Syntax Analysis

Outline

Context-Free Grammars (CFGs)

Parsing

Top-Down

Recursive Descent

Table-Driven

Bottom-Up

LR Parsing Algorithm

How to Build LR Tables

Parser Generators

Grammar Issues for Programming Languages

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Syntax Analysis - Part 1

Top-Down Parsing

- LL Grammars A subclass of all CFGs
- Recursive-Descent Parsers Programmed "by hand"
- Non-Recursive Predictive Parsers Table Driven
- Simple, Easy to Build, Better Error Handling

Bottom-Up Parsing

- LR Grammars A larger subclass of CFGs
- Complex Parsing Algorithms Table Driven
- Table Construction Techniques
- Parser Generators use this technique
- Faster Parsing, Larger Set of Grammars
- Complex
- Error Reporting is Tricky

Output of Parser?

Succeed is string is recognized ... and fail if syntax errors

Syntax Errors?

Good, descriptive, helpful message! Recover and continue parsing!

Build a "Parse Tree" (also called "derivation tree")

Build Abstract Syntax Tree (AST) In memory (with objects, pointers) Output to a file

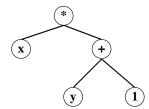
Execute Semantic Actions

Build AST

Type Checking

Generate Code

Don't build a tree at all!



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Syntax Analysis - Part 1

"Typos"

Errors in Programs

```
<u>Lexical</u>
if x<1 then y = 5:
```

```
<u>Syntactic</u>
if ((x<1) & (y>5))) ...
```

{ ... { ... _ ... }

```
<u>Semantic</u>
if (x+5) then ...
Type Errors
```

Undefined IDs, etc.

Logical Errors

```
if (i<9) then ...
Should be <= not <</pre>
```

Bugs

Compiler cannot detect Logical Errors

Compiler

Always halts

Any checks guaranteed to terminate

"Decidable"

Other Program Checking Techniques

Debugging

Testing

Correctness Proofs

"Partially Decidable"

Okay? \Rightarrow The test terminates.

Not Okay? \Rightarrow The test may not terminate!

You may need to run some programs to see if they are okay.

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Syntax Analysis - Part 1

Skip tokens until we see a ";"

Checks most of the source

Misses a second error... Oh, well...

Resume Parsing

```
Detect All Errors (Except Logical!)

Messages should be helpful.

Difficult to produce clear messages!

Example:

Syntax Error

Example:

Line 23: Unmatched Paren

if ((x == 1) then

Compiler Should Recover

Keep going to find more errors

Example:

x := (a + 5)) * (b + 7));

We're in the middle of a statement

This error missed
```

Requirements

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Error detected here

```
Difficult to generate clear and accurate error messages.
   Example
       function foo () {
         if (...) {
         } else {
            . . .
                             Missing } here
       <eof> .
                             Not detected until here
   Example
       var myVarr: Integer;
       x := myVar;
                              Misspelled ID here
                            Detected here as
                            "Undeclared ID"
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```

```
For Mature Languages
       Catalog common errors
       Statistical studies
       Tailor compiler to handle common errors well
   Statement <u>terminators</u> versus <u>separators</u>
             Terminators: C, Java, PCAT
                                             {A;B;C;}
             Separators: Pascal, Smalltalk, Haskell
   Pascal Examples
       begin
            var t: Integer;
            t := x;
            x := y;
                                Tend to insert a; here
            y := t
       <u>end</u>
       <u>if</u> (...) <u>then</u>
                              ☐ Tend to insert a; here
           x := 1
       <u>else</u>
           y := 2;
       z := 3;
       function foo (x: Integer; y: Integer)...
                                           Tend to put a comma here
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```

Error-Correcting Compilers

- Issue an error message
- Fix the problem
- Produce an executable

Example

Error on line 23: "myVarr" undefined.
"myVar" was used.

Is this a good idea???

Compiler *guesses* the programmer's intent

A shifting notion of what constitutes a correct / legal / valid program

May encourage programmers to get sloppy

Declarations provide redundancy

⇒ Increased reliability

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Syntax Analysis - Part 1

Error Avalanche

One error generates a cascade of messages

The real messages may be buried under the avalanche.

Missing **#include** or **import** will also cause an avalanche.

Approaches:

Only print 1 message per token [or per line of source]

Only print a particular message once

Error: Variable "myVarr" is undeclared

All future notices for this ID have been suppressed

Abort the compiler after 50 errors.

Error Recovery Approaches: Panic Mode

Discard tokens until we see a "synchronizing" token.

Example

- Simple to implement
- Commonly used
- The key...

Good set of synchronizing tokens Knowing what to do then

• May skip over large sections of source

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Syntax Analysis - Part 1

Error Recovery Approaches: Phrase-Level Recovery

Compiler corrects the program

by deleting or inserting tokens

...so it can proceed to parse from where it was.

<u>Example</u>

while (x = 4) y := a+b; ...

Insert do to "fix" the statement.

• The key...

Don't get into an infinite loop

- ...constantly inserting tokens
- ...and never scanning the actual source

Error Recovery Approaches: Error Productions

Augment the CFG with "Error Productions"

Now the CFG accepts anything!

If "error productions" are used...

Their actions:

```
{ print ("Error...") }
```

Used with...

- LR (Bottom-up) parsing
- Parser Generators

Error Recovery Approaches: Global Correction

Theoretical Approach

Find the minimum change to the source to yield a valid program (Insert tokens, delete tokens, swap adjacent tokens)

Impractical algorithms - too time consuming

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1:

Syntax Analysis - Part 1

CFG: Context Free Grammars

Example Rule:

```
Stmt \rightarrow \underline{if} Expr \underline{then} Stmt \underline{else} Stmt
```

Terminals

Keywords

else "else"

Token Classes

ID INTEGER REAL

Punctuation

```
; ";" <u>;</u>
```

Non-terminals

Any symbol appearing on the lefthand side of any rule

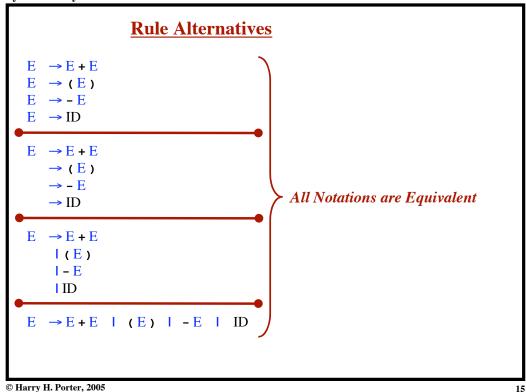
Start Symbol

Usually the non-terminal on the lefthand side of the first rule

Rules (or "Productions")

```
BNF: Backus-Naur Form / Backus-Normal Form

Stmt ::= <u>if</u> Expr <u>then</u> Stmt <u>else</u> Stmt
```



```
Syntax Analysis - Part 1
                          Notational Conventions
   Terminals
       a b c ...
   Nonterminals
       A B C ...
       S
       Expr
   Grammar Symbols (Terminals or Nonterminals)
       X Y Z U V W ...
                               A sequence of zero
   Strings of Symbols
                               Or more terminals
       αβγ...
                               And nonterminals
   Strings of Terminals
       x y z u v w ...
                                 Including ε
   Examples
       A \rightarrow \alpha B
             A rule whose righthand side ends with a nonterminal
             A rule whose righthand side begins with a string of terminals (call it "x")
```

Derivations

- 1. $E \rightarrow E + E$
- 2. $\rightarrow E \star E$
- $3. \rightarrow (E)$
- 4. → E
- $5. \rightarrow ID$

A "Derivation" of "(id*id)"

$$E \Rightarrow (E) \Rightarrow (E*E) \Rightarrow (\underline{id}*E) \Rightarrow (\underline{id}*\underline{id})$$

"Sentential Forms"

A sequence of terminals and nonterminals in a derivation $(id \times E)$

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Derives in one step ⇒

If $A \rightarrow \beta$ is a rule, then we can write

$$\alpha A \gamma \Rightarrow \alpha \beta \gamma$$

Any sentential form containing a nonterminal (call it A) ... such that A matches the nonterminal in some rule.

Derives in zero-or-more steps \Rightarrow^*

$$E \Rightarrow^* (id*id)$$

If $\alpha \Rightarrow^* \beta$ and $\beta \Rightarrow \gamma$, then $\alpha \Rightarrow^* \gamma$

Derives in one-or-more steps ⇒+

Given

G A grammar

S The Start Symbol

Define

L(G) The language generated $L(G) = \{ w \mid S \Rightarrow + w \}$

"Equivalence" of CFG's

If two CFG's generate the same language, we say they are "equivalent." $G_1 \approx G_2$ whenever $L(G_1) = L(G_2)$

In making a derivation...

Choose which nonterminal to expand

Choose which rule to apply

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Syntax Analysis - Part 1

Leftmost Derivations

In a derivation... always expand the *leftmost* nonterminal.

- E+E
- (E) + E
- (E*E)+E
- (id*E)+E
- (id*id)+E
- (id*id)+id

 \rightarrow (E)

→ - E

→ ID

Let \Rightarrow_{LM} denote a step in a leftmost derivation (\Rightarrow_{LM}^* means zero-or-more steps)

At each step in a leftmost derivation, we have

$$wA\gamma \Rightarrow_{LM} w\beta\gamma$$
 where $A \rightarrow \beta$ is a rule

(Recall that w is a string of terminals.)

Each sentential form in a leftmost derivation is called a "left-sentential form."

If $S \Rightarrow_{LM}^* \alpha$ then we say α is a "left-sentential form."

Rightmost Derivations

In a derivation... always expand the *rightmost* nonterminal.

- ⇒ E+E
- \Rightarrow E+id
- \Rightarrow (E) + <u>id</u>
- \Rightarrow (E*E) + id
- \Rightarrow (E*<u>id</u>)+<u>id</u>
- \Rightarrow $(\underline{id}*\underline{id})+\underline{id}$

- 1. $E \rightarrow E + E$ 2. $\rightarrow E \star E$
- $3. \rightarrow (E)$
- 4. → -
- 5. → ID

Let \Rightarrow_{RM} denote a step in a rightmost derivation (\Rightarrow_{RM} * means zero-or-more steps)

At each step in a rightmost derivation, we have

$$\alpha A w \Rightarrow_{RM} \alpha \beta w$$
 where $A \rightarrow \beta$ is a rule

(Recall that w is a string of terminals.)

Each sentential form in a rightmost derivation is called a "right-sentential form."

If $S \Rightarrow_{RM}^* \alpha$ then we say α is a "right-sentential form."

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Syntax Analysis - Part 1

Bottom-Up Parsing

Bottom-up parsers discover rightmost derivations!

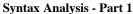
Parser moves from input string back to S.

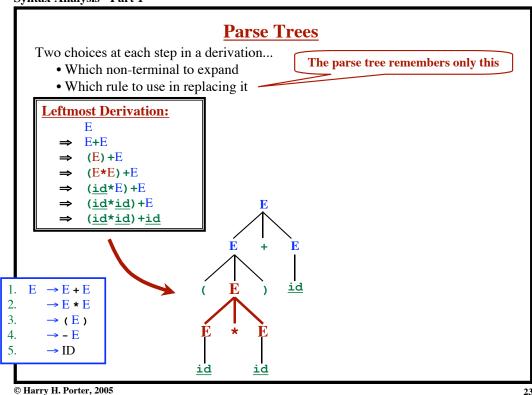
Follow $S \Rightarrow_{RM}^* W$ in reverse.

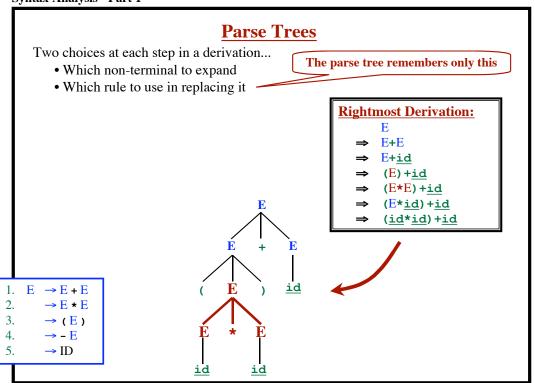
At each step in a rightmost derivation, we have

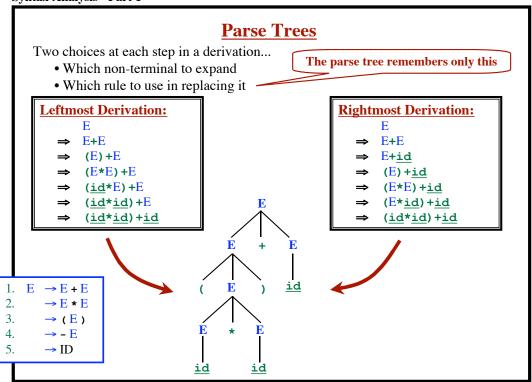
$$\alpha Aw \Rightarrow_{RM} \alpha \beta w$$
 where $A \rightarrow \beta$ is a rule

String of terminals (i.e., the rest of the input, which we have not yet seen)









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Given a leftmost derivation, we can build a parse tree. Given a rightmost derivation, we can build a parse tree.



Every parse tree corresponds to...

- A single, unique leftmost derivation
- A single, unique rightmost derivation

Ambiguity:

However, one input string may have several parse trees!!!

Therefore:

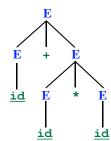
- Several leftmost derivations
- Several rightmost derivations

Ambuiguous Grammars

Leftmost Derivation #1

Е

- \Rightarrow E+E
- $\Rightarrow id+E$
- $\Rightarrow \underline{id} + E * E$
- \Rightarrow <u>id</u>+<u>id</u>*E
- ⇒ <u>id</u>+<u>id</u>*<u>id</u>



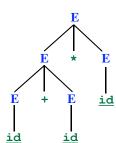
1. $E \rightarrow E + E$ 2. $\rightarrow E * E$ 3. $\rightarrow (E)$ 4. $\rightarrow -E$ 5. $\rightarrow ID$

Input: id+id*id

Leftmost Derivation #2

E

- ⇒ E*E
- **⇒** E+E*E
- $\Rightarrow \underline{id} + E * E$
- \Rightarrow id+id*E
- ⇒ <u>id</u>+<u>id</u>*<u>id</u>



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Syntax Analysis - Part 1

Ambiguous Grammar

More than one Parse Tree for some sentence.

The grammar for a programming language may be ambiguous Need to modify it for parsing.

Also: Grammar may be left recursive. Need to modify it for parsing.

Translating a Regular Expression into a CFG

First build the NFA.

For every state in the NFA...

Make a nonterminal in the grammar

For every edge labeled **c** from A to B...

Add the rule

 $A \rightarrow cB$

For every edge labeled ε from A to B...

Add the rule

 $A \rightarrow B$

For every final state B...

Add the rule

 $B \rightarrow \epsilon$

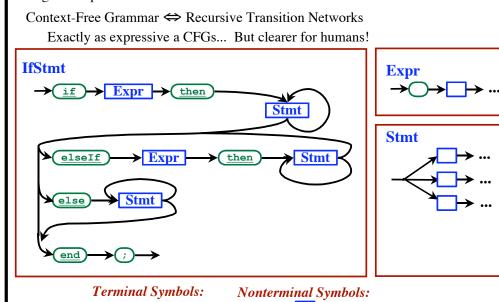
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Syntax Analysis - Part 1

Recursive Transition Networks

Regular Expressions ⇔ NFA ⇔ DFA



The Dangling "Else" Problem This grammar is ambiguous! Stmt → if Expr then Stmt → if Expr then Stmt else Stmt → ...Other Stmt Forms... Example String: if E₁ then if E₂ then S₁ else S₂ Interpretation #1: if E₁ then (if E₂ then S₁) else S₂ if E₁ then S else S₂ Interpretation #2: if E₁ then (if E₂ then S₁ else S₂) Interpretation #2: if E₁ then (if E₂ then S₁ else S₂) Interpretation #2: if E₁ then (if E₂ then S₁ else S₂)

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Syntax Analysis - Part 1

The Dangling "Else" Problem

<u>Goal:</u> "Match <u>else</u>-clause to the closest <u>if</u> without an <u>else</u>-clause already." <u>Solution:</u>

Stmt → <u>if</u> Expr <u>then</u> Stmt

→ <u>if</u> Expr <u>then</u> WithElse <u>else</u> Stmt

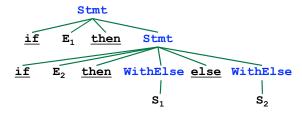
→ ...Other Stmt Forms...

WithElse → <u>if</u> Expr <u>then</u> WithElse <u>else</u> WithElse

→ ...Other Stmt Forms...

Any Stmt occurring between <u>then</u> and <u>else</u> must have an <u>else</u>. i.e., the <u>Stmt</u> must not end with "<u>then</u> Stmt".

<u>Interpretation #2:</u> if E_1 then (if E_2 then S_1 else S_2)



The Dangling "Else" Problem

Goal: "Match else-clause to the closest if without an else-clause already." Solution:

Stmt → <u>if</u> Expr <u>then</u> Stmt

→ <u>if</u> Expr <u>then</u> WithElse <u>else</u> Stmt

→ ...Other Stmt Forms...

→ <u>if</u> Expr <u>then</u> WithElse <u>else</u> WithElse WithElse

→ ...Other Stmt Forms...

Any Stmt occurring between then and else must have an else. i.e., the Stmt must not end with "then Stmt".

<u>Interpretation #1:</u> if E_1 then (if E_2 then S_1) else S_2



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Syntax Analysis - Part 1

The Dangling "Else" Problem

Goal: "Match else-clause to the closest if without an else-clause already." Solution:

Stmt → <u>if</u> Expr <u>then</u> Stmt

→ <u>if</u> Expr <u>then</u> WithElse <u>else</u> Stmt

→ ...Other Stmt Forms...

WithElse → <u>if</u> Expr <u>then</u> WithElse <u>else</u> WithElse

→ ...Other Stmt Forms...

Any Stmt occurring between then and else must have an else.

i.e., the Stmt must not end with "then Stmt".

<u>Interpretation #1:</u> if E_1 then (if E_2 then S_1) else S_2



then WithElse else WithElse

The Dangling "Else" Problem

<u>Goal:</u> "Match <u>else</u>-clause to the closest <u>if</u> without an <u>else</u>-clause already." <u>Solution:</u>

Stmt → <u>if</u> Expr <u>then</u> Stmt

→ <u>if</u> Expr <u>then</u> WithElse <u>else</u> Stmt

→ ...Other Stmt Forms...

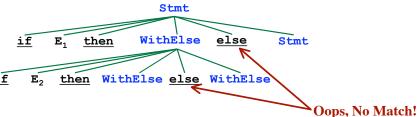
WithElse → <u>if</u> Expr <u>then</u> WithElse <u>else</u> WithElse

→ ...Other Stmt Forms...

Any Stmt occurring between <u>then</u> and <u>else</u> must have an <u>else</u>.

i.e., the Stmt must not end with "then Stmt".

<u>Interpretation #1:</u> if E_1 then (if E_2 then S_1) else S_2



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Syntax Analysis - Part 1

Top-Down Parsing

Find a left-most derivation

Find (build) a parse tree

Start building from the root and work down...

As we search for a derivation...

Must make choices:

- Which rule to use
- Where to use it

May run into problems!

Option 1:

"Backtracking"

Made a bad decision

Back up and try another choice

Option 2:

Always make the right choice.

