

<b>1 Algebra</b> Absolute Value Inequalities: $ f(x)  < a \Rightarrow -a < f(x) < a$ $ f(x)  > a \Rightarrow f(x) > a$ or $f(x) < -a$	
<b>2 Important probability distributions</b> <b>Bernoulli</b> Parameter $p \in [0, 1]$ . Discrete, describes the success or failure in a single trial. $p_X(k) = \begin{cases} p, & \text{if } k = 1 \\ (1 - p), & \text{if } k = 0 \end{cases}$ $E[X] = p$ $Var(X) = p(1 - p)$ <b>Exponential</b> Parameter $\lambda$ . Continuous $f_X(x) = \begin{cases} \lambda \exp(-\lambda x), & \text{if } x \geq 0 \\ 0, & \text{o.w.} \end{cases}$ $F_X(x) = \begin{cases} 1 - \exp(-\lambda x), & \text{if } x \geq 0 \\ 0, & \text{o.w.} \end{cases}$ $E[X] = \frac{1}{\lambda}$ $Var(X) = \frac{1}{\lambda^2}$ <b>Normal (Gaussian)</b> Parameters $\mu$ and $\sigma^2 > 0$ . Continuous $f(x) = \frac{1}{\sqrt{2\pi\sigma}} \exp\left(-\frac{(x-\mu)^2}{2\sigma^2}\right)$ $E[X] = \mu$ $Var(X) = \sigma^2$ Useful properties:  <b>Poisson</b> <b>Uniform</b>	
<b>3 Expectation and Variance</b> <b>Expectation</b> <b>Variance</b> <b>Covariance</b> <b>Variance and expectation of mean of n iid random variables</b> Let $X_1, \dots, X_n \stackrel{iid}{\sim} P_\mu$ , where $E(X_i) = \mu$ and $Var(X_i) = \sigma^2$ for all $i = 1, 2, \dots, n$ and $\overline{X_n} = \frac{1}{n} \sum_{i=1}^n X_i$ .  Variance of the Mean:  $Var(\overline{X_n}) = \left(\frac{\sigma^2}{n}\right)^2 Var(X_1 + X_2, \dots, X_n) = \frac{\sigma^2}{n}.$  Expectation of the mean:  $E[\overline{X_n}] = \frac{1}{n} E[X_1 + X_2, \dots, X_n] = \mu.$	
<b>4 LLN and CLT</b> Let $X_1, \dots, X_n \stackrel{iid}{\sim} P_\mu$ , where $E(X_i) = \mu$ and $Var(X_i) = \sigma^2$ for all $i = 1, 2, \dots, n$	

Weak and strong law of large numbers:

$$\overline{X_n} = \frac{1}{n} \sum_{i=1}^n X_i \xrightarrow[n \rightarrow \infty]{P, a.s.} \mu.$$

Central Limit Theorem:

$$\sqrt{(n)} \frac{\overline{X_n} - \mu}{\sqrt{(\sigma^2)}} \xrightarrow[n \rightarrow \infty]{(d)} N(0, 1)$$

$$\sqrt{(n)} (\overline{X_n} - \mu) \xrightarrow[n \rightarrow \infty]{(d)} N(0, \sigma^2)$$

## 5 Statistical models

## 6 Estimators

## 7 Confidence intervals

## Onesided

## Twosided

## Delta Method

## 8 Hypothesis tests

## Onesided

## Twosided

## P-Value