithm starts at

write the rest.

### 3.3 Nature inspired

The nature is solving problems by applying different approaches instinctively. Computer scientists used that observed knowledge from the nature to write Nature Inspired (**NI**) algorithms that has a similar procedure. Our brain could solve problems that could not be solved by an algorithm until now. Funnily this is often the truth for games for example poker.

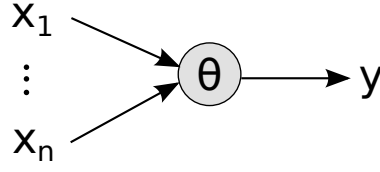


Fig. 3: TLU [5]

**3.3.1 Neural nets** Many researcher try to explore the process of the human brain. Neural networks tries to model the nervous system and to adapt all the processes [6]. The neurons are modeled as Threshold Logic Unit (TLU) that consists of several input values  $x_1$  to  $x_n$  and one output value  $y$  [5].

For computing the output value is always for every input value one weight  $w_i$  and the threshold  $\theta$ . The formula

$$y = \begin{cases} 1, & \text{if } \sum_{i=1}^n w_i x_i \geq \theta, \\ 0, & \text{otherwise.} \end{cases} \quad (7)$$

is used to calculate the output  $y$  that is either 0 or 1. Normally the weights are learned by a given input and output. With only one TLU only linear separable spaces could be learned perfectly. To solve that problem there is the possibility to create a network of TLUs and map that problem to a higher dimensional space [5].

**3.3.2 Evolutionary algorithm** An Evolutionary Algorithm (EA) tries to use the biological behavior of the population [3]. This algorithms follow two main ideas. Firstly there are operators like the recombination (crossover) or mutation that allows to create different individuals. Secondly every iteration is a selection to guarantee a good quality. The procedure is shown at the algorithm 1.

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**Algorithm 1** Evolutionary Algorithm [3]

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*Initialize* Population with random candidate solutions;  
*Evaluate* each candidate;  
**while** Termination condition not satisfied **do**  
    *Select* parents;  
    *Recombine* pairs of parents;  
    *Mutate* the resulting offspring;  
    *Evaluate* new candidates;  
    *Select* individuals for the next generation;  
**end while**

---

First of all there is the initialization phase to create a pool with random individuals. After that the score of each of them has to be evaluated. Often there is a problem for

optimization problems with a fast evaluation. This duration is strictly linked with the duration of the whole algorithm.

The while loop needs to have a termination condition. On the one hand this could be a predefined score that the best individual in one generation could have. On the other hand it could be a time limit that should not be exceeded. Every iterations starts with a selection of the parents. These are used to create new individuals by performing crossovers and mutations. The challenge is made of finding good functions for that operations. Since the pool size is limit there is a selection of the fittest in every iteration.

Often evolutionary algorithms are used for optimization problems because there hopefully better than a random search.

## 4 Techniques Implemented

After explaining the theory of several approaches we now describe our implementations. The proposed algorithm are not always fitting to the principle of the games or has a lot of parameter that has to be adjusted to have good results. We first point out some basic strategies for example staying alive.

### 4.1 Stay Alive

We implemented two different Stay Alive Agents that has the aim just to act safe and hopefully randomly win the game. Even if there is the possibility to simulation an action, there is all the time an uncertainty. All objects of the games in our competition could - but has not - to act randomly. If we are using the *advance* function that allows us to simulate one step that just one possible state of the future. This implies even if we are not dying at our simulation we could die at the real game.

One approach is to simulate the next action  $n$  times. If the agent does not die for this simulations the next action should be safe. The problem is to set a good value for  $n$ . If the value is too large not all the possible actions could be tested. Otherwise if it's too small the probability that it's even unsafe grows. From the resulting safe action set there could be randomly chosen the final action.