Never have to backtrack: "Predictive Parser"

Possible for some grammars (LL Grammars)

May be able to fix some grammars (but not others)

- Eliminate Left Recursion
- Left-Factor the Rules



Input: aabbde

S

1. $S \rightarrow Aa$ 2. $\rightarrow Ce$ 3. $A \rightarrow aaB$

4. → aaba

5. $B \rightarrow bbb$

6. $C \rightarrow aaD$

7. $D \rightarrow bbd$

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Syntax Analysis - Part 1

Backtracking

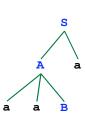




- 1. $S \rightarrow Aa$
- 2. → Ce
- 3. $A \rightarrow aaB$
- 4. → aaba5. B → bbb
- 6. $C \rightarrow aaD$
- 7. $D \rightarrow bbd$



Input: aabbde



1. $S \rightarrow Aa$ 2. $\rightarrow Ce$

3. $A \rightarrow aaB$

4. → aaba

5. $B \rightarrow bbb$

6. $C \rightarrow aaD$

7. $D \rightarrow bbd$

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Syntax Analysis - Part 1

Backtracking

Input: aabbde



1. $S \rightarrow Aa$

2. → Ce

3. $A \rightarrow aaB$

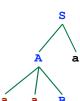
4. → aaba5. B → bbb

6. $C \rightarrow aaD$

7. $D \rightarrow bbd$



Input: aabbde



1. $S \rightarrow Aa$ 2. → Ce 3. $A \rightarrow aaB$

→ aaba

5. $B \rightarrow bbb$

6. $C \rightarrow aaD$

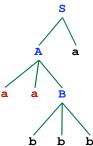
7. $D \rightarrow bbd$

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Syntax Analysis - Part 1

Backtracking

Input: aabbde



1. $S \rightarrow Aa$

→ Ce 2.

3. $A \rightarrow aaB$

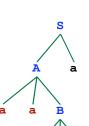
→ aaba 5. $B \rightarrow bbb$

6. $C \rightarrow aaD$

7. $D \rightarrow bbd$



Input: aabbde



1. $S \rightarrow Aa$ 2. $\rightarrow Ce$

3. $A \rightarrow aaB$

4. → aaba5. B → bbb

6. **C** → **aa**D

7. $D \rightarrow bbd$

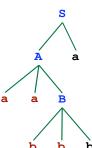
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Syntax Analysis - Part 1

Backtracking

Input: aabbde



1. $S \rightarrow Aa$

2. → Ce

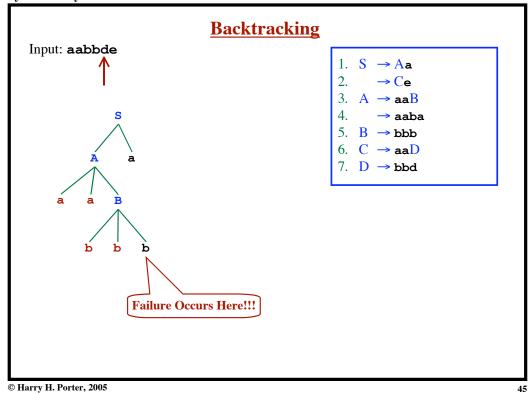
3. $A \rightarrow aaB$

→ aaba

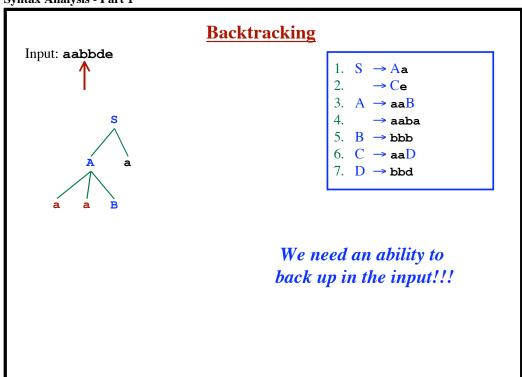
5. $B \rightarrow bbb$

6. $C \rightarrow aaD$

7. $D \rightarrow bbd$



Syntax Analysis - Part 1





Input: aabbde



1. $S \rightarrow Aa$ 2. $\rightarrow Ce$

3. A → **aa**B

4. → aaba

5. $B \rightarrow bbb$

6. $C \rightarrow aaD$

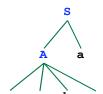
7. $D \rightarrow bbd$

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Syntax Analysis - Part 1

Backtracking

Input: aabbde



1. $S \rightarrow Aa$

2. → Ce

3. $A \rightarrow aaB$

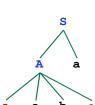
4. → aaba5. B → bbb

6. $C \rightarrow aaD$

7. $D \rightarrow bbd$



Input: aabbde



1. $S \rightarrow Aa$

2. → Ce

3. $A \rightarrow aaB$

4. → aaba5. B → bbb

6. C → aaD

7. $D \rightarrow bbd$

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Syntax Analysis - Part 1

Backtracking

Input: aabbde



1. $S \rightarrow Aa$

2. → **Ce**

3. $A \rightarrow aaB$

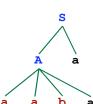
4. → aaba5. B → bbb

6. $C \rightarrow aaD$

7. $D \rightarrow bbd$



Input: aabbde



1. $S \rightarrow Aa$ 2. $\rightarrow Ce$

3. A → aaB4. → aaba

5. $B \rightarrow bbb$

6. $C \rightarrow aaD$

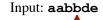
7. $D \rightarrow bbd$

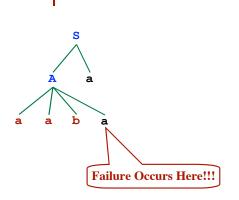
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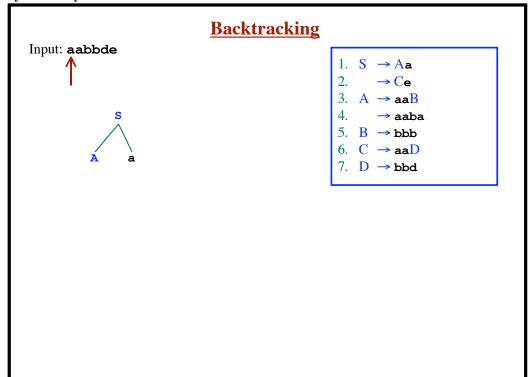
Syntax Analysis - Part 1

Backtracking





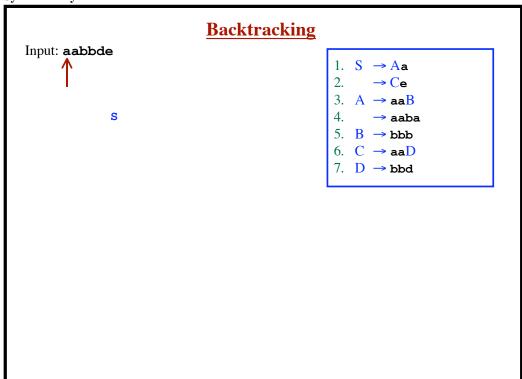
- 1. $S \rightarrow Aa$
- 2. → Ce
- 3. $A \rightarrow aaB$
- 4. → aaba
- 5. $B \rightarrow bbb$
- 6. $C \rightarrow aaD$
- 7. $D \rightarrow bbd$

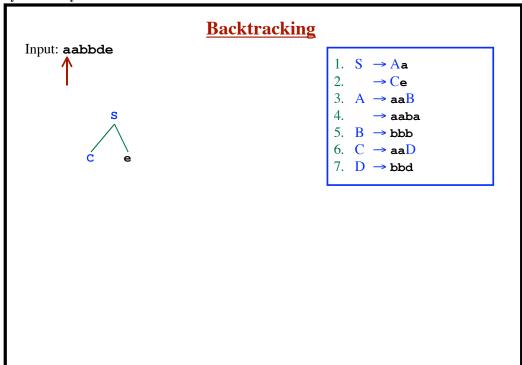


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Syntax Analysis - Part 1

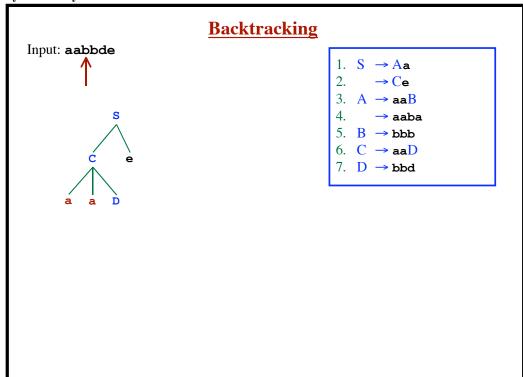




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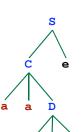
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Syntax Analysis - Part 1





Input: aabbde



1. $S \rightarrow Aa$

2. → Ce

3. $A \rightarrow aaB$

4. → aaba

5. $B \rightarrow bbb$

6. $C \rightarrow aaD$ 7. $D \rightarrow bbd$

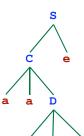
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Syntax Analysis - Part 1

Backtracking

Input: aabbde



1. $S \rightarrow Aa$

2. → **Ce**

3. $A \rightarrow aaB$

4. → aaba5. B → bbb

6. $C \rightarrow aaD$

7. $D \rightarrow bbd$

Predictive Parsing

Will never backtrack!

Requirement:

For every rule:

```
A \to \alpha_1 + \alpha_2 + \alpha_3 + \dots + \alpha_N
```

We must be able to choose the correct alternative by looking only at the next symbol May peek ahead to the next symbol (token).

Example

$$A \rightarrow aB$$
 $\Rightarrow cD$
 $\Rightarrow E$

Assuming a,c ∉ FIRST (E)

Example

```
Stmt → <u>if</u> Expr ...

→ <u>for</u> LValue ...

→ <u>while</u> Expr ...

→ <u>return</u> Expr ...

→ <u>ID</u> ...
```

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Syntax Analysis - Part 1

Predictive Parsing

LL(1) Grammars

Can do predictive parsing

Can select the right rule

Looking at only the next 1 input symbol

Predictive Parsing

LL(1) Grammars

Can do predictive parsing
Can select the right rule

Looking at only the next 1 input symbol

LL(k) Grammars

Can do predictive parsing Can select the right rule

Looking at only the next **k** input symbols

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*C*1

Syntax Analysis - Part 1

Predictive Parsing

LL(1) Grammars

Can do predictive parsing

Can select the right rule

Looking at only the next 1 input symbol

LL(k) Grammars

Can do predictive parsing

Can select the right rule

Looking at only the next k input symbols

Techniques to modify the grammar:

- Left Factoring
- Removal of Left Recursion

Predictive Parsing

LL(1) Grammars

Can do predictive parsing

Can select the right rule

Looking at only the next 1 input symbol

LL(k) Grammars

Can do predictive parsing

Can select the right rule

Looking at only the next k input symbols

Techniques to modify the grammar:

- Left Factoring
- Removal of Left Recursion

But these may not be enough!

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Syntax Analysis - Part 1

Predictive Parsing

LL(1) Grammars

Can do predictive parsing

Can select the right rule

Looking at only the next 1 input symbol

LL(k) Grammars

Can do predictive parsing

Can select the right rule

Looking at only the next k input symbols

Techniques to modify the grammar:

- Left Factoring
- Removal of Left Recursion

But these may not be enough!

LL(k) Language

Can be described with an LL(k) grammar.

Left-Factoring

Problem:

```
Stmt → <u>if</u> Expr <u>then</u> Stmt <u>else</u> Stmt

→ <u>if</u> Expr <u>then</u> Stmt

→ OtherStmt
```

With predictive parsing, we need to know which rule to use! (While looking at just the next token)

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Syntax Analysis - Part 1

Left-Factoring

Problem:

```
Stmt → <u>if</u> Expr <u>then</u> Stmt <u>else</u> Stmt

→ <u>if</u> Expr <u>then</u> Stmt

→ OtherStmt
```

With predictive parsing, we need to know which rule to use!
(While looking at just the next token)

Solution:

```
Stmt \rightarrow <u>if</u> Expr <u>then</u> Stmt ElsePart

\rightarrow OtherStmt

ElsePart \rightarrow <u>else</u> Stmt | ε
```

Left-Factoring

Problem:

Stmt → <u>if</u> Expr <u>then</u> Stmt <u>else</u> Stmt

→ <u>if</u> Expr <u>then</u> Stmt

→ OtherStmt

With predictive parsing, we need to know which rule to use! (While looking at just the next token)

Solution:

Stmt $\rightarrow \underline{if}$ Expr \underline{then} Stmt ElsePart \rightarrow OtherStmt

ElsePart \rightarrow else Stmt | ϵ

General Approach:

Before: A $\rightarrow \alpha\beta_1 \mid \alpha\beta_2 \mid \alpha\beta_3 \mid ... \mid \delta_1 \mid \delta_2 \mid \delta_3 \mid ...$

After: $A \rightarrow \alpha C \mid \delta_1 \mid \delta_2 \mid \delta_3 \mid ...$ $C \rightarrow \beta_1 \mid \beta_2 \mid \beta_3 \mid ...$

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Syntax Analysis - Part 1

Left-Factoring

Problem:

Stmt
$$\rightarrow$$
 if Expr then Stmt else Stmt

A \rightarrow if Expr then Stmt ϵ β_1
 \rightarrow OtherStmt

 β_2

With predictive parsing, we need to know which rule to use!
(While looking at just the next token)

Solution:

Stmt
$$\rightarrow \underline{if}$$
 Expr \underline{then} Stmt ElsePart \rightarrow OtherStmt

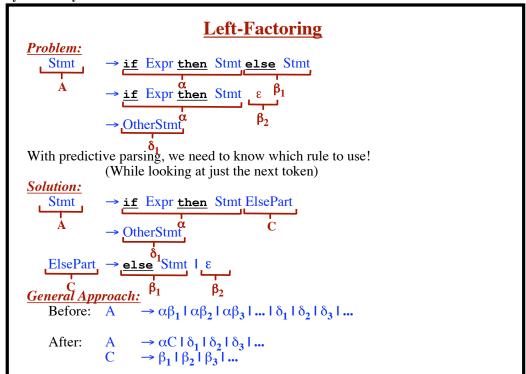
ElsePart \rightarrow <u>else</u> Stmt | ϵ

General Approach:

Before: A
$$\rightarrow \alpha\beta_1 \mid \alpha\beta_2 \mid \alpha\beta_3 \mid ... \mid \delta_1 \mid \delta_2 \mid \delta_3 \mid ...$$

After: A
$$\rightarrow \alpha C \mid \delta_1 \mid \delta_2 \mid \delta_3 \mid ...$$

C $\rightarrow \beta_1 \mid \beta_2 \mid \beta_3 \mid ...$



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Syntax Analysis - Part 1

Left Recursion

Whenever

 $A \Rightarrow^+ A\alpha$

Simplest Case: Immediate Left Recursion

Given:

$$A \rightarrow A\alpha \mid \beta$$

Transform into:

$$A \rightarrow \beta A'$$

 $A' \rightarrow \alpha A' \mid \epsilon$ where A' is a new nonterminal

More General (but still immediate):

$$A \rightarrow A\alpha_1 + A\alpha_2 + A\alpha_3 + \dots + \beta_1 + \beta_2 + \beta_3 + \dots$$

Transform into:

$$\begin{split} \mathbf{A} &\rightarrow \beta_1 \mathbf{A}^{\scriptscriptstyle{\dagger}} \mid \; \beta_2 \mathbf{A}^{\scriptscriptstyle{\dagger}} \mid \; \beta_3 \mathbf{A}^{\scriptscriptstyle{\dagger}} \mid \; \dots \\ \mathbf{A}^{\scriptscriptstyle{\dagger}} &\rightarrow \alpha_1 \mathbf{A}^{\scriptscriptstyle{\dagger}} \mid \; \alpha_2 \mathbf{A}^{\scriptscriptstyle{\dagger}} \mid \; \alpha_3 \mathbf{A}^{\scriptscriptstyle{\dagger}} \mid \; \dots \; \mid \; \epsilon \end{split}$$

Left Recursion in More Than One Step

Example:

 $S \to A\underline{\mathbf{f}} \ | \ \underline{\mathbf{b}}$ $A \to A\underline{\mathbf{c}} \mid S\underline{\mathbf{d}} \mid \underline{\mathbf{e}}$ Is A left recursive? Yes.

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Syntax Analysis - Part 1

Left Recursion in More Than One Step

Example:

```
S \rightarrow A\underline{\mathbf{f}} \mid \underline{\mathbf{b}}
A \rightarrow A\underline{c} \mid S\underline{d} \mid \underline{e}
```

Is A left recursive? Yes.

Is S left recursive?

Example:

```
S \rightarrow A\underline{\mathbf{f}} \mid \underline{\mathbf{b}}
A \rightarrow A\underline{\mathbf{c}} \mid S\underline{\mathbf{d}} \mid \underline{\mathbf{e}}
```

Is A left recursive? Yes.

Is S left recursive? Yes, but not immediate left recursion. S \Rightarrow A $\underline{\mathbf{f}}$ \Rightarrow S $\underline{\mathbf{df}}$

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Syntax Analysis - Part 1

Left Recursion in More Than One Step

Example:

```
S \rightarrow A\underline{\mathbf{f}} \mid \underline{\mathbf{b}}
A \rightarrow A\underline{\mathbf{c}} \mid S\underline{\mathbf{d}} \mid \underline{\mathbf{e}}
```

Is A left recursive? Yes.

Is S left recursive? Yes, but not immediate left recursion. S \Rightarrow Af \Rightarrow Sdf

Approach:

Look at the rules for S only (ignoring other rules)... No left recursion.

Example:

$$S \rightarrow A\underline{\mathbf{f}} \mid \underline{\mathbf{b}}$$

$$A \rightarrow A\underline{\mathbf{c}} \mid S\underline{\mathbf{d}} \mid \underline{\mathbf{e}}$$

Is A left recursive? Yes.

Is S left recursive? Yes, but not immediate left recursion. $S \Rightarrow Af \Rightarrow Sdf$

Approach:

Look at the rules for S only (ignoring other rules)... No left recursion. Look at the rules for A...

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Syntax Analysis - Part 1

Left Recursion in More Than One Step

Example:

```
S \to A\underline{\mathbf{f}} \mid \underline{\mathbf{b}}
A \to A\underline{\mathbf{c}} \mid S\underline{\mathbf{d}} \mid \underline{\mathbf{e}}
```

Is A left recursive? Yes.

Is S left recursive? Yes, but not immediate left recursion. $S \Rightarrow Af \Rightarrow Sdf$

Approach:

Look at the rules for S only (ignoring other rules)... No left recursion. Look at the rules for A...

Do any of A's rules start with S? Yes.

$$A \rightarrow S\underline{d}$$

Example:

$$S \rightarrow A\underline{\mathbf{f}} \mid \underline{\mathbf{b}}$$

$$A \rightarrow A\underline{\mathbf{c}} \mid S\underline{\mathbf{d}} \mid \underline{\mathbf{e}}$$

Is A left recursive? Yes.

Is S left recursive? Yes, but not immediate left recursion. $S \Rightarrow Af \Rightarrow Sdf$

Approach:

Look at the rules for S only (ignoring other rules)... No left recursion.

Look at the rules for A...

Do any of A's rules start with S? Yes.

 $A \rightarrow Sd$

Get rid of the S. Substitute in the righthand sides of S.

 $A \rightarrow A\underline{fd} \mid \underline{bd}$

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Syntax Analysis - Part 1

Left Recursion in More Than One Step

Example:

$$S \to A\underline{\mathbf{f}} \mid \underline{\mathbf{b}}$$

$$A \to A\underline{\mathbf{c}} \mid S\underline{\mathbf{d}} \mid \underline{\mathbf{e}}$$

Is A left recursive? Yes.

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Approach:

Look at the rules for S only (ignoring other rules)... No left recursion.

Look at the rules for A...

Do any of A's rules start with S? Yes.

$$A \rightarrow Sd$$

Get rid of the S. Substitute in the righthand sides of S.

$$A \rightarrow Afd \mid bd$$

The modified grammar:

$$S \to A\underline{\mathbf{f}} \mid \underline{\mathbf{b}}$$

$$A \to A\underline{\mathbf{c}} \mid A\underline{\mathbf{fd}} \mid \underline{\mathbf{bd}} \mid \underline{\mathbf{e}}$$

Example:

$$S \to A\underline{\mathbf{f}} \mid \underline{\mathbf{b}}$$

$$A \to A\underline{\mathbf{c}} \mid S\underline{\mathbf{d}} \mid \underline{\mathbf{e}}$$

Is A left recursive? Yes.

Is S left recursive? Yes, but not immediate left recursion. $S \Rightarrow Af \Rightarrow Sdf$

Approach:

Look at the rules for S only (ignoring other rules)... No left recursion.

Look at the rules for A...

Do any of A's rules start with S? Yes.

