

For the circuit shown above, answer the following questions:

1. Calculate Z_T :

- A) $(1.20\text{k} + j4.10\text{k}) \Omega$
- B) $(1.20\text{k} - j8.10\text{k}) \Omega$
- C) $(1.20\text{k} - j4.10\text{k}) \Omega$**
- D) $(1.20\text{k} + j8.10\text{k}) \Omega$

$$X_C = 6.1\text{K} \Omega \quad X_L = 2.0\text{K} \Omega$$

$$Z_T = R + jX_L - jX_C = 1.2\text{K} + j2\text{K} - j6.1 = (1.20\text{k} - j4.10\text{k})$$

2. Determine V_L :

- A) 2.8 Vrms $\angle -136^\circ$
- B) 2.0 Vrms $\angle -136^\circ$**
- C) 2.0 Vrms $\angle -14^\circ$
- D) 2.8 Vrms $\angle -14^\circ$

$$I_T = E_s / Z_T = 4.24\text{Vrms} \angle 60^\circ / 4.27\text{K} \angle -73.7^\circ$$

$$I_T = 993\mu\text{Arms} \angle 134^\circ$$

$$V_L = jX_L * I_T = 1.98 \text{ Vrms} \angle 224^\circ \rightarrow -136^\circ$$

3. At what frequency is X_L equivalent to X_C ?

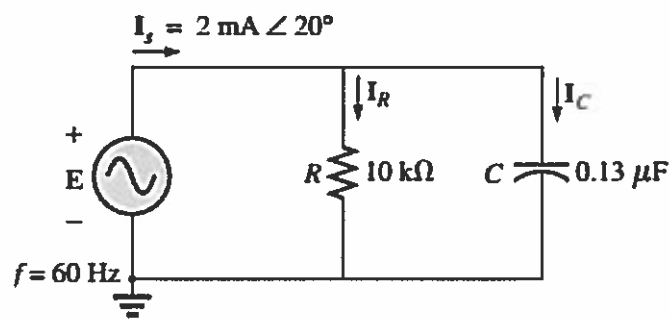
- A) 443 Hz
- B) 886 Hz
- C) 5560 Hz**
- D) 11.1K Hz

$$F_R = 1 / (2 * \pi * \sqrt{L * C}) = 1 / (2 * \pi * \sqrt{0.1 * 8200\text{pF}}) = 5558\text{Hz}$$

4. At the frequency at which $X_L = X_C$, $|Z_T|$ will:

- A) Increase from its value at 20,000 r/s
- B) Decrease from its value at 20,000 r/s**
- C) Stay the same as its value at 20,000 r/s
- D) Reach its maximum value

X_L will cancel X_C leaving only R



$$I_s = 2\text{mA}_{\text{RMS}} \angle 20^\circ$$

For the circuit shown above, answer the following questions:

5. Find Y_T , the total admittance looking into the network from the source:

- (A) $111\mu \text{ mhos} \angle 26^\circ$ $Y_T = (1/R) + (1/-jX_C)$ where $X_C = 20.4K \Omega$
 B) $500\mu \text{ mhos} \angle -79^\circ$ $Y_T = (1/R) + (1/-jX_C)$
 C) $500\mu \text{ mhos} \angle 26^\circ$ $Y_T = 100\text{u mhos} + j 49.0\text{u mhos} = 111\mu \text{ mhos} \angle 26^\circ$
 D) $111\mu \text{ mhos} \angle -64^\circ$

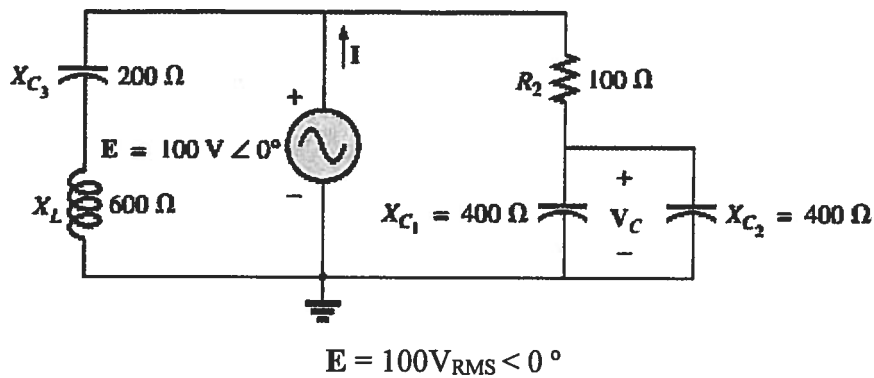
6. Determine the value of E :

- A) $18 V_{\text{RMS}} \angle 84^\circ$ $E = I_s / Y_T = 2\text{ma} \angle 20^\circ / 111\mu \text{ mhos} \angle 26^\circ = 18\text{Vrms} \angle -6.1^\circ$
 (B) $18 V_{\text{RMS}} \angle -6^\circ$
 C) $20 V_{\text{RMS}} \angle 20^\circ$
 D) $4 V_{\text{RMS}} \angle -6^\circ$

