

# **IBM Training**

## **Student Exercises**

### (Machine Learning and Optimization)

**Lab-4: Forecast COVID-19  
outbreaks – find optimal ways to  
transfer sick patients**

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## Introduction

This lab will introduce users to the use of IBM's predictive analytics and decision optimization technologies to solve COVID-19 problems. The coronavirus has infected millions people leading to sever illness symptoms resulting in hundreds of thousands deaths. During the initial outbreak not all areas where effected the same. Hospitals located in COVID-19 epidemic outbreak locations were overwhelmed with sick and dying patients. This lab will apply predictive analytics to analyze different factors among people to predict future COVID-19 infection rates in an area. Based on areas predicted to have high COVID-19 infections – this lab will apply optimization techniques to optimize the planning of transferring COVID-19 patients from hospitals located in epidemic areas to hospitals with less COVID-19 patients. Our hope is to educate people who are involved in the COVID-19 response decision-making process, in applying IBM's predictive and optimization technologies to help them improve planning and responding to next wave of COVID-19 cases.

## Objectives

The goal of this lab is to educate user on how to apply IBM predictive analytics and optimization tools to different applications of COVID-19 like (1) predicting future infections and (2) optimizing response for better decision making. Students will use Watson Studio to load and step through a notebook that applies Decision Optimization to optimize the transport of affected people between hospitals to avoid being overcapacity. Working through this notebook – we intend students learn these skills.

1. Learn how to load data form different places (departments, current situation, etc) to be used for analysis.
2. Learn how to represent the current situation on a map using folium. folium makes it easy to visualize data that's been manipulated in Python on an interactive leaflet map.
3. Learn how to use a LinearRegression from sklearn to predict new cases to come for each department.
4. Learn how to use Decision Optimization to model and optimize plan transfers.
5. Learn how to use folium to display the optimized future patient transfers plan i.e. all the transfers from the solution.

## COVID-19 Use Case - Planning the Patient Transfers

These days, one of the critical problem for our governments is to manage the heterogeneous propagation of the virus over the territories. Not all areas are infected at the same level. While confinement of the population and prohibition of travel is reducing the propagation of the virus, the transfer of sick people between different areas can reduce the stress of hospitals in the most critical regions. In France, transfers are now generalized, using military planes (see here or here), helicopters or high-speed trains, but also locally with ambulances.

The problem of finding optimal ways to relocate sick people among areas can benefit from a combination of Machine Learning (ML) and Decision Optimization (DO).

Based on the recent evolution of the number of critical reanimation cases in each area, predictive models can be trained to forecast the evolution per area on the coming days. This data, in addition to the capacity of the hospitals for each of the areas and some description of the constraints applying on the possible transfers can then be used in a decision optimization model. This schema where Machine Learning is used first to extract additional unknown information and Decision Optimization is used to prescribe the best next actions is a very common use case.

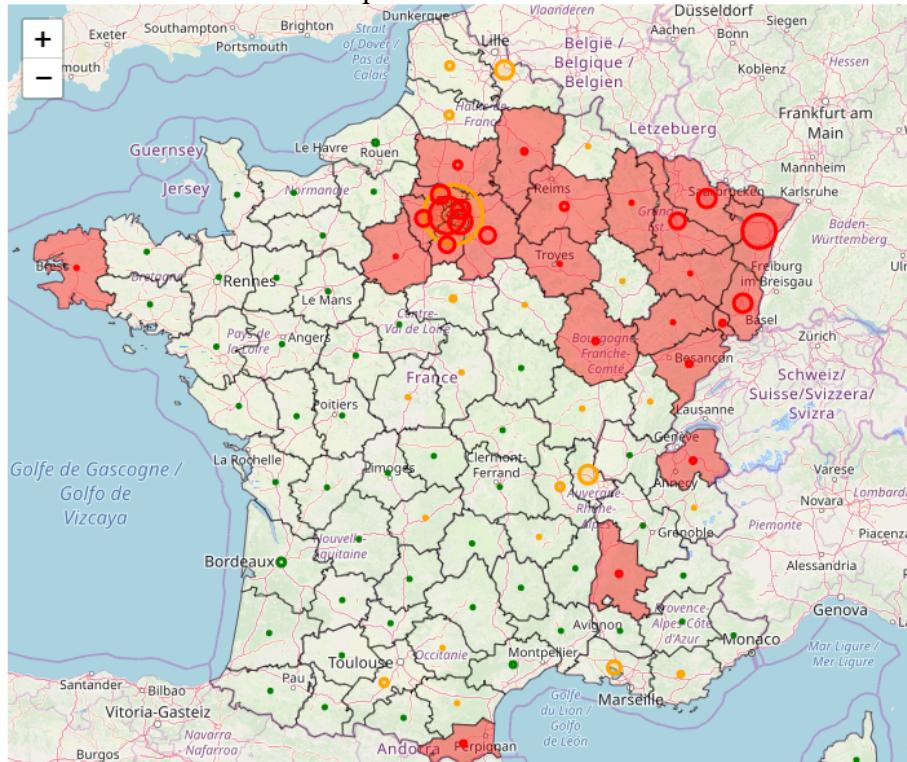
You can find [here an example notebook](#).

## Import and display input data

We use data from the French government [data.gouv.fr](https://www.data.gouv.fr/fr/datasets/donnees-relatives-a-lepidemie-de-covid-19/#) site:

<https://www.data.gouv.fr/fr/datasets/donnees-relatives-a-lepidemie-de-covid-19/#> in addition to some imported data on the different French administrative “departments” (GPS coordinates of frontier and center).

Using Folium, we can easily represent this data on a map. The circles show the number of reanimation cases in each department. Red circles show above normal capacity.



## Current situation

## Simplistic predictive model

A very simplistic predictive model is trained for illustration. We use `LinearRegression` from `sklearn`, knowing obviously that the epidemic is not linear at all. But this gives an idea of how ML would work here.

```

import numpy as np
from sklearn.linear_model import LinearRegression
NB_PERIODS = 3
def predict_more(d, n):
    X = hosp_data[d].index.tolist()
    X.reverse()
    X=np.array(X).reshape(-1,1)
    y = hosp_data[d]['rea'].tolist()
    y.reverse()
    y=np.array(y).reshape(-1,1)
    regsr=LinearRegression()
    regsr.fit(X,y)
    to_predict_x = [i for i in range(len(X), len(X)+n)]
    to_predict_x= np.array(to_predict_x).reshape(-1,1)
    predicted_y= regsr.predict(to_predict_x)
    delta_y = [ int(round(max(0, predicted_y[i][0]-y[len(y)-1][0]))) for i in range(n)]
    return delta_y
    new_rea = {d:predict_more(d, NB_PERIODS) for d in deps}
print(new_rea)

```

The outcome is a prediction of the expected number of new reanimation cases to occur in the next few days we will plan (here `NB_PERIODS = 3`).

## Sample Decision Optimization model

Our hypothesis for the optimization model is that two different types of transfers can be done:

- long distance transfers (planes, trains) with the number of transfers limited over the whole country, several people can be transferred at a time.
- short distance transfers (ambulances) with the number of transfers limited per area, and with just one person at a time.