 $A \rightarrow Sd$

Get rid of the S. Substitute in the righthand sides of S.

$$A \rightarrow A\underline{fd} \mid \underline{bd}$$

The modified grammar:

$$S \rightarrow A\underline{\mathbf{f}} \mid \underline{\mathbf{b}}$$

$$A \rightarrow A\underline{c} \mid A\underline{fd} \mid \underline{bd} \mid \underline{e}$$

Now eliminate immediate left recursion involving A.

$$S \to A\underline{\mathbf{f}} \mid \underline{\mathbf{b}}$$
$$A \to \underline{\mathbf{bd}} A' \mid \underline{\mathbf{e}} A'$$

 $A' \rightarrow \underline{\mathbf{c}} A' \mid \underline{\mathbf{fd}} A' \mid \underline{\mathbf{\epsilon}}$

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Syntax Analysis - Part 1

Left Recursion in More Than One Step

The Original Grammar:

$$S \rightarrow A\underline{\mathbf{f}} \mid \underline{\mathbf{b}}$$

$$A \rightarrow A\underline{\mathbf{c}} \mid S\underline{\mathbf{d}} \mid \underline{\mathbf{e}}$$

Left Recursion in More Than One Step The Original Grammar: $S \rightarrow Af \mid b$ $A \rightarrow Ac \mid Sd \mid Be$ $B \rightarrow Ag \mid Sh \mid k$ Assume there are still more nonterminals; Look at the next one...

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Syntax Analysis - Part 1

Left Recursion in More Than One Step The Original Grammar: $S \rightarrow A\underline{f} \mid \underline{b}$ $A \rightarrow A\underline{c} \mid S\underline{d} \mid B\underline{e}$ $B \rightarrow A\underline{g} \mid S\underline{h} \mid \underline{k}$ So Far: $S \rightarrow A\underline{f} \mid \underline{b}$ $A \rightarrow \underline{b}\underline{d}A' \mid \underline{B}\underline{e}A'$ $A' \rightarrow \underline{c}A' \mid \underline{f}\underline{d}A' \mid \underline{\epsilon}$

Left Recursion in More Than One Step The Original Grammar: $S \rightarrow A\underline{f} \mid \underline{b}$ $A \rightarrow A\underline{c} \mid S\underline{d} \mid B\underline{e}$ $B \rightarrow A\underline{g} \mid S\underline{h} \mid \underline{k}$ So Far: $S \rightarrow A\underline{f} \mid \underline{b}$ $A \rightarrow \underline{b}\underline{d}A' \mid B\underline{e}A'$ $A' \rightarrow \underline{c}A' \mid \underline{f}\underline{d}A' \mid \underline{\epsilon}$ $B \rightarrow A\underline{g} \mid S\underline{h} \mid \underline{k}$ © Harry H. Porter, 2005

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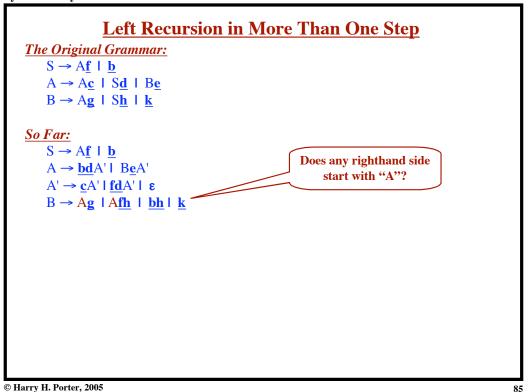
Syntax Analysis - Part 1

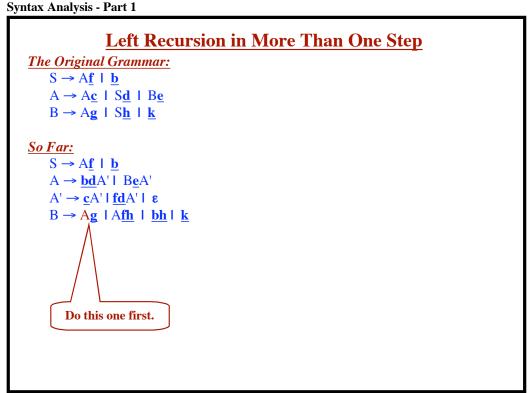
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Left Recursion in More Than One Step

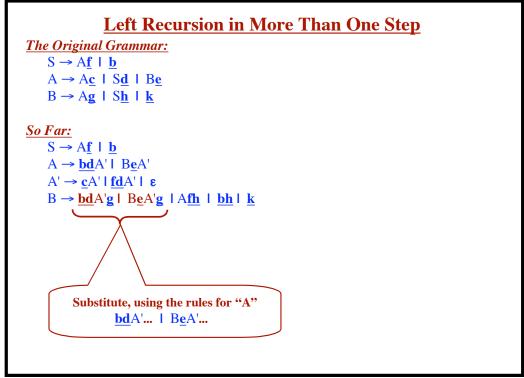
The Original Grammar:
S \rightarrow A\underline{f} \mid \underline{b}
A \rightarrow A\underline{c} \mid S\underline{d} \mid B\underline{e}
B \rightarrow A\underline{g} \mid S\underline{h} \mid \underline{k}

So Far:
S \rightarrow A\underline{f} \mid \underline{b}
A \rightarrow \underline{b}\underline{d}A' \mid B\underline{e}A'
A' \rightarrow \underline{c}A' \mid \underline{f}\underline{d}A' \mid \underline{\epsilon}
B \rightarrow A\underline{g} \mid A\underline{f}\underline{h} \mid \underline{b}\underline{h} \mid \underline{k}

Substitute, using the rules for "S"
A\underline{f}... \mid \underline{b}...
```







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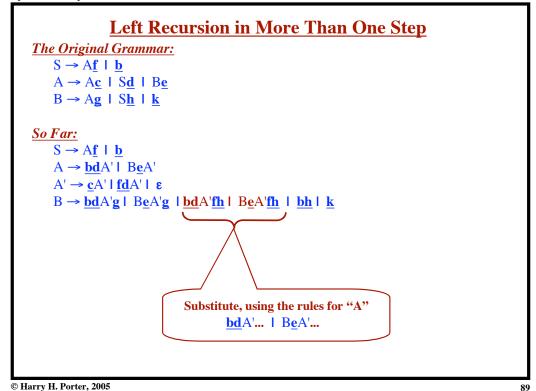
Syntax Analysis - Part 1

```
Left Recursion in More Than One Step

The Original Grammar:
S \rightarrow A\underline{f} \mid \underline{b}
A \rightarrow A\underline{c} \mid S\underline{d} \mid B\underline{e}
B \rightarrow A\underline{g} \mid S\underline{h} \mid \underline{k}

So Far:
S \rightarrow A\underline{f} \mid \underline{b}
A \rightarrow \underline{b}\underline{d}A' \mid B\underline{e}A'
A' \rightarrow \underline{c}A' \mid \underline{f}\underline{d}A' \mid \epsilon
B \rightarrow \underline{b}\underline{d}A'\underline{g} \mid B\underline{e}A'\underline{g} \mid A\underline{f}\underline{h} \mid \underline{b}\underline{h} \mid \underline{k}

Do this one next.
```



```
Syntax Analysis - Part 1

Left Recursion in More Than One Step

The Original Grammar:

S \rightarrow Af \mid b
A \rightarrow Ac \mid Sd \mid Be
B \rightarrow Ag \mid Sh \mid k

So Far:

S \rightarrow Af \mid b
A \rightarrow bdA' \mid BeA'
A' \rightarrow cA' \mid fdA' \mid \epsilon
B \rightarrow bdA'g \mid BeA'g \mid bdA'fh \mid BeA'fh \mid bh \mid k

Finally, eliminate any immediate Left recursion involving "B"
```

$\begin{array}{c} \textbf{Left Recursion in More Than One Step} \\ \hline \textbf{The Original Grammar:} \\ \hline S \rightarrow A\underline{f} \mid \underline{b} \\ \hline A \rightarrow A\underline{c} \mid S\underline{d} \mid B\underline{e} \\ \hline B \rightarrow A\underline{g} \mid S\underline{h} \mid \underline{k} \\ \hline \\ \textbf{So Far:} \\ \hline S \rightarrow A\underline{f} \mid \underline{b} \\ \hline A \rightarrow \underline{b}\underline{d}A' \mid B\underline{e}A' \\ \hline A' \rightarrow \underline{c}A' \mid \underline{f}\underline{d}A' \mid \underline{\epsilon} \\ \hline B \rightarrow \underline{b}\underline{d}A'\underline{g}B' \mid \underline{b}\underline{d}A'\underline{f}\underline{h}B' \mid \underline{b}\underline{h}B' \mid \underline{k}B' \\ \hline B' \rightarrow \underline{e}A'\underline{g}B' \mid \underline{e}A''\underline{f}\underline{h}B' \mid \underline{\epsilon} \\ \end{array}$

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Syntax Analysis - Part 1

```
Left Recursion in More Than One Step

The Original Grammar:

S \rightarrow A\underline{f} \mid \underline{b}
A \rightarrow A\underline{c} \mid S\underline{d} \mid B\underline{e} \mid C
B \rightarrow A\underline{g} \mid S\underline{h} \mid \underline{k}
C \rightarrow B\underline{k}\underline{m}A \mid AS \mid \underline{j}

So Far:

