

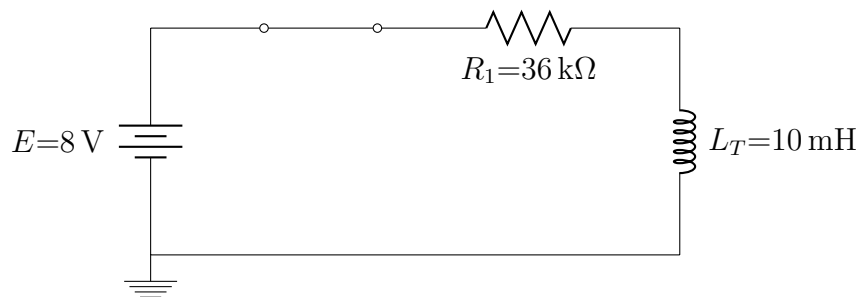
Figure 1: Use this circuit for questions 1 through 3

1. Calculate the total inductance L_T of the circuit in Fig. 1

$$L_T = \frac{1}{\frac{1}{L_1} + \frac{1}{L_2}} = \frac{L_1 \cdot L_2}{L_1 + L_2} = \frac{12.5 \text{ mH} \cdot 50 \text{ mH}}{12.5 \text{ mH} + 50 \text{ mH}} = \boxed{10 \text{ mH}}$$

2. Storage Phase (switch is closed)

- (a) Redraw the circuit in Fig. 1 for the storage phase



- (b) Determine the time constant τ of the circuit in Fig. 1 during the storage phase

$$\tau = \frac{L_T}{R_1} = \frac{10 \text{ mH}}{36 \text{ k}\Omega} = \boxed{0.278 \text{ }\mu\text{sec}}$$

- (c) The switch closes at $t = 0$. Write a mathematical expression for the current i_L through the total inductor L_T

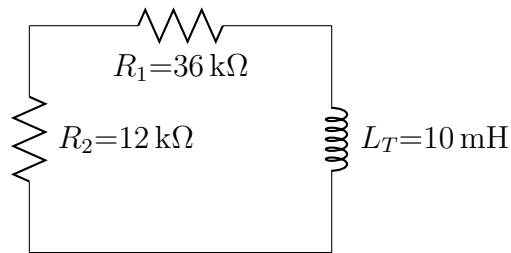
$$i_L = \frac{E}{R_1}(1 - e^{-t/\tau}) = \frac{8 \text{ V}}{36 \text{ k}\Omega}(1 - e^{-t/0.278 \text{ }\mu\text{sec}}) = \boxed{0.222 \text{ mA}(1 - e^{-t/0.278 \text{ }\mu\text{sec}})}$$

- (d) The switch closes at $t = 0$. Write a mathematical expression for the voltage v_L across the total inductor L_T

$$v_L = E(1 - e^{-t/\tau}) = \boxed{8 \text{ V}(e^{-t/0.278 \text{ }\mu\text{sec}})}$$

3. Decay Phase (switch is opened after reaching steady state)

(a) Redraw the circuit in Fig. 1 for the decay phase



(b) Determine the time constant τ of the circuit in Fig. 1 during the decay phase

$$\tau = \frac{L_T}{R_1 + R_2} = \frac{10 \text{ mH}}{36 \text{ k}\Omega + 12 \text{ k}\Omega} = \boxed{0.208 \text{ }\mu\text{sec}}$$

(c) The switch is opened after reaching steady state, write a mathematical expression for the current i_L through the total inductor L_T .

$$i_L = i_{Lmax}(e^{-t/0.208 \text{ }\mu\text{sec}}) = \boxed{0.222 \text{ mA}(e^{-t/0.208 \text{ }\mu\text{sec}})}$$

(d) The switch is opened after reaching steady state, write a mathematical expression for the voltage drop v_L across the total inductance L_T .

$$v_L = -V_i(e^{-t/0.208 \text{ }\mu\text{sec}})$$

where

$$V_i = (1 + \frac{R_2}{R_1})E = -(1 + \frac{12 \text{ k}\Omega}{36 \text{ k}\Omega})8 = 10.67 \text{ V}$$

therefore

$$v_L = -v_i(e^{-t/0.208 \text{ }\mu\text{sec}}) = \boxed{-10.67(e^{-t/0.208 \text{ }\mu\text{sec}})}$$

or use KVL.