The parameters we use (completely invented) are:

```

MAX_NB_LONG_TRANSFERS_PER_PERIOD = 3
MAX_CASES_PER_LONG_TRANSFERS = 20
MAX_NB_SHORT_TRANSFERS_PER_DEPARTMENT = 3
LONG_DISTANCE = 200

```

We use our `docplex` API to model the problem:

```

from docplex.mp.model import Model
mdl = Model("Plan Transfers")

```

The decision variables represent the transfer links to be used in the best (optimal) transfer plan (an integer variable for the number of persons transferred and a binary variable indicating whether the link is used or not, with a constraint linking both). Another set of auxiliary variables represents the occupancy for each department and each period.

```

use_link_vars = mdl.binary_var_cube(deps, deps, transfer_periods, name="use_link")
link_vars = mdl.integer_var_cube(deps, deps, transfer_periods, lb=0,
                                ub=MAX_CASES_PER_LONG_TRANSFERS, name="link")
occupancy_vars = mdl.integer_var_matrix(deps, all_periods, lb=0, name="occupancy")

```

Then we formulate all the constraints:

```

# Initial state
mdl.add_constraints(occupancy_vars[d, 0] == initial[d] for d in deps)
# structural constraint between user_link and link
mdl.add_constraints(use_link_vars[d, d1, t] == (link_vars[d, d1, t] >= 1) for d in deps for d1 in deps
for t in transfer_periods)

```

```

# Short transfers bounds
mdl.add_constraints(link_vars[d1, d2, t] <= 1 for d1 in deps for d2 in deps if not is_long[d1][d2] for t in transfer_periods)
# number of transfers from a department less than current number of cases
mdl.add_constraints(mdl.sum(link_vars[d, d1, t] for d1 in deps) <= occupancy_vars[d, t] for d in deps for t in transfer_periods)
# maximum number of LONG transfers
mdl.add_constraints(mdl.sum(use_link_vars[d1, d2, t] for d1 in deps for d2 in deps if is_long[d1][d2]) <= MAX_NB_LONG_TRANSFERS_PER_PERIOD for t in transfer_periods)
# maximum number of SHORT transfers
mdl.add_constraints(mdl.sum(use_link_vars[d1, d2, t] for d1 in deps if not is_long[d1][d2] for t in transfer_periods) <= MAX_NB_SHORT_TRANSFERS_PER_DEPARTMENT for d2 in deps )
# conservation constraints including new cases to come
mdl.add_constraints(occupancy_vars[d, t+1] == new_rea[d][t] + occupancy_vars[d, t] +
mdl.sum(link_vars[d1, d, t] for d1 in deps) - mdl.sum(link_vars[d, d1, t] for d1 in deps) for d in deps for t in transfer_periods)

And the objectives. The main objective is to reduce the total overcapacity on the areas, but we should also limit unnecessary transfers.

final_overcapacity = mdl.sum(mdl.max(0, occupancy_vars[d, NB_PERIODS] - capacity[d]) for d in deps)
mdl.add_kpi(final_overcapacity)

nb_long_transfers = mdl.sum(use_link_vars[d1, d2, t] for d1 in deps for d2 in deps if is_long[d1][d2] for t in transfer_periods)
mdl.add_kpi(nb_long_transfers)

nb_short_transfers = mdl.sum(use_link_vars[d1, d2, t] for d1 in deps for d2 in deps if not is_long[d1][d2] for t in transfer_periods)
mdl.add_kpi(nb_short_transfers)

mdl.minimize(1000 * final_overcapacity + 10 * nb_long_transfers + nb_short_transfers)

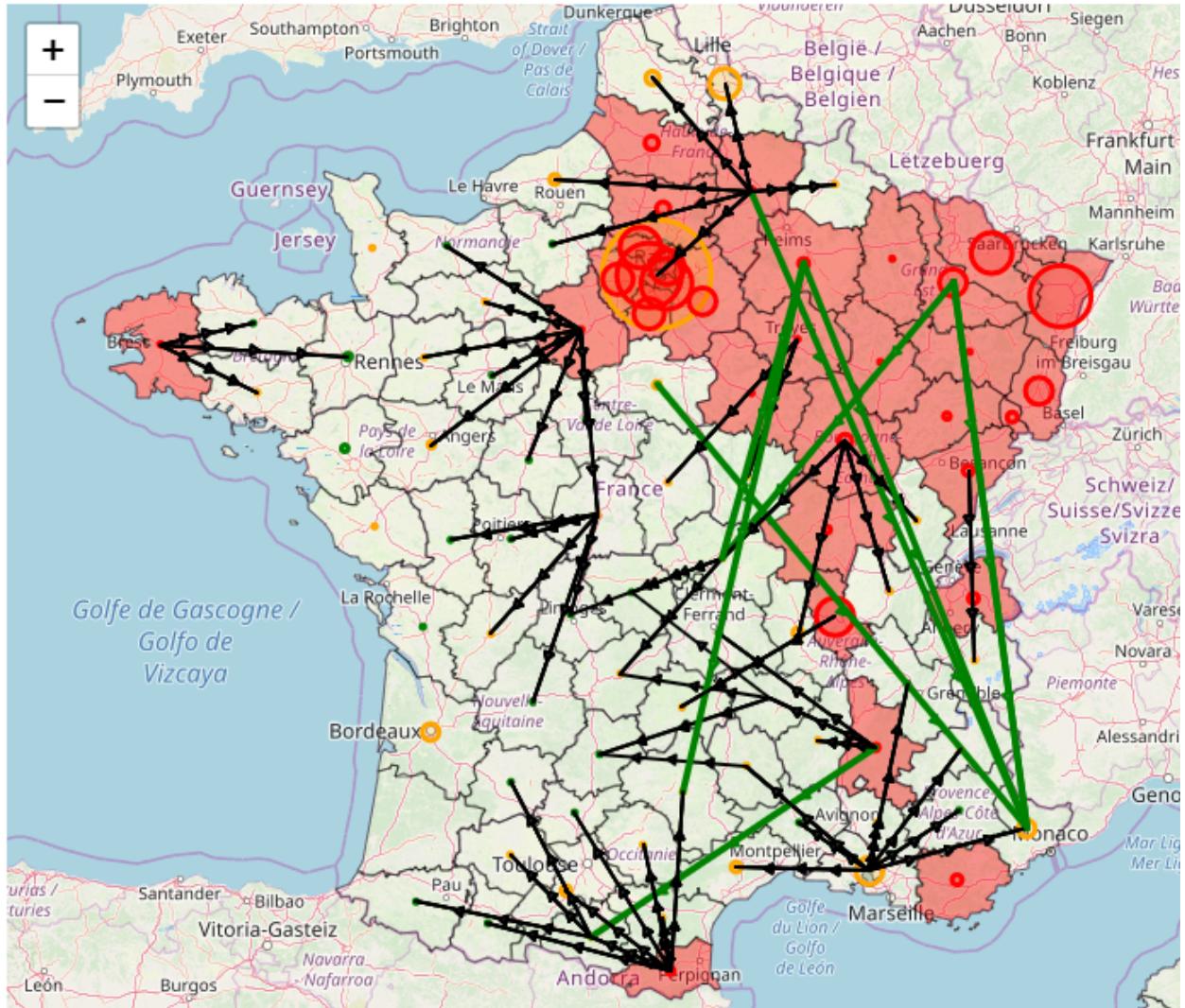
We can then solve the problem (using the CPLEX engine) and get the prescribed decisions.

mdl.set_time_limit(20)
mdl.solve(log_output=True)

```

## Display the solution

Using the same Folium package, we can represent the proposed transfers on a map.  
The long-distance transfers are represented in green and the short distance ones in black.



## Proposed solution.

## Conclusions

I want to insist again on the fact this is not a ready-to-use solution, but a demonstration of how ML and DO technology could be used to propose mathematically optimal transfer decisions. You can find [here the complete notebook](#).

In practice, additional data, constraints and objectives should be taken into account. For example, we can easily imagine that the level of criticality of individual infected persons would be taken into account. Also the characteristics of hospitals in the different areas, including the neighborhood of the airport or train station, should be taken into account.

Note also my model only considered transfers within France, while some transfers already took place from France to Germany and Luxembourg.

**This notebook is hence only provided as an example which can be used to discover or learn optimization.** You can freely try this notebook on [Watson Studio Cloud](#).

If you are in a position to use such technology in practice for the Covid-19 situation, don't hesitate to contact us, we are willing to help.

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# Instructions

## Plan transfers between areas

This notebook shows how we can use Decision Optimization to optimize the move of affected people between hospitals to avoid being overcapacity.

The problem is solved per department.

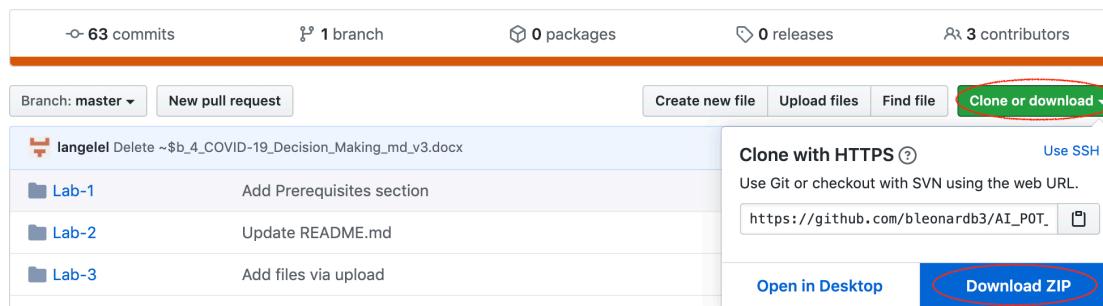
There are 5 parts in this notebooks:

1. Load the data form different places (departements, current situation, etc)
2. represent the current situation on a map
3. predict new cases to come for each department
4. plan transfers
5. display all the transfers from the solution

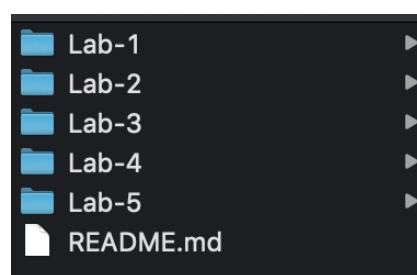
**DISCLAIMER:** this notebook is thought to demonstrate through an example how Machine Learning and Decision Optimization could be used, but it is partially based on fake data and knowledge of the real problem, and some significant work would be required to incorporate real data and real constraints and objectives so that the outcome could be useful.

## Download files from github

1. If you have not clone the "Applying AI and Analytics to COVID-19 Project" from the github site – please enter this URL [https://github.com/leonardb3/AI\\_POT\\_06-11-2020/tree/master/Lab-4](https://github.com/leonardb3/AI_POT_06-11-2020/tree/master/Lab-4) into a web browser to access the github site.
2. Click on the "Clone or download" button. Click the "Download Zip" button. Save and unzip the "AI\_POT\_06-11-2020-master.zip" file to your local file system.

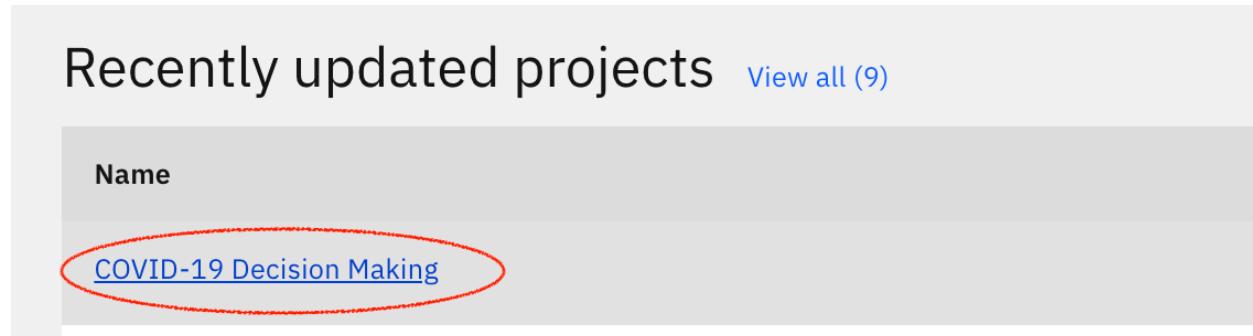


3. You should see these files in your file system.



## Access Watson Studio COVID-19 Project

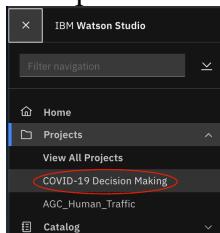
1. Enter this URL <https://dataplatform.cloud.ibm.com/> into your web browser. Login to Watson Studio. Click on your COVID-19 project.
2. In your "Recently updated projects" click on your "COVID-19 Project" to open it.



Recently updated projects [View all \(9\)](#)

Name
<a href="#">COVID-19 Decision Making</a>

3. If you don't see your project once you login – click the hamburger icon  in the top left of your screen. Click your project in the dropdown menu.

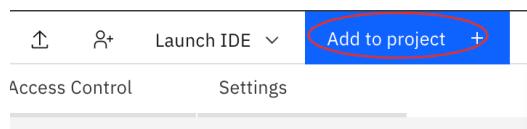


4. You should see a project view of your COVID-19 project.

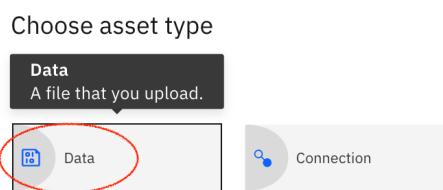
## Upload dataset

This exercise you will add a .csv file to your project. You will use this data file to read in the hospitals and their locations into a Pandas series.

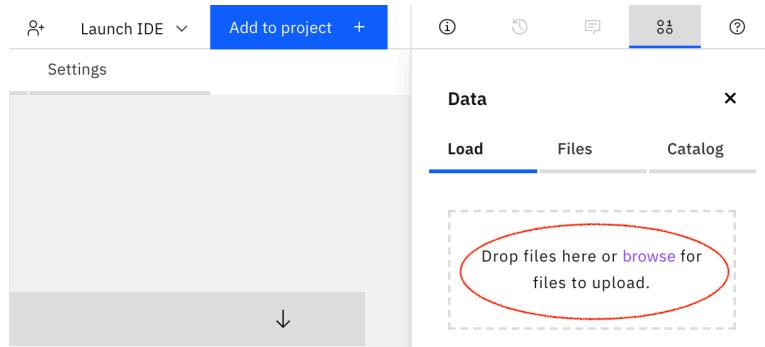
1. Click "Add to project"



2. Click "Data"



3. In the "Data" pane on the righthand side. Navigate to the "Lab-4" folder > grab and drop the "departements.csv" file into the "Load" drop files box.



4. You should see the "departements.csv" file displayed in your project > Data assets section.

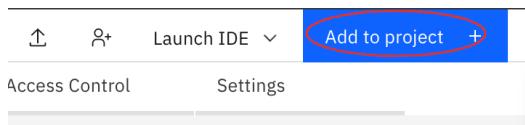
The screenshot shows the 'Data assets' section. It displays a table with one row. The first column has a checkbox and the text 'CSV'. The second column contains the file name 'departements.csv', which is also circled in red. The third column is labeled 'Type' and shows 'Data Asset'. Above the table, it says '0 assets selected.'