Fig. 4: Advancing safe actions

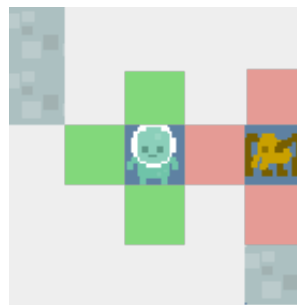


Fig. 5: Grid search for safe actions



Suppose there is a game situation like in fig. 4 the action *RIGHT* is definitely unsafe what should after an amount of  $n$ -action be clear.

Another idea is to analyse the grid around the agent. Assume that each enemy could only move one field at the grid at one game step there is a  $5 \times 5$  grid that needs to be analyzed. If an enemy at this grid exists one action is maybe unsafe. If not the enemy won't die for sure.

At the fig. 5 you can see the action that could be excluded without doing any simulation at the game. The possible next fields (excluded the current position if agent does nothing) are marked green. The possible positions of the enemy are red. The action *RIGHT* is by using the grid search unsafe. At first glance it looks faster and better to only look at the grid, but there might be some problems for unknown games:

- One problem is to classify the game objects at the grid. The grid search is only good if we know that this objects represents an enemy. Otherwise we also classify walls as unsafe.
- Not every enemy could move to all directions. have a look at the figure

## 4.2 Heuristic based

If the action is only safe the will be the problem that no target is forced because the selection happens randomly. Therefore a heuristic is used to evaluate one state and get a score. When we previously know the game that would be one good approach. But whenever the game is unknown the result will be completely different. One heuristic could be very good for example where the agent could kill an enemy. But if in another game the enemy will kill us the heuristic let commit us suicide.

To fix that we had two different ideas. On the one hand we could implement a dynamic heuristic that is changing over time and learn from the environment. On the other hand there could be a third instance that we called *Explorer* that is learning from the environment and creating a knowledge-base. To use this idea always for further approaches we forced on the second idea.

During the construction time the agent only explores the environment. First of all he creates a list with all interesting targets that exists at the level. For all of them he sends pheromones into the grid and simulate until the agent dies. For all the simulation there is a global class the *Simulator* that automatically make inferences from the observations. The knowledge base is the environment class that contains information to blocking, scoring, winning and loosing game objects (sprites). This two classes follows the singleton pattern and could be created by using the factory (cf. fig. 6). Additional information that you can see at the figure is the game detection that is explained later and the field tracker that keeps information about all fields at the grid and how often the agent visited each one.

When the explorer find the winning or scoring objects a heuristic is initialized. We used a heuristic with that calculates the distance to one target by using the mannhattan distance. To reach this target we use an astar algorithm with three modifications.

Every game step the astar algorithm is executed from scratch even if we found the target in the last iteration. We use an safety approach for the first action to ensure the next action we maybe choose is safe. For that we use the principle of the stay alive agent. The astar algorithm needs to hold all the states in memory. This leads to a very fast growing

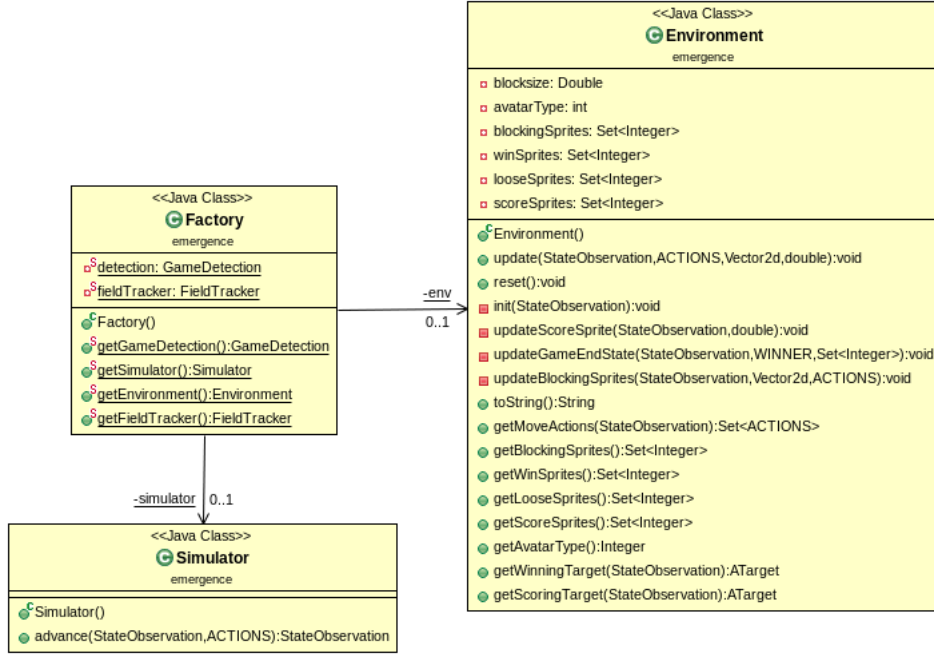


Fig. 6: Class diagram of the simulator and environment structure

open list with a lot of states. We introduce a *maxStates* variable. Whenever the open list of the astar algorithm is larger than this variable the list is cut in a half. Additionally we use for our simulations the simulator and use the knowledge base. Normally all children of a state are added to the open list. We only add all the children to the list of that we assume we will get a new position. Since we know from the Environment class which objects are blocking, we could use that information for a smarter iteration.

### 4.3 MCTS Tree

The theory of MCTS-treesearch is described in section 3. The standard approach was modified to fit our problem. The whole MCTS algorithm is computed in the class *MCTSStrategy* which is used by the *MCTSAgent* and the *MCTSHeuristicAgent*.

**4.3.1 tree policy** Our tree policy iterates through the tree, starting at the root node. When a node is not fully expanded, a randomly chosen children node is generated. We tried out some other ways to choose the children, but random selection worked best. If we reach a fully expanded node the tree policy uses a modified UCT formula

$$UCT = \frac{c.Q}{c.V + ep * r} + \sqrt{\frac{\ln(n.V + 1)}{c.V}} \quad (8)$$

to decide the children node. Where

```
double exploitation = child.Q / (child.visited + epsilon * r.nextDouble()); double
exploration = Math.sqrt(Math.log(n.visited + 1) / (child.visited));
```

\* The tree policy iterates through the tree, starting at the node n, until \* one node is not fully expanded. When a node is not fully expanded, it \* returns a random unexpected children of this node.

- tree policy
- default policy
- act choosig -i most visited node

#### 4.4 Evolutionary algorithm

The theory of the evolution has to be mapped to the gaming problem. Each candidate of our population is a list of actions that could be executed. To evaluate the fitness of a candidate we are using the simulation function that is provided by the game. The score

$$s = \sum_{t=0}^n (H(s_t) - H(s_{t-1})) \quad (9)$$

is calculated by using the function

$$H(s_i, s_{i-1}) = \begin{cases} 10, & \text{if isWinner} \\ -10, & \text{if isLooser} \\ score(s_i) - score(s_{i-1}), & \text{otherwise.} \end{cases} \quad (10)$$

what we called delta heuristic function.

We implemented two very naive operations on the pool. The crossover is done by select for 50 % the action of the first or the second individual (cf. fig. 7).

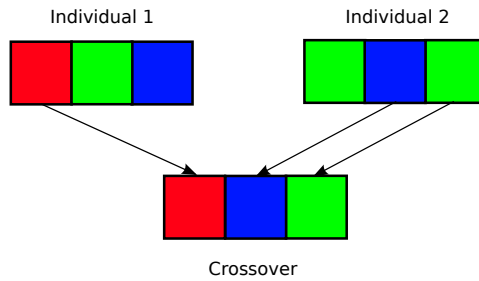


Fig. 7: Crossover of an individual

The mutation is implemented by doing an crossover with an random individual. We fixed for all evaluations runs the mutation probability to 0.7 which implies a crossover probability of 0.3.

We had several problems with the limited time for the evolution. For that we want to have always a good starting pool and use our information from the last game step. All candidates from the last final pool of the last game step are used for the initialization.

