

1 Algebra Absolute Value Inequalities: $ f(x) < a \Rightarrow -a < f(x) < a$ $ f(x) > a \Rightarrow f(x) > a$ or $f(x) < -a$
2 Important probability distributions Bernoulli Parameter $p \in [0, 1]$. Discrete, describes the success or failure in a single trial. $p_x(k) = \begin{cases} p, & \text{if } k = 1 \\ (1 - p), & \text{if } k = 0 \end{cases}$ $E[X] = p$ $Var(X) = p(1 - p)$ Exponential Parameter λ . Continuous $f_x(x) = \begin{cases} \lambda \exp(-\lambda x), & \text{if } x \geq 0 \\ 0, & \text{o.w.} \end{cases}$ $F_x(x) = \begin{cases} 1 - \exp(-\lambda x), & \text{if } x \geq 0 \\ 0, & \text{o.w.} \end{cases}$ $E[X] = \frac{1}{\lambda}$ $Var(X) = \frac{1}{\lambda^2}$ Normal (Gaussian) Parameters μ and $\sigma^2 > 0$. Continuous $f(x) = \frac{1}{\sqrt{2\pi\sigma}} \exp\left(-\frac{(x-\mu)^2}{2\sigma^2}\right)$ $E[X] = \mu$ $Var(X) = \sigma^2$ Useful properties:
Poisson Uniform
3 Expectation and Variance Expectation Variance Covariance Variance and expectation of mean of n iid random variables Let $X_1, \dots, X_n \stackrel{iid}{\sim} P_\mu$, where $E(X_i) = \mu$ and $Var(X_i) = \sigma^2$ for all $i = 1, 2, \dots, n$ and $\overline{X_n} = \frac{1}{n} \sum_{i=1}^n X_i$. Variance of the Mean: $Var(\overline{X_n}) = \left(\frac{\sigma^2}{n}\right)^2 Var(X_1 + X_2, \dots, X_n) = \frac{\sigma^2}{n}.$ Expectation of the mean: $E[\overline{X_n}] = \frac{1}{n} E[X_1 + X_2, \dots, X_n] = \mu.$
4 Law of large Numbers 5 Central Limit theorem 6 Statistical models 7 Estimators

8 Confidence intervals
Onesided
Twosided
Delta Method
9 Hypothesis tests
Onesided
Twosided
P-Value