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Intro to Data Mining

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### Project 6c

1. Fit the given data for model

$$X_3 = \beta_1 \sin(X_2) + \beta_2 X_3^2 + \beta_4 X_4 + \beta_5 \ln(X_5) + C.$$

Figure 1: Variation Multilinear Model Summary

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )	
(Intercept)	-8.2825	3.2568	-2.543	0.0130	*
b1	8.7047	3.1088	2.800	0.0065	**
b2	5.3452	0.1124	47.568	< 2e-16	***
b4	-2.7565	0.3691	-7.468	1.22e-10	***
b5	3.2023	0.3878	8.258	3.86e-12	***

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 1.869 on 75 degrees of freedom

Multiple R-squared: 0.998, Adjusted R-squared: 0.9979

F-statistic: 9526 on 4 and 75 DF, p-value: < 2.2e-16

We can see that for our model, we do have a model. All of our coefficients are statistically significant. have an  $R^2$  value of about 99 percent, meaning that we can account for 99 percent of the variation of the data. We almost have a perfect fit for our data and our equation is:

$$x_3 = 8.7047 \cdot \sin(x_2) + 5.3452 \cdot (x_2^3) + -2.7565 \cdot x_4 + 3.2023 \cdot \ln(x_5) - 8.2825$$

2. Compute the root mean square error (RMSE) for your model.

Figure 2: Variation Multilinear RMS

```
> y_pred <- predict(var_model, newdata = data.frame(Amatrix))
>
> RMSE <- sqrt(sum((y_pred - y)^2))/sqrt(length(y))
> RMSE
[1] 1.810087
```

We can see that the RMSE is 1.810087. We can say that we are an average of 1.81 points away from our actual data with our model.

- 3.

Use the above model to estimate the value of X3 when X2 = 1.5, X4 = 5 and X5 = 10.

Figure 3: Prediction Model

```
> pred <- predict(var_model, newdata=data.frame(b1 = sin(1.5),
> pred <- predict(var_model, newdata=data.frame(b1 = sin(1.5),
+                                             b2 = (1.5)^3, b4 = 5,
+                                             b5 = log(10)))
> pred
      1
12.0316
>
>
>
> exact <- 8.7047*sin(1.5) + 5.3452*(1.5)^3 + -2.7565*5 + 3.2023*log(10) -8.2
825
>
> abs(exact - pred)
      1
8.784121e-05
```

Using our prediction model, we get that 12.0316 is the value if  $x_2 = 1.5$ ,  $x_4 = 5$  and  $x_5 = 10$ .

This is 8.784121e-05 away from our actual value. This shows us that our prediction values are very close to our actual value. This fact combined with a 0.998  $R^2$  value tells us that we have a near perfect model for our data.