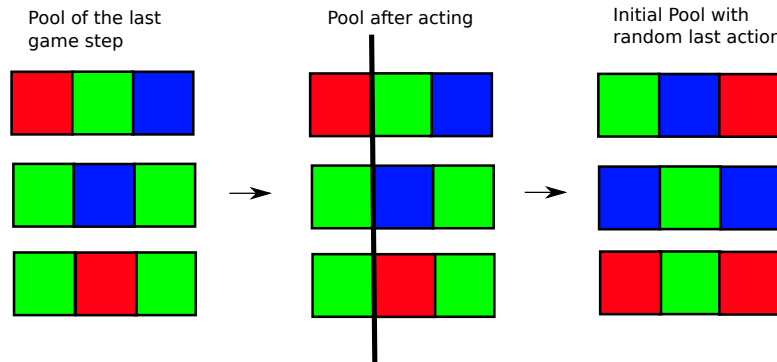


Fig. 8: Sliding Window

For that we use the principle of a sliding window (cf. fig. 8). The first action from the last pool is removed because the agent was acting like this at the last game step. Then to keep the action length fix there is added one random action to the action path. By using that principle we are not throwing our last simulations away.

There is also the problem that for different games the simulation time differs. If we have many game objects that need to be updated and checked for collision, the simulation time increases. But to find a good value for the pool size we need to know the calculation time. As a fix for this we introduced the adaptive path length that reduces or increases the actions of every individual. For that we forced to get always the fourth generation. On the one hand if we stay for example at the initial pool because the evaluation takes to long we will reduce the path length. On the other hand if the agents acts like the seventh generation we force to have a long time planing by increasing the path length.

Another problem that we tried to fix is to avoid situations where no individual has a positive score or many has a score of zero. That means each candidate is not gaining points. Our first implementations solved such a tie randomly. The randomness could be disabled by using a heuristic. If we would always use the same heuristic that would not work for all the games because they have different aims. So we used a heuristic switch after  $n$  time steps to have also a long time planing strategy.

#### 4.5 Game Detection

Another technique we have implemented is a detection of a known game. We know the 10 games from the test-set and the 10 games from the validation-set, the 10 test-set games are unknown. The Goal of the Gamedetection is to improve the score and the number of wins in the two known game-sets without decreasing the score and the number of wins in the unknown test-set. To do that, the standard parameters of the Algorithm

are used when no game is detected, otherwise the optimal parameters for this game are used. These parameters we figured out for some difficult games in which the standard parameters give bad results. To detect a game we generate a String of all Objects (npc, movable, immovable, ect...) and store the Hash value of this String. All the hashes from the known games are stored, in a running Game we generate another String of these Objects and compare the generated hash value to the stored ones.

## 5 Experimental Study

For computation only the following Machine was used.

CPU	4x Inted(R) Core(TM) i5-4210U CPU @ 1.70Ghz
Memory	8 GB DDR3 L
Operating System	Ubuntu 14.04.1 LTS

Only this machine was used because with the same agent and parameters we achived on different machines very different results. The computational power from the cpu was ?ausschlaggebend for our choice. The reason of the different results is that the agent every gametick only has 40ms to return an action. The results from a powerful CPU were better and more stable (the derivation was ?kleiner) than the results from an ?schlechter CPU. To evaluate the results we stored them in csv files and generated tables.

For every evaluation is first of all a table with all there parameter settings. Additionally there are the average winning rate and the standard deviation listed. All the results are also visualized by boxplots. There you can see the minimum and maximum average wins overall iterations. Furthermore the blue rectangle shows the qartile values. The red line in the middle is the median and the blue dot is the mean (average wins). Do not mix quartiles with the standard deviation that is something completely different.

In the following sections each of the approaches is evaluated.

### 5.1 Heuristic based Algorithm

The heuristic based algorithm has several parameter that changes the behaviour of the agent (cf. table 1). Firstly we just changed the maximal states field that provides a limit for saved states at the AStar algorithm. As you can see the average winning rate increases by changing to a higher maximal states limit up to 20. But if the variable is set to 25 we had a worse result. This might be that if this value is to low the target is not found by the AStar algorithm. Moreover if it is to large to many states are saved and we get trouble with the memory or the garbage collector.