<input type="checkbox"/>	Name	Type
<input type="checkbox"/>	CSV departements.csv	Data Asset

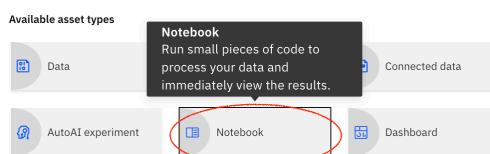
## Create a Notebook

This exercise you will add a notebook to your project

1. Click "Add to project"



2. Click "Notebook"



3. Click the "From URL" tab > Enter a notebook name "COVID-19 Decision Making" > enter a description "This project forecasts COVID-19 outbreaks and creates an optimized transfer sick patient plan." > make sure you select "Default Python 3.6 XS + DO (2 vCPU 8 GB RAM)" in the "Select runtime" selection list > copy this URL [https://github.com/bleonardb3/AI\\_POT\\_06-11-2020/blob/master/Lab-4/FranceCovid19.ipynb](https://github.com/bleonardb3/AI_POT_06-11-2020/blob/master/Lab-4/FranceCovid19.ipynb) into the "Notebook URL" textbox > click "Create" button.

## New notebook

Blank      From file      **From URL**

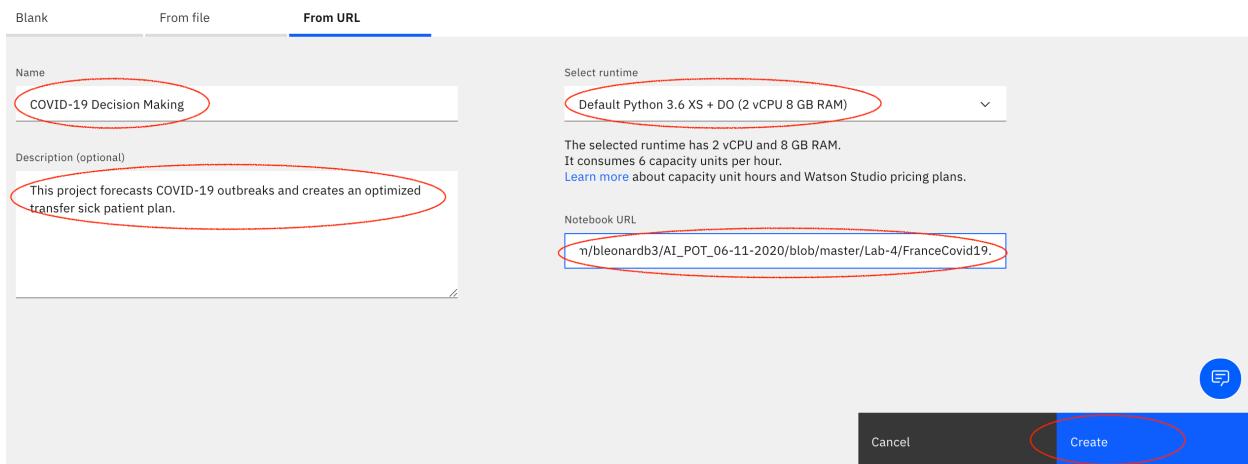
Name: COVID-19 Decision Making

Description (optional): This project forecasts COVID-19 outbreaks and creates an optimized transfer sick patient plan.

Select runtime: Default Python 3.6 XS + DO (2 vCPU 8 GB RAM)

Notebook URL: n/bleonardb3/AI\_POT\_06-11-2020/blob/master/Lab-4/FranceCovid19.

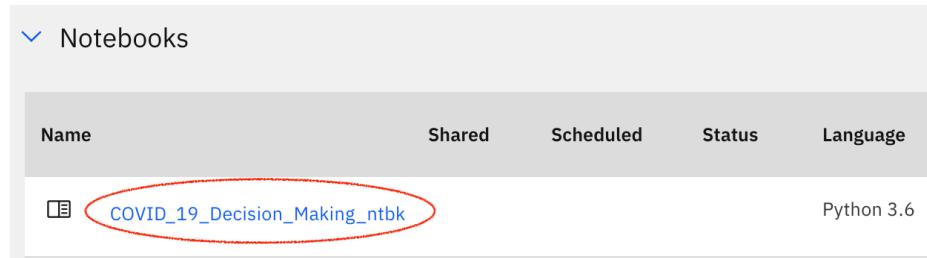
Cancel      **Create**



4. Click on your COVID-19 notebook project.

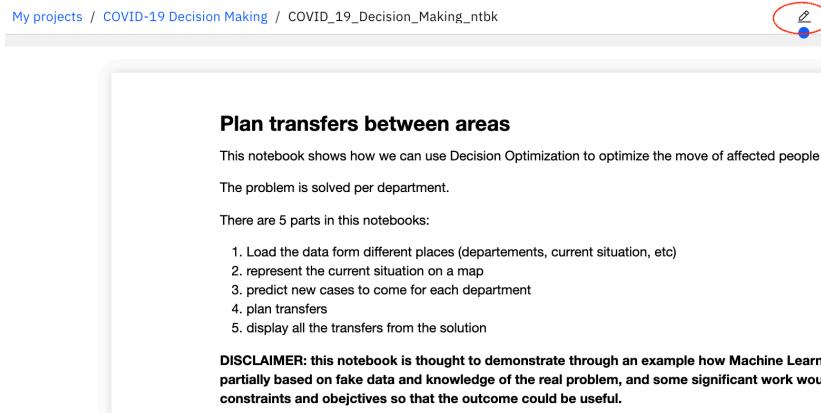
▼ Notebooks

Name	Shared	Scheduled	Status	Language
COVID_19_Decision_Making_ntbk				Python 3.6



5. Your notebook project should look similar to this image. Click on the edit pencil icon

My projects / COVID-19 Decision Making / COVID\_19\_Decision\_Making\_ntbk



**Plan transfers between areas**

This notebook shows how we can use Decision Optimization to optimize the move of affected people between areas.

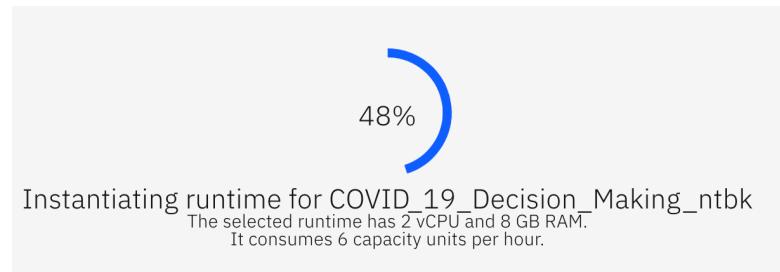
The problem is solved per department.

There are 5 parts in this notebooks:

1. Load the data from different places (departments, current situation, etc)
2. represent the current situation on a map
3. predict new cases to come for each department
4. plan transfers
5. display all the transfers from the solution

**DISCLAIMER:** this notebook is thought to demonstrate through an example how Machine Learning can be used to solve real world problems. It is partially based on fake data and knowledge of the real problem, and some significant work would be required to make it work in a real scenario. The outcome could be useful.

6. You will see a progress circle showing how much of the notebook is loaded.



7. Instructions to run a Jupyter Notebook. A Jupyter notebook consists of a series of cells. These cells are of 2 types (1) documentation cells containing markdown, and (2) code cells (denoted by a bracket on the left of the cell) where you write Python code, R, or Scala code depending on the type of notebook. Code cells can be run by putting the cursor in the code cell and pressing **<Shift><Enter>** on the keyboard. Alternatively, you can execute the cells by clicking on **Run icon** on the menu bar that will run the current cell (where the cursor is located) and then select the cell below. In this way, repeatedly clicking on **Run** executes all the cells in the notebook. When a code cell is executed the brackets on the left change to an asterisk '\*' to indicate the code cell is executing. When completed, a sequence number appears.