S \rightarrow A\underline{f} \mid \underline{b}
A \rightarrow \underline{b}\underline{d}A' \mid B\underline{e}A' \mid CA'
A' \rightarrow \underline{c}A' \mid f\underline{d}A' \mid \varepsilon
B \rightarrow \underline{b}\underline{d}A'\underline{g}B' \mid \underline{b}\underline{d}A'\underline{f}\underline{h}B' \mid \underline{b}\underline{h}B' \mid \underline{k}B' \mid CA'\underline{g}B' \mid CA'\underline{f}\underline{h}B'
B' \rightarrow \underline{e}A'\underline{g}B' \mid \underline{e}A'\underline{f}\underline{h}B' \mid \varepsilon
```

Algorithm to Eliminate Left Recursion Assume the nonterminals are ordered A_1 , A_2 , A_3 ,... (In the example: S, A, B) for each nonterminal A_i (for i = 1 to N) do for each nonterminal A_j (for j = 1 to i-1) do Let $A_j \rightarrow \beta_1 \mid \beta_2 \mid \beta_3 \mid ... \mid \beta_N$ be all the rules for A_j if there is a rule of the form $A_i \rightarrow A_j \alpha$ then replace it by $A_i \rightarrow \beta_1 \alpha \mid \beta_2 \alpha \mid \beta_3 \alpha \mid ... \mid \beta_N \alpha$ endIf endFor Eliminate immediate left recursion A_1 among the A_i rules

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endFor

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Inner Loop

A_i ← Outer Loop

Syntax Analysis - Part 1

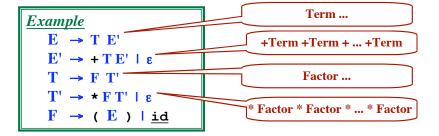
Table-Driven Predictive Parsing Algorithm

Assume that the grammar is LL(1)

i.e., Backtracking will never be needed

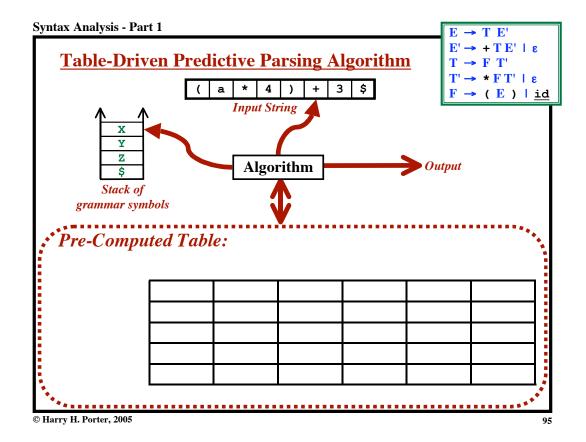
Always know which righthand side to choose (with one look-ahead)

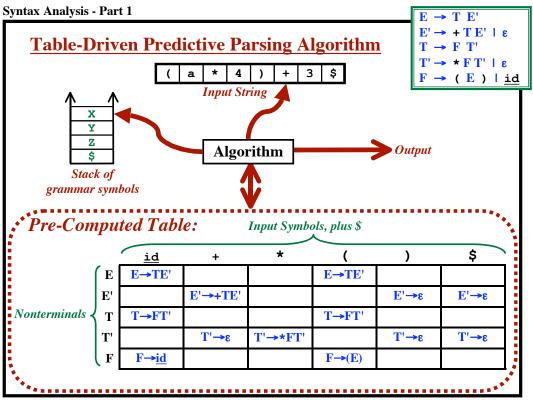
- No Left Recursion
- · Grammar is Left-Factored.

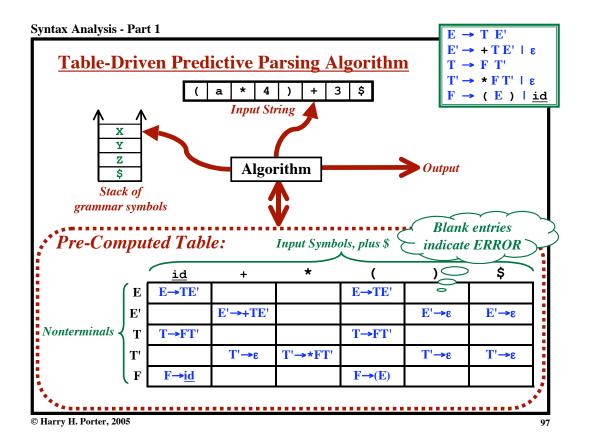


Step 1: From grammar, construct table.

Step 2: Use table to parse strings.

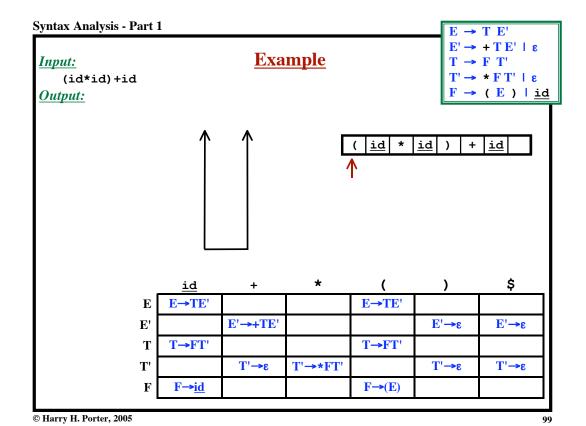


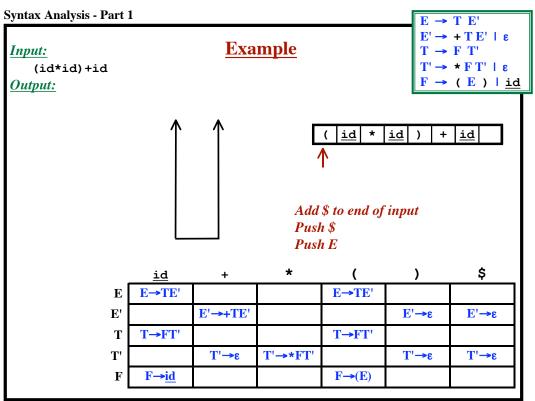


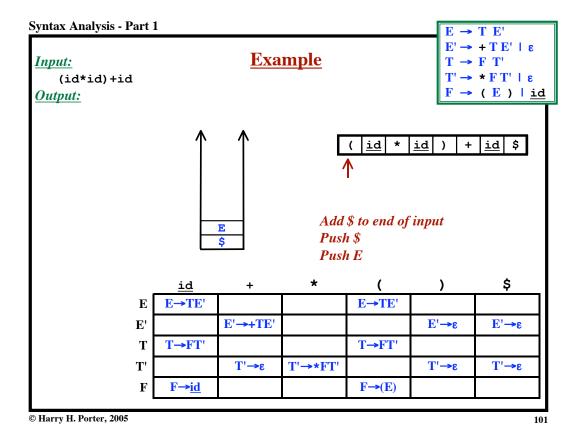


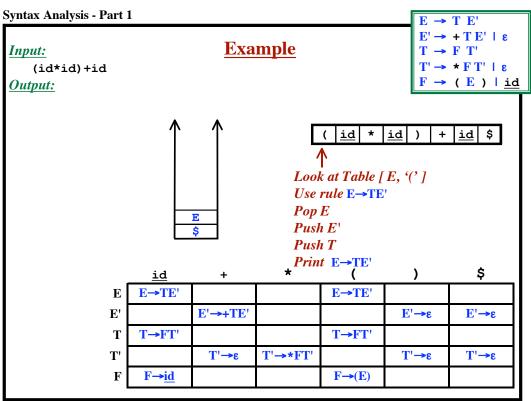
Syntax Analysis - Part 1

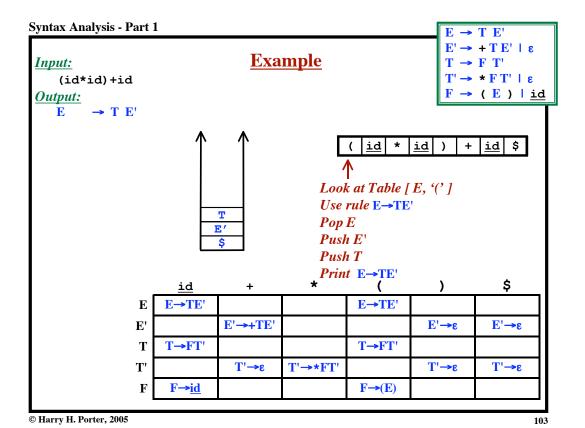
```
Predictive Parsing Algorithm
Set input ptr to first symbol; Place $ after last input symbol
Push $
Push S
repeat
  X = stack top
  a = current input symbol
  \underline{if} X is a terminal \underline{or} X = $ then
    if X == a then
       Pop stack
       Advance input ptr
     <u>else</u>
       Error
    endIf
  elseIf Table[X,a] contains a rule then // call it X \rightarrow Y_1 Y_2 \dots Y_K
    Pop stack
    Push Y<sub>K</sub>
     . . .
                                                                           Y_1
    Push Y2
                                                                           Y,
    Push Y<sub>1</sub>
    Print ("X \rightarrow Y<sub>1</sub> Y<sub>2</sub> ... Y<sub>K</sub>")
  else // Table[X,a] is blank
                                                                           Y,
    Syntax Error
                                                  Α
                                                                           Α
  endIf
until X == $
```

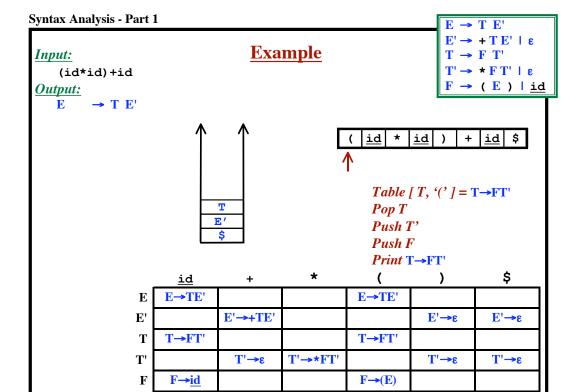


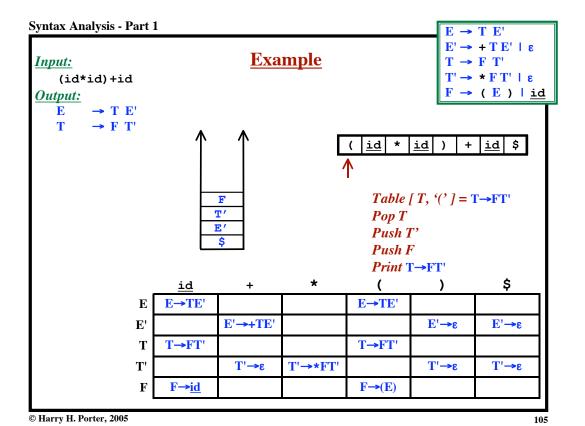


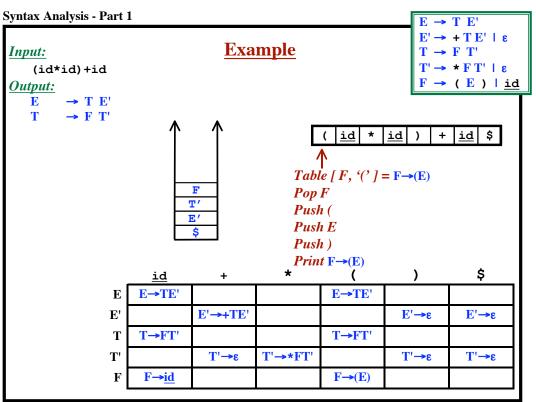


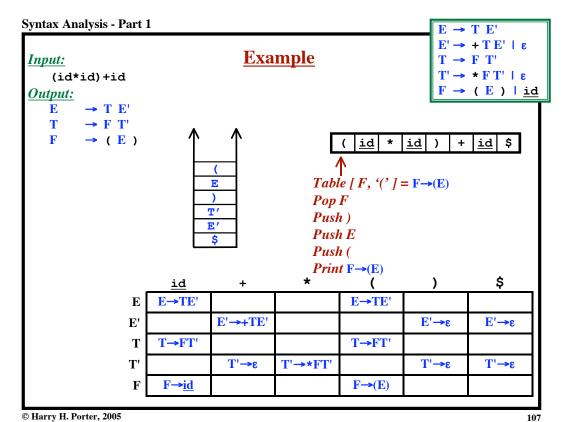


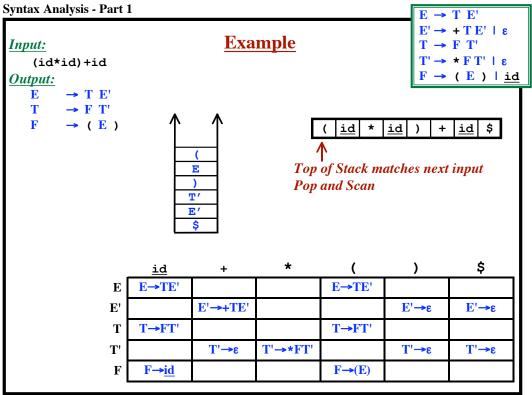


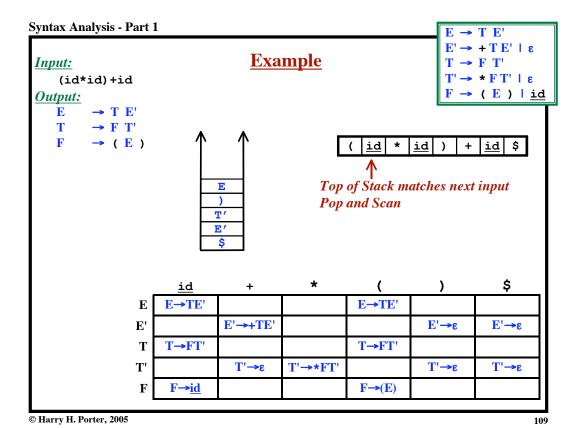


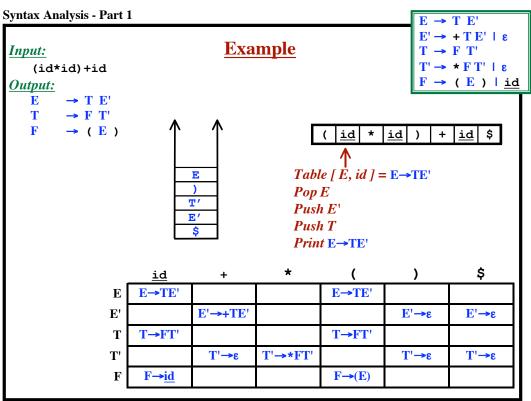


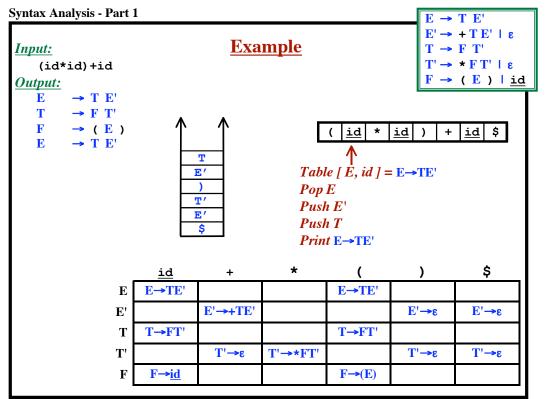


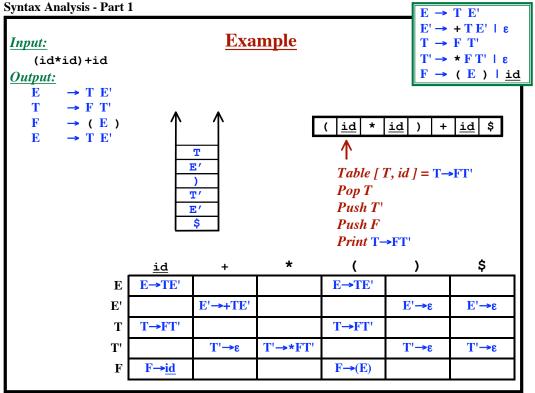


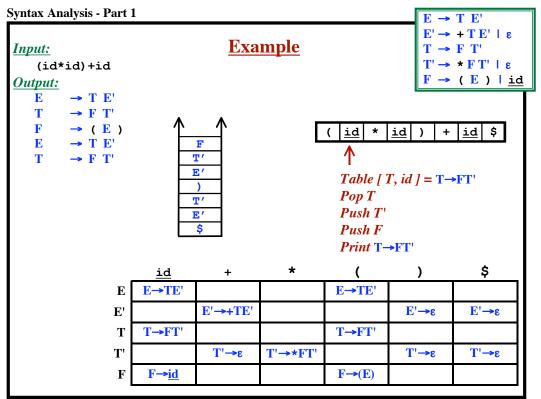




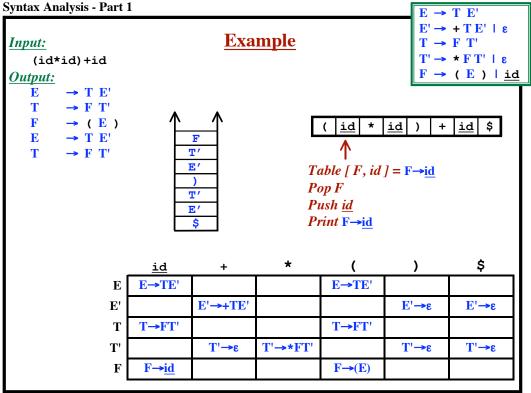


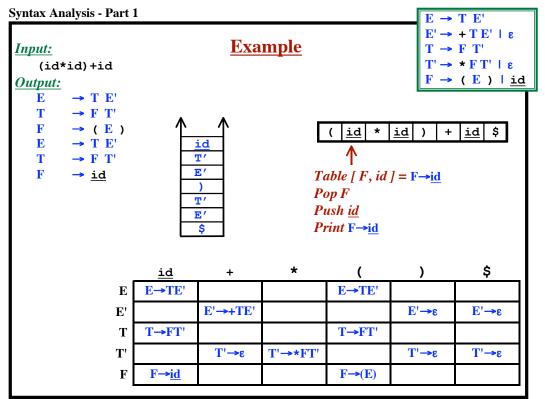


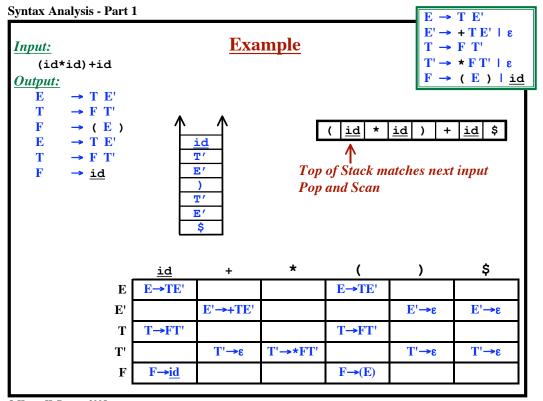


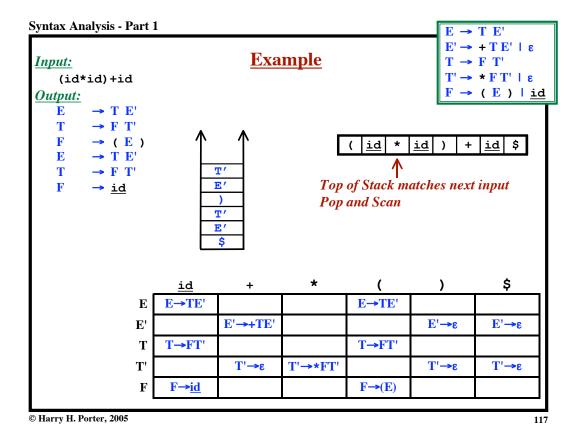


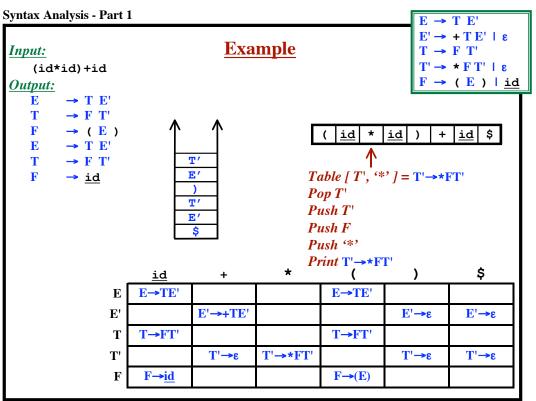
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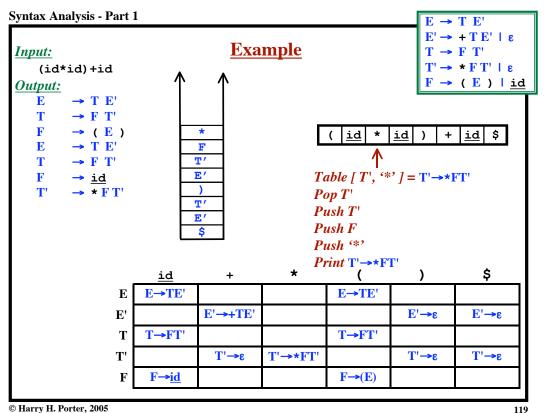




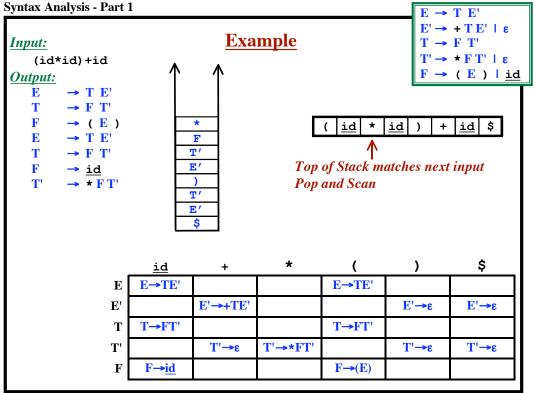


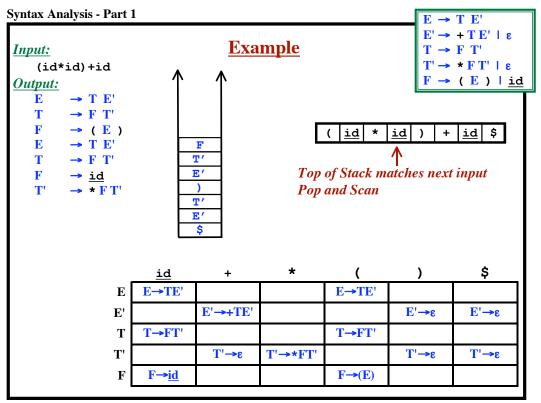




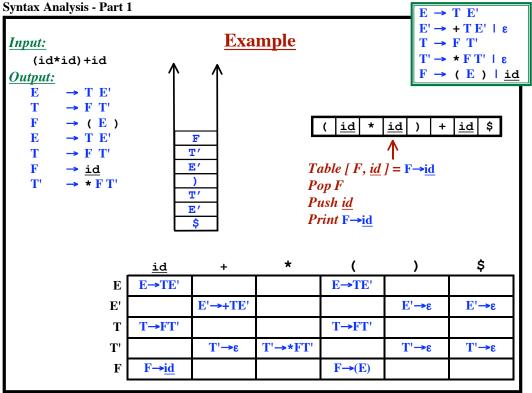


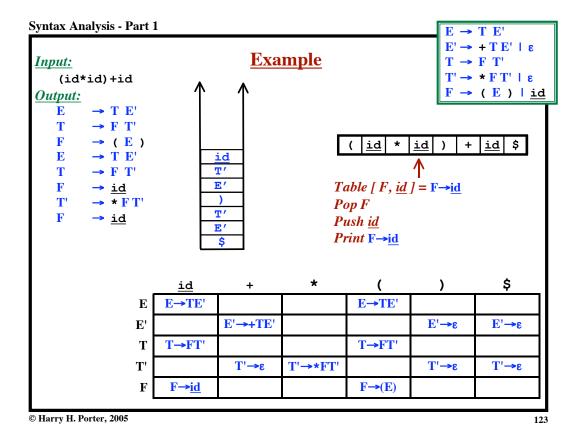


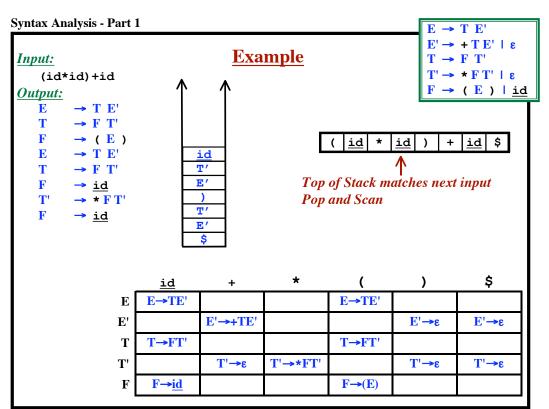


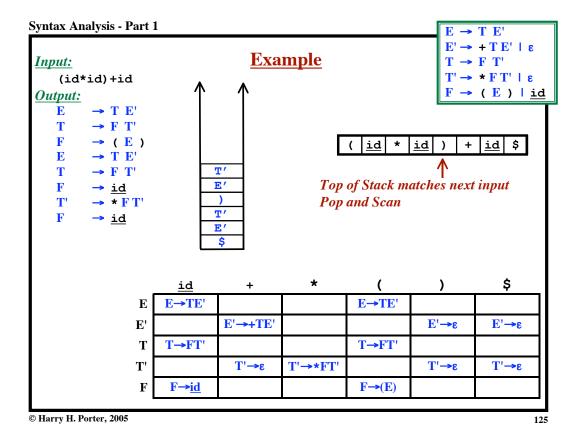


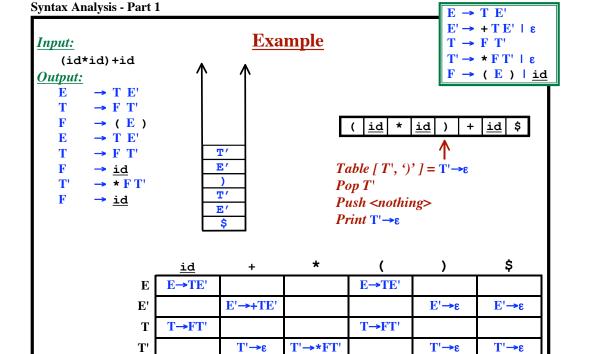








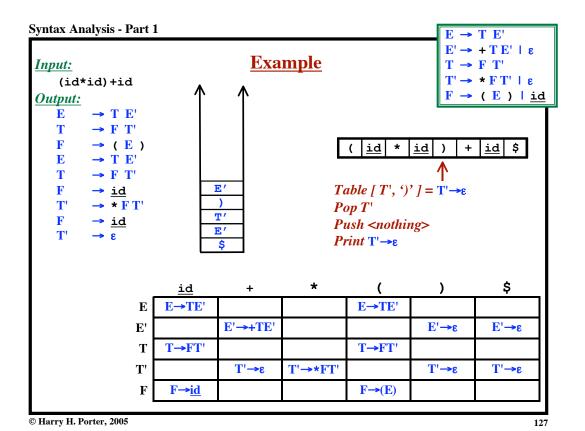


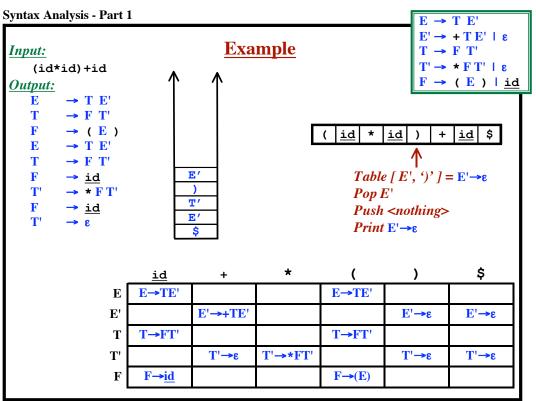


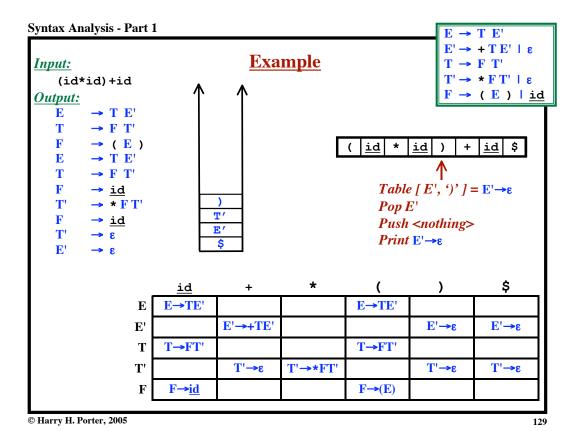
 $F \rightarrow (E)$

 \mathbf{F}

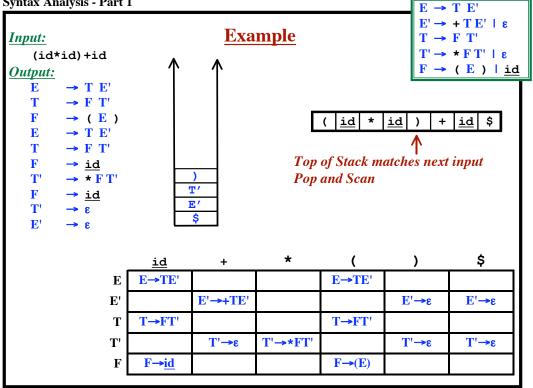
F→<u>id</u>

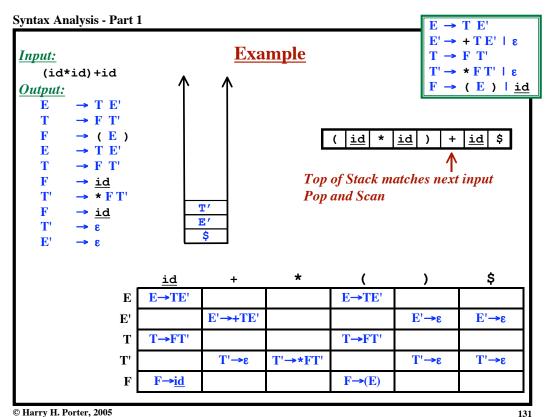




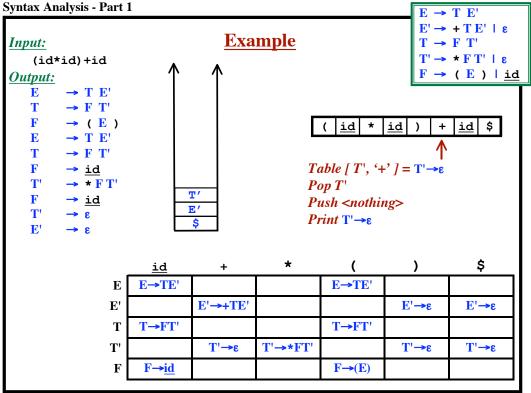


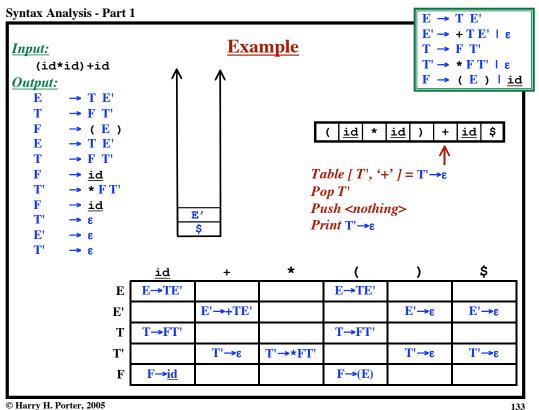


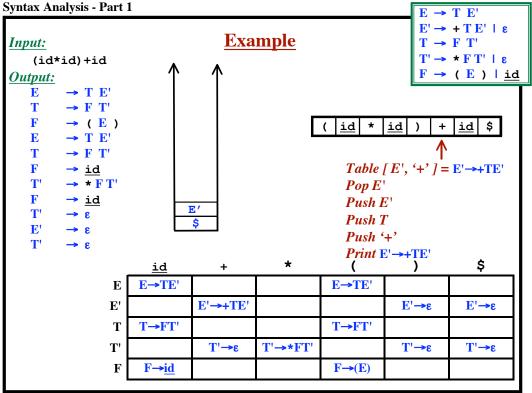


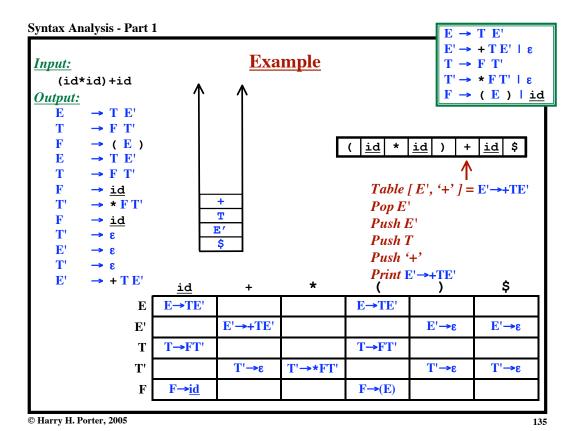


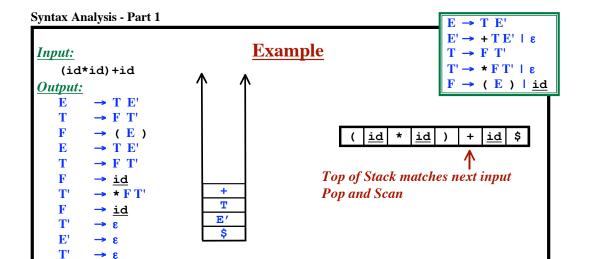












E→TE'

T→FT'

 $F \rightarrow (E)$

Ε'→ε

T'→ε

\$

Ε'→ε

<u>T</u>'→ε

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T'→*FT'

E'→+TE'

T'→ε

 \mathbf{E}'

→ + T E'

Е Е'

T

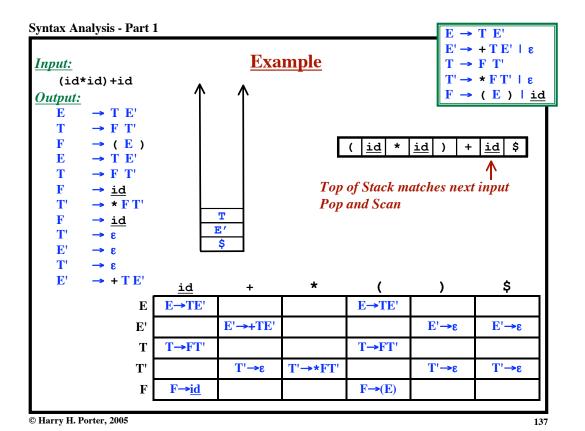
T'

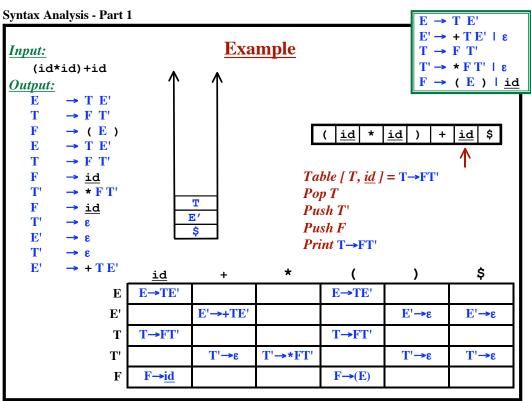
 \mathbf{F}

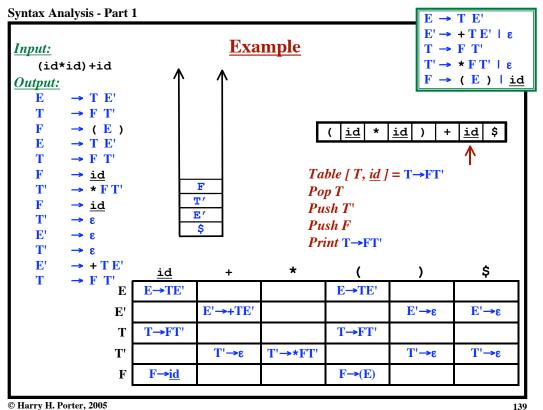
<u>id</u> E→TE'

T→FT'

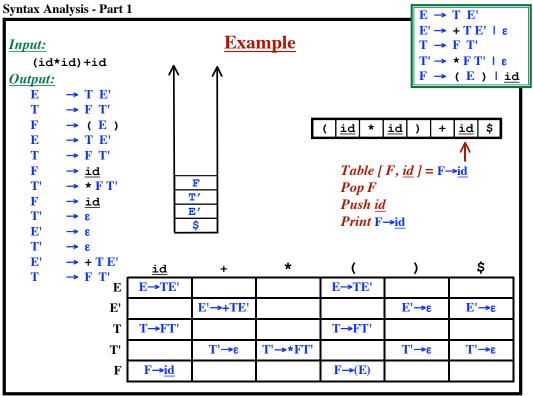
F→<u>id</u>

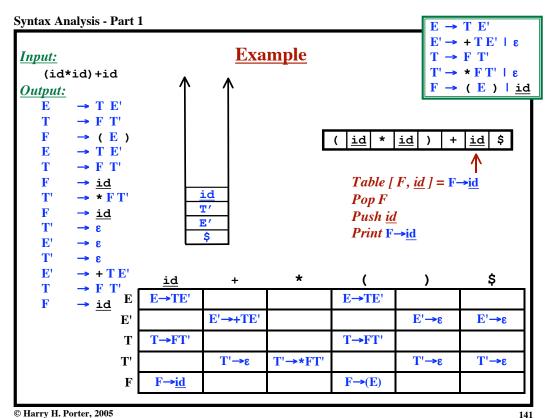




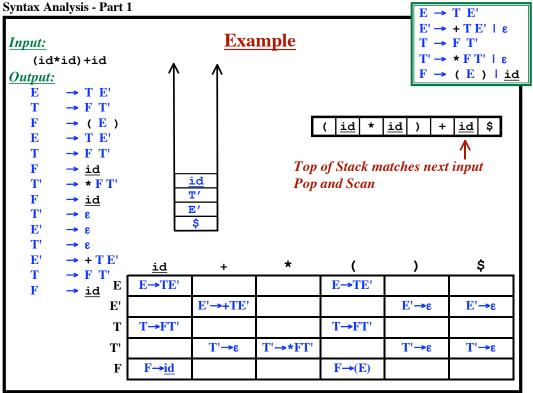


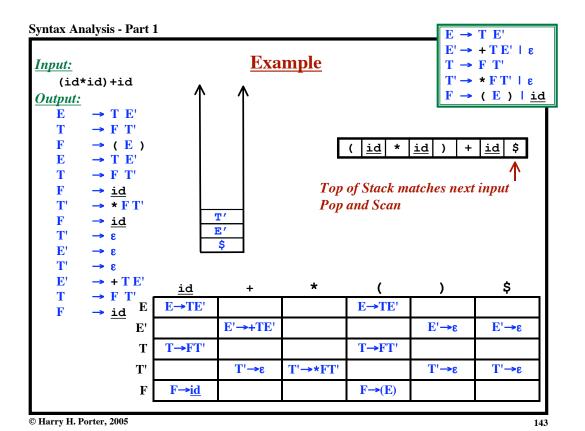


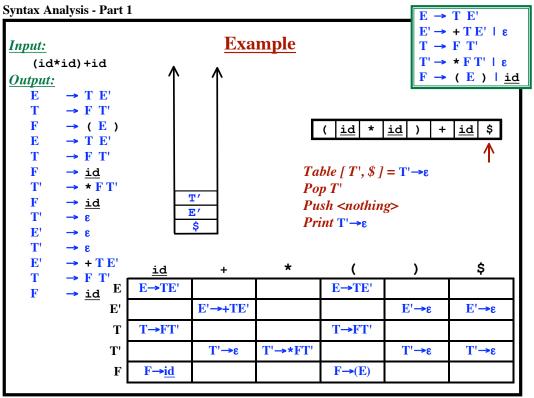


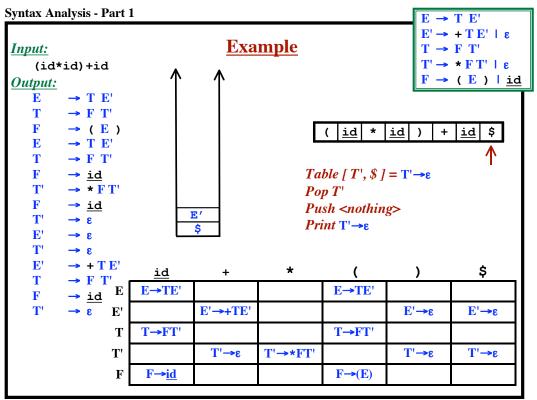






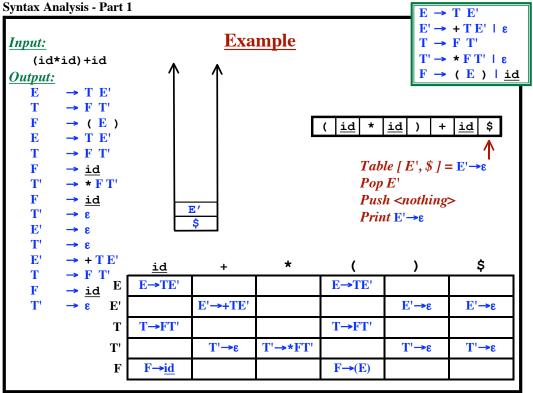


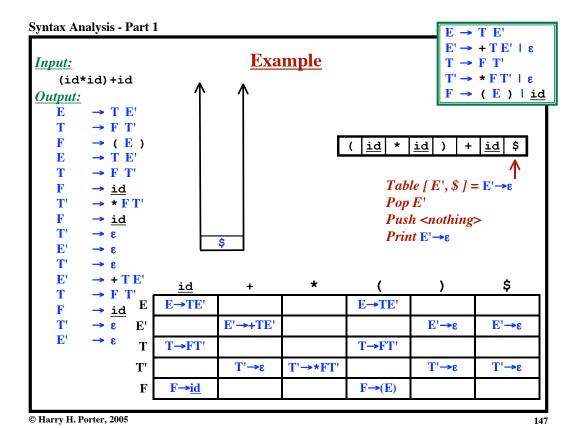


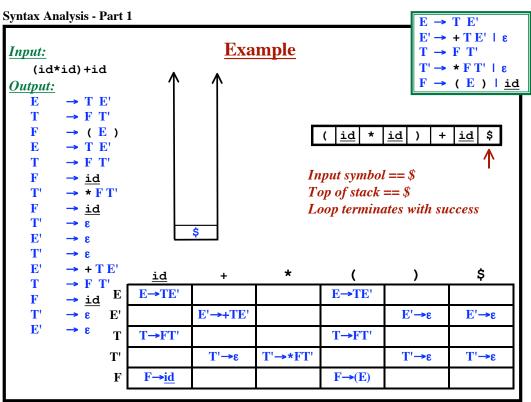


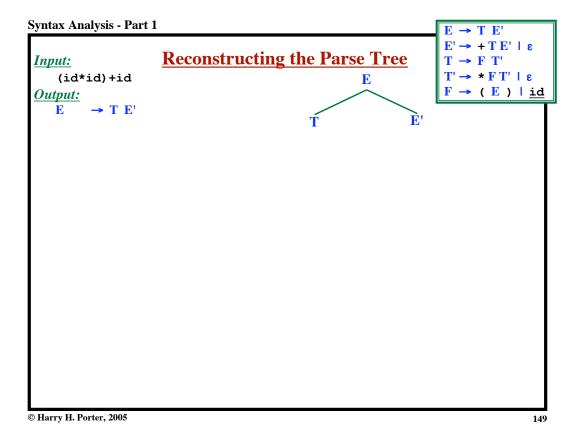


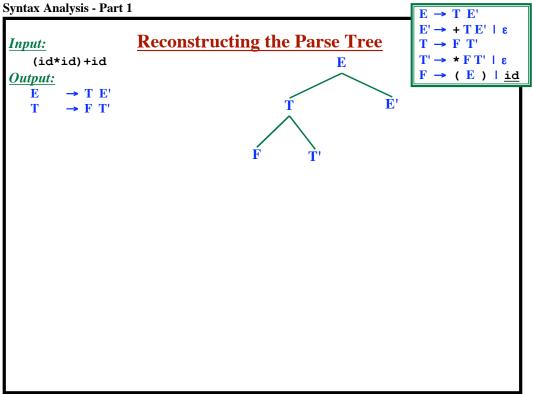
145

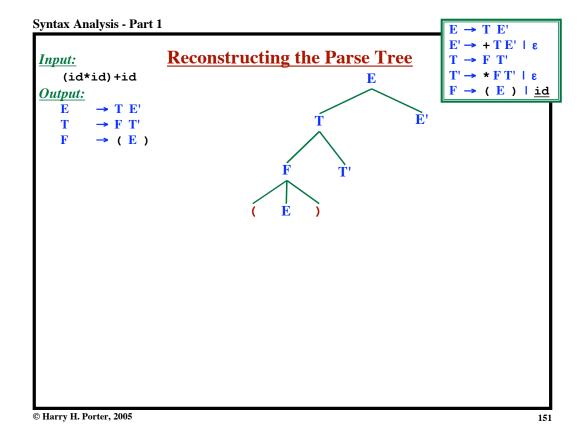


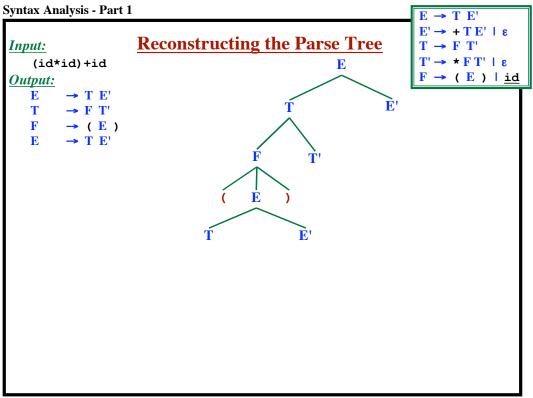


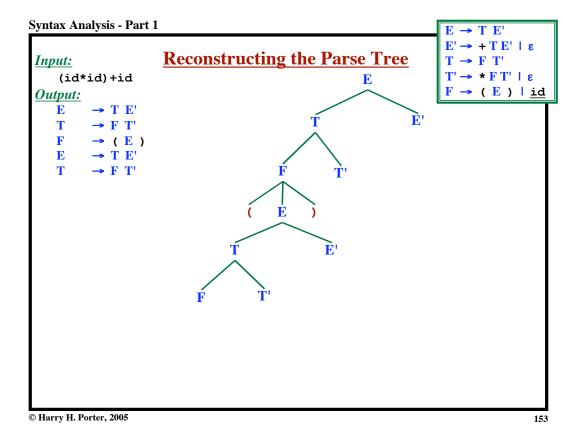


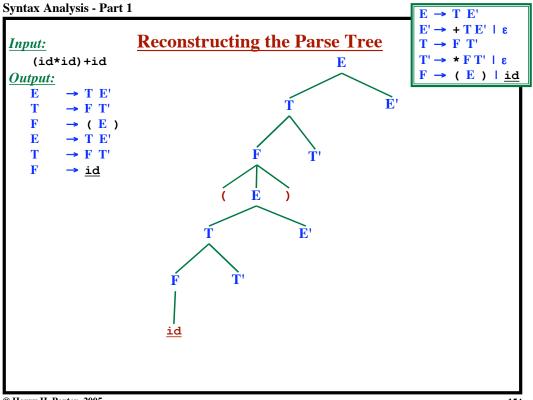


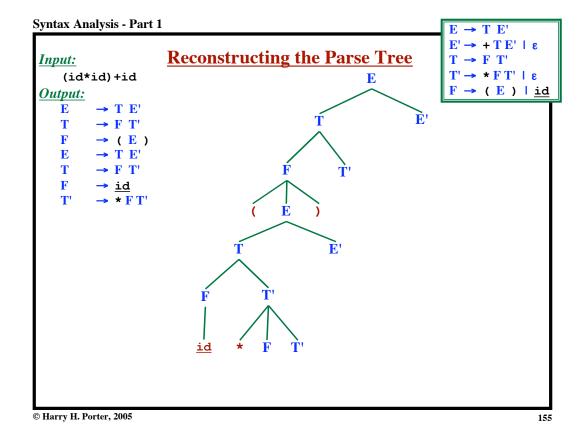


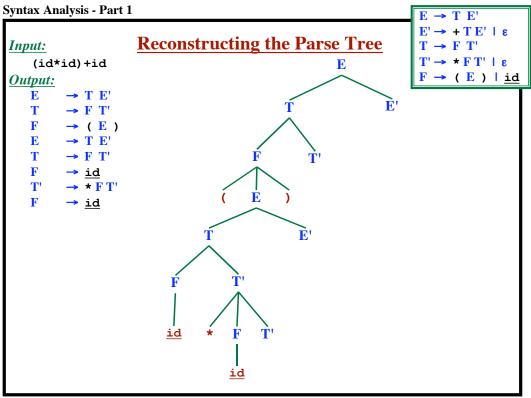


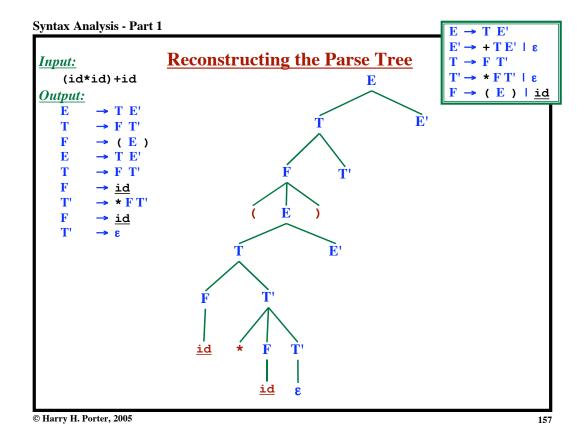


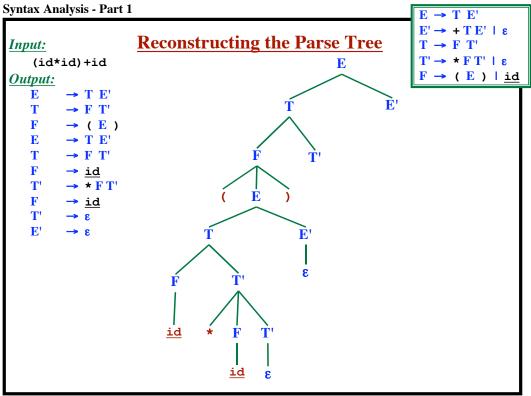


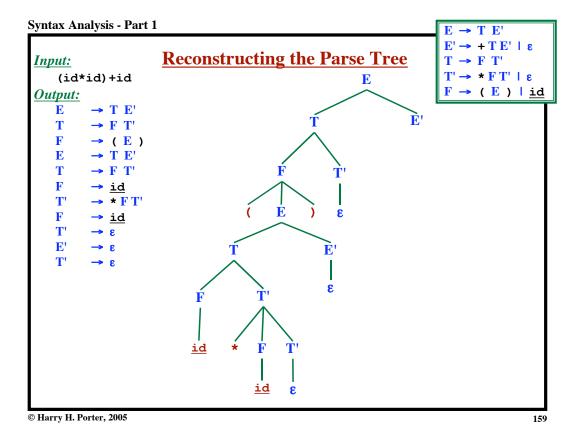


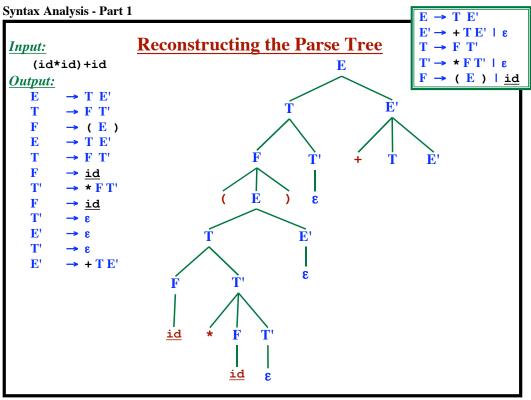


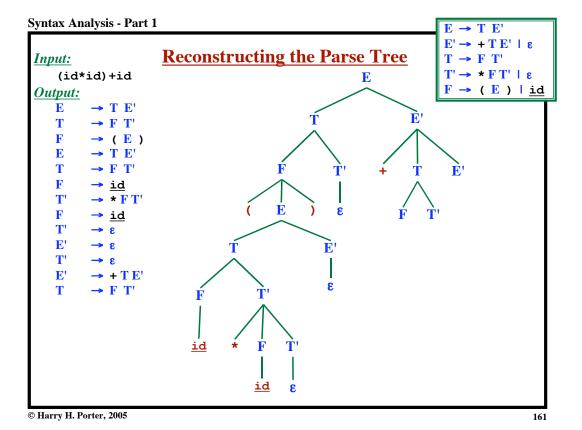


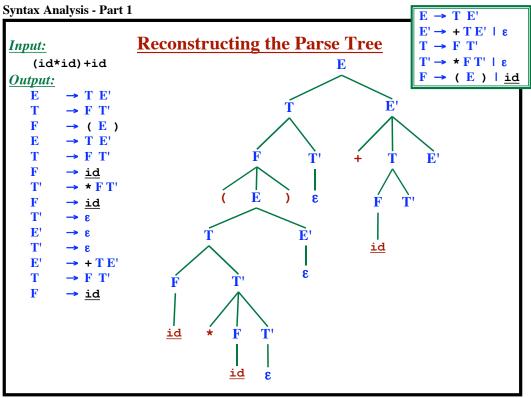


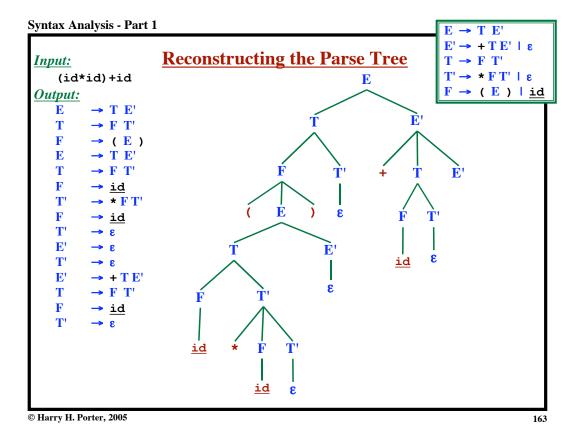


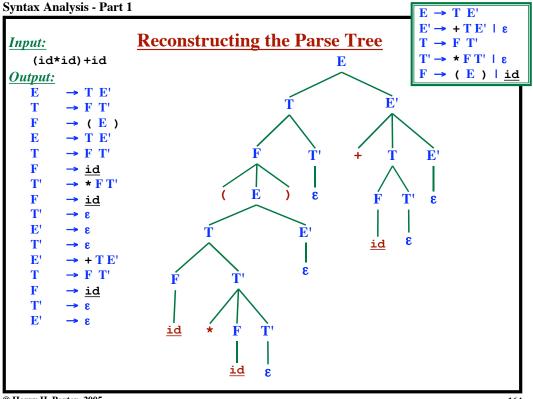












