

Errata from *Linear Algebra*

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Introduction

This document contains errata from [1]. Locations in the text are indicated by coordinates (p, n) , where p is a page number and n is a line number on page p . Positive line numbers count from the top of the page, whereas negative line numbers count from the bottom of the page. Displayed equations, diagrams, and figures are counted as single lines.

Minor, purely typographical inconsistencies like those between “ $1 \dots n$ ” and “ $1, \dots, n$ ”, or between “family x_α ” and “family (x_α) ” and “family $\{x_\alpha\}$ ”, are not listed but occur frequently.

Errata are currently only listed for Chapters 0–VI (except § 3 of Chapter VI).

Chapter 0

- (2, 8): in the definition of subgroup, “subset H ” should be “nonempty subset H ”.
- (3, -12): a homomorphism between fields must also preserve the multiplicative identity.
- (3, -13): a subfield must also contain the multiplicative identity.

Chapter I

- (9, 16): in the definition of linear dependence, “non-trivial linear combination of the x_α ” should be “non-trivial linear combination of the x_α equal to zero”.
- (12, 1): $\lambda^i = 0$ should be $\lambda^i \neq 0$.

- (12, 5): throughout the proof of (ii), n should be m .
- (12, -5): “The a partial order” should be “A partial order”.
- (12, -4): “maximal element” should be “upper bound”.
- (13, 8): $x \in E$ should be $x \in S - T$.
- (13, 9), (13, 10): $T \cup x$ should be $T \cup \{x\}$ and $x \cup T$ should be $\{x\} \cup T$.
- (14, 1): “element f_a ” should be “elements f_a ”.
- (14, 3), (14, 5): in the displayed equations, $j = 1$ should be $i = 1$.
- (15, -2): in problem 10, $\{x_\alpha\}_{\alpha \neq \beta}$ should be $\{a\} \cup \{x_\alpha\}_{\alpha \neq \beta}$.
- (20, 16): “ $\varphi(S)$ is a system of generators for $\varphi(S)$ ” should be “ $\varphi(S)$ is a system of generators for F ”.
- (22, -15): in part (v) of Problem 5, the concept of a generated subspace has not yet been defined.
- (23, 7): in the definition of subspace, “subset of E ” should be “nonempty subset of E ”.
- (27, -11): in the displayed equation, λ_i should be λ^i (two occurrences). Also, it should be noted that $y_i \in E_1$ and $z_i \in E_2$.
- (29, -16): “*canonical projection* of E onto E_1 ” should be “*canonical projection* of E onto E/E_1 ”.
- (40, -8): in the second displayed equation in problem 6, $u \in E'_2$ should be $y \in E'_2$.

Chapter II

- (47, -6): “assume that there” should be “assume that”.
- (52, -8): $\psi : E_1 \leftarrow F$ should be $\psi : E \leftarrow F$.
- (52, -3): “left inverse” should be “left inverse ψ ”.

- (53, 13): “inverse” should be “left inverse”.
- (53, -1): in problem 1, the inclusion $L(E; F) \subset C(E; F)$ is wrong.
- (59, -5): in (2.25), it should be noted that $\delta_{\rho\sigma}$ is a Kronecker delta.¹
- (62, 10): in (2.34), y should be y_j .
- (63, -7): in problem 7, “second set” should be “disjoint set”.
- (67, -1): in the displayed equation, $y^* \in F$ should be $y^* \in F^*$.
- (68, -7): in the displayed equation, $\langle y^*(\varphi + \psi)x \rangle$ should be $\langle y^*, (\varphi + \psi)x \rangle$.
- (76, 9): “imension” should be “dimension”.
- (76, -7): in the displayed equation (and really the rest of subsection 2.31), φ_v^μ should be φ_μ^v .
- (77, -7): φ should be Φ .

Chapter III

- (83, -10): in the displayed equation, $(b_1^\mu \dots b_n^\mu)$ should be $(\alpha_1^\mu \dots \alpha_n^\mu)$.
- (84, -7): “columns of the matrix α_v^μ ” should be “columns of the matrix $\alpha_v^{*\mu}$ ”.
- (84, -6): $y = y^{*\mu}$ should be $y^* = y^{*\mu}$.
- (85, 13): in the displayed equation, it should be noted that $A = (\alpha_v^\mu)$.
- (88, 1): in the main theorem, “system of n equations in m unknowns” should be “system of m equations in n unknowns”.
- (89, 12): it should be noted that $\dim E = n$ and $\dim F = m$.
- (89, -8): in the displayed equation, α_v^μ should be α_v^μ .
- (91, 5): “ E automorphism of E ” should be “automorphism of E ”.
- (91, 9): in the displayed equation, $M(\varphi)^{-1}$ should be $M(\varphi^{-1})$.

