



JOHNS HOPKINS

WHITING SCHOOL
of ENGINEERING



Introduction to Neural Networks

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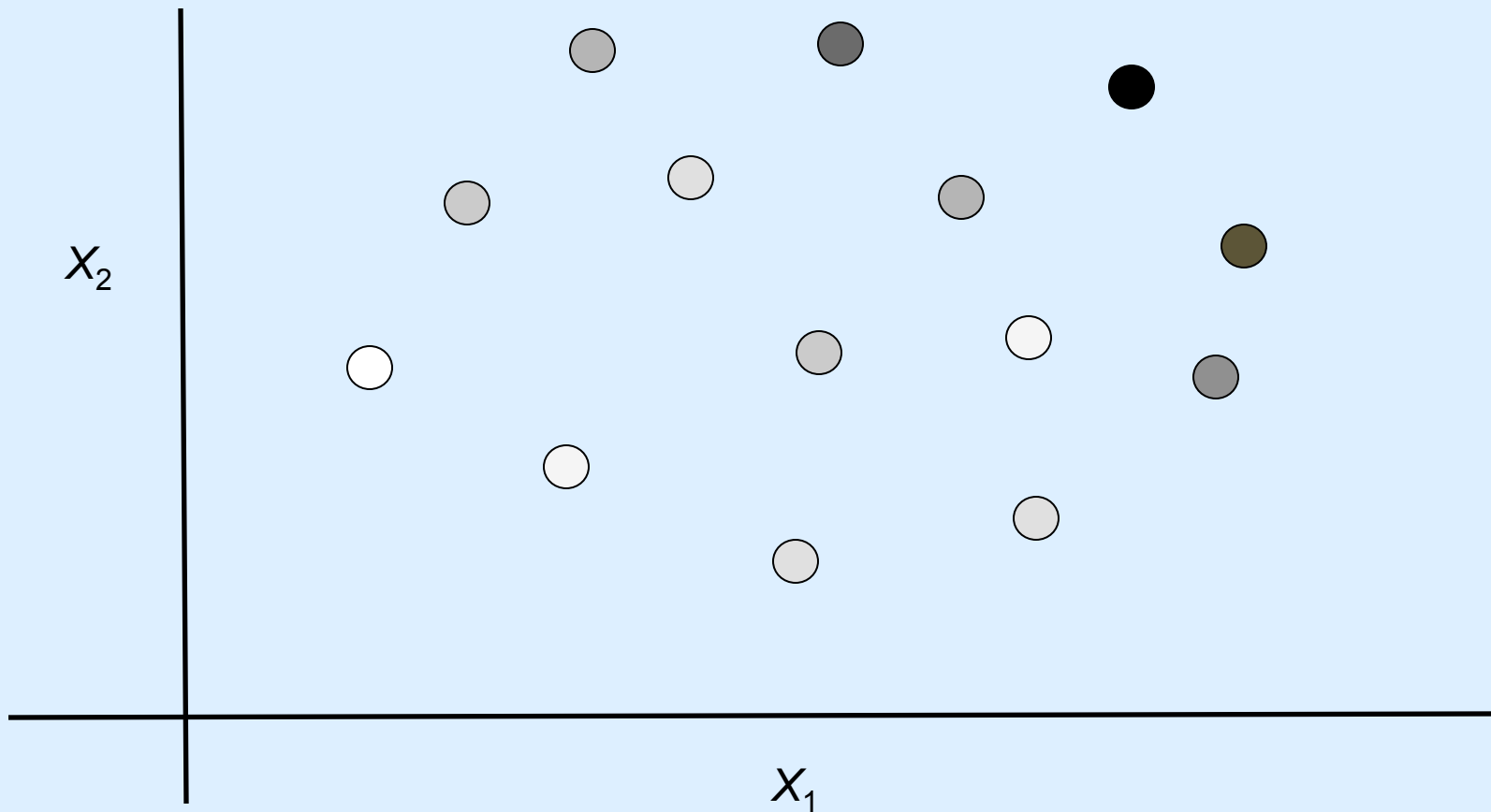
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Module 7.1: The Training Process

This Sub-Module Covers ...

- What a typical training scenario looks like.
- Issues that arise during the training process.
 - Overtraining and efficiency
 - Lay the groundwork for describing procedures to handle multiple input/output data pairs and related issues
 - Motivate important performance measures covered in subsequent sub-modules

A Classification Problem



Can A Neural Network Model a Polynomial?

- From the manner of training a Neural Network, they can
 - Interpolate data given the training data.
 - Can they model a polynomial?
- How can we mathematically define a polynomial given specific data?

Collocation Method of Polynomials

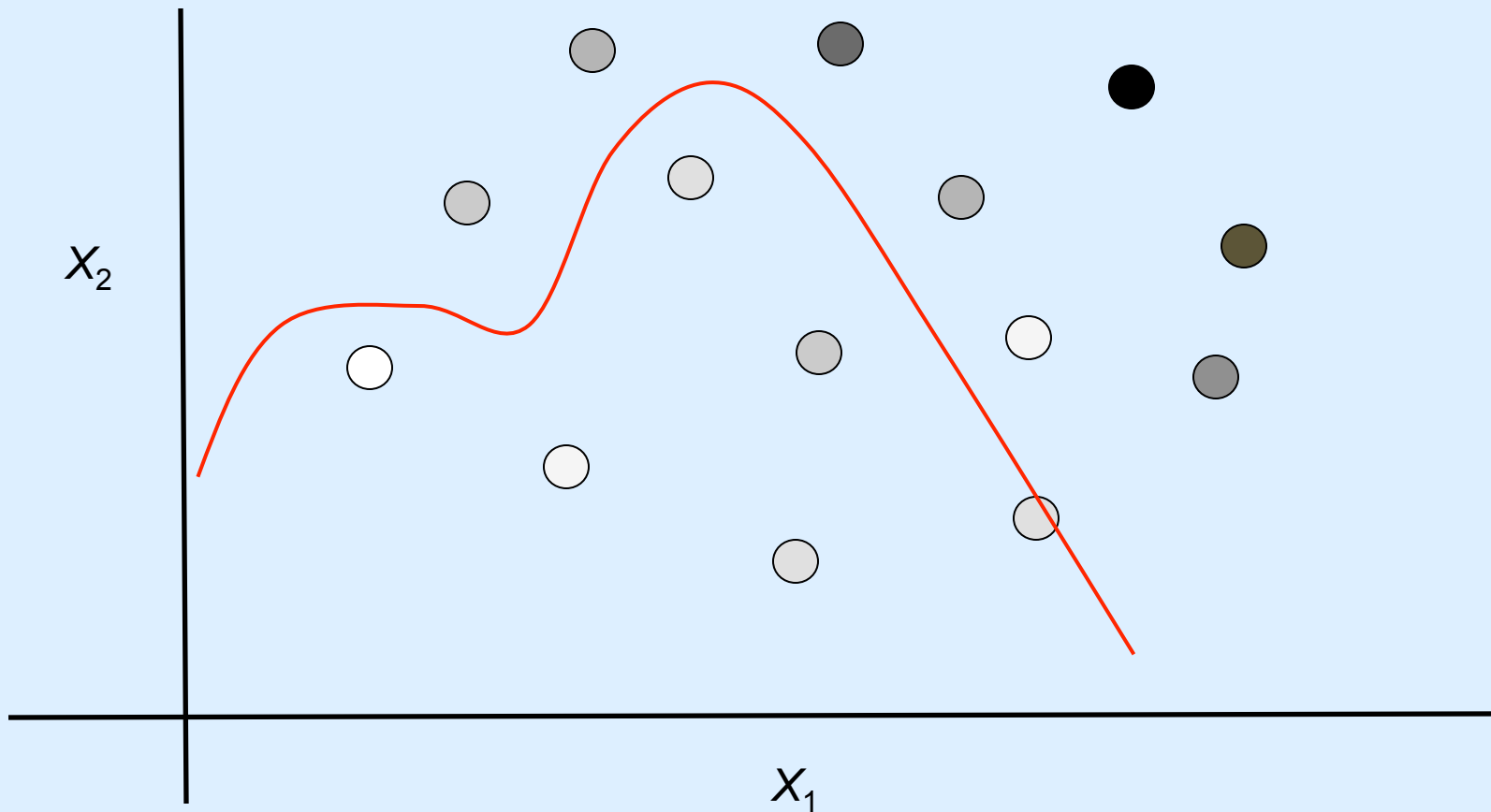
To define an n -degree polynomial function $P_n(x)$ that goes “through” a specified set of points (x,y) , define

$$P_n(x) = \sum_{i=0}^n f_i L_i(x)$$

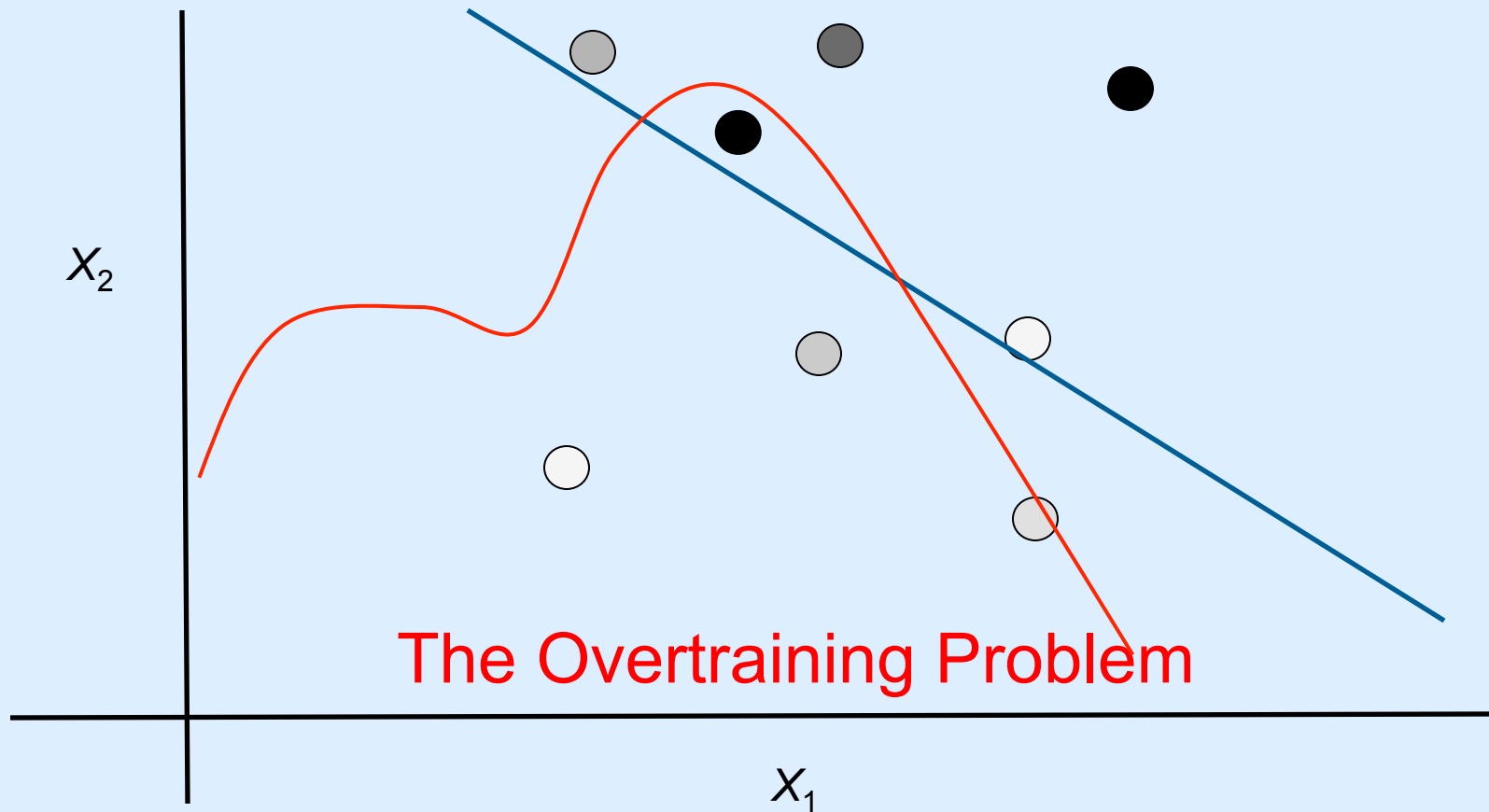
where

$$L_i(x) = \prod_{\substack{k=0 \\ k \neq i}}^n \frac{(x - x_k)}{(x_i - x_k)}$$

A Classification Problem



A Classification Problem



Training: Supervised Learning

- Want to use a neural network to handle data in some **future** scenario.
- Need to train the network with data we already have to do this.
- But we also need to assess how well the network works.
- Obviously, we can't use the same data we trained the network with to assess its performance. Why?

Training: Supervised Learning

- A common approach is to minimize errors in a FFBP setup.
- Obtain raw data:
 - parts corresponding to inputs,
 - parts corresponding to associated outputs.
- Divide the data into two parts: Training Data and Testing data.
- Take the training data and **train and train and train**, (but not too much) until errors are as small as possible.
- Then test the trained network using the testing data set to see how well it works using various performance criteria.
- Then make adjustments as necessary.

Partitioning Data Sets and Statistical Analysis

- Many ways to partition data
 - Just once as in the following example, or
 - Many times using different 'partitions' and then average the results (the weights) from each partition.
- Many statistical methods do this type of partitioning. Popular methods include:
 - Bootstrap Method
 - Jackknife Method
- Basically idea is to use the same data but create many training/testing sets. Randomly select out the training set and the testing set. E.g. for 20 I/O pairs, using 10 I/O pairs for training, 10 I/O pairs for testing. But

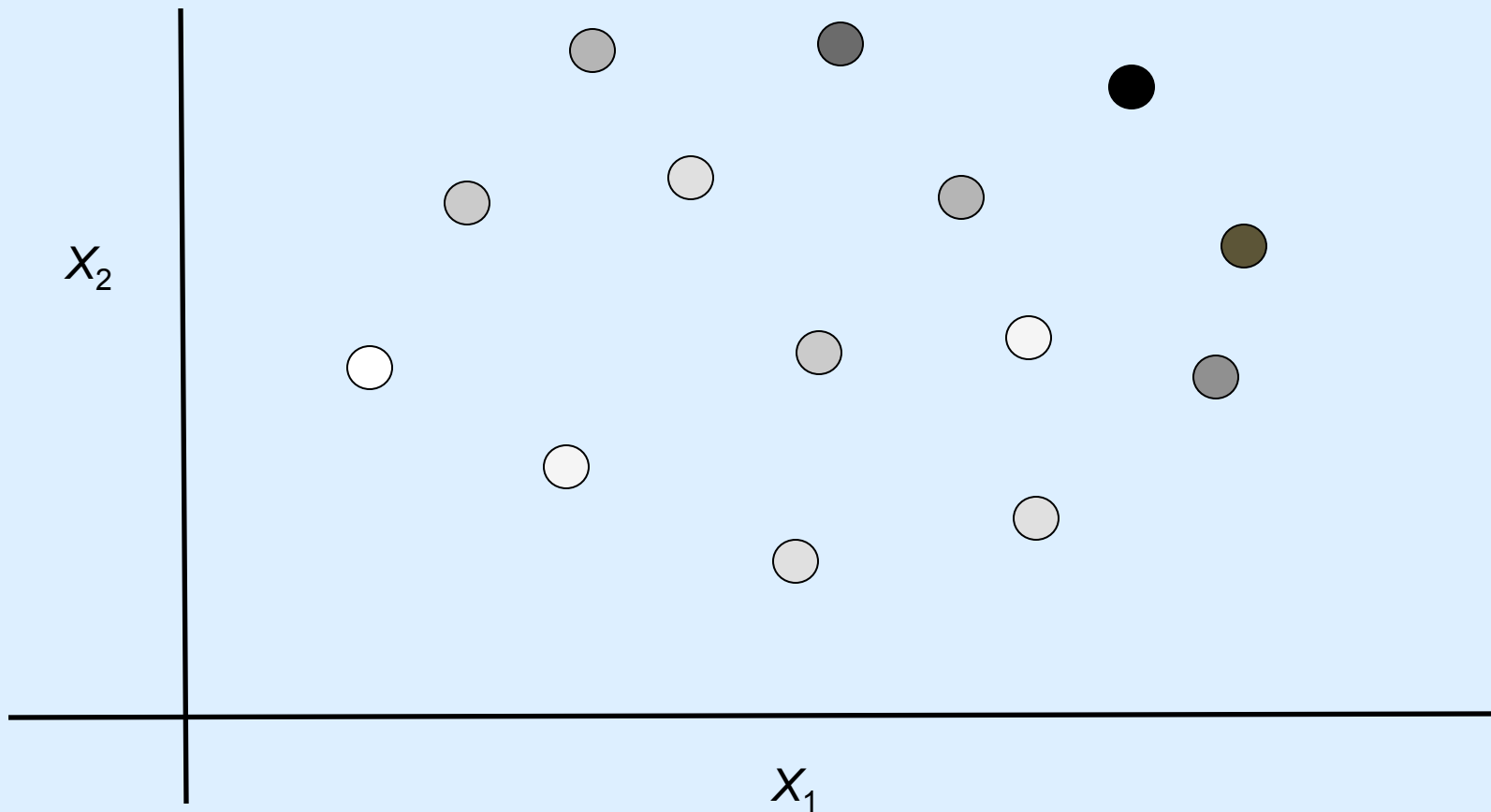
$$\binom{20}{10} = \frac{20!}{10!10!} = 184,756$$

This Scenario Requires

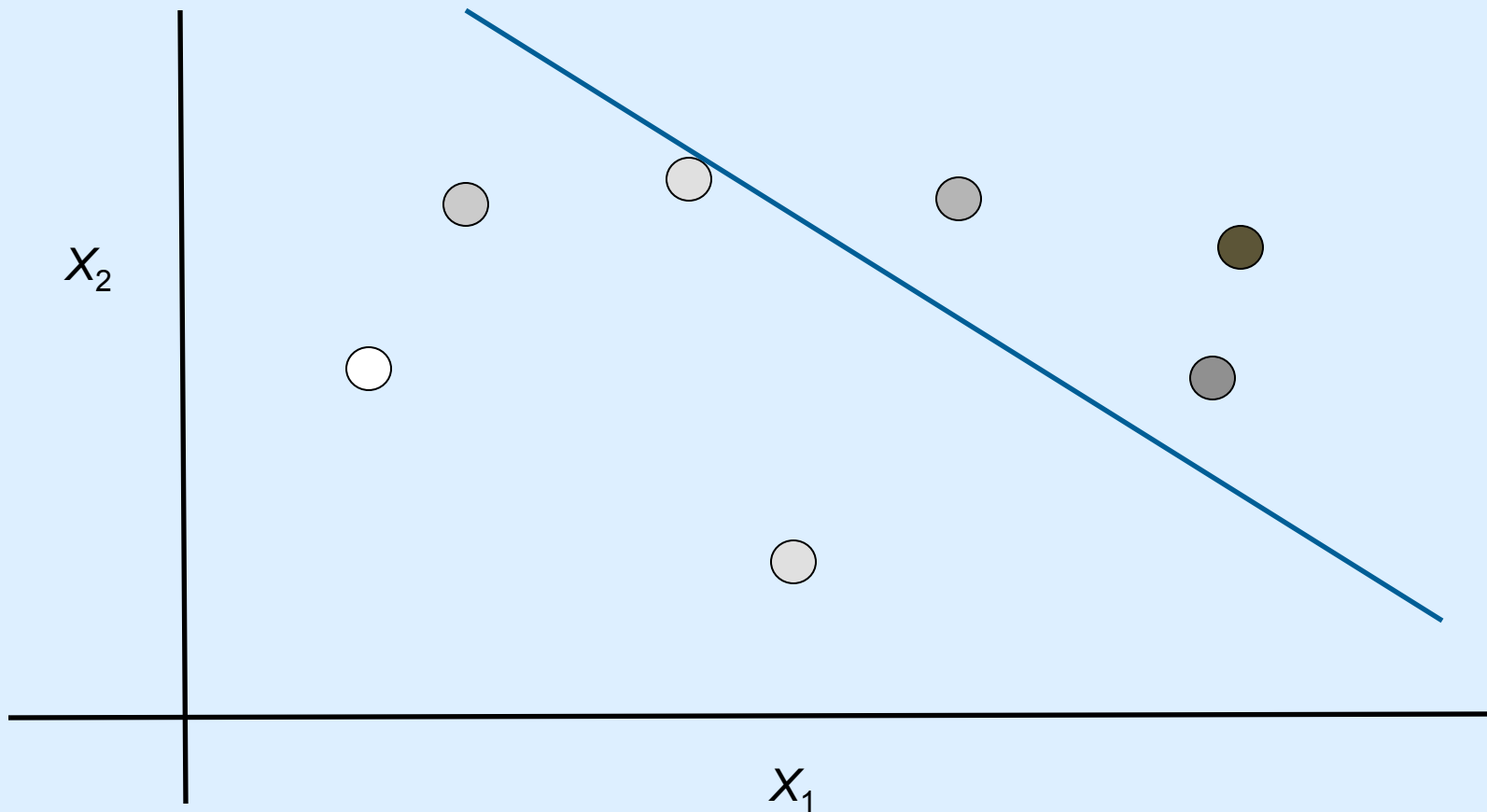
- A means for evaluating network performance (obviously).
 - Performance refers to how well the neural network performs the desired function for which it is being trained.
 - We will, for now, **assume some method of measuring performance** and get into the details in later sub-modules.
- Also means being able to use the neural network and associated data effectively and efficiently!
 - Computational efficiency is important for training AND assessing performance.

Efficiency

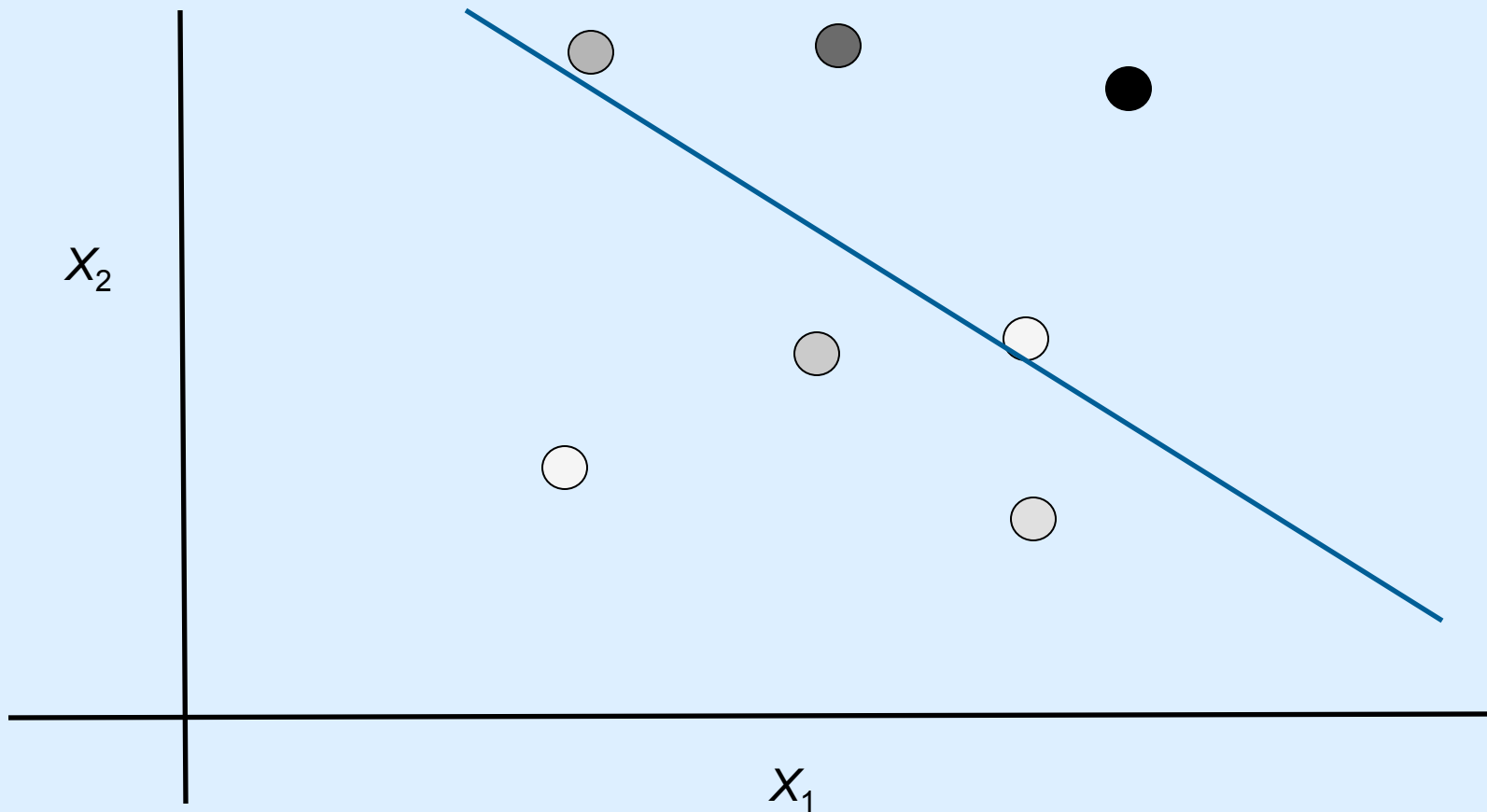
A Classification Problem



A Classification Problem



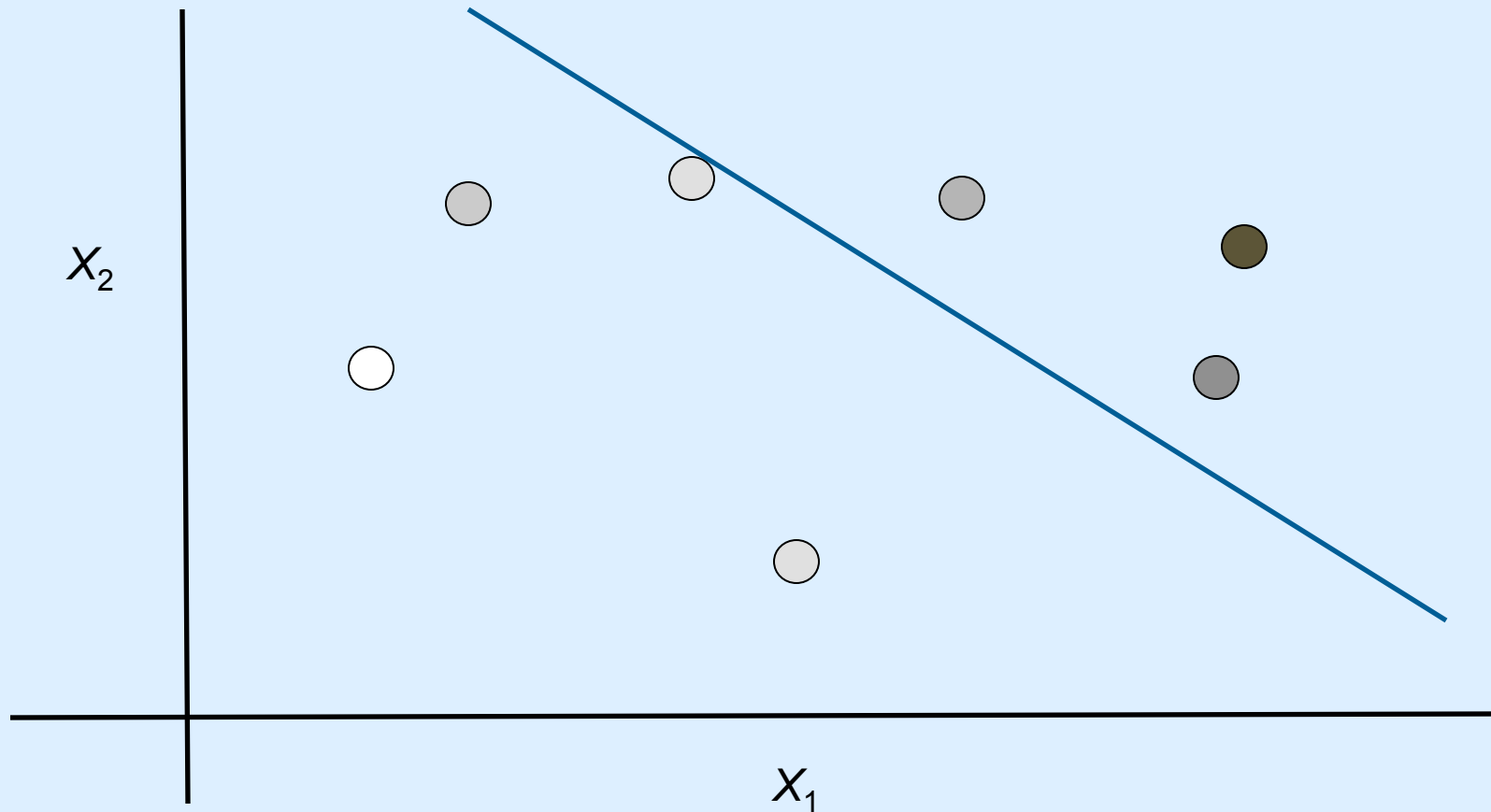
A Classification Problem