```
Syntax Analysis - Part 1
                                                                                                        E \rightarrow T E'
                                                                                                        E' \rightarrow + T E' \mid \epsilon
                                 Reconstructing the Parse Tree
                                                                                                        T \rightarrow F T'
 Input:
       (id*id)+id
                                                                                                        T' \rightarrow * F T' \mid \epsilon
                                      Leftmost Derivation:
                                                                                                        \mathbf{F} \rightarrow (\mathbf{E}) \mid \underline{\mathbf{id}}
 Output:
                                      \mathbf{E}
               → T E'
      \mathbf{E}
                                      T E'
      \mathbf{T}
               → F T'
                                      F T' E'
      \mathbf{F}
               → ( E )
                                      (E) T'E'
      \mathbf{E}
               → T E'
                                      (TE') T'E'
      \mathbf{T}
               → F T'
                                      (F T'E') T'E'
               <u>→ id</u>
                                      (<u>id</u> T'E') T'E'
               → * F T'
      T'
                                      (\underline{id}*FT'E')T'E'
               → <u>id</u>
                                      (id*idT'E')T'E'
                                      ( <u>id</u> * <u>id</u> E') T'E'
                                      ( <u>id</u> * <u>id</u> ) T' E'
                                      ( <u>id</u> * <u>id</u> ) <u>E</u>'
               → + T E'
      \mathbf{E}'
                                      (\underline{id} * \underline{id}) + TE'
      T
               → F T'
                                      (\underline{id} * \underline{id}) + F T' E'
               → id
                                      (\underline{id} * \underline{id}) + \underline{id} T'E'
      T'
                                      (id*id)+idE'
                                       (\underline{id} * \underline{id}) + \underline{id}
```

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Syntax Analysis - Part 1

"FIRST" Function

Let $\boldsymbol{\alpha}$ be a string of symbols (terminals and nonterminals)

Define:

