

Solution of Question 4.

Part (i)

The asymptotic time complexity of this problem depends on the iterations of for loop.

i.e.

For first iteration, $i = 1 = 2^0$

For second iteration $i = 2 = 2^1$

For last iteration, $i = n = 2^x$

Where $x = \log_2(n)$.

Therefore, Time Complexity is $O(\log_2(n))$.

Part(ii)

Outer for loop runs for n times. Inner for loop also runs for n times and it contains function i.e that also runs for n times. So $n(n \times n)$ i.e

$O(n^3)$

Upper bound is: $O(n^3)$

Lower bound is: $\Omega(n^3)$

Part(iib)

For $i < j$, $W[i][j]$ contains the sum $P[i] + P[i+1] + \dots + P[j]$

Part(iic)

We can use the value of W already computed in the previous iteration. This will improve the time complexity to $O(n^2)$. It's more like memo function.

```
for (x = 0; x < n; x++) {
```

```
    W[x][x] = P[x];
```

```
    for (y = x+1; y < n; y++) {
```

```
        W[x][y] = W[x][y-1] + P[y];
```

```
    }}
```