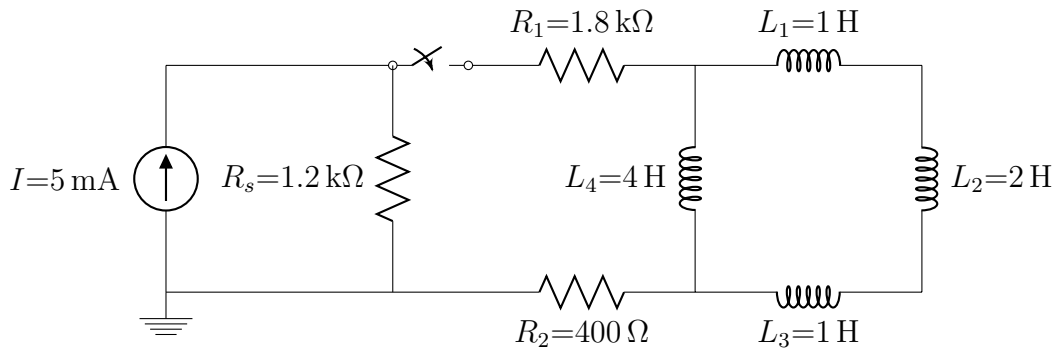


Figure 2: Use this circuit for questions 4 through 8

4. Determine the total inductance of the circuit L_T in Fig. 2

$$L'_1 = L_1 + L_2 + L_3 = 1 \text{ H} + 2 \text{ H} + 1 \text{ H} = 4 \text{ H}$$

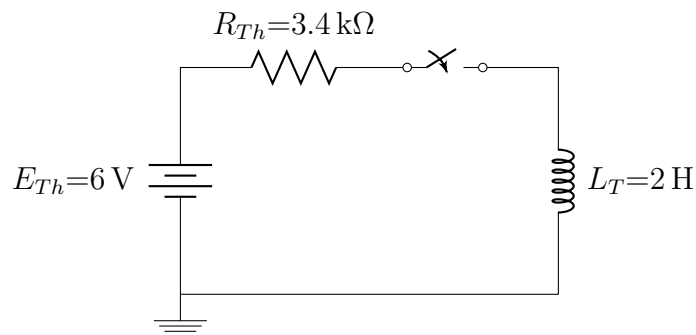
$$L_T = L_4 || L'_1 = \frac{L_4 \cdot L'_1}{L_4 + L'_1} = \frac{4 \text{ H} \cdot 4 \text{ H}}{4 \text{ H} + 4 \text{ H}} = \boxed{2 \text{ H}}$$

5. Determine the Thevenin voltage E_{Th} and Thevenin resistance R_{Th} of the circuit in Fig. 2

$$E_{Th} = I \cdot R_s = 5 \text{ mA} \cdot 1.2 \text{ k}\Omega = \boxed{6 \text{ V}}$$

$$R_{Th} = R_1 + R_s + R_2 = 1.8 \text{ k}\Omega + 1.2 \text{ k}\Omega + 400 \Omega = \boxed{3.4 \text{ k}\Omega}$$

6. Redraw the circuit in Fig. 2 using the Thevenin voltage E_{Th} , Thevenin resistance R_{Th} , and total inductance L_T



7. Determine the time constant τ of the circuit in Fig. 2 during the storage cycle

$$\tau = \frac{L_T}{R_{Th}} = \frac{2 \text{ H}}{3.4 \text{ k}\Omega} = \boxed{588.2 \text{ }\mu\text{ sec}}$$

8. After closing the switch, what is the final steady-state voltage value across R_{Th} ?

$$v_R = E(1 - e^{-t/\tau})$$

Therefore the final steady state voltage is

$$E = 6 \text{ V}$$

Alternate:

- 1) Use KVL (with $I_{L\max}$ flowing through R_{TH})

or

- 2) Recall: since we are in steady-state, L_T acts like a short-circuit and hence $V_{RTH} = E_{TH} = 6\text{V}$.