7. As the frequency is increased above 60Hz, what happens to I_R and I_C ?

- A) I_R remains the same but I_C will decrease
 B) I_R and I_C will remain the same
 (C) I_R remains the same but I_C will increase
 D) I_C remains the same but I_R will increase

$$\text{as } f \uparrow, X_C \downarrow, I_C \uparrow \\ \text{and } I_R \rightarrow$$



For the circuit shown above, answer the following questions:

8. Find Z_T , the total impedance looking into the network from the source:

- A) $783 \Omega \angle -7^\circ$
- B) $563 \Omega \angle -86^\circ$
- C) $783 \Omega \angle +86^\circ$
- ☒ D) $400 \Omega \angle -37^\circ$

$$\vec{Z}_T = \vec{Z}_1 \parallel (\vec{Z}_2 + \vec{Z}_3)$$

$$\vec{Z}_1 = (-j200 + j600) \Omega$$

$$\vec{Z}_2 = 100 \Omega$$

$$\vec{Z}_3 = -j200 \Omega$$

$$\vec{Z}_T = (+j400) \Omega \parallel (100 - j200) \Omega$$

$$\boxed{\vec{Z}_T = 400 \Omega \angle -36.9^\circ}$$

9. Determine the value of V_C :

- ☒ A) $89.4 V_{RMS} \angle -26.6^\circ$
- B) $97.1 V_{RMS} \angle -14.0^\circ$
- C) $66.7 V_{RMS} \angle -41.0^\circ$
- D) $53.2 V_{RMS} \angle -14.0^\circ$

$$\vec{V}_C = \vec{E} \left(\frac{\vec{Z}_3}{\vec{Z}_2 + \vec{Z}_3} \right) = 100 V_{RMS} \angle 0^\circ \frac{-j200 \Omega}{(100 - j200) \Omega}$$

$$\boxed{\vec{V}_C = 89.4 V_{RMS} \angle -26.6^\circ}$$

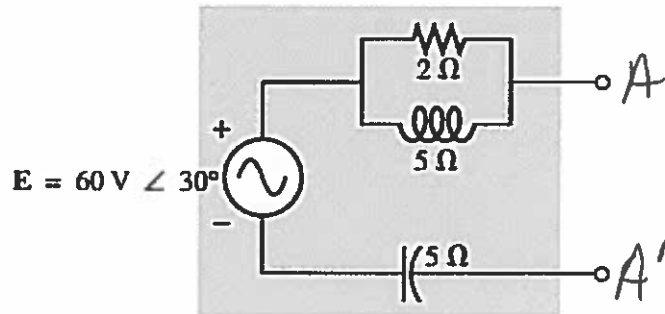
10. If the source frequency is 5 kHz, find the value of C_1 :

- ☒ A) 79.6 nF
- B) 796 nF
- C) 38.9 nF
- D) 398 nF

$$X_{C1} = \frac{1}{2\pi f C_1}$$

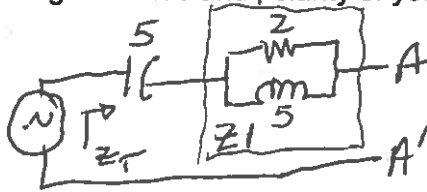
$$400 \Omega = \frac{1}{2\pi (5 \text{ kHz}) C_1}$$

$$\therefore \boxed{C_1 = 79.6 \text{ nF}}$$



$$E = 60V_{RMS} \angle 30^\circ$$

11. Convert the voltage source shown above to an equivalent current source. Make sure you label the terminals on both sources appropriately and draw the complete schematic diagram including the value and polarity of your current source:



$$Z_1 = \frac{2 \angle 0^\circ \cdot 5 \angle -90^\circ}{2 + j5} = 1.86 \angle -21.8^\circ$$