After that we tried to change the safety strategy to the grid and the intelligent search. Both results are worse than the SafetyAdvance Strategy. Since the SafeGridSearch highly depends on the Explorer and the classification of the object this might be the cause.

Detail the experimental setup used to test the different algorithms. Present the results in an understandable manner (graphics, tables, etc.). Draw conclusions about what things worked (and why) and which didn't (and why). ...

combinations really failed. explain it.

why we use this parameters??? something is missing...why not an exhaustive search for finding the best parameter..no time? to less computational power...

ID	Max. States	Safety Strategy	Safety Iterations	Avg Wins	Std of Wins
1	5	SafetyAdvance	5	0.517	0.0257099203
2	15	SafetyAdvance	5	0.529	0.0197230829
3	20	SafetyAdvance	5	<b>0.532</b>	0.0271293199
4	25	SafetyAdvance	5	0.521	0.0192093727
5	20	SafetyGridSearch	-	0.498	0.0235796522
6	20	SafetyIntelligent	5	0.527	0.0184661853

Table 1: results of the heuristic based algorithms

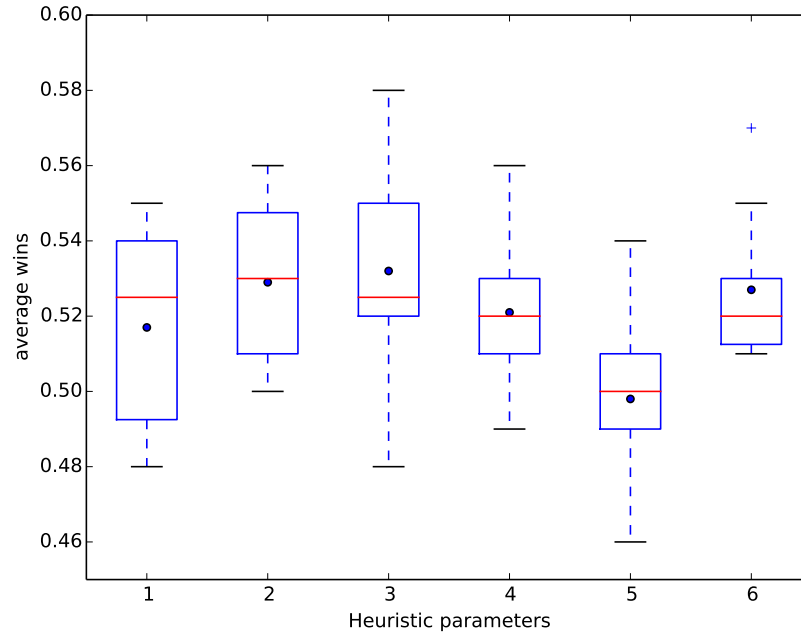


Fig. 9: boxplot of the heuristic based algorithms

With the SafetyIntelligent we got no further improvement but it is nearly good as the SafetyAdvance approach.

The boxplot (cf. fig. 9) visualizes the quartiles. The best parameter setup has also the largest quartile range. When you look at the table also the largest standard deviation (which doesn't have to be the same). If the target is not found the agent is staying alive. The risk of a longer search to reach a simulation state that collides with the target could be the reason for the higher variance of the results.

## 5.2 MCTS

We also tried to combine several approaches for example using the heuristic explorer for a better mcts iteration.

## 5.3 Evolutionary Algorithm

For the evolutionary algorithm we had a set up with different parameters.