```
FIRST (\alpha) = The set of terminals that could occur first in any string derivable from \alpha = { \mathbf{a} \mid \alpha \Rightarrow^* \mathbf{aw}, plus \mathbf{\epsilon} if \alpha \Rightarrow^* \mathbf{\epsilon} }
```

"FIRST" Function

Let α be a string of symbols (terminals and nonterminals)

Define:

FIRST (α) = The set of terminals that could occur first in any string derivable from α = { a | $\alpha \Rightarrow *$ aw, plus ϵ if $\alpha \Rightarrow * \epsilon$ }

Example:

```
E \rightarrow T E'
E' \rightarrow + T E' \mid \varepsilon
T \rightarrow F T'
T' \rightarrow * F T' \mid \varepsilon
F \rightarrow (E) \mid \underline{id}
```

FIRST(F) = ?

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Syntax Analysis - Part 1

"FIRST" Function

Let α be a string of symbols (terminals and nonterminals)

Define:

FIRST (α) = The set of terminals that could occur first in any string derivable from α = { $\mathbf{a} \mid \alpha \Rightarrow^* \mathbf{a} \mathbf{w}$, plus $\mathbf{\epsilon}$ if $\alpha \Rightarrow^* \mathbf{\epsilon}$ }

Example:

$$E \rightarrow T E'$$

$$E' \rightarrow + T E' \mid \epsilon$$

$$T \rightarrow F T'$$

$$T' \rightarrow * F T' \mid \epsilon$$

$$F \rightarrow (E) \mid \underline{id}$$

 $FIRST(F) = \{ (, \underline{id}) \}$ FIRST(T') = ?

"FIRST" Function

Let $\boldsymbol{\alpha}$ be a string of symbols (terminals and nonterminals)

Define:

FIRST (α) = The set of terminals that could occur first in any string derivable from α = { a | $\alpha \Rightarrow *$ aw, plus ϵ if $\alpha \Rightarrow * \epsilon$ }

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```
E \rightarrow T E'
E' \rightarrow + T E' \mid \varepsilon
T \rightarrow F T'
T' \rightarrow * F T' \mid \varepsilon
F \rightarrow (E) \mid \underline{id}
```

```
FIRST (F) = \{ (, \underline{id}) \}
FIRST (T') = \{ *, \epsilon \}
FIRST (T) = ?
```

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Syntax Analysis - Part 1

"FIRST" Function

Let α be a string of symbols (terminals and nonterminals)

Define:

FIRST (α) = The set of terminals that could occur first in any string derivable from α = { $\mathbf{a} \mid \alpha \Rightarrow^* \mathbf{aw}$, plus $\mathbf{\epsilon}$ if $\alpha \Rightarrow^* \mathbf{\epsilon}$ }

Example:

$$E \rightarrow T E'$$

$$E' \rightarrow +T E' \mid \epsilon$$

$$T \rightarrow F T'$$

$$T' \rightarrow *F T' \mid \epsilon$$

$$F \rightarrow (E) \mid \underline{id}$$

```
FIRST (F) = { (, \underline{id} }

FIRST (T') = { *, \varepsilon}

FIRST (T) = { (, \underline{id} }

FIRST (E') = ?
```

"FIRST" Function

Let $\boldsymbol{\alpha}$ be a string of symbols (terminals and nonterminals)

Define:

FIRST (α) = The set of terminals that could occur first in any string derivable from α = { $a \mid \alpha \Rightarrow^* aw$, plus ε if $\alpha \Rightarrow^* \varepsilon$ }

Example:

```
E \rightarrow T E'
E' \rightarrow + T E' \mid \varepsilon
T \rightarrow F T'
T' \rightarrow * F T' \mid \varepsilon
F \rightarrow (E) \mid \underline{id}
```

```
FIRST (F) = { (, \underline{id} }

FIRST (T') = { *, \varepsilon}

FIRST (T) = { (, \underline{id} }

FIRST (E') = { +, \varepsilon}

FIRST (E) = ?
```

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Syntax Analysis - Part 1

"FIRST" Function

Let α be a string of symbols (terminals and nonterminals)

Define:

FIRST (α) = The set of terminals that could occur first in any string derivable from α = { $\mathbf{a} \mid \alpha \Rightarrow^* \mathbf{aw}$, plus $\mathbf{\epsilon}$ if $\alpha \Rightarrow^* \mathbf{\epsilon}$ }

Example:

```
E \rightarrow T E'
E' \rightarrow + T E' \mid \epsilon
T \rightarrow F T'
T' \rightarrow * F T' \mid \epsilon
F \rightarrow (E) \mid \underline{id}
```

```
FIRST (F) = { (, \underline{id} }

FIRST (T') = { *, \varepsilon}

FIRST (T) = { (, \underline{id} }

FIRST (E') = { +, \varepsilon}

FIRST (E) = { (, \underline{id} }
```

To Compute the "FIRST" Function

For all symbols X in the grammar...

if X is a terminal then

FIRST(X) = { X }

if X → ε is a rule then

add ε to FIRST(X)

if x → Y₁ Y₂ Y₃ ... Y_K is a rule then

if a ∈ FIRST(Y₁) then

add a to FIRST(X)

if ε ∈ FIRST(Y₁) and a ∈ FIRST(Y₂) then

add a to FIRST(X)

if ε ∈ FIRST(Y₁) and ε ∈ FIRST(Y₂) and a ∈ FIRST(Y₃) then

add a to FIRST(X)

...

if ε ∈ FIRST(Y₁) for all Y₁ then

add ε to FIRST(X)

Repeat until nothing more can be added to any sets.

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Syntax Analysis - Part 1

```
To Compute the FIRST(X_1X_2X_3...X_N)
```

```
Result = {}
Add everything in FIRST(X_1), except \varepsilon, to result
```

```
To Compute the FIRST(X_1X_2X_3...X_N)

Result = {}
Add everything in FIRST(X_1), except \varepsilon, to result if \varepsilon \in \text{FIRST}(X_1) then
Add everything in FIRST(X_2), except \varepsilon, to result

endIf
```

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Syntax Analysis - Part 1

To Compute the FIRST($X_1X_2X_3...X_N$) Result = {} Add everything in FIRST(X_1), except ϵ , to result if $\epsilon \in \text{FIRST}(X_1)$ then Add everything in FIRST(X_2), except ϵ , to result if $\epsilon \in \text{FIRST}(X_2)$ then Add everything in FIRST(X_3), except ϵ , to result $\frac{\text{endIf}}{\text{endIf}}$

To Compute the FIRST($X_1X_2X_3...X_N$) Result = {} Add everything in FIRST(X_1), except ϵ , to result if $\epsilon \in \text{FIRST}(X_1)$ then Add everything in FIRST(X_2), except ϵ , to result if $\epsilon \in \text{FIRST}(X_2)$ then Add everything in FIRST(X_3), except ϵ , to result if $\epsilon \in \text{FIRST}(X_3)$ then Add everything in FIRST(X_4), except ϵ , to result $\frac{\text{endIf}}{\text{endIf}}$

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Syntax Analysis - Part 1

```
To Compute the FIRST(X_1X_2X_3...X_N)

Result = {}
Add everything in FIRST(X_1), except E, to result if E \in FIRST(X_1) then
Add everything in FIRST(X_2), except E, to result if E \in FIRST(X_2) then
Add everything in FIRST(E \in FIRST(X_3)), except E \in FIRST(X_3) then
Add everything in FIRST(E \in FIRST(X_3)), except E \in FIRST(X_3) then
Add everything in FIRST(E \in FIRST(X_3)) then
Add everything in FIRST(E \in FIRST(X_3)), except E \in FIRST(X_3), except E \in FIRST(X_3),
```

```
To Compute the FIRST(X_1X_2X_3...X_N)
 Result = {}
Add everything in FIRST(X_1), except \varepsilon, to result
 \underline{\text{if}} \ \epsilon \in \text{FIRST}(\underline{X}_1) \ \underline{\text{then}}
                      Add everything in FIRST(X_2), except \varepsilon, to result
                      \underline{if} \in FIRST(X_2) \underline{then}
                                            Add everything in FIRST(X_3), except \varepsilon, to result
                                              \underline{if} \in FIRST(X_3) \underline{then}
                                                                    Add everything in FIRST(X_4), except \epsilon, to result
                                                                                           \underline{\text{if}} \ \epsilon \in \text{FIRST}(X_{N-1}) \ \underline{\text{then}}
                                                                                                                 Add everything in FIRST(X_{_{\rm N}})\,, except \epsilon, to result
                                                                                                                   \underline{\text{if}}~\epsilon \in \text{FIRST}(\underline{X}_N)~\underline{\text{then}}
                                                                                                                                      // Then X_1 \Rightarrow \tilde{x} \in \overline{X_2} \Rightarrow \tilde{x} \in X_3 \Rightarrow \tilde{x} \in X_N \Rightarrow
                                                                                                                                        Add & to result
                                                                                                                   endIf
                                                                                           endIf
                                              endIf
                         endIf
 <u>endIf</u>
```

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Syntax Analysis - Part 1

```
To Compute FOLLOW(A<sub>i</sub>) for all Nonterminals in the Grammar add $ to FOLLOW(S) repeat

if A \rightarrow \alpha B\beta is a rule then
add every terminal in FIRST(\beta) except $ to FOLLOW(B)

if FIRST(\beta) contains $ then
add everything in FOLLOW(A) to FOLLOW(B)

endIf
endIf
if A \rightarrow \alpha B is a rule then
add everything in FOLLOW(A) to FOLLOW(B)

endIf
until We cannot add anything more
```

Previously computed FIRST sets...

```
FIRST (F) = \{ (, id) \}
FIRST (T') = \{ *, \epsilon \}
FIRST (T) = \{ (, id) \}
FIRST (E') = \{ +, \epsilon \}
FIRST (E) = \{ (, id) \}
```

```
E \rightarrow T E'
E' \rightarrow + T E' \mid \epsilon
T \rightarrow F T'
T' \rightarrow * F T' \mid \epsilon
F \rightarrow (E) \mid \underline{id}
```

The FOLLOW sets...

```
FOLLOW (E) = { ? 

FOLLOW (E') = { ? 

FOLLOW (T) = { ? 

FOLLOW (T') = { ? 

FOLLOW (F) = { ? }
```

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Syntax Analysis - Part 1

Example of FOLLOW Computation

Previously computed FIRST sets...

```
FIRST (F) = \{ (, \underline{id}) \}

FIRST (T') = \{ *, \epsilon \}

FIRST (T) = \{ (, \underline{id}) \}

FIRST (E') = \{ *, \epsilon \}

FIRST (E) = \{ (, \underline{id}) \}
```

$$E \rightarrow T E'$$

$$E' \rightarrow +T E' \mid \epsilon$$

$$T \rightarrow F T'$$

$$T' \rightarrow *F T' \mid \epsilon$$

$$F \rightarrow (E) \mid \underline{id}$$

The FOLLOW sets...

```
FOLLOW (E) = {
FOLLOW (E') = {
FOLLOW (T') = {
FOLLOW (F) = {
```

Add \$ to FOLLOW(S)

Previously computed FIRST sets...

```
FIRST (F) = \{ (, id) \}
FIRST (T') = \{ *, \epsilon \}
FIRST (T) = \{ (, id) \}
FIRST (E') = \{ +, \epsilon \}
FIRST (E) = \{ (, id) \}
```

```
E \rightarrow T E'
E' \rightarrow + T E' \mid \epsilon
T \rightarrow F T'
T' \rightarrow * F T' \mid \epsilon
F \rightarrow (E) \mid \underline{id}
```

The FOLLOW sets...

```
FOLLOW (E) = { $,
FOLLOW (E') = {
FOLLOW (T') = {
FOLLOW (F) = {
```

Add \$ to FOLLOW(S)

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Syntax Analysis - Part 1

Example of FOLLOW Computation

Previously computed FIRST sets...

```
FIRST (F) = \{ (, id) \}
FIRST (T') = \{ *, \epsilon \}
FIRST (T) = \{ (, id) \}
FIRST (E') = \{ +, \epsilon \}
FIRST (E) = \{ (, id) \}
```

$$E \rightarrow T E'$$

$$E' \rightarrow +T E' \mid \epsilon$$

$$T \rightarrow F T'$$

$$T' \rightarrow *F T' \mid \epsilon$$

$$F \rightarrow (E) \mid \underline{id}$$

The FOLLOW sets...

```
FOLLOW (E) = { $,
FOLLOW (E') = {
FOLLOW (T) = {
FOLLOW (T') = {
FOLLOW (F) = {
```

Look at rule

```
F \rightarrow (E) \mid \underline{id}
What can follow E?
```

Previously computed FIRST sets...

```
FIRST (F) = \{ (, id) \}
FIRST (T') = \{ *, \epsilon \}
FIRST (T) = \{ (, id) \}
FIRST (E') = \{ +, \epsilon \}
FIRST (E) = \{ (, id) \}
```

$E \rightarrow T E'$ $E' \rightarrow + T E' \mid \epsilon$ $T \rightarrow F T'$ $T' \rightarrow * F T' \mid \epsilon$ $F \rightarrow (E) \mid \underline{id}$

The FOLLOW sets...

```
FOLLOW (E) = { $, }

FOLLOW (E') = {

FOLLOW (T) = {

FOLLOW (T') = {

FOLLOW (F) = {
```

Look at rule $F \rightarrow (E) \mid \underline{id}$ What can follow E?