$$= 1.73 - j0.69$$

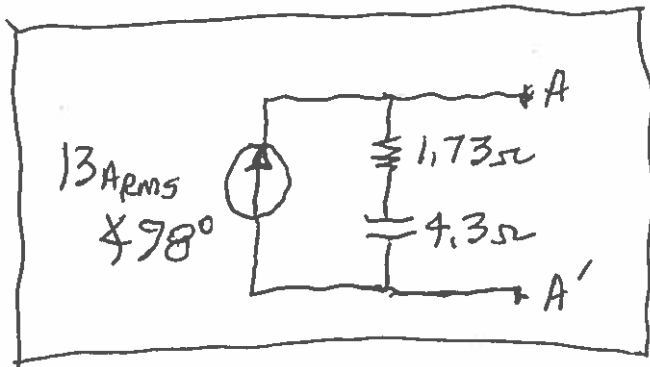
$$Z_T = -j5 + (1.73 - j0.69)$$

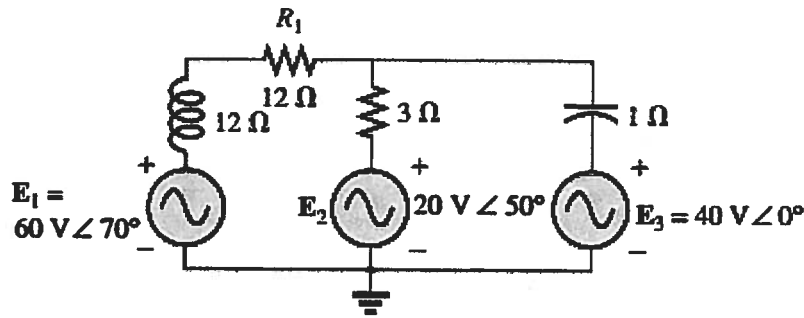
$$Z_T = 1.73 - j4.3$$

$$Z_T = 4.63 \angle -68.1^\circ$$

$$I_{SC} = \frac{60V \angle 30^\circ}{4.63 \angle -68.1^\circ}$$

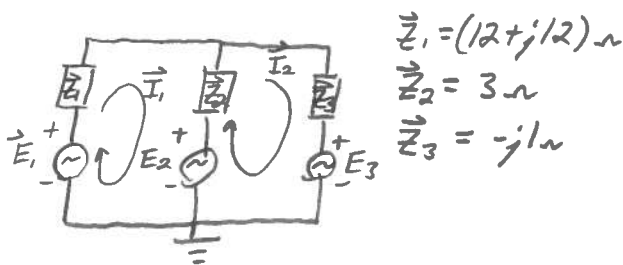
$$= 12.96 \angle 98.1^\circ A_{RMS}$$





Voltage source values in RMS

12. Develop the MESH equations for the circuit shown above. Convert the circuit to impedance boxes and show your MESH currents on this circuit. Box-in your MESH equations once you have them in their simplest form:



$$\begin{aligned} \vec{E}_1 &= 60V_{RMS} \angle 70^\circ \\ \vec{E}_2 &= 20V_{RMS} \angle 50^\circ \\ \vec{E}_3 &= 40V_{RMS} \angle 0^\circ \end{aligned}$$

$$AX = B \text{ FOR } A$$

$$A = \begin{bmatrix} (15 + j12) & (-3) \\ (-3) & (3 - j1) \end{bmatrix}$$

$$B = \begin{bmatrix} 41.77 \angle 79.43^\circ \\ 31.17 \angle 150.6^\circ \end{bmatrix}$$

$$X = \begin{bmatrix} \vec{I}_1 \\ \vec{I}_2 \end{bmatrix}$$

$$X = A^{-1}B = \begin{bmatrix} 3.099 \angle 72.53^\circ \\ 10.85 \angle 153.7^\circ \end{bmatrix}$$

\vec{I}_1
 \vec{I}_2

$$\vec{I}_1: \vec{E}_1 - \vec{I}_1 \vec{Z}_1 - (\vec{I}_1 - \vec{I}_2) \vec{Z}_2 - \vec{E}_2 = 0$$

$$\vec{I}_1 (\vec{Z}_1 + \vec{Z}_2) - \vec{I}_2 \vec{Z}_2 = \vec{E}_1 - \vec{E}_2 \quad (1)$$

$$\vec{I}_2: \vec{E}_2 - (\vec{I}_2 - \vec{I}_1) \vec{Z}_2 - \vec{I}_2 \vec{Z}_3 - \vec{E}_3 = 0$$

$$-\vec{I}_1 \vec{Z}_2 + \vec{I}_2 (\vec{Z}_2 + \vec{Z}_3) = \vec{E}_2 - \vec{E}_3 \quad (2)$$

OR:

$$\begin{aligned} \vec{I}_1 (15 + j12) - \vec{I}_2 (3) &= 41.77 \angle 79.43^\circ \\ -\vec{I}_1 (3) + \vec{I}_2 (3 - j1) &= 31.17 \angle 150.6^\circ \end{aligned}$$

13. Find the average power delivered by source E3 in the circuit shown above:

$$P_{AVE} = |\vec{E}_3|_{RMS} |\vec{I}_3|_{RMS} \cos(\theta_{\vec{E}_3} - \theta_{\vec{I}_3})$$

$$|\vec{E}_3|_{RMS} = 40V, \theta_{\vec{E}_3} = 0^\circ$$

$$\vec{I}_3 = -\vec{I}_2 = 10.85A_{RMS} \angle -26.3^\circ$$

$$\therefore |\vec{I}_3|_{RMS} = 10.85A, \theta_{\vec{I}_3} = -26.3^\circ$$

$$P_{AVE} = (40V)(10.85A) \cos(26.3^\circ)$$

$$\boxed{389.1W}$$