8. Import the necessary files.

```
In [1]: import brunel
import pandas as pd
import math
import csv
import collections
```

9. This lab uses use data from the French government [data.gouv.fr](https://www.data.gouv.fr/fr/datasets/donnees-relatives-a-lepidemie-de-covid-19/#) site: <https://www.data.gouv.fr/fr/datasets/donnees-relatives-a-lepidemie-de-covid-19/#>. First we will import data about hospitals' COVID-19 patients.

```
In [2]: url ="https://www.data.gouv.fr/fr/datasets/r/63352e38-d353-4b54-bfd1-f1b3ee1cabd7"
df=pd.read_csv(url, sep=";")
df.head()
```

```
Out[2]:      dep sexe        jour hosp  rea  rad  dc
0   01     0 2020-03-18     2    0    1    0
1   01     1 2020-03-18     1    0    1    0
2   01     2 2020-03-18     1    0    0    0
3   02     0 2020-03-18    41   10   18   11
4   02     1 2020-03-18    19    4   11    6
```

10. Let's remove some departments which are not concerned by possible moves.

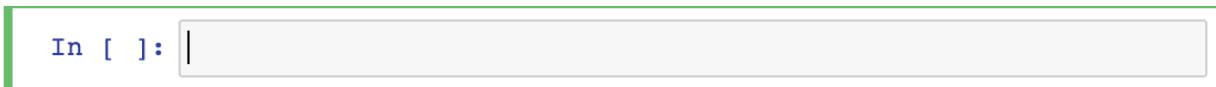
```
In [3]: deps = df.dep.unique()
deps = deps[deps != '971']
deps = deps[deps != '972']
deps = deps[deps != '973']
deps = deps[deps != '974']
deps = deps[deps != '976']
deps = deps[~pd.isna(deps)]
```

11. Let's create a dictionary of aggregated data per department.

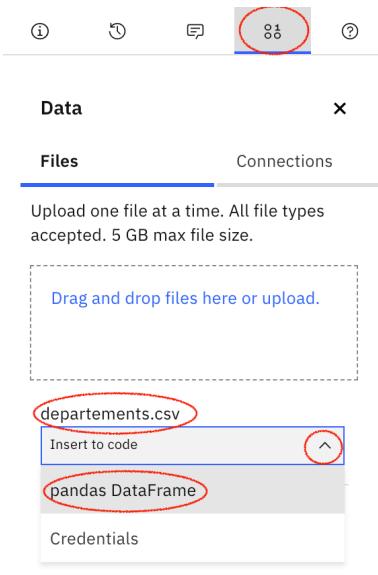
```
In [4]: hosp_data = {}
for d in deps:
    data = df[df.dep==d]
    data = data.groupby('jour').sum().reset_index().drop(columns=['sexe'])
    data['jour']=pd.to_datetime(data['jour'])
    data = data.sort_values(by=['jour'], ascending=False)
    hosp_data[d] = data
```

12. We will use some GPS data on departments from a loaded data asset. Follow these instructions to import the "departements.csv" that you uploaded in your "Data Assets" above. The departements.csv file contains different French administrative "departments" and their GPS coordinates of frontier and center.

12.1. Place your cursor in the blank cell.



12.2. Click on the 0/1 icon located in the upper right. In the Data expand menu locate the file "departements.csv". Click on the "Insert to code" dropdown menu select "pandas DataFrame"



12.3. Change these lines of code:

```
df_data_1 = pd.read_csv(body)
df_data_1.head()
to

deps_data = pd.read_csv(body)
deps_data.head()
```

12.4. Your code cell should look similar to this image.

```
In [5]:
import types
import pandas as pd
from botocore.client import Config
import ibm_boto3

def __iter__(self): return 0

# @hidden_cell
# The following code accesses a file in your IBM Cloud Object Storage. It includes your credentials
# You might want to remove those credentials before you share the notebook.
client_40296b37f7e14ef5bd0156dcbbe23a9b = ibm_boto3.client(service_name='xxxxxxxx',
    ibm_api_key_id='xxxxxxxxxxxxxxxxxxxxxxxxxxxxxx',
    ibm_auth_endpoint="https://xxxxxxxxxx",
    config=Config(signature_version='xxxxxxxx'),
    endpoint_url='https://xxxxxxxxxxxx.com')

body = client_40296b37f7e14ef5bd0156dcbbe23a9b.get_object(Bucket='covid19decisionmaking-donotdelete'
# add missing __iter__ method, so pandas accepts body as file-like object
if not hasattr(body, "__iter__"): body.__iter__ = types.MethodType(__iter__, body)

deps_data = pd.read_csv(body)
deps_data.head()
```

12.5. Execute this code cell to import the departements.csv file into a pandas dataframe.

**Out[5]:**

Nd	DEPARTEMENT	CAPACITY	LONGITUDE	LATITUDE
0	AIN	26	5d20'56" E	46d05'58"
1	AISNE	43	3d33'30" E	49d33'34"
2	ALLIER	33	3d11'18" E	46d23'37"
3	ALPES-DE-HAUTE-PROVENCE	13	6d14'38" E	44d06'22"
4	HAUTES-ALPES	24	6d15'47" E	44d39'49"

13. Execute the "strip\_zero" function. This is used to fix incompatibilities is using the "deps" list data with the deps\_data series data structure.

```
In [6]: def strip_zero(val):
    if val[0]=='0':
        return (str(int(val)))
    return val
```

14. Convert the departments LONGITUDE and LATITUDE from strings to real numbers.

```
In [7]: def coord(val):
    neg = (val[-1] == 'O')
    #print (pos)
    cl = val.split('d')[0]
    #print (cl)
    c2 = val.split('d')[1].split("'''")[0]
    #print (c2)
    c3 = val.split('d')[1].split("'''")[1].split("'''")[0]
    #print (c3)
    res = float(cl) + float(c2)/60 + float(c3)/3600
    if neg:
        res = -res
    return res

deps_data['LONGITUDE'] = deps_data['LONGITUDE'].apply(lambda x: coord(x))
deps_data['LATITUDE'] = deps_data['LATITUDE'].apply(lambda x: coord(x))

deps_data = deps_data.set_index(['Nd'])
deps_data.head()
```

Out[7]:

DEPARTEMENT CAPACITY LONGITUDE LATITUDE

Nd					
1	AIN	26	5.348889	46.099444	
2	AISNE	43	3.558333	49.559444	
3	ALLIER	33	3.188333	46.393611	
4	ALPES-DE-HAUTE-PROVENCE	13	6.243889	44.106111	
5	HAUTES-ALPES	24	6.263056	44.663611	

15. Calculate the magnitude circle based on the number of COVID-19 patients for a given area.

```
In [8]: def distance(lt1, lg1, lt2, lg2):
    R = 6373.0

    lat1 = math.radians(lt1)
    lon1 = math.radians(lg1)
    lat2 = math.radians(lt2)
    lon2 = math.radians(lg2)

    dlon = lon2 - lon1
    dlat = lat2 - lat1

    a = math.sin(dlat / 2)**2 + math.cos(lat1) * math.cos(lat2) * math.sin(dlon / 2)**2
    c = 2 * math.atan2(math.sqrt(a), math.sqrt(1 - a))

    distance = R * c
    return distance
```

## 2. Display the current situation on a map

We will use folium to represent the data on maps.

