



NAME: \_\_\_\_\_

## 1 Objective: Two Way ANOVA

In this lab we'll follow Littell/Freund/Stroup, SAS System for Linear Models, in their treatment of a 2 way anova example.

## 2 Key Words

proc univariate, proc glm, two way ANOVA, multiple comparison, factorial experiment.

## 3 Brief Description

Suppose we have:

3 Methods of promoting seed growth : M

5 Varieties of turf grass seed : V

6 pots planted with each M, V Combination.

Suppose the resulting 90 pots randomly placed in growing chamber and Y = yield measured at the end of four weeks.

This gives a  $3 \times 5$  completely randomized factorial experiment. The data are in the file **grass.dat**, with each of the 6 yields given in each row. In addition the yields were multiplied by 10 to save entering decimal.

## 4 Lab Steps

[A] Read in the data and put it in ANOVA format.

[1] The following code reads the data structured as given:

```
DATA grass1;
    infile 'C:\...\grass.dat';
    input m $ v y1-y6;
run;

PROC print data=grass1;
run;
```

[2] We need this in ANOVA format one long list of yields with corresponding treatment levels. Use this code to transform:

```
DATA grass;
    set grass1;
    drop y1-y6;
    y=y1/10; output;
    y=y2/10; output;
    y=y3/10; output;
    y=y4/10; output;
    y=y5/10; output;
    y=y6/10; output;
run;

PROC print data = grass;
run;
```

[B] Plot cell means.

[1] Find cell means.

```
PROC means data = grass noprint;
    by m v;
    output out = cellmn mean = ymean;
run;

PROC print data = cellmn;
run;
```

[2] Plot cell means vs v using m as symbol.

```
PROC plot data = cellmn;
    plot ymean*v = m;
run;
```

[3] SKETCH AND TURN IN the plot, connecting the same methods A, B, C.

[4] Which method produces most yield?

[5] Is there interaction, i.e. does the magnitude of the difference in cell means depend on the variety?  
Or are the plots parallel? Explain in a short paragraph.

[C] Perform an ANOVA test for interaction.

[1] Use the following `proc glm`:

```
PROC glm data = grass;
    class m v;
    model y=m v m*v;
run;
```

[2] What is the F-stt p-value for testing  $H_0$ : no interaction? (That is given by type III ss for  $m*v$ ).

[D] Now, perform Duncan test of equality, of method means by variety. To do this, we must sort by variety.

[1] Sorting by variety:

```
PROC sort data = grass out = grass2;
    by v;
run;
```

- [2] Perform two way anova (proc glm)

```
PROC glm data = grass2;
    by v;
    class m;
    model y = m;
    means m/duncan;
run;
```

- [3] Look back at your plot. Because of randomness in data, you might think method A & C are the same and B less for variety 2. Look at Duncan's output for that variety. What does Duncan conclude? TURN IN: explain in a short paragraph.
- [4] Look at plot for variety 3, What does Duncan say? TURN IN: explain in a short paragraph.

[E] Now try contrasts and estimation. NOTE: CAN ONLY ESTIMATE LINEAR COMBINATIONS OF CELL MEANS.

- [1] Recall relation between cell means and overparameterized model (We have notational difficulties here. So write MU for mu, m for model, v for variety).

$$MU_{ij} = MU + m_i + v_j + (mv)_{ij}$$

- [2] Recall the three steps need to code estimates and contrasts into SAS:

- [a] Write linear combination to be estimated in terms of cell means.
- [b] Convert to model parameters using \*\*\*\*.
- [c] Gather like terms.

- [3] Suppose you want to estimate  $.4*MU_{A1} + .6*MU_{B1}$ .

Perform the steps listed and then complete the code to get estimate:

```
PROC glm data = grass;
    class m v;
    model y = m v m*v;
    estimate '.4A+.6B_in_V1' intercept ??? m ??? v ??? m*v ???;
run;
```

TURN IN CODE, ESTIMATE AND STD ERR:

Check your answer using the appropriate weighted average of cell means from [B1].

- [4] Suppose you want to estimate  $.4*MU_{A1} + .6*MU_{B1} - MU_{C1}$ .

Perform the steps listed and then complete the code to get estimate:

```
... estimate '.4 A + .6 B - C in V1' intercept ??? m ??? v ??? m*v ???;
```

TURN IN CODE, ESTIMATE AND STD ERR:

- [5] Suppose you want to estimate  $.4*MU_{Abar} + .6*MU_{Bbar} - MU_{Cbar}$ , the simple average of method means across the variety all 5 varieties (This makes sense if NO INTERACTION, which is not the case, but do it anyway).

Perform the steps listed and then complete the code to get estimate:

```
... estimate '.4 A + .6 B in V1' intercept ??? m ??? v ??? m*v ???;
```

TURN IN CODE, ESTIMATE AND STD ERR: