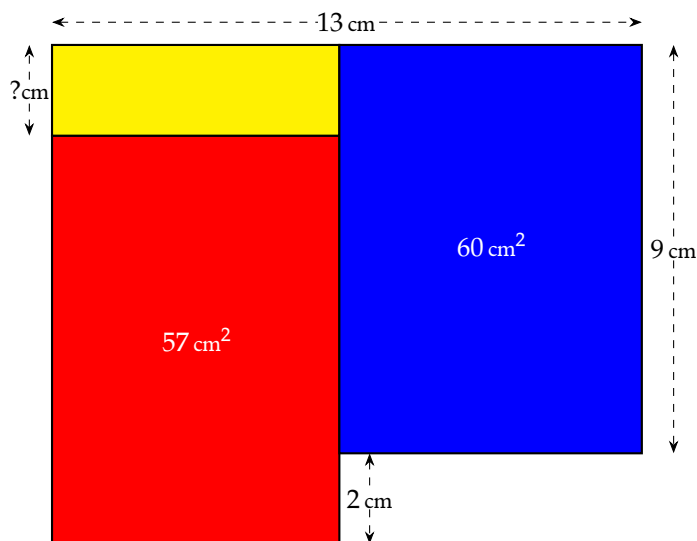




Here are the full, or partial solutions.

### Year 8 and below



### Solution

We know the height of the blue rectangle and its area, so we can work out its width.

Width of blue rectangle:  $\frac{60}{9} = \frac{20}{3}$

So the width of the red and yellow rectangles must be  $13 - \frac{20}{3} = \frac{19}{3}$

As the area of the red rectangle is 57 cm², its height must be:

$$57 \div \frac{19}{3} = 57 \times \frac{3}{19} = 9$$

Since the total height of the yellow and red rectangles is 11 cm, the yellow rectangle must be 2 cm high.

## Year 9 and above

Find the value of the shaded angle in the circle in the triangle in the semi-circle. You need to know some basic circle theorems for this.

### Solution

We add some labels to help:  $I$  is the centre of the circle.

Since we are told the shape is a semi-circle,  $PQ$  is a diameter.

So the angle subtended by lines from  $P$  and  $Q$  to the circumference must be  $90^\circ$ .

This is a special case of the theorem that says that the angle subtended at the centre of a circle ( $2\phi$ ) by two points ( $A$  and  $B$ ) on the circumference is double the angle the same two points subtend at the circumference ( $\phi$ ). See the diagram below. In this case  $2\phi = 180^\circ$  at the centre  $O$ , so at the circumference (at  $R$ ), the angle is half this.

That is,  $\angle PRQ = 90^\circ$

The circle inside  $\triangle PQR$  is called the 'incircle' of the triangle. The sides of the triangle  $PQR$  are tangent to the circle at  $L$ ,  $M$  and  $N$ .

A radius of the circle meets a tangent line at right-angles, at the point of tangency.

That is,  $\angle IMR = \angle INR = 90^\circ$ .

Therefore  $\angle MIN = 90^\circ$ .

We use the same theorem again: Points  $M$  and  $N$  on the circumference of the circle subtend an angle of  $90^\circ$  at the centre  $I$  of the circle.

So the angle that points  $M$  and  $N$  subtend on the circumference of the circle at point  $L$  must be half that.

The value of the yellow-shaded angle is  $45^\circ$ .