16. Install folium.

```
In [9]: !pip install folium

Collecting folium
  Downloading https://files.pythonhosted.org/packages/a4/f0/44e69d50519880287cc41e7c8a6acc58daa
9a9acf5f6afc52bcc70f69a6d/folium-0.11.0-py2.py3-none-any.whl (93kB)
    |██████████| 102kB 7.7MB/s ta 0:00:011
Requirement already satisfied: numpy in /opt/conda/envs/Python36/lib/python3.6/site-packages (from folium) (1.15.4)
Requirement already satisfied: requests in /opt/conda/envs/Python36/lib/python3.6/site-packages (from folium) (2.21.0)
Requirement already satisfied: jinja2>=2.9 in /opt/conda/envs/Python36/lib/python3.6/site-packages (from folium) (2.10)
Collecting branca>=0.3.0 (from folium)
  Downloading https://files.pythonhosted.org/packages/13/fb/9eacc24ba3216510c6b59a4ea1cd53d87f2
5ba76237d7f4393abeaf4c94e/branca-0.4.1-py3-none-any.whl
Requirement already satisfied: chardet<3.1.0,>=3.0.2 in /opt/conda/envs/Python36/lib/python3.6/
site-packages (from requests->folium) (3.0.4)
Requirement already satisfied: certifi>=2017.4.17 in /opt/conda/envs/Python36/lib/python3.6/
site-packages (from requests->folium) (2020.4.5.1)
Requirement already satisfied: urllib3<1.25,>=1.21.1 in /opt/conda/envs/Python36/lib/python3.6/
site-packages (from requests->folium) (1.24.1)
Requirement already satisfied: idna<2.9,>=2.5 in /opt/conda/envs/Python36/lib/python3.6/site-
packages (from requests->folium) (2.8)
Requirement already satisfied: MarkupSafe>=0.23 in /opt/conda/envs/Python36/lib/python3.6/site-
packages (from jinja2>=2.9->folium) (1.1.0)
Installing collected packages: branca, folium
Successfully installed branca-0.4.1 folium-0.11.0
```

## 17. Let's now represent the situation for each department

```
In [10]: import folium

m = folium.Map(
    location=[45.5236, 5.6750],
    zoom_start=6
)

initial = {}
capacity = {}

for d, dep in deps_data.iterrows():
    if (d in ['1', '2', '3', '4', '5', '6', '7', '8', '9']):
        d = '0' + str(d)

    sz = int(hosp_data[d]['rea'].iat[0])
    initial[d] = sz
    capacity[d] = int(1.2*dep['CAPACITY'])

url = 'https://france-geojson.gregoiredavid.fr/repo/departements.geojson'

def style_function(feature):
    d = feature['properties']['code']
    return {
        'fillOpacity': 0.4 if initial[d]>capacity[d] else 0,
        'weight': 0.5,
        'color': 'black',
        'fillColor': 'red' if initial[d]>capacity[d] else 'white'
    }

folium.GeoJson(
    url,
    name='geojson',
    style_function=style_function
).add_to(m)

for d, dep in deps_data.iterrows():
    lt = dep['LATITUDE']
    lg = dep['LONGITUDE']
    nm = dep['DEPARTEMENT']

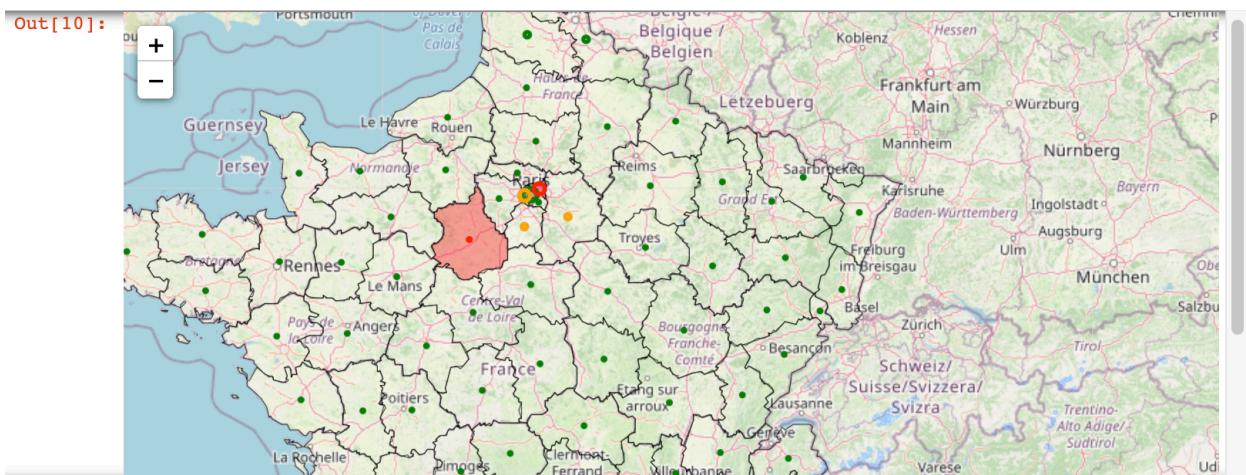
    if (d in ['1', '2', '3', '4', '5', '6', '7', '8', '9']):
        d = '0' + str(d)
```

```

sz = int(hosp_data[d]['rea'].iat[0])
initial[d] = sz
#folium.Marker([lt, lg]).add_to(here_map)
color = 'green'
if initial[d]>0.5*capacity[d]:
    color = 'orange'
if initial[d]>capacity[d]:
    color='red'
folium.Circle(
    radius=sz*50,
    location=[lt, lg],
    popup=folium.Popup(nm + ' (' + str(d)+')<br>' +str(sz) +' reas.<br>Capacity: '+str(capacity[d]),
    color=color,
    fill=True,
    fill_color=color
).add_to(m)

```

m



## 18. Create dataframe with status before transfers and calculate the total over capacity

```

In [16]: before = pd.DataFrame(columns=['Nd', 'capacity', 'value', 'overcapacity'], data=[[d, capacity[d], i
print (before)

total_overall_before = before['overcapacity'].sum()
print(total_overall_before)

```

Nd	capacity	value	overcapacity
0 01	31	0	0
1 02	51	16	0
2 03	39	2	0
3 04	15	0	0
4 05	28	0	0
5 06	160	2	0
6 07	22	2	0
7 08	25	6	0
8 09	25	2	0
9 10	19	6	0
10 11	37	2	0
11 12	34	0	0
12 13	296	77	0
13 14	110	2	0
14 15	20	0	0
15 16	27	2	0

### 3. Predict the new cases

19. We use a very dummay linear regresion to predict the new cases to appear on each department

```
In [17]: import numpy as np
from sklearn.linear_model import LinearRegression

NB_PERIODS = 3

def predict_more(d, n):
    X = hosp_data[d].index.tolist()
    X.reverse()
    X=np.array(X).reshape(-1,1)
    y = hosp_data[d]['rea'].tolist()
    y.reverse()
    y=np.array(y).reshape(-1,1)

    regsr=LinearRegression()
    regsr.fit(X,y)

    to_predict_x = [i for i in range(len(X), len(X)+n)]
    to_predict_x= np.array(to_predict_x).reshape(-1,1)
    predicted_y= regsr.predict(to_predict_x)
    delta_y = [ int(round(max(0, predicted_y[i][0]-y[len(y)-1][0]))) for i in range(n)]
    return delta_y

new_rea ={ d:predict_more(d, NB_PERIODS) for d in deps}
print (new_rea)
```