Table 2

ID	Safety Iterations	Path Length	Size of Pop.	Fittest Pop.	Dyn. Path Length	Min. Gen.	Avg Wins	Std of Wins
1	2	6	14	5	no	-	0.459	0.023
2	4	6	10	4	no	-	0.458	0.024
3	5	4	14	5	no	-	0.466	0.028
4	5	6	10	5	no	-	0.459	0.032
5	5	6	13	4	yes	5	0.451	0.041
6	5	6	14	3	no	-	0.471	0.018
7	5	6	14	5	no	-	0.461	0.025
8	5	6	14	5	yes	2	0.479	0.021
9	5	6	14	5	yes	4	0.463	0.027
10	5	6	14	5	yes	6	0.449	0.041
11	5	6	14	7	no	-	0.474	0.028
12	5	6	18	5	no	-	0.462	0.035
13	5	8	14	5	no	-	0.453	0.029
14	8	6	14	5	no	-	0.477	0.022

## 5.4 Evaluation of all approaches

## 6 Conclusions and Future Work

This paper presents a comparison of several approach to play general video games. We selected for each research area (HR, RL, NI) one algorithm and implemented that. For

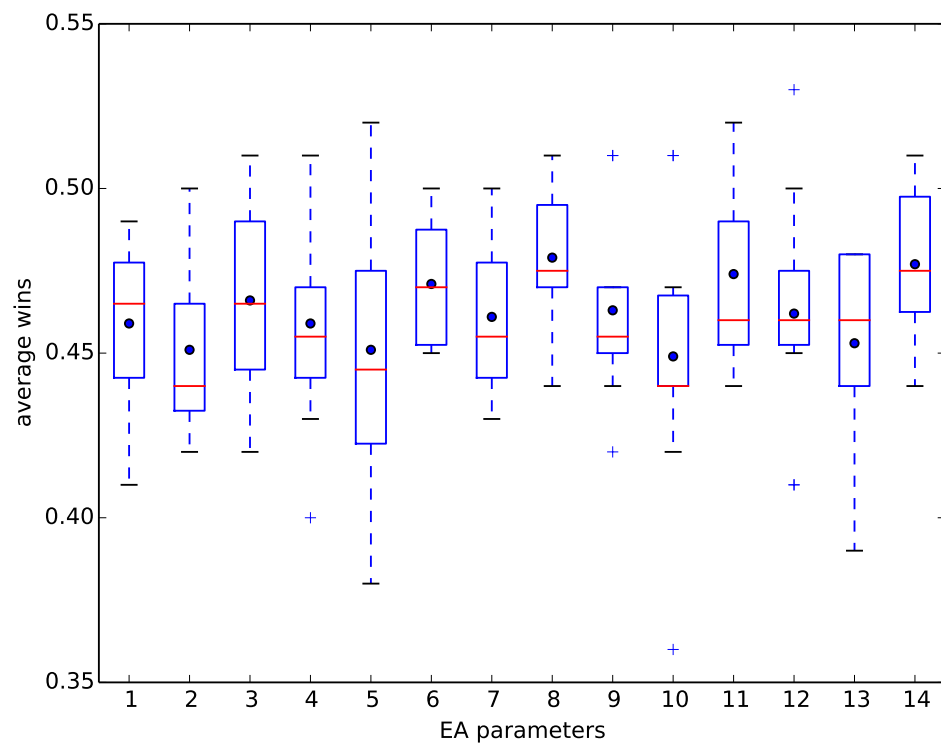


Fig. 10: result of the evolutionary algorithms



For the evaluation we forced to look at the data for example average wins, score and time steps. We ignored the in-game behaviour of our agents completely and only looked at the statistics. Furthermore we were limited by time and computational power which restricts the iterations of our experiment. To get more significant results experimental setup with more than 1000 iterations would stand for an higher validity.

Explain the main contributions of this work: what are the most important findings. Finally, explain how could this work be extended. What would be the next steps?

## Acronyms

<b>AI</b>	Artificial Intelligence
<b>EA</b>	Evolutionary Algorithm
<b>RL</b>	Reinforcement Learning
<b>MDP</b>	Markov Decision Process
<b>MCTS</b>	Monte Carlo Tree Search
<b>TLU</b>	Threshold Logic Unit
<b>NI</b>	Nature Inspired
<b>HR</b>	Heuristic

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