

Method	Input	Iteration	Idea behind method	Required for convergence	Pros	Cons
Bisection	$f(x)$, interval (a,b)	X_{n+1} = midpoint of the interval where $f(a)f(b) < 0$.	From a starting window (a,b) , continually cut the window in half retaining that $f(a_{\text{new}})f(b_{\text{new}}) < 0$. This will make the window smaller and zoom it in on the true root.	$F(x)$ is continuous, $f(a)f(b) < 0$	Always finds solution.	Linear of rate 0.5.
Fixed Point	$F(x)$, x_0	$G(x) = g(x_{n-1})$	We find a $g(r) = r$ from a expression $f(x) = 0$. Then, $g(r) = r$ will converge on our answer using $g(x) = x + c \cdot f(x)$ as long as the neighborhood of the solution has derivative less than 1.	$G'(x) < 1$ near x^* , x_0 near x .	At least linear	Can diverge for some functions.
Newton	$F(x)$, x_0	$x_n = x_{n-1} - \frac{f(x_{n-1})}{f'(x_{n-1})}$	We use the slope around each guess to find the next point, which can be faster	$F(x)$ is twice differentiable, x_0 near root	Quadratic once it is in neighborhood of root	Can move randomly until it gets near root.
Secant	$F(x)$, x_0	$x_n = x_{n-1} - \frac{1}{m_{\text{sec}}} f(x_{n-1})$	Similar to Newton, but we don't need to find derivative of $f(x)$	Same as Newton	Rate of convergence is ~ 1.61 , doesn't need derivative	Not as fast as Newton