{'01': [0, 0, 0], '02': [5, 4, 3], '03': [0, 0, 0], '04': [0, 0, 0], '05': [0, 0, 0], '06': [3, 2, 1], '07': [9, 8, 8], '08': [0, 0, 0], '09': [0, 0, 0], '10': [0, 0, 0], '11': [0, 0, 0], '12': [0, 0, 0], '13': [28, 25, 22], '14': [0, 0, 0], '15': [1, 0, 0], '16': [0, 0, 0], '17': [0, 0, 0], '18': [0, 0, 0], '19': [5, 4, 4], '21': [0, 0, 0], '22': [3, 3, 3], '23': [7, 7, 7], '24': [0, 0, 0], '25': [0, 0, 0], '26': [0, 0, 0], '27': [1, 1, 1], '28': [1, 1, 0], '29': [0, 0, 0], '2A': [0, 0, 0], '2B': [2, 2, 2], '30': [9, 8, 8], '31': [1, 0, 0], '32': [0, 0, 0], '33': [0, 0, 0], '34': [0, 0, 0], '35': [0, 0, 0], '36': [1, 1, 0], '37': [6, 5, 5], '38': [3, 2, 1], '39': [0, 0, 0], '40': [0, 0, 0], '41': [5, 5, 4], '42': [16, 14, 13], '43': [0, 0, 0], '44': [0, 0, 0], '45': [10, 9, 8], '46': [0, 0, 0], '47': [1, 1, 1], '48': [0, 0, 0], '49': [4, 3, 2], '50': [0, 0, 0], '51': [0, 0, 0], '52': [5, 4, 4], '53': [1, 1, 1], '54': [0, 0, 0], '55': [0, 0, 0], '56': [3, 2, 2], '57': [0, 0, 0], '58': [0, 0, 0], '59': [12, 8, 4], '60': [0, 0, 0], '61': [1, 1, 1], '62': [9, 8, 7], '63': [0, 0, 0], '64': [0, 0, 0], '65': [1, 1, 0], '66': [0, 0, 0], '67': [0, 0, 0], '68': [0, 0, 0], '69': [23, 19, 15], '70': [0, 0, 0], '71': [1, 1, 0], '72': [0, 0, 0], '73': [0, 0, 0], '74': [0, 0, 0], '75': [30, 18, 6], '76': [0, 0, 0], '77': [25, 22, 20], '78': [0, 0, 0], '79': [0, 0, 0], '80': [0, 0, 0], '81': [0, 0, 0], '82': [3, 3, 3], '83': [0, 0, 0], '84': [0, 0, 0], '85': [4, 4, 4], '86': [0, 0, 0], '87': [0, 0, 0], '88': [0, 0, 0], '89': [13, 12, 12], '90': [0, 0, 0], '91': [22, 19, 17], '92': [5, 0, 0], '93': [34, 32, 29], '94': [47, 42, 37], '95': [0, 0, 0]}

### 4. Optimize the transfers using Decision Optimization

20. Now let's create an optimization model.

**Not knowing the real capacities and the real constraints and objectives, we have imagined that some limited short and long transfers could be organized in order to minimize the total over capacity.**

```
In [12]: from docplex.mp.environment import Environment
env = Environment()
env.print_information()

* system is: Linux 64bit
* Python version 3.6.9, located at: /opt/conda/envs/Python36/bin/python
* docplex is present, version is 2.14.186
* CPLEX library is present, version is 12.10.0.0, located at: /opt/conda/envs/Python36/lib/pyth
on3.6/site-packages
* pandas is present, version is 0.24.1
```

21. Parameters are the number of possible moves, and the maximum number of cases per move.

```
In [14]: from docplex.mp.model import Model
mdl = Model("Plan Transfers")

MAX_NB_LONG_TRANSFERS_PER_PERIOD = 3
MAX_CASES_PER_LONG_TRANSFERS = 20

MAX_NB_SHORT_TRANSFERS_PER_DEPARTMENT = 3

LONG_DISTANCE = 200
```

22. For each "Department" determine if the distance between itself and all other departments is either a "SHORT" or "LONG" transportation route.

```
In [15]: is_long = {d1: {d2: distance(deps_data['LATITUDE'][strip_zero(d1)], deps_data['LONGITUDE'][strip_zero(d1)], deps_data['LATITUDE']'
```

23. Create a "Plan Transfers" short transfer bounds.

```
In [16]: transfer_periods = list(range(NB_PERIODS))
all_periods = list(range(NB_PERIODS+1))

# Binary vars representing the "assigned" libraries for each coffee shop
use_link_vars = mdl.binary_var_cube(deps, deps, transfer_periods, name="use_link")
link_vars = mdl.integer_var_cube(deps, deps, transfer_periods, lb=0, ub=MAX_CASES_PER_LONG_TRANSFERS, name="link")
occupancy_vars = mdl.integer_var_matrix(deps, all_periods, lb=0, name="occupancy")

# Short transfers bounds
mdl.add_constraints(link_vars[d1, d2, t] <= 1 for d1 in deps for d2 in deps if not is_long[d1][d2] for t in transfer_periods)

mdl.print_information()

Model: Plan Transfers
- number of variables: 55680
- binary=27648, integer=28032, continuous=0
- number of constraints: 4890
- linear=4890
- parameters: defaults
- objective: none
- problem type is: MILP
```

24. Add the constraints

```
In [17]: # Initial state
mdl.add_constraints(occupancy_vars[d, 0] == initial[d] for d in deps)

# structural constraint between user_link and link
mdl.add_constraints(use_link_vars[d, d1, t] == (link_vars[d, d1, t] >= 1) for d in deps for d1 in deps for t in transfer_periods)

# number of transfers from a department less than current number of cases
mdl.add_constraints(mdl.sum(link_vars[d, d1, t] for d1 in deps) <= occupancy_vars[d, t] for d in deps for t in transfer_periods)

# maximum number of LONG transfers
mdl.add_constraints(mdl.sum(use_link_vars[d1, d2, t] for d1 in deps for d2 in deps if is_long[d1][d2]) <= MAX_NB_LONG_TRANSFERS)

# maximum number of SHORT transfers
mdl.add_constraints(mdl.sum(use_link_vars[d1, d2, t] for d1 in deps if not is_long[d1][d2] for t in transfer_periods) <= MAX_NB_SHORT_TRANSFERS)

# conservation constraints including new cases to come
mdl.add_constraints(occupancy_vars[d, t+1] == new_rea[d][t] + occupancy_vars[d, t] + mdl.sum(link_vars[d1, d, t] for d1 in deps))

mdl.print_information()

Model: Plan Transfers
- number of variables: 83328
- binary=55296, integer=28032, continuous=0
- number of constraints: 60957
- linear=33309, equiv=27648
- parameters: defaults
- objective: none
- problem type is: MILP
```

25. Objective is to minimize the total over capacity at the end.

```
In [18]: final_overcapacity = mdl.sum(mdl.max(0, occupancy_vars[d, NB_PERIODS] - capacity[d]) for d in deps)
mdl.add_kpi(final_overcapacity)

nb_long_transfers = mdl.sum(use_link_vars[d1, d2, t] for d1 in deps for d2 in deps if is_long[d1][d2] for t in transfer_periods)
mdl.add_kpi(nb_long_transfers)

nb_short_transfers = mdl.sum(use_link_vars[d1, d2, t] for d1 in deps for d2 in deps if not is_long[d1][d2] for t in transfer_periods)
mdl.add_kpi(nb_short_transfers)

mdl.minimize(1000 * final_overcapacity + 10 * nb_long_transfers + nb_short_transfers)
```