¹This notation is defined later in a footnote on p. 76.

- (91, -3): in problem 3, “linear transformation” should be “a linear transformation”.
- (93, -13): “inverse of the matrix of the transformation $x_v \rightarrow \bar{x}_v$ ” should be “transpose of the inverse of the matrix of the transformation $x_v \rightarrow \bar{x}_v$ ”.
- (95, 12): $\mu = 1, \dots, n$ should be $\mu = 1, \dots, m$.
- (96, 1): multiplication of basis vectors by nonzero scalars should be added to the list of elementary basis transformations.
- (96, -7): $2 \leq v \leq m$ should be $2 \leq v \leq n$.
- (98, 3): (3.36) should be

$$\xi^r = (\kappa_r^r)^{-1} \left(\omega^r - \sum_{v=r+1}^n \kappa_v^r \xi^v \right)$$

Chapter IV

- (105, -8): “Proposition II” should be “Proposition III”.
- (106, 5): “(4.14)” should be “(4.12)”.
- (107, 13): in (4.14), $p = \dim E$ should be $p = \dim E_1$.
- (109, 1): the problem numbers on this page should be incremented by 1.
- (109, 10): in problem 6, it must be assumed that E is real.
- (109, -11): in problem 8, the trace of a linear transformation has not yet been defined.
- (113, 1): “(4.21)” should be “(4.22)”.
- (113, -10): in the displayed equation, x^*_i should be x^{*i} .
- (115, 1): “(4.14)” should be “(4.12)”.
- (115, 4): in the displayed equation, $\widehat{\varphi a_j}$ should be $\widehat{\varphi a_i}$.
- (115, 9): it should be noted that $M(\varphi) = (\alpha_v^\mu)$.

- (115, -10): the displayed equation should be $\beta_j^i = \det C_i^j$.
- (116, 11): “(4.36)” should be “(4.38)”.
- (116, -1): in the displayed matrix B_i^j , the first column should have entries $1, \alpha_1^j, \dots, \alpha_{i-1}^j, \alpha_{i+1}^j, \dots, \alpha_n^j$.
- (117, 3): “(4.38)” should be “(4.16)”, or a reference to Problem 6.
- (117, 7): “(4.35) and (4.30)” should be “(4.38) and (4.40)”.
- (117, -14): “minor” should be “submatrix”.
- (122, 2): on the third line of the displayed equation, σ should be ρ .
- (130, -14): in problem 11, it must be assumed that E is real.
- (135, -3): “4.30” should be “4.29”.
- (136, -6): “4.17” should be “4.16”, and it should be noted that ξ_v^i are the components of x_v with respect to some basis.
- (139, -13): $(a'_1, b_2 \dots b_n)$ should be $(a'_1, b_3 \dots b_n)$.
- (139, -10): in the displayed equation, $i = 1 \dots n$ should be $i = 1 \dots n - 1$.

Chapter V

- (146, 1): $(\varphi, \psi) \rightarrow \psi\varphi$ should be $(\psi, \varphi) \rightarrow \psi\varphi$.
- (148, 10): the displayed list should also include elements of the form asb for $s \in S$ and $a, b \in A$.
- (148, -17): it must be assumed that $A \neq 0$ (equivalently $e \neq 0$) for it to follow that $\lambda = 0$.
- (151, 2): the extra “can be” should be deleted.
- (158, 14): “cheeked” should be “checked”.
- (160, -13): “let be” should be “be”.

- (160, -8): it must be assumed that $E \neq 0$ for $A(E; E)^2 \neq 0$.
- (161, -1): “non-zero, I , ideal” should be “non-zero ideal I ,”.
- (165, 12), (166, 7): it should be clarified that Γ is assumed to be a field under the restrictions of the operations in $A_\Delta(E; E)$.

Chapter VI

- (168, -16): it should be noted that the zero map is homogeneous of every degree (hence *the* degree is not well-defined in that case).
- (172, -4): “product” should be “products”.
- (173, -3): in problem 6, $\deg \varphi^* = -k$.
- (175, 4): the displayed statement should be $xe_k \in A_{l+k}$.
- (176, 1): E should be A .
- (177, 2): in the second part of problem 1, it must be assumed that $A \neq 0$ to conclude that $k = 0$.
- (177, 14): in problem 5, “ ≤ 0 (≥ 0)” should be “ ≥ 0 (≤ 0)”.

References

- [1] Greub, W. *Linear Algebra*, 4th ed. Springer, 1975.