

**Computational Physics / PHYS-GA 2000 / Problem Set #3**  
**Due September 24, 2024**

You *must* label all axes of all plots, including giving the *units*!!

1. Read Example 4.3 in Newman. Using successively larger matrices ( $10 \times 10$ ,  $30 \times 30$ , etc.) find empirically and plot how the matrix multiplication computation rises with matrix size. Does it rise as  $N^3$  as predicted? Use both an explicit function (i.e. the one in the example) and use the `dot()` method. How do they differ?
2. Exercise 10.2 in Newman.
3. Exercise 10.4 in Newman.
4. Demonstrate that the central limit theorem works. Do so by generating random variate  $y = N^{-1} \sum_{i=0}^N x_i$ , where  $x_i$  is a random variate distributed as  $\exp(-x)$  (you can use the `np.random` library to generate the exponentially-distributed variates). First, calculate analytically how you expect the mean (that one should be easy) and variance of  $y$  to vary with  $N$ . Show visually that for large  $N$  the distribution of  $y$  tends towards Gaussian. Show as a function of  $N$  how the mean, variance, skewness, and kurtosis of the distribution change. Estimate at which  $N$  the skewness and kurtosis have reached about 1% of their value for  $N = 1$ .