26. Have the "docplex" solve the optimization model.

```
In [19]: mdl.set_time_limit(20)
mdl.solve(log_output=True)
```

```

Performing restart 1

Repeating presolve.
Tried aggregator 2 times.
MIP Presolve eliminated 2 rows and 192 columns.
MIP Presolve modified 11084 coefficients.
Aggregator did 96 substitutions.
Reduced MIP has 41747 rows, 45539 columns, and 179834 nonzeros.
Reduced MIP has 24700 binaries, 20839 generals, 0 SOSSs, and 17081 indicators.
Presolve time = 0.44 sec. (263.28 ticks)
Tried aggregator 1 time.
Reduced MIP has 41747 rows, 45539 columns, and 179834 nonzeros.
Reduced MIP has 24700 binaries, 20839 generals, 0 SOSSs, and 17081 indicators.
Presolve time = 0.27 sec. (143.52 ticks)
Resolve time = 1.30 sec. (587.15 ticks)
*   821+    0                  104.0000      90.0000      13.46%
    821    0      100.0000      9      104.0000      Cuts: 24      5147      3.85%
*   821    0      integral      0      100.0000      Cuts: 11      5332      0.00%
    821    0      cutoff      100.0000      100.0000      5332      0.00%

Flow cuts applied:  2
Mixed integer rounding cuts applied:  16
Zero-half cuts applied:  2
Lift and project cuts applied:  1
Gomory fractional cuts applied:  8

Root node processing (before b&c):
  Real time      =  5.83 sec. (6896.49 ticks)
Parallel b&c, 2 threads:
  Real time      = 10.44 sec. (8356.22 ticks)
  Sync time (average) =  0.75 sec.
  Wait time (average) =  0.00 sec.

-----
Total (root+branch&cut) = 16.26 sec. (15252.71 ticks)

```

**Out[19]:** docplex.mp.solution.SolveSolution(obj=100,values={use\_link\_07\_13\_1:1,use..

## 27. Extract and print the moves

```

In [20]: edges = [(t, d1, d2, int(link_vars[d1, d2, t])), is_long[d1][d2]] for t in transfer_periods for d1 in deps for d2 in deps if int(
print(edges)

[(0, '28', '18', 1, False), (0, '28', '27', 1, False), (0, '91', '18', 1, False), (0, '91', '27', 1, False), (0, '91', '51',
1, False), (0, '91', '76', 1, False), (0, '91', '78', 1, False), (0, '93', '01', 20, True), (0, '93', '05', 20, True), (0, '9
3', '38', 20, True), (1, '07', '13', 1, False), (1, '89', '70', 1, False), (1, '91', '10', 1, False), (1, '91', '27', 1, Fals
e), (1, '93', '56', 20, True), (1, '93', '79', 20, True), (1, '94', '10', 1, False), (1, '94', '18', 1, False), (1, '94', '3
5', 20, True), (1, '94', '76', 1, False), (2, '28', '53', 1, False), (2, '28', '78', 1, False), (2, '91', '50', 20, True),
(2, '91', '77', 1, False), (2, '94', '02', 1, False), (2, '94', '10', 1, False), (2, '94', '30', 20, True), (2, '94', '80',
1, False)]

```

## 28. Recreate structure for final situation, and calculate final over capacity.

```
In [21]: final = { d: int(occupancy_vars[d, NB_PERIODS].solution_value) for d in deps }

after = pd.DataFrame(columns=['Nd', 'capacity', 'value', 'overcapacity'], data=[[d, capacity[d], final[d], max(0, final[d]-capacity[d])] for d in range(Nd)])
print(after)

total_overall_after = after['overcapacity'].sum()
print(total_overall_after)

Nd    capacity   value  overcapacity
0      01        31     20            0
1      02        51     28            0
2      03        39      2            0
3      04        15      0            0
4      05        28     20            0
5      06       160      3            0
6      07        22     22            0
7      08        25      5            0
8      09        25      2            0
9      10        19      9            0
10     11        37      2            0
94     94        88     88            0
95     95       117     16            0

[96 rows x 4 columns]
0
```

## 5. Display the solution

29. And represent the moves and the changes for impacted departments.

- Black links are the local transfers.
- Green links are the long distance transfers

```
In [47]: def style_function(feature):
    d = feature['properties']['code']
    return {
        'fillOpacity': 0.4 if final[d]>capacity[d] else 0,
        'weight': 0.5,
        'color': 'black',
        'fillColor': 'red' if final[d]>capacity[d] else 'white'
    }

def get_angle(p1, p2):
    """
    This function Returns angle value in degree from the location p1 to location p2

    Parameters it accepts :
    p1 : namedtuple with lat lon
    p2 : namedtuple with lat lon

    This function Return the vlaue of degree in the data type float

    Please also refers to for better understanding : https://gist.github.com/jeromer/2005586
    """

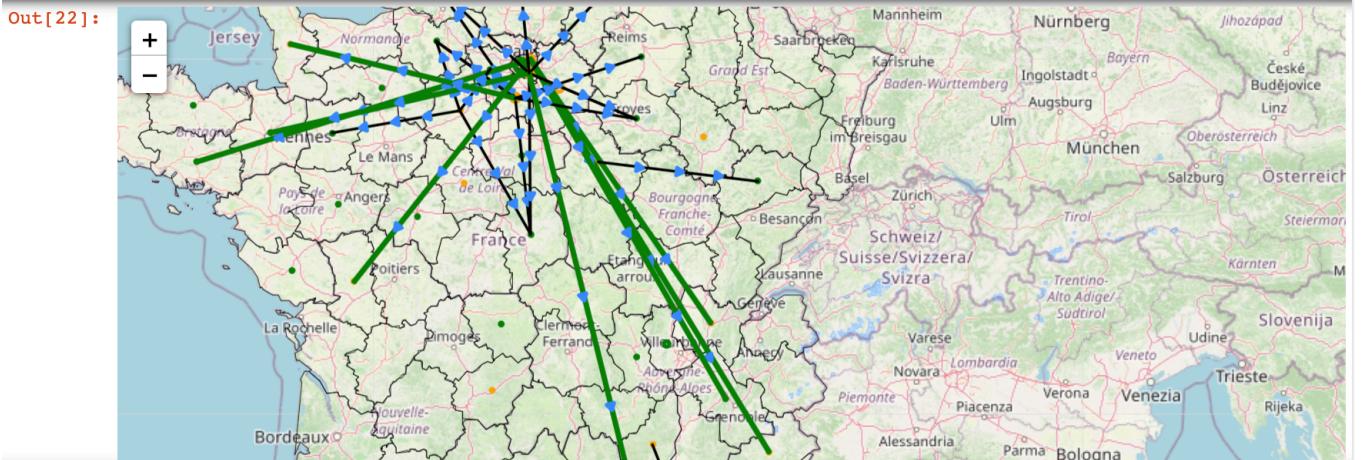
    longitude_diff = np.radians(p2.lon - p1.lon)

    latitude1 = np.radians(p1.lat)
    latitude2 = np.radians(p2.lat)

    x_vector = np.sin(longitude_diff) * np.cos(latitude2)
    y_vector = (np.cos(latitude1) * np.sin(latitude2)
                - (np.sin(latitude1) * np.cos(latitude2)
                   * np.cos(longitude_diff)))
    angle = np.degrees(np.arctan2(x_vector, y_vector))

    # Checking and adjusting angle value on the scale of 360
    if angle < 0:
        return angle + 360
    return angle

def get_arrows(locations, color, size, n_arrows):
    """
    Get a list of correctly placed and rotated
    arrows/markers to be plotted
    
```



Great job! Now you are ready to help communities and businesses develop optimization plans to respond to predicted COVID-19 infections.