STATS 205: Final Project Write-Up

Brian Liu 6/14/2019

1. Background of the data and why it is interesting or important

The data we are using is the data from WHO suicide statistics from Kaggle. This gives population-based statistics on suicide rate (Szamil 2018).

The reason this data is interesting and important is that suicide is prevalent in many times and places around the world, but many places and times have different suicide rates. When it comes to suicide, there are many potential factors or attributes that may be correlated with an increased risk of suicide, such as:

- a person's sex
- the age group a person belongs to
- the generation a person was born in

The goal is to find significant correlations between these factors and suicide rates: that is, does x factor positively predict suicide rate?

The simple inspiration is suicide prevention: If we can identify the factors that correlate positively with, or predict high suicide rates, then we can target our suicide prevention efforts towards populations with those high-risk factors or attributes.

2. Explanation of the method studied and its properties

We will use the statistical techniques of nonparametric bootstrap and parametric bootstrap methods to aid in prediction, with linear regression as well (Kendall coefficient), and use cross-validation to test if, given new data for a population, this population is at risk of suicide. In other words, predict if the suicide rate would be abnormally or significantly high, and then compare the performance between the two methods (nonparametric and parametric).

Bootstrapping

In statistics, bootstrapping is any test or metric that relies on random sampling with replacement. Bootstrapping allows assigning measures of accuracy (defined in terms of bias, variance, confidence intervals, prediction error or some other such measure) to sample estimates (Efron and Tibshirani 1993; Efron 2003). This technique allows estimation of the sampling distribution of almost any statistic using random sampling methods. Generally, it falls in the broader class of resampling methods ("Bootstrap Methods," n.d.).

Bootstrapping is the practice of estimating properties of an estimator (such as its variance) by measuring those properties when sampling from an approximating distribution. One standard choice for an approximating distribution is the empirical distribution function of the observed data. In the case where a set of observations can be assumed to be from an independent and identically distributed population, this can be implemented by constructing a number of resamples with replacement, of the observed dataset (and of equal size to the observed dataset).

It may also be used for constructing hypothesis tests. It is often used as an alternative to statistical inference based on the assumption of a parametric model when that assumption is in doubt, or

where parametric inference is impossible or requires complicated formulas for the calculation of standard errors.

Nonparametric vs. Parametric bootstrap

Whereas nonparametric bootstraps make no assumptions about how your observations are distributed, and resample your original sample, parametric bootstraps resample a known distribution function, whose parameters are estimated from your sample. These bootstrap estimates are either used to attach confidence limits nonparametrically - or a second parametric model is fitted using parameters estimated from the distribution of the bootstrap estimates, from which confidence limits are obtained analytically. The advantages and disadvantages of this approach, compared to nonparametric bootstrapping, can be summarised as follows.

In the nonparametric bootstrap, samples are drawn from a discrete set of n observations. This can be a serious disadvantage in small sample sizes because spurious fine structure in the original sample, but absent from the population sampled, may be faithfully reproduced in the simulated data. Another concern is that because small samples have only a few values, covering a restricted range, nonparametric bootstrap samples underestimate the amount of variation in the population you originally sampled. As a result, statisticians generally see samples of 10 or less as too small for reliable nonparametric bootstrapping.

Small samples convey little reliable information about the higher moments of their population distribution function - in which case, a relatively simple function may be adequate.

Although parametric bootstrapping provides more power than the nonparametric bootstrap, it does so on the basis of an inherently arbitrary choice of model. Whilst the cumulative distribution of even quite small samples deviate little from that of their population, it can be far from easy to select the most appropriate mathematical function a priori. Maximum likelihood estimators are commonly used for parametric bootstrapping despite the fact that this criterion is nearly always based upon their large sample behaviour.

Choosing an appropriate parametric error structure for a statistic based upon small samples can be awkward to justify. Bootstrap t statistics present an additional problem, partly because of problems in estimating standard errors analytically, partly because of difficulties in working out a suitable number of degrees of freedom for your pivot's (presumed, but often large-sample-based) distribution.

So although parametric bootstrapping can be relatively straightforward to perform, and may be used to construct confidence intervals for the sample median of small samples, the bootstrap and estimator distribution functions are often very different. In addition, confidence limits may enclose invalid parameter values, and the coverage error is no better than nonparametric intervals.

Confusingly, whilst the parametric bootstrap is sometimes described as a basic bootstrap, resampling residuals is sometimes referred to as being 'semi parametric' - which is also used to describe test-inversion and smoothed sample bootstraps. Resampling residuals is most popularly used to obtain bootstrap confidence intervals for regression coefficients, for example in nonparametric regression. ("A Parametric or Non-Parametric Bootstrap?" n.d.)

Linear regression - Kendall rank correlation coefficient

In statistics, the Kendall rank correlation coefficient, commonly referred to as Kendall's tau coefficient (after the Greek letter τ), is a statistic used to measure the ordinal association between two measured quantities. A tau test is a non-parametric hypothesis test for statistical dependence based on the tau coefficient.

It is a measure of rank correlation: the similarity of the orderings of the data when ranked by each of the quantities. It is named after Maurice Kendall, who developed it in 1938 (Kendall 1938), though Gustav Fechner had proposed a similar measure in the context of time series in 1897 ("Measures of Association for Ordinal Data," n.d.).

Intuitively, the Kendall correlation between two variables will be high when observations have a similar (or identical for a correlation of 1) rank (i.e. relative position label of the observations within the variable: 1st, 2nd, 3rd, etc.) between the two variables, and low when observations have a dissimilar (or fully different for a correlation of -1) rank between the two variables.

Both Kendall's τ and Spearman's ρ can be formulated as special cases of a more general correlation coefficient.

Cross validation

Cross-validation, sometimes called rotation estimation (Geisser 1993) ("A Study of Cross-Validation and Bootstrap for Accuracy Estimation and Model Selection," n.d.) (Devijver and Kittler 1982), or out-of-sample testing is any of various similar model validation techniques for assessing how the results of a statistical analysis will generalize to an independent data set. It is mainly used in settings where the goal is prediction, and one wants to estimate how accurately a predictive model will perform in practice. In a prediction problem, a model is usually given a dataset of known data on which training is run (training dataset), and a dataset of unknown data (or first seen data) against which the model is tested (called the validation dataset or testing set). 2 et al. (n.d.)] ("Newbie Question: Confused About Train, Validation and Test Data!" n.d.). The goal of cross-validation is to test the model's ability to predict new data that was not used in estimating it, in order to flag problems like overfitting or selection bias [6] and to give an insight on how the model will generalize to an independent dataset (i.e., an unknown dataset, for instance from a real problem).

One round of cross-validation involves partitioning a sample of data into complementary subsets, performing the analysis on one subset (called the training set), and validating the analysis on the other subset (called the validation set or testing set). To reduce variability, in most methods multiple rounds of cross-validation are performed using different partitions, and the validation results are combined (e.g. averaged) over the rounds to give an estimate of the model's predictive performance.

In summary, cross-validation combines (averages) measures of fitness in prediction to derive a more accurate estimate of model prediction performance.[7]

3. Data analysis or simulation study

We will use the crude rate of suicide per 100,000 people.

This analysis provides information on age-standardized rates. . .

```
who_suicide_statistics_df <- read.csv("who_suicide_statistics.csv")
head(who_suicide_statistics_df)</pre>
```

```
country year
                                  age suicides_no population
                     sex
## 1 Albania 1985 female 15-24 years
                                               NA
                                                       277900
## 2 Albania 1985 female 25-34 years
                                               NA
                                                       246800
## 3 Albania 1985 female 35-54 years
                                               NA
                                                       267500
## 4 Albania 1985 female 5-14 years
                                               NA
                                                       298300
## 5 Albania 1985 female 55-74 years
                                               NA
                                                       138700
## 6 Albania 1985 female
                           75+ years
                                               NA
                                                        34200
```

```
## [6] "population"
    Filter and save countries with missing suicide rate.
library(tidyverse)
## Registered S3 methods overwritten by 'ggplot2':
    method
##
                    from
##
     [.quosures
                    rlang
##
     c.quosures
                    rlang
##
    print.quosures rlang
## -- Attaching packages ----- tidyverse 1.2.1 --
## v ggplot2 3.1.1
                       v purrr
                                 0.3.2
## v tibble 2.1.1
                       v dplyr
                                 0.8.1
## v tidyr
           0.8.3
                      v stringr 1.4.0
## v readr
            1.3.1
                      v forcats 0.4.0
## -- Conflicts ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()
                    masks stats::lag()
filtered_suicide_df <- drop_na(who_suicide_statistics_df, "suicides_no")
head(filtered_suicide_df)
##
      country year
                                  age suicides_no population
                      sex
## 25 Albania 1987 female 15-24 years
                                               14
                                                      289700
## 26 Albania 1987 female 25-34 years
                                                      257200
                                                4
## 27 Albania 1987 female 35-54 years
                                                6
                                                      278800
## 28 Albania 1987 female 5-14 years
                                                0
                                                      311000
## 29 Albania 1987 female 55-74 years
                                                0
                                                      144600
## 30 Albania 1987 female
                           75+ years
                                                       35600
                                                1
    After filtering countries with missing suicide rate, take a random sample of 100 countries and
    make sure each continent has approximately equal countries.
Filter countries by continent:
library(countrycode)
filtered_suicide_df$continent <- countrycode(sourcevar = filtered_suicide_df[, "country"],
                            origin = "country.name",
                            destination = "continent")
## Warning in countrycode(sourcevar = filtered_suicide_df[, "country"], origin = "country.name", : Some
## Warning in countrycode(sourcevar = filtered_suicide_df[, "country"], origin = "country.name", : Some
head(filtered_suicide_df)
##
      country year
                                  age suicides_no population continent
## 25 Albania 1987 female 15-24 years
                                               14
                                                      289700
                                                                Europe
## 26 Albania 1987 female 25-34 years
                                                4
                                                      257200
                                                                Europe
## 27 Albania 1987 female 35-54 years
                                                6
                                                      278800
                                                                Europe
## 28 Albania 1987 female 5-14 years
                                                0
                                                      311000
                                                                Europe
## 29 Albania 1987 female 55-74 years
                                                0
                                                      144600
                                                                Europe
## 30 Albania 1987 female
                           75+ years
                                                1
                                                       35600
                                                                Europe
```

"age"

"suicides_no"

colnames(who_suicide_statistics_df)

"year"

"sex"

[1] "country"

```
write.csv(filtered_suicide_df, 'filtered_suicide.csv')
Let us find out which continents are counted:
# Get list of continents
list_of_continents <- unique(filtered_suicide_df$continent); list_of_continents</pre>
## [1] "Europe"
                    "Americas" "Asia"
                                            "Oceania"
                                                        "Africa"
                                                                     NA
Therefore,
                           \frac{100 \text{ countries}}{6 \text{ continents}} \approx 16 \text{ to } 17 \text{ countries per continent}
we should randomly sample 17 countries from each continent.
Notably, there are countries that are not on any of the listed continents. Let us see which ones those are:
not_in_a_continent = filtered_suicide_df[is.na(filtered_suicide_df$continent),]
write.csv(not_in_a_continent, 'not_in_a_continent.csv')
head(not_in_a_continent)
##
                                           age suicides_no population continent
            country year
## 32317 Rodrigues 2001 female 15-24 years
                                                                               <NA>
## 32318 Rodrigues 2001 female 25-34 years
                                                          0
                                                                               <NA>
                                                                      NA
## 32319 Rodrigues 2001 female 35-54 years
                                                          0
                                                                      NA
                                                                               <NA>
## 32320 Rodrigues 2001 female 5-14 years
                                                          0
                                                                               <NA>
                                                                      NΑ
## 32321 Rodrigues 2001 female 55-74 years
                                                                               <NA>
## 32322 Rodrigues 2001 female
                                    75+ years
                                                                      NA
                                                                               <NA>
unique(not_in_a_continent$country)
## [1] Rodrigues
                               Virgin Islands (USA)
## 141 Levels: Albania Anguilla Antigua and Barbuda Argentina ... Zimbabwe
Let us make the choice not to include these countries in the analysis, since there are only two countries.
# Take off `NA` from list of continents
list_of_continents <- list_of_continents[-length(list_of_continents)]</pre>
list_of_continents
                    "Americas" "Asia"
## [1] "Europe"
                                            "Oceania" "Africa"
We will now create six dataframes, filtered by list of countries for each continent.
# library(rlist)
countries_per_continent <- list()</pre>
for (i in seq_along(list_of_continents))
{
    countries_per_continent[[i]] <- filtered_suicide_df[filtered_suicide_df$continent == list_of_contin
}
length(countries_per_continent)
## [1] 5
length(countries_per_continent)
## [1] 5
```

```
for (i in seq_along(countries_per_continent))
    print(head(countries_per_continent[[i]]))
    print(length(countries_per_continent[[i]]))
    cat("\n")
}
##
      country year
                                   age suicides_no population continent
                      sex
## 25 Albania 1987 female 15-24 years
                                                        289700
                                                                  Europe
## 26 Albania 1987 female 25-34 years
                                                                  Europe
                                                 4
                                                        257200
## 27 Albania 1987 female 35-54 years
                                                 6
                                                        278800
                                                                  Europe
## 28 Albania 1987 female 5-14 years
                                                 0
                                                        311000
                                                                  Europe
## 29 Albania 1987 female 55-74 years
                                                        144600
                                                                  Europe
## 30 Albania 1987 female
                                                         35600
                             75+ years
                                                  1
                                                                  Europe
## [1] 7
##
##
                                     age suicides_no population continent
        country year
                         sex
## 373 Anguilla 1983 female 15-24 years
                                                   0
                                                              NA
                                                                  Americas
## 374 Anguilla 1983 female 25-34 years
                                                   0
                                                              NA
                                                                  Americas
## 375 Anguilla 1983 female 35-54 years
                                                   0
                                                              NA
                                                                  Americas
## 376 Anguilla 1983 female 5-14 years
                                                   0
                                                              NA
                                                                  Americas
## 377 Anguilla 1983 female 55-74 years
                                                   0
                                                              NA
                                                                  Americas
## 378 Anguilla 1983 female
                               75+ years
                                                   0
                                                              NA
                                                                  Americas
## [1] 7
##
##
        country year
                         sex
                                     age suicides_no population continent
## 1501 Armenia 1981 female 15-24 years
                                                   5
                                                          348000
                                                                      Asia
## 1502 Armenia 1981 female 25-34 years
                                                   6
                                                          242200
                                                                      Asia
## 1503 Armenia 1981 female 35-54 years
                                                   6
                                                          333500
                                                                      Asia
## 1504 Armenia 1981 female 5-14 years
                                                   0
                                                          295200
                                                                      Asia
## 1505 Armenia 1981 female 55-74 years
                                                   10
                                                          164300
                                                                      Asia
## 1506 Armenia 1981 female
                                                   7
                               75+ years
                                                           43100
                                                                      Asia
## [1] 7
##
          country year
##
                           sex
                                       age suicides_no population continent
## 2161 Australia 1979 female 15-24 years
                                                    71
                                                           1236800
                                                                     Oceania
## 2162 Australia 1979 female 25-34 years
                                                     86
                                                           1138500
                                                                     Oceania
## 2163 Australia 1979 female 35-54 years
                                                    171
                                                           1572100
                                                                     Oceania
## 2164 Australia 1979 female 5-14 years
                                                      1
                                                           1246500
                                                                     Oceania
## 2165 Australia 1979 female 55-74 years
                                                   135
                                                           1137800
                                                                     Oceania
## 2166 Australia 1979 female
                                75+ years
                                                     15
                                                            309900
                                                                     Oceania
## [1] 7
##
##
                                        age suicides_no population continent
           country year
                            sex
## 7669 Cabo Verde 2011 female 15-24 years
                                                       1
                                                              56039
                                                                       Africa
## 7670 Cabo Verde 2011 female 25-34 years
                                                       0
                                                              38528
                                                                       Africa
## 7671 Cabo Verde 2011 female 35-54 years
                                                       2
                                                              49078
                                                                       Africa
## 7672 Cabo Verde 2011 female 5-14 years
                                                       0
                                                              56558
                                                                       Africa
## 7673 Cabo Verde 2011 female 55-74 years
                                                       2
                                                              19887
                                                                       Africa
## 7674 Cabo Verde 2011 female
                                  75+ years
                                                       0
                                                               7582
                                                                       Africa
## [1] 7
```

This text links to very important information about why a for loop doesn't print anything.¹

¹Basically, for loops are functions themselves. R prints out the result of a command automatically, but functions are not

Link to Pandoc Markdown formatting

Randomly sample 17 countries from each continent:

```
list of continents
## [1] "Europe"
                  "Americas" "Asia"
                                         "Oceania" "Africa"
for (i in seq_along(countries_per_continent))
    print(list_of_continents[i])
    countries <- unique(countries_per_continent[[i]]$country)</pre>
    print(countries)
    print(length(countries))
    cat("\n")
}
## [1] "Europe"
  [1] Albania
                                Austria
##
                                                        Belarus
    [4] Belgium
                                Bosnia and Herzegovina Bulgaria
##
  [7] Croatia
                                Czech Republic
                                                        Denmark
## [10] Estonia
                                Finland
                                                        France
## [13] Germany
                                Greece
                                                        Hungary
## [16] Iceland
                                Ireland
                                                        Italy
## [19] Latvia
                                Lithuania
                                                        Luxembourg
## [22] Malta
                                Monaco
                                                        Montenegro
## [25] Netherlands
                                Norway
                                                        Poland
## [28] Portugal
                                Republic of Moldova
                                                        <NA>
## [31] Romania
                                Russian Federation
                                                        San Marino
## [34] Serbia
                                Slovakia
                                                        Slovenia
## [37] Spain
                                Sweden
                                                        Switzerland
## [40] TFYR Macedonia
                                Ukraine
                                                        United Kingdom
## 141 Levels: Albania Anguilla Antigua and Barbuda Argentina ... Zimbabwe
## [1] 42
##
## [1] "Americas"
   [1] Anguilla
                                            Antigua and Barbuda
##
   [3] Argentina
                                            Aruba
   [5] Bahamas
##
                                            Barbados
##
  [7] Belize
                                            Bermuda
  [9] Bolivia
                                            Brazil
## [11] British Virgin Islands
                                            Canada
## [13] Cayman Islands
                                            Chile
## [15] Colombia
                                            Costa Rica
## [17] Cuba
                                            Dominica
## [19] Dominican Republic
                                            Ecuador
## [21] El Salvador
                                            Falkland Islands (Malvinas)
## [23] French Guiana
                                            Grenada
## [25] Guadeloupe
                                            Guatemala
## [27] Guyana
                                            Haiti
## [29] Honduras
                                            Jamaica
## [31] Martinique
                                            Mexico
                                            Netherlands Antilles
## [33] Montserrat
```

inherently a command, and since for loops are functions, nothing will be printed. The solution is to have print(command()) within the for loop to get output for your for loop. You will never again spend hours trying to find out why a for loop doesn't print anything because you're no longer an R newbie.

```
## [35] Nicaragua
                                           Panama
## [37] Paraguay
                                           Peru
## [39] Puerto Rico
                                           <NA>
                                           Saint Lucia
## [41] Saint Kitts and Nevis
## [43] Saint Pierre and Miquelon
                                           Saint Vincent and Grenadines
## [45] Suriname
                                           Trinidad and Tobago
## [47] Turks and Caicos Islands
                                           United States of America
## [49] Uruguay
                                           Venezuela (Bolivarian Republic of)
## 141 Levels: Albania Anguilla Antigua and Barbuda Argentina ... Zimbabwe
## [1] 50
##
## [1] "Asia"
## [1] Armenia
                                       Azerbaijan
## [3] Bahrain
                                       Brunei Darussalam
## [5] Cyprus
                                       Georgia
## [7] Hong Kong SAR
                                       Iran (Islamic Rep of)
## [9] Iraq
                                       Israel
## [11] Japan
                                       Jordan
## [13] Kazakhstan
                                       Kuwait
## [15] Kyrgyzstan
                                       Macau
## [17] Malaysia
                                       Maldives
## [19] Mongolia
                                       Occupied Palestinian Territory
## [21] Oman
                                       Philippines
## [23] Qatar
                                       Republic of Korea
## [25] <NA>
                                       Saudi Arabia
## [27] Singapore
                                       Sri Lanka
## [29] Syrian Arab Republic
                                       Tajikistan
## [31] Thailand
                                       Turkey
## [33] Turkmenistan
                                       United Arab Emirates
## [35] Uzbekistan
## 141 Levels: Albania Anguilla Antigua and Barbuda Argentina ... Zimbabwe
## [1] 35
##
## [1] "Oceania"
## [1] Australia
                   Fiji
                               Kiribati
                                           New Zealand <NA>
## 141 Levels: Albania Anguilla Antigua and Barbuda Argentina ... Zimbabwe
## [1] 5
##
## [1] "Africa"
## [1] Cabo Verde
                              Egypt
                                                    Mauritius
## [4] Mayotte
                              Morocco
                                                    Reunion
## [7] <NA>
                              Sao Tome and Principe Seychelles
## [10] South Africa
                              Tunisia
                                                    Zimbabwe
## 141 Levels: Albania Anguilla Antigua and Barbuda Argentina ... Zimbabwe
```

Since there are only 5 countries in Oceania and 12 countries in Africa, we will use all 5 countries of Oceania and all 12 countries of Africa.

```
samples_of_countries <- list()
num_samples <- 17
for (i in seq_along(countries_per_continent))
{
    countries <- unique(countries_per_continent[[i]]$country)
    current_sample <- list()</pre>
```

```
if (length(countries) >= num_samples)
        current_sample <- sample(countries, 17)</pre>
    } else {
        current_sample <- sample(countries, length(countries))</pre>
    samples_of_countries[[i]] <- current_sample</pre>
}
Let's see the countries that we will be sampling:
total <- 0
for (i in seq_along(samples_of_countries))
    print(list_of_continents[i])
    print(samples_of_countries[[i]])
    print(length(samples_of_countries[[i]]))
    total <- total + length(samples_of_countries[[i]])</pre>
    cat("\n")
}
## [1] "Europe"
## [1] Norway
                             Poland
                                                  Austria
## [4] Serbia
                             <NA>
                                                  TFYR Macedonia
## [7] United Kingdom
                             Switzerland
                                                  Ukraine
## [10] Albania
                             Finland
                                                  Ireland
## [13] Italy
                             Republic of Moldova Romania
                             Czech Republic
## [16] Greece
## 141 Levels: Albania Anguilla Antigua and Barbuda Argentina ... Zimbabwe
## [1] 17
##
## [1] "Americas"
## [1] Saint Lucia
                                   Nicaragua
## [3] Bermuda
                                   Antigua and Barbuda
## [5] Chile
                                   Saint Pierre and Miquelon
## [7] Bahamas
                                   Peru
## [9] Bolivia
                                   Trinidad and Tobago
## [11] Grenada
                                   Guadeloupe
## [13] Haiti
                                   Colombia
## [15] Panama
                                   <NA>
## [17] Suriname
## 141 Levels: Albania Anguilla Antigua and Barbuda Argentina ... Zimbabwe
## [1] 17
##
## [1] "Asia"
                                        Azerbaijan
## [1] Armenia
## [3] Occupied Palestinian Territory Kyrgyzstan
## [5] Cyprus
                                        Japan
## [7] Syrian Arab Republic
                                        Singapore
## [9] <NA>
                                        Kuwait
## [11] Macau
                                        Thailand
## [13] United Arab Emirates
                                        Brunei Darussalam
## [15] Turkmenistan
                                        Philippines
## [17] Mongolia
## 141 Levels: Albania Anguilla Antigua and Barbuda Argentina ... Zimbabwe
```

```
## [1] 17
##
## [1] "Oceania"
## [1] <NA>
                   Kiribati
                               Fiji
                                            Australia
                                                        New Zealand
## 141 Levels: Albania Anguilla Antigua and Barbuda Argentina ... Zimbabwe
## [1] 5
##
## [1] "Africa"
   [1] Seychelles
                              Egypt
                                                     Morocco
  [4] Mayotte
                              Cabo Verde
                                                     Tunisia
## [7] Mauritius
                              Reunion
                                                     <NA>
## [10] Zimbabwe
                              South Africa
                                                     Sao Tome and Principe
## 141 Levels: Albania Anguilla Antigua and Barbuda Argentina ... Zimbabwe
## [1] 12
total
```

[1] 68

Let's filter the original dataframe only to include countries that we have sampled:

```
countries_to_test <- list()
a <- 0
for (i in seq_along(samples_of_countries))
{
    # find out a way to access each country name
    # print each country name
    for (j in seq_along(samples_of_countries[[i]]))
    {
        sample <- samples_of_countries[[i]]
        country_string <- toString(sample[[j]]))
        countries_to_test[a] <- country_string
        a <- a + 1
    }
}
length(countries_to_test)</pre>
```

```
## [1] 67
# countries_to_test
```

4. Interpretation of the results or discussion

5. References

2, Alexander Galkin Alexander Galkin 5, mohsen najafzadehmohsen najafzadeh 2, innovIsmailinnovIsmail 75753, Ryan ZottiRyan Zotti 3, Frank HarrellFrank Harrell 56.9k4115247, Yu ZhouYu Zhou 22122, et al. n.d. "What Is the Difference Between Test Set and Validation Set?" *Cross Validated.* https://stats.stackexchange.com/questions/19048/what-is-the-difference-between-test-set-and-validation-set/19051#19051.

"A Parametric or Non-Parametric Bootstrap?" n.d. Parametric or Non-Parametric Bootstrap. https://influentialpoints.com/Training/nonparametric-or-parametric_bootstrap.htm.

"A Study of Cross-Validation and Bootstrap for Accuracy Estimation and Model Selection." n.d. *ACM Digital Library*. Morgan Kaufmann Publishers Inc. https://dl.acm.org/citation.cfm?id=1643047.

"Bootstrap Methods." n.d. From Wolfram MathWorld. http://mathworld.wolfram.com/BootstrapMethods. html.

Devijver, Pierre A., and Josef Kittler. 1982. Pattern Recognition: A Statistical Approach. Sung Kang.

Efron, Bradley. 2003. Second Thoughts on the Bootstrap. Department of Biostatistics, Stanford University.

Efron, Bradley, and Robert Tibshirani. 1993. An Introduction to the Bootstrap. Chapman; Hall.

Geisser, Seymour. 1993. Predictive Inference: An Introduction. Chapman & Hall.

Kendall, M. G. 1938. "A New Measure of Rank Correlation." Biometrika 30 (1/2): 81. https://doi.org/10.2307/2332226.

"Measures of Association for Ordinal Data." n.d. Measures of Association, 64–85. https://doi.org/10.4135/9781412984942.n5.

"Newbie Question: Confused About Train, Validation and Test Data!" n.d. Newbie Question: Confused About Train, Validation and Test Data! | Heaton Research. https://web.archive.org/web/20150314221014/http://www.heatonresearch.com/node/1823.

Szamil. 2018. "WHO Suicide Statistics." Kaggle. https://www.kaggle.com/szamil/who-suicide-statistics.