## Higher Order Nonhomogeneous Equations

## MATH 211 - 01

1. Solve the following higher order homogeneous equations.

a. 
$$y'' + 2y' + y = x$$

b. 
$$y'' + 5y' + 6y = 3x^2$$

c. 
$$y'' - 7y' + 6y = e^x$$

d. 
$$y'' - 2y' + 7y = xe^{2x}$$

e. 
$$2y'' + 5y = \sin x$$

f. 
$$3y'' - 2y' + 4y = \cos 2x$$

g. 
$$y'' + y = \sin x$$

h. 
$$y''' - y' = 3e^x$$

i. 
$$2y^{(4)} - 8y'' = 2$$

j. 
$$y^{(4)} - 4y'' + 4y = \sin x + e^x$$

k. 
$$y''' - 3y'' + 3y' - y = x^2 e^x$$

2. Solve the following initial value problems.

a. 
$$y'' + 6y' + 9y = x^2 - 2x$$
,  $y(0) = 0$ ,  $y'(0) = -1$ 

b. 
$$y'' - y' = \sin 2x$$
,  $y(0) = 1$ ,  $y'(0) = 0$ 

c. 
$$y'' + 3y' = \cos x$$
,  $y(0) = 1$ ,  $y'(0) = 1$ 

d. 
$$y^{(5)} - y''' = 2$$
,  $y(0) = y'(0) = y''(0) = 0$ ,  $y'''(0) = y^{(4)}(0) = 1$