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Syntax Analysis - Part 1

Example of FOLLOW Computation

Previously computed FIRST sets...

```
FIRST (F) = { (, \underline{id} }

FIRST (T') = { *, \varepsilon}

FIRST (T) = { (, \underline{id} }

FIRST (E') = { +, \varepsilon}

FIRST (E) = { (, \underline{id} }
```

$$E \rightarrow T E'$$

$$E' \rightarrow +T E' \mid \epsilon$$

$$T \rightarrow F T'$$

$$T' \rightarrow *F T' \mid \epsilon$$

$$F \rightarrow (E) \mid \underline{id}$$

The FOLLOW sets...

```
FOLLOW (E) = { $, }

FOLLOW (E') = {

FOLLOW (T) = {

FOLLOW (T') = {

FOLLOW (F) = {
```

Look at rule

```
E → T E'
Whatever can follow E
can also follow E'
```

Previously computed FIRST sets...

```
FIRST (F) = \{ (, id) \}
FIRST (T') = \{ *, \epsilon \}
FIRST (T) = \{ (, id) \}
FIRST (E') = \{ +, \epsilon \}
FIRST (E) = \{ (, id) \}
```

```
E \rightarrow T E'
E' \rightarrow +T E' \mid \epsilon
T \rightarrow F T'
T' \rightarrow *F T' \mid \epsilon
F \rightarrow (E) \mid \underline{id}
```

The FOLLOW sets...

```
FOLLOW (E) = { $, )

FOLLOW (E') = { $, )

FOLLOW (T) = {

FOLLOW (T') = {

FOLLOW (F) = {
```

E → T E'
Whatever can follow E
can also follow E'

Look at rule

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Syntax Analysis - Part 1

Example of FOLLOW Computation

Previously computed FIRST sets...

```
FIRST (F) = { (, \underline{id} }

FIRST (T') = { *, \varepsilon}

FIRST (T) = { (, \underline{id} }

FIRST (E') = { +, \varepsilon}

FIRST (E) = { (, \underline{id} }
```

$$E \rightarrow T E'$$

$$E' \rightarrow +T E' \mid \epsilon$$

$$T \rightarrow F T'$$

$$T' \rightarrow *F T' \mid \epsilon$$

$$F \rightarrow (E) \mid \underline{id}$$

The FOLLOW sets...

```
FOLLOW (E) = { $, }

FOLLOW (E') = { $, }

FOLLOW (T) = {

FOLLOW (T') = {

FOLLOW (F) = {
```

Look at rule

```
E'_0 \rightarrow + T E'_1
Whatever is in FIRST(E'<sub>1</sub>)
can follow T
```

Previously computed FIRST sets...

```
\begin{aligned} & \text{FIRST (F)} & = \{ \text{ (, } \underline{\texttt{id}} \text{ )} \\ & \text{FIRST (T')} & = \{ \text{ *, } \epsilon \} \\ & \text{FIRST (T)} & = \{ \text{ (, } \underline{\texttt{id}} \text{ )} \\ & \text{FIRST (E')} & = \{ \text{ +, } \epsilon \} \\ & \text{FIRST (E)} & = \{ \text{ (, } \underline{\texttt{id}} \text{ )} \end{aligned}
```

$E \rightarrow T E'$ $E' \rightarrow +T E' \mid \epsilon$ $T \rightarrow F T'$ $T' \rightarrow *F T' \mid \epsilon$ $F \rightarrow (E) \mid \underline{id}$

The FOLLOW sets...

```
FOLLOW (E) = { $, }

FOLLOW (E') = { $, }

FOLLOW (T) = { +,

FOLLOW (T') = {

FOLLOW (F) = {
```

Look at rule $E'_0 \rightarrow + T E'_1$ Whatever is in FIRST(E'_1) can follow T

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Syntax Analysis - Part 1

Example of FOLLOW Computation

Previously computed FIRST sets...

```
FIRST (F) = { (, \underline{id} }

FIRST (T') = { *, \varepsilon}

FIRST (T) = { (, \underline{id} }

FIRST (E') = { +, \varepsilon}

FIRST (E) = { (, \underline{id} }
```

```
E \rightarrow T E'
E' \rightarrow +T E' \mid \epsilon
T \rightarrow F T'
T' \rightarrow *F T' \mid \epsilon
F \rightarrow (E) \mid \underline{id}
```

The FOLLOW sets...

```
FOLLOW (E) = { $, }

FOLLOW (E') = { $, }

FOLLOW (T) = { +,

FOLLOW (T') = {

FOLLOW (F) = {
```

Look at rule

$$T'_0 \rightarrow \star F T'_1$$

Whatever is in FIRST(T'_1)
can follow F

Previously computed FIRST sets...

```
FIRST (F) = \{ (, id) \}
FIRST (T') = \{ *, \epsilon \}
FIRST (T) = \{ (, id) \}
FIRST (E') = \{ +, \epsilon \}
FIRST (E) = \{ (, id) \}
```

```
E \rightarrow T E'
E' \rightarrow + T E' \mid \epsilon
T \rightarrow F T'
T' \rightarrow * F T' \mid \epsilon
F \rightarrow (E) \mid \underline{id}
```

The FOLLOW sets...

```
FOLLOW (E) = { $, }

FOLLOW (E') = { $, }

FOLLOW (T) = { +,

FOLLOW (T) = {

FOLLOW (F) = { *,
```

Look at rule $T'_0 \rightarrow * F T'_1$ Whatever is in FIRST(T'_1) can follow F

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Syntax Analysis - Part 1

Example of FOLLOW Computation

Previously computed FIRST sets...

```
FIRST (F) = { (, \underline{id} }

FIRST (T') = { *, \varepsilon}

FIRST (T) = { (, \underline{id} }

FIRST (E') = { +, \varepsilon}

FIRST (E) = { (, \underline{id} }
```

$$E \rightarrow T E'$$

$$E' \rightarrow +T E' \mid \epsilon$$

$$T \rightarrow F T'$$

$$T' \rightarrow *F T' \mid \epsilon$$

$$F \rightarrow (E) \mid \underline{id}$$

The FOLLOW sets...

```
FOLLOW (E) = { $, )

FOLLOW (E') = { $, )

FOLLOW (T) = { +,

FOLLOW (T') = {

FOLLOW (F) = { *,
```

Look at rule

```
Everything in FOLLOW(E'<sub>0</sub>)
E'_{1} = + T E'_{1}
Since E'<sub>1</sub> can go to \varepsilon
i.e., \varepsilon \in FIRST(E')
Everything in FOLLOW(E'<sub>0</sub>)
can follow T
```

Previously computed FIRST sets...

```
\begin{aligned} & \text{FIRST (F)} & = \{ \text{ (, } \underline{\text{id}} \text{ )} \\ & \text{FIRST (T')} & = \{ \text{ *, } \epsilon \} \\ & \text{FIRST (T)} & = \{ \text{ (, } \underline{\text{id}} \text{ )} \\ & \text{FIRST (E')} & = \{ \text{ +, } \epsilon \} \\ & \text{FIRST (E)} & = \{ \text{ (, } \underline{\text{id}} \text{ )} \end{aligned}
```

$E \rightarrow T E'$ $E' \rightarrow +T E' \mid \epsilon$ $T \rightarrow F T'$ $T' \rightarrow *F T' \mid \epsilon$ $F \rightarrow (E) \mid \underline{id}$

The FOLLOW sets...

```
FOLLOW (E) = { $, }

FOLLOW (E') = { $, }

FOLLOW (T) = { +, $, }

FOLLOW (T') = {

FOLLOW (F) = { *,
```

```
Look at rule E'_0 \rightarrow + T E'_1 Since E'_1 can go to \epsilon i.e., \epsilon \in FIRST(E') Everything in FOLLOW(E'_0) can follow T
```

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Syntax Analysis - Part 1

Example of FOLLOW Computation

Previously computed FIRST sets...

```
FIRST (F) = \{ (, \underline{id}) \}

FIRST (T') = \{ *, \epsilon \}

FIRST (T) = \{ (, \underline{id}) \}

FIRST (E') = \{ +, \epsilon \}

FIRST (E) = \{ (, \underline{id}) \}
```

$$E \rightarrow T E'$$

$$E' \rightarrow +T E' \mid \epsilon$$

$$T \rightarrow F T'$$

$$T' \rightarrow *F T' \mid \epsilon$$

$$F \rightarrow (E) \mid \underline{id}$$

The FOLLOW sets...

```
FOLLOW (E) = { $, }

FOLLOW (E') = { $, }

FOLLOW (T) = { +, $, }

FOLLOW (T') = {

FOLLOW (F) = { *,
```

Look at rule

T → F T'
Whatever can follow T
can also follow T'

Previously computed FIRST sets...

```
FIRST (F) = \{ (, id) \}
FIRST (T') = \{ *, \epsilon \}
FIRST (T) = \{ (, id) \}
FIRST (E') = \{ +, \epsilon \}
FIRST (E) = \{ (, id) \}
```

$E \rightarrow T E'$ $E' \rightarrow + T E' \mid \epsilon$ $T \rightarrow F T'$ $T' \rightarrow * F T' \mid \epsilon$ $F \rightarrow (E) \mid \underline{id}$

The FOLLOW sets...

```
FOLLOW (E) = { $, }

FOLLOW (E') = { $, }

FOLLOW (T) = { +, $, }

FOLLOW (T) = { +, $, }

FOLLOW (F) = { *,
```

Look at rule T → F T' Whatever can follow T can also follow T'

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Syntax Analysis - Part 1

Example of FOLLOW Computation

Previously computed FIRST sets...

```
\begin{aligned} & \text{FIRST (F)} & = \{ \ (, \underline{id} \ ) \\ & \text{FIRST (T')} & = \{ \ \star, \varepsilon \} \\ & \text{FIRST (T)} & = \{ \ (, \underline{id} \ ) \\ & \text{FIRST (E')} & = \{ \ \star, \varepsilon \} \\ & \text{FIRST (E)} & = \{ \ (, \underline{id} \ ) \} \end{aligned}
```

$$E \rightarrow T E'$$

$$E' \rightarrow +T E' \mid \epsilon$$

$$T \rightarrow F T'$$

$$T' \rightarrow *F T' \mid \epsilon$$

$$F \rightarrow (E) \mid \underline{id}$$

The FOLLOW sets...

```
FOLLOW (E) = { $, }

FOLLOW (E') = { $, }

FOLLOW (T) = { +, $, }

FOLLOW (T') = { +, $, }

FOLLOW (F) = { *,
```

Look at rule $T'_0 \rightarrow \star F T'_1$ Since T'_1 can go to ϵ i.e., $\epsilon \in FIRST(T')$

Everything in FOLLOW(T'₀)
can follow F

```
→ T E'
Previously computed FIRST sets...
                                                                \rightarrow + T E' | \epsilon
    FIRST (F)
                     = \{ (, id) \}
                                                                 → F T'
    FIRST (T')
                     = \{ \star, \varepsilon \}
                                                            T' \rightarrow *FT' \mid \epsilon
    FIRST (T)
                     = \{ (, id) \}
    FIRST (E')
                     =\{+, \mathbf{\epsilon}\}
                                                                 → ( E ) | <u>id</u>
    FIRST (E)
                     = \{ (, id) \}
The FOLLOW sets...
    FOLLOW (E) = \{ \$, \}
    FOLLOW (E') = \{ \$, \}
    FOLLOW (T) = \{+, \$, \}
                                                       Look at rule
    FOLLOW (T') = \{+, \$, \}
                                                             T'_0 \rightarrow *FT'_1
    FOLLOW (F) = \{ *, +, \$, \}
                                                       Since T'<sub>1</sub> can go to E
                                                            i.e., \varepsilon \in FIRST(T')
                                                       Everything in FOLLOW(T'<sub>0</sub>)
                                                          can follow F
```

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Syntax Analysis - Part 1

Example of FOLLOW Computation

```
→ T E'
Previously computed FIRST sets...
                                                         E' \rightarrow + T E' \mid \epsilon
   FIRST (F)
                    = { (, id }
                                                             → F T'
   FIRST (T')
                    = \{ \star, \varepsilon \}
                                                             \rightarrow * F T' | \epsilon
                    = { (, id }
   FIRST (T)
   FIRST (E')
                    =\{+, \mathbf{\epsilon}\}
                                                              → ( E ) | <u>id</u>
   FIRST (E)
                    = \{ (, id) \}
The FOLLOW sets...
   FOLLOW (E) = \{ \$, \} \}
   FOLLOW (E') = \{ \$, \} 
                                                Nothing more can be added.
   FOLLOW (T) = \{+, \$, \}
   FOLLOW (T') = \{+, \$, \}
   FOLLOW (F) = \{ *, +, \$, \}
```

Building the Predictive Parsing Table

The Main Idea:

Assume we're looking for an A i.e., A is on the stack top.
Assume b is the current input symbol.

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Syntax Analysis - Part 1

Building the Predictive Parsing Table

The Main Idea:

Assume we're looking for an A i.e., A is on the stack top.
Assume b is the current input symbol.

If $A \rightarrow \alpha$ is a rule and b is in FIRST(α) then expand A using the $A \rightarrow \alpha$ rule!

Building the Predictive Parsing Table

The Main Idea:

```
Assume we're looking for an A

i.e., A is on the stack top.

Assume b is the current input symbol.
If A→α is a rule and b is in FIRST(α)

then expand A using the A→α rule!

What if ε is in FIRST(α)? [i.e., α ⇒* ε]

If b is in FOLLOW(A)
then expand A using the A→α rule!
```

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Syntax Analysis - Part 1

Building the Predictive Parsing Table

The Main Idea:

Assume we're looking for an A

```
i.e., A is on the stack top.
Assume b is the current input symbol.
If A→α is a rule and b is in FIRST(α)
    then expand A using the A→α rule!
What if ε is in FIRST(α)? [i.e., α ⇒* ε]
    If b is in FOLLOW(A)
        then expand A using the A→α rule!
If ε is in FIRST(α) and $ is the current input symbol then if $ is in FOLLOW(A)
        then expand A using the A→α rule!
```

Example: The "Dangling Else" Grammar

- 1. $S \rightarrow \underline{if} E \underline{then} S S'$
- 2. $S \rightarrow otherStmt$
- 3. $S' \rightarrow \underline{\text{else}} S$
- 4. $S' \rightarrow \varepsilon$
- 5. $E \rightarrow boolExpr$

"if b then if b then otherStmt else otherStmt"

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Syntax Analysis - Part 1

Example: The "Dangling Else" Grammar

- 1. $S \rightarrow \underline{i} E \underline{t} S S'$
- 2. S → <u>o</u>
- 3. $S' \rightarrow \underline{e} S$
- 4. $S' \rightarrow \varepsilon$
- 5. $\mathbf{E} \rightarrow \mathbf{b}$



- 1. $S \rightarrow \underline{if} E \underline{then} S S'$
- 2. $S \rightarrow otherStmt$
- 3. $S' \rightarrow \underline{\mathsf{else}} S$
- 4. $S' \rightarrow \varepsilon$
- 5. $E \rightarrow boolExpr$

 $\underline{i} \underline{b} \underline{t} \underline{i} \underline{b} \underline{t} \underline{o} \underline{e} \underline{o} \leftarrow \text{``if } \underline{b} \underline{t} \text{hen } \underline{i} \underline{f} \underline{b} \underline{t} \text{hen } \underline{o} \text{therStmt } \underline{e} \text{lse } \underline{o} \text{therStmt''}$

Syntax Analysis - Part 1

Example: The "Dangling Else" Grammar

```
1. S \rightarrow \underline{i} E \underline{t} S S'

2. S \rightarrow \underline{o}

3. S' \rightarrow \underline{e} S

4. S' \rightarrow \varepsilon

5. E \rightarrow \underline{b}
```

<u>ibtibtoeo</u>

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Syntax Analysis - Part 1

Example: The "Dangling Else" Grammar

```
1. S \rightarrow \underline{i} E \underline{t} S S'

2. S \rightarrow \underline{o}

3. S' \rightarrow \underline{e} S

4. S' \rightarrow \varepsilon

5. E \rightarrow \underline{b}
```

<u>ibtibtoeo</u>

```
\begin{split} & FIRST(\underline{S}) = \{ \ \underline{\underline{\mathbf{i}}}, \underline{\mathbf{o}} \ \} \\ & FIRST(\underline{S}') = \{ \ \underline{\underline{\mathbf{e}}}, \underline{\varepsilon} \ \} \\ & FIRST(\underline{E}) = \{ \ \underline{\underline{\mathbf{b}}} \ \} \end{split} \qquad \begin{aligned} & FOLLOW(\underline{S}') = \{ \ \underline{\underline{\mathbf{e}}}, \frac{\boldsymbol{\varsigma}}{\boldsymbol{\varsigma}} \ \} \\ & FOLLOW(\underline{E}) = \{ \ \underline{\underline{\mathbf{t}}} \ \} \end{aligned}
```

Example: The "Dangling Else" Grammar

1. $S \rightarrow \underline{i} E \underline{t} S S'$ 2. $S \rightarrow \underline{o}$

3. $S' \rightarrow \underline{e} S$

4. $S' \rightarrow \varepsilon$

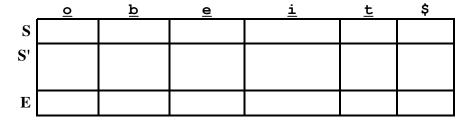
5. $\mathbf{E} \rightarrow \mathbf{b}$

Look at Rule 1: $S \rightarrow \underline{\underline{i}} \to \underline{\underline{t}} \to \underline{\underline{t}} \to S'$ If we are looking for an S

and the next symbol is in FIRST($\underline{i} \to \underline{t} \to S'$)... Add that rule to the table

<u>ibtibtoeo</u>

$$\begin{split} & FIRST(\underline{S}) = \{ \ \underline{\underline{\mathbf{i}}}, \ \underline{\mathbf{o}} \ \} \\ & FIRST(\underline{S}') = \{ \ \underline{\underline{\mathbf{e}}}, \ \epsilon \ \} \\ & FIRST(\underline{E}) = \{ \ \underline{\underline{\mathbf{b}}} \ \} \\ & FOLLOW(\underline{S}') = \{ \ \underline{\underline{\mathbf{e}}}, \ \$ \ \} \\ & FOLLOW(\underline{E}) = \{ \ \underline{\underline{\mathbf{t}}} \ \} \end{split}$$



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20'

Syntax Analysis - Part 1

Example: The "Dangling Else" Grammar

- 1. $S \rightarrow \underline{i} E \underline{t} S S'$
- 2. $S \rightarrow \underline{o}$
- 3. $S' \rightarrow \underline{\mathbf{e}} S$
- 4. $S' \rightarrow \varepsilon$
- 5. $\mathbf{E} \rightarrow \mathbf{\underline{b}}$

Look at Rule 1: $S \rightarrow \underline{\mathbf{i}} E \underline{\mathbf{t}} S S'$

If we are looking for an S

and the next symbol is in FIRST($\underline{\textbf{i}}$ E $\underline{\textbf{t}}$ S S')... Add that rule to the table

<u>ibtibtoeo</u>

$$\begin{split} & FIRST(\underline{S}) = \{ \ \underline{\underline{\textbf{i}}} \ , \underline{\textbf{o}} \ \} \\ & FIRST(\underline{S}') = \{ \ \underline{\underline{\textbf{e}}} \ , \underline{\textbf{\epsilon}} \ \} \\ & FIRST(\underline{E}) = \{ \ \underline{\underline{\textbf{b}}} \ \} \\ & FOLLOW(\underline{S}') = \{ \ \underline{\underline{\textbf{e}}} \ , \underline{\textbf{\$}} \ \} \\ & FOLLOW(\underline{E}) = \{ \ \underline{\underline{\textbf{t}}} \ \} \end{split}$$

	<u>o</u>	<u>b</u>	<u>e</u>	<u>i</u>	<u>t</u>	\$
\mathbf{S}				$S \rightarrow \underline{i}E\underline{t}SS'$		
S'						
E						

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Example: The "Dangling Else" Grammar

1. $S \rightarrow \underline{i} E \underline{t} S S'$

2. $S \rightarrow \underline{o}$

3. $S' \rightarrow \underline{e} S$

5.

4. $S' \rightarrow \varepsilon$

 $E \rightarrow \underline{b}$

Look at Rule 2: $S \rightarrow \underline{o}$

If we are looking for an S

and the next symbol is in FIRST(o)...

Add that rule to the table

$\underline{i} \underline{b} \underline{t} \underline{i} \underline{b} \underline{t} \underline{o} \underline{e} \underline{o}$

 $\begin{aligned} & FIRST(\underline{S}) = \{ \ \underline{\underline{\iota}}, \ \underline{o} \ \} \\ & FIRST(\underline{S'}) = \{ \ \underline{\underline{e}}, \ \epsilon \ \} \\ & FIRST(\underline{E}) = \{ \ \underline{\underline{e}}, \ \epsilon \ \} \end{aligned} \qquad \begin{aligned} & FOLLOW(\underline{S'}) = \{ \ \underline{\underline{e}}, \ \xi \ \} \\ & FIRST(\underline{E}) = \{ \ \underline{\underline{b}} \ \} \end{aligned} \qquad \begin{aligned} & FOLLOW(\underline{E}) = \{ \ \underline{\underline{t}} \ \} \end{aligned}$

<u>o</u>	<u>b</u>	<u>e</u>	<u>i</u>	<u>t</u>	\$
			$S \rightarrow \underline{i} E \underline{t} S S'$		
	<u>O</u>	<u>o</u> <u>b</u>	<u>o</u> <u>b</u> <u>e</u>		

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Syntax Analysis - Part 1

Example: The "Dangling Else" Grammar

- 1. $S \rightarrow \underline{i} E \underline{t} S S'$
- 2. S → <u>o</u>
- 3. $S' \rightarrow \underline{e} S$
- 4. $S' \rightarrow \varepsilon$
- 5. $E \rightarrow \underline{b}$

Look at Rule 2: $S \rightarrow o$

If we are looking for an S

and the next symbol is in FIRST(o)... Add that rule to the table

<u>ibtibtoeo</u>

$$\begin{split} & FIRST(\underline{S}) = \{ \ \underline{\underline{\textbf{i}}}, \underline{\textbf{o}} \ \} \\ & FIRST(\underline{S}') = \{ \ \underline{\underline{\textbf{e}}}, \epsilon \ \} \\ & FIRST(\underline{E}) = \{ \ \underline{\underline{\textbf{b}}} \ \} \\ & FOLLOW(\underline{S}') = \{ \ \underline{\underline{\textbf{e}}}, \$ \ \} \\ & FOLLOW(\underline{E}) = \{ \ \underline{\underline{\textbf{t}}} \ \} \end{split}$$

<u>o</u>	<u>b</u>	<u>e</u>	<u>i</u>	<u>t</u>	\$
<u>S</u> → <u>o</u>			$S \rightarrow \underline{i} E \underline{t} S S'$		
	<u>o</u> S → <u>o</u>	<u>o</u> <u>b</u> S → <u>o</u>	<u>o</u> <u>b</u> <u>e</u> S → <u>o</u>	$ \begin{array}{c cccc} \underline{o} & \underline{b} & \underline{e} & \underline{i} \\ S \to \underline{o} & & & & \\ S \to \underline{i} \underline{E} \underline{t} S S' \end{array} $	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$

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2.

Example: The "Dangling Else" Grammar

 $S \rightarrow \underline{o}$ 3. $S' \rightarrow \underline{e} S$ 4. $S' \rightarrow \varepsilon$

 $S \rightarrow \underline{i} E \underline{t} S S'$

5. $E \rightarrow \underline{b}$ Look at Rule 5: $E \rightarrow \underline{b}$ If we are looking for an E and the next symbol is in FIRST(b)... Add that rule to the table

$\underline{i}\,\underline{b}\,\underline{t}\,\underline{i}\,\underline{b}\,\underline{t}\,\underline{o}\,\underline{e}\,\underline{o}$

 $FIRST(S) = \{ \underline{i}, \underline{o} \}$ $FOLLOW(S) = \{ \underline{\mathbf{e}}, \$ \}$ $FIRST(S') = \{ \underline{\mathbf{e}}, \varepsilon \}$ $FOLLOW(S') = \{ \underline{\mathbf{e}}, \$ \}$ $FIRST(\mathbf{E}) = \{ \mathbf{\underline{b}} \}$ $FOLLOW(\mathbf{E}) = \{ \mathbf{\underline{t}} \}$

	<u> </u>	<u>b</u>	<u>e</u>	<u>i</u>	<u>t</u>	Ş
\mathbf{S}	<u>S</u> → <u>o</u>			$S \rightarrow \underline{i}E\underline{t}SS'$		
S'						
E						
E						

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Syntax Analysis - Part 1

Example: The "Dangling Else" Grammar

 $S \rightarrow \underline{i} E \underline{t} S S'$

2. $S \rightarrow \underline{o}$ 3. $S' \rightarrow e S$

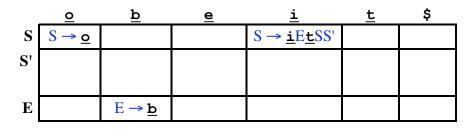
4. $S' \rightarrow \varepsilon$

5. $E \rightarrow \underline{b}$ Look at Rule 5: $E \rightarrow b$ If we are looking for an E and the next symbol is in FIRST(b)...

Add that rule to the table

<u>ibtibtoeo</u>

 $FIRST(S) = \{ \underline{i}, \underline{o} \}$ $FOLLOW(S) = \{ \underline{\mathbf{e}}, \$ \}$ $FIRST(S') = \{ \underline{\mathbf{e}}, \varepsilon \}$ $FOLLOW(S') = \{ \underline{\mathbf{e}}, \$ \}$ $FIRST(\mathbf{E}) = \{ \mathbf{\underline{b}} \}$ $FOLLOW(\mathbf{E}) = \{ \, \underline{\mathbf{t}} \, \}$



Example: The "Dangling Else" Grammar

```
1. S \rightarrow \underline{i} E \underline{t} S S'

2. S \rightarrow \underline{o}

3. S' \rightarrow \underline{e} S

4. S' \rightarrow \varepsilon

5. E \rightarrow \underline{b}
```

Look at Rule 3: $S' \to \underline{e} S$ If we are looking for an S'and the next symbol is in FIRST($\underline{e} S$)... Add that rule to the table

$\underline{i} \underline{b} \underline{t} \underline{i} \underline{b} \underline{t} \underline{o} \underline{e} \underline{o}$

```
\begin{split} & FIRST(\underline{S}) = \{ \ \underline{\underline{i}}, \underline{o} \ \} \\ & FIRST(\underline{S}') = \{ \ \underline{e}, \epsilon \ \} \\ & FIRST(\underline{E}) = \{ \ \underline{b} \ \} \end{split} \qquad \begin{aligned} & FOLLOW(\underline{S}') = \{ \ \underline{e}, \$ \ \} \\ & FOLLOW(\underline{E}) = \{ \ \underline{b} \ \} \end{aligned}
```

<u>0</u>	<u>b</u>	<u>e</u>	<u>i</u>	<u>t</u>	\$
<u>S</u> → <u>o</u>			$S \rightarrow \underline{i} E \underline{t} S S'$		
	<u>E</u> → <u>b</u>				
	$\frac{\underline{o}}{S \to \underline{o}}$	_			

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Syntax Analysis - Part 1

Example: The "Dangling Else" Grammar

1. $S \rightarrow \underline{i} E \underline{t} S S'$ 2. $S \rightarrow \underline{o}$

3. $S' \rightarrow \underline{\mathbf{e}} S$ 4. $S' \rightarrow \varepsilon$

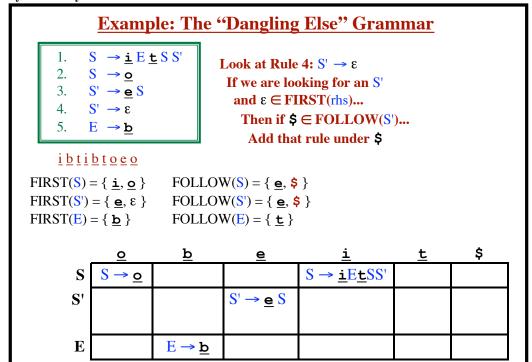
5. $E \rightarrow \underline{b}$

Look at Rule 3: $S' \rightarrow \underline{e} S$ If we are looking for an S'and the next symbol is in FIRST($\underline{e} S$)... Add that rule to the table

<u>ibtibtoeo</u>

$$\begin{split} & FIRST(\underline{S}) = \{ \ \underline{\underline{\textbf{i}}}, \ \underline{\textbf{o}} \ \} \\ & FIRST(\underline{S}') = \{ \ \underline{\underline{\textbf{e}}}, \ \epsilon \ \} \\ & FIRST(\underline{E}) = \{ \ \underline{\underline{\textbf{b}}} \ \} \\ & FOLLOW(\underline{S}') = \{ \ \underline{\underline{\textbf{e}}}, \ \xi \ \} \\ & FOLLOW(\underline{E}) = \{ \ \underline{\underline{\textbf{t}}} \ \} \end{split}$$

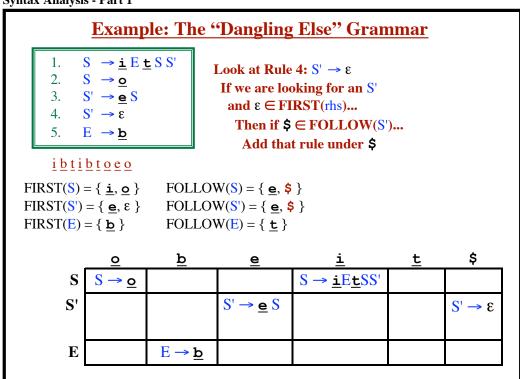
	<u>o</u>	<u>b</u>	<u>e</u>	<u>i</u>	<u>t</u>	\$
\mathbf{S}	$S \rightarrow \underline{o}$			$S \rightarrow \underline{i} E \underline{t} S S'$		
S'			$S' \rightarrow \underline{\mathbf{e}} S$			
\mathbf{E}		<u>E</u> → <u>b</u>				

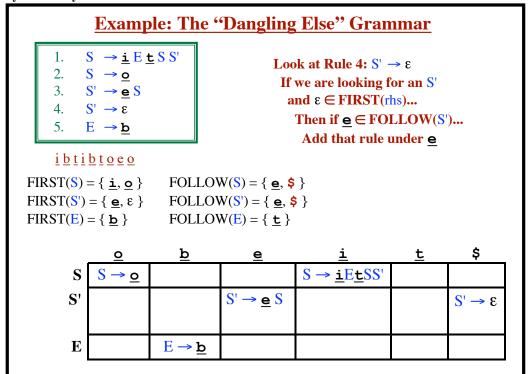


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Syntax Analysis - Part 1

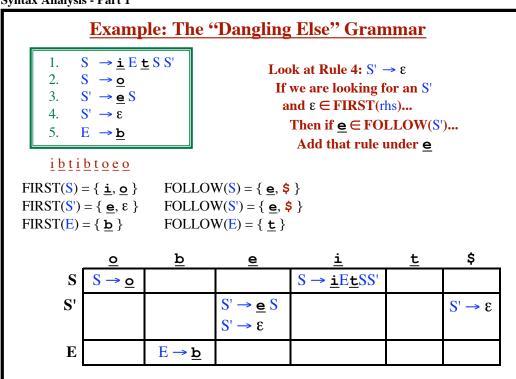




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21'

Syntax Analysis - Part 1



Example: The "Dangling Else" Grammar

1.
$$S \rightarrow \underline{i} E \underline{t} S S'$$

2.
$$S \rightarrow o$$

3.
$$S' \rightarrow \underline{\underline{e}} S$$

4. $S' \rightarrow \varepsilon$

5. $E \rightarrow \underline{b}$

CONFLICT!

Two rules in one table entry.

<u>ibtibtoeo</u>

$$\begin{split} & FIRST(\underline{S}) = \{ \ \underline{\underline{\mathbf{i}}}, \underline{\underline{\mathbf{o}}} \ \} \\ & FIRST(\underline{S}') = \{ \ \underline{\underline{\mathbf{e}}}, \underline{\varepsilon} \ \} \\ & FIRST(\underline{E}) = \{ \ \underline{\underline{\mathbf{b}}} \ \} \\ & FOLLOW(\underline{S}') = \{ \ \underline{\underline{\mathbf{e}}}, \underline{\$} \ \} \\ & FOLLOW(\underline{E}) = \{ \ \underline{\underline{\mathbf{t}}} \ \} \end{split}$$

	<u>o</u>	<u>b</u>	<u>e</u>	<u>i</u>	<u>t</u>	\$
\mathbf{S}	<u>S</u> → <u>o</u>			$S \rightarrow \underline{i}E\underline{t}SS'$		
S'			$S' \to \underline{\mathbf{e}} S$ $S' \to \varepsilon$			$S' \rightarrow \epsilon$
			$S' \rightarrow \epsilon$			
E		<u>E</u> → <u>b</u>				

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Syntax Analysis - Part 1

Example: The "Dangling Else" Grammar

- $S \rightarrow \underline{i} E \underline{t} S S'$
- 2. $S \rightarrow \underline{o}$
- 3. $S' \rightarrow \underline{e} S$
- 4. $S' \rightarrow \varepsilon$
- 5. $E \rightarrow \underline{b}$

CONFLICT!

Two rules in one table entry. The grammar is not LL(1)!

<u>ibtibtoeo</u>

$$\begin{split} & FIRST(\underline{S}) = \{ \ \underline{\underline{\mathbf{i}}}, \ \underline{\mathbf{o}} \ \} \\ & FIRST(\underline{S}') = \{ \ \underline{\underline{\mathbf{e}}}, \ \epsilon \ \} \\ & FIRST(\underline{E}) = \{ \ \underline{\underline{\mathbf{b}}} \ \} \\ & FOLLOW(\underline{S}') = \{ \ \underline{\underline{\mathbf{e}}}, \ \xi \ \} \\ & FOLLOW(\underline{E}) = \{ \ \underline{\underline{\mathbf{t}}} \ \} \end{split}$$

	<u>o</u>	<u>b</u>	<u>e</u>	<u>i</u>	<u>t</u>	\$
S	$S \rightarrow \underline{o}$			$S \rightarrow \underline{i}E\underline{t}SS'$		
S'			$S' \to \underline{\mathbf{e}} S$ $S' \to \varepsilon$			$S' \rightarrow \epsilon$
			$S' \rightarrow \epsilon$			
E		$E \rightarrow \underline{b}$				



Input: Grammar G

Output: Parsing Table, such that TABLE [A,b] = Rule to use or "ERROR/Blank"

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Syntax Analysis - Part 1

Algorithm to Build the Table

Input: Grammar G

Output: Parsing Table, such that **TABLE** [A,b] = Rule to use or "ERROR/Blank"

Compute FIRST and FOLLOW sets

Input: Grammar G

Algorithm to Build the Table

Output: Parsing Table, such that TABLE [A,b] = Rule to use or "ERROR/Blank"

```
Compute FIRST and FOLLOW sets
for each rule A \rightarrow \alpha do
  for each terminal b in FIRST(\alpha) do
     add A \rightarrow \alpha to TABLE [A,b]
  <u>endFor</u>
```

endFor

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Syntax Analysis - Part 1

Algorithm to Build the Table

```
Input: Grammar G
Output: Parsing Table, such that TABLE [A, b] = Rule to use or "ERROR/Blank"
Compute FIRST and FOLLOW sets
for each rule A \rightarrow \alpha do
  for each terminal b in FIRST(\alpha) do
     add A \rightarrow \alpha to TABLE [A, b]
  {\tt endFor}
  \underline{\text{if}} & is in FIRST(\alpha) \underline{\text{then}}
     for each terminal b in FOLLOW(A) do
         add A \rightarrow \alpha to TABLE [A,b]
     <u>endFor</u>
   endIf
<u>endFor</u>
```

Algorithm to Build the Table Input: Grammar G Output: Parsing Table, such that TABLE [A, b] = Rule to use or "ERROR/Blank" Compute FIRST and FOLLOW sets for each rule $A \rightarrow \alpha$ do for each terminal b in FIRST(α) do add $A \rightarrow \alpha$ to TABLE [A,b] endFor if ε is in FIRST(α) then for each terminal b in FOLLOW(A) do add $A \rightarrow \alpha$ to TABLE [A,b] endFor \underline{if} \$ is in FOLLOW(A) \underline{then} add $A \rightarrow \alpha$ to TABLE [A, \$] endIfendIf endFor

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Syntax Analysis - Part 1

```
Algorithm to Build the Table
Input: Grammar G
Output: Parsing Table, such that TABLE [A, b] = Rule to use or "ERROR/Blank"
Compute FIRST and FOLLOW sets
for each rule A \rightarrow \alpha do
  for each terminal b in FIRST(\alpha) do
     add A \rightarrow \alpha to TABLE [A,b]
  endFor
  if & is in FIRST(\alpha) then
     for each terminal b in FOLLOW(A) do
       add A \rightarrow \alpha to TABLE [A,b]
     endFor
     if $ is in FOLLOW(A) then
       add A \rightarrow \alpha to TABLE [A, $]
     endIf
  endIf
<u>endFor</u>
TABLE [A,b] is undefined? Then set TABLE [A,b] to "error"
```

Algorithm to Build the Table **Input:** Grammar G Output: Parsing Table, such that TABLE [A, b] = Rule to use or "ERROR/Blank" Compute FIRST and FOLLOW sets for each rule $A \rightarrow \alpha$ do for each terminal b in FIRST(α) do add $A \rightarrow \alpha$ to TABLE [A,b] endFor if ε is in FIRST(α) then for each terminal b in FOLLOW(A) do add $A \rightarrow \alpha$ to TABLE [A,b] endFor if \$ is in FOLLOW(A) then add $A \rightarrow \alpha$ to TABLE [A, \$] endIf endIf endFor TABLE [A,b] is undefined? Then set TABLE [A,b] to "error" TABLE [A,b] is multiply defined? The algorithm fails!!! Grammar G is not LL(1)!!!

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Syntax Analysis - Part 1

```
LL(1) Grammars
LL(1) grammars
                                                          Using only one symbol of look-ahead
    • Are never ambiguous.
    • Will never have left recursion.
                                                         Find Leftmost derivation
                                                    Scanning input left-to-right
Furthermore...
    If we are looking for an "A" and the next symbol is "b",
             Then only one production must be possible.
More Precisely...
 If A \rightarrow \alpha and A \rightarrow \beta are two rules
    If \alpha \Rightarrow^* \underline{a}... and \beta \Rightarrow^* \underline{b}...
             then we require \underline{\mathbf{a}} \neq \underline{\mathbf{b}}
             (i.e., FIRST(\alpha) and FIRST(\beta) must not intersect)
    If \alpha \Rightarrow * \epsilon
             then \beta \Rightarrow^* \epsilon must not be possible.
             (i.e., only one alternative can derive \varepsilon.)
    If \alpha \Rightarrow^* \epsilon and \beta \Rightarrow^* b...
             then b must not be in FOLLOW(A)
```

Error Recovery

We have an error whenever...

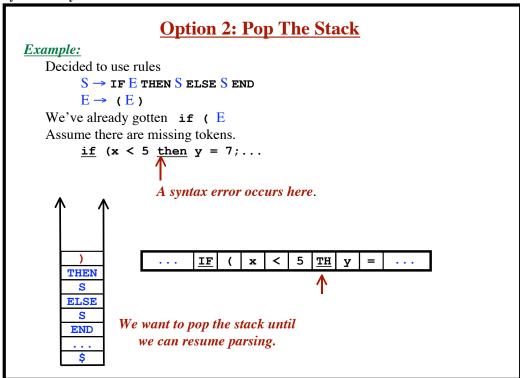
- Stacktop is a terminal, but stacktop ≠ input symbol
- Stacktop is a nonterminal but TABLE[A,b] is empty

Options

- 1. Skip over input symbols, until we can resume parsing Corresponds to ignoring tokens
- 2. Pop stack, until we can resume parsing Corresponds to inserting missing material
- 3. Some combination of 1 and 2
- 4. "Panic Mode" Use Synchronizing tokens
 - Identify a set of synchronizing tokens.
 - Skip over tokens until we are positioned on a synchronizing token.
 - Pop stack until we can resume parsing.

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Syntax Analysis - Part 1 Option 1: Skip Input Symbols Example: Decided to use rule $S \rightarrow IF E THEN S ELSE S END$ Stack tells us what we are expecting next in the input. We've already gotten IF and E Assume there are extra tokens in the input. \underline{if} (x<5))) \underline{then} y = 7; ... A syntax error occurs here. TH THEN ELSE We want to skip tokens until END we can resume parsing.



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Syntax Analysis - Part 1

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Skip tokens until we see something in FIRST(A), FIRST(B), FIRST(C), ...

Include FIRST(A), FIRST(B), FIRST(C), ... in the SynchSet.

Pop stack until NextToken ∈ FIRST(NonTerminalOnStackTop)

Error Recovery - Table Entries

Each blank entry in the table indicates an error.

Tailor the error recovery for each possible error.

Fill the blank entry with an error routine.

The error routine will tell what to do.

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Syntax Analysis - Part 1

Error Recovery - Table Entries

Each blank entry in the table indicates an error.

Tailor the error recovery for each possible error.

Fill the blank entry with an error routine.

The error routine will tell what to do.

Example:

	<u>id</u>	SEMI	RPAREN	LPAREN	 \$
E			E4		
E '			E5		

Error Recovery - Table Entries

Each blank entry in the table indicates an error.

Tailor the error recovery for each possible error.

Fill the blank entry with an error routine.

The error routine will tell what to do.

Example:

