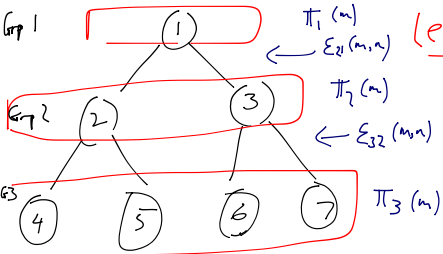


level by level grouping: no issue



$$\pi_i(n) = P(Y_i = n | \underline{\theta}^{(i)})$$

$$E_{i,p(i)}(n, n) = P(Y_i = n | Y_{p(i)} = n, \underline{\theta}^{(i)})$$

for group i , and 'parent group', $p(i)$.

For $E_{i,p(i)}$ Yhoo's and Lagrangians derive to:

$$E_{i,p(i)}(n, n) = \frac{\sum_{j \in i} P(Y_j = n, Y_{p(i)} = n | \underline{\theta}^{(i)})}{\sum_{j \in i} P(Y_{p(i)} = n | \underline{\theta}^{(i)})}$$

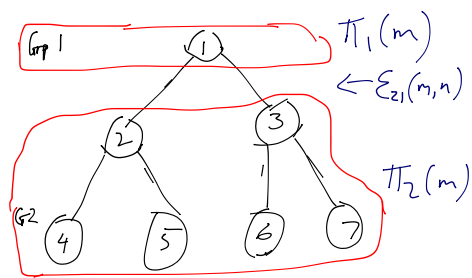
$$= \frac{1}{|i|} \times \frac{1}{\pi_{p(i)}(n)} \times \sum_{j \in i} P(Y_j = n, Y_{p(i)} = n | \underline{\theta}^{(i)})$$

(as per course)

Take group 3, for example.

$$\begin{aligned} i &= 4, \dots, 7 \\ p(i) &= 2, 2, 3, 3 \\ &\rightarrow \sum_{i=4}^7 P(Y_{p(i)} = n | \underline{\theta}^{(i)}) \\ &= 2(P(Y_2 = n | \underline{\theta}^{(4)}) + P(Y_3 = n | \underline{\theta}^{(4)})) \\ &= 4 \times \left(\frac{1}{2} [P(Y_2 = n | \underline{\theta}^{(4)}) + P(Y_3 = n | \underline{\theta}^{(4)})] \right) \\ &= 4 \times \pi_2(n) \quad (\text{as defined in course, plus I think I've verified it on my own}) \end{aligned}$$

No issue as all nodes in group 3's parents are tied together to same param, π_2 .



Multi-level groups: ISSUE

For $E_{i,p(i)}$ Yhoo's and Lagrangians derive to:

$$E_{i,p(i)}(n, n) = \frac{\sum_{j \in i} P(Y_j = n, Y_{p(i)} = n | \underline{\theta}^{(i)})}{\sum_{j \in i} P(Y_{p(i)} = n | \underline{\theta}^{(i)})}$$

$$\neq \frac{1}{|i|} \times \frac{1}{\pi_{p(i)}(n)} \times \sum_{j \in i} P(Y_j = n, Y_{p(i)} = n | \underline{\theta}^{(i)})$$

(as per course)

Take group 2, for example.

$$\begin{aligned} i &= 2, \dots, 7 \\ p(i) &= 1, 1, 2, 2, 3, 3 \\ &\rightarrow \sum_{i=2}^7 P(Y_{p(i)} = n | \underline{\theta}^{(i)}) \\ &= 2[P(Y_1 = n | \underline{\theta}^{(2)}) + P(Y_2 = n | \underline{\theta}^{(2)}) + P(Y_3 = n | \underline{\theta}^{(2)})] \\ &\neq |i| \times \pi_1(n), \text{ as required in course.} \\ &= 6 \quad \text{also, } \pi_1(n) \neq \pi_{p(i)}(n), \text{ for all } i. \end{aligned}$$

Issue, as $p(i) \neq 1, \forall i=2, \dots, 7$, as i 's are across two levels of the tree.

Only way this interpretation works is if you treat G_2 as the same level with no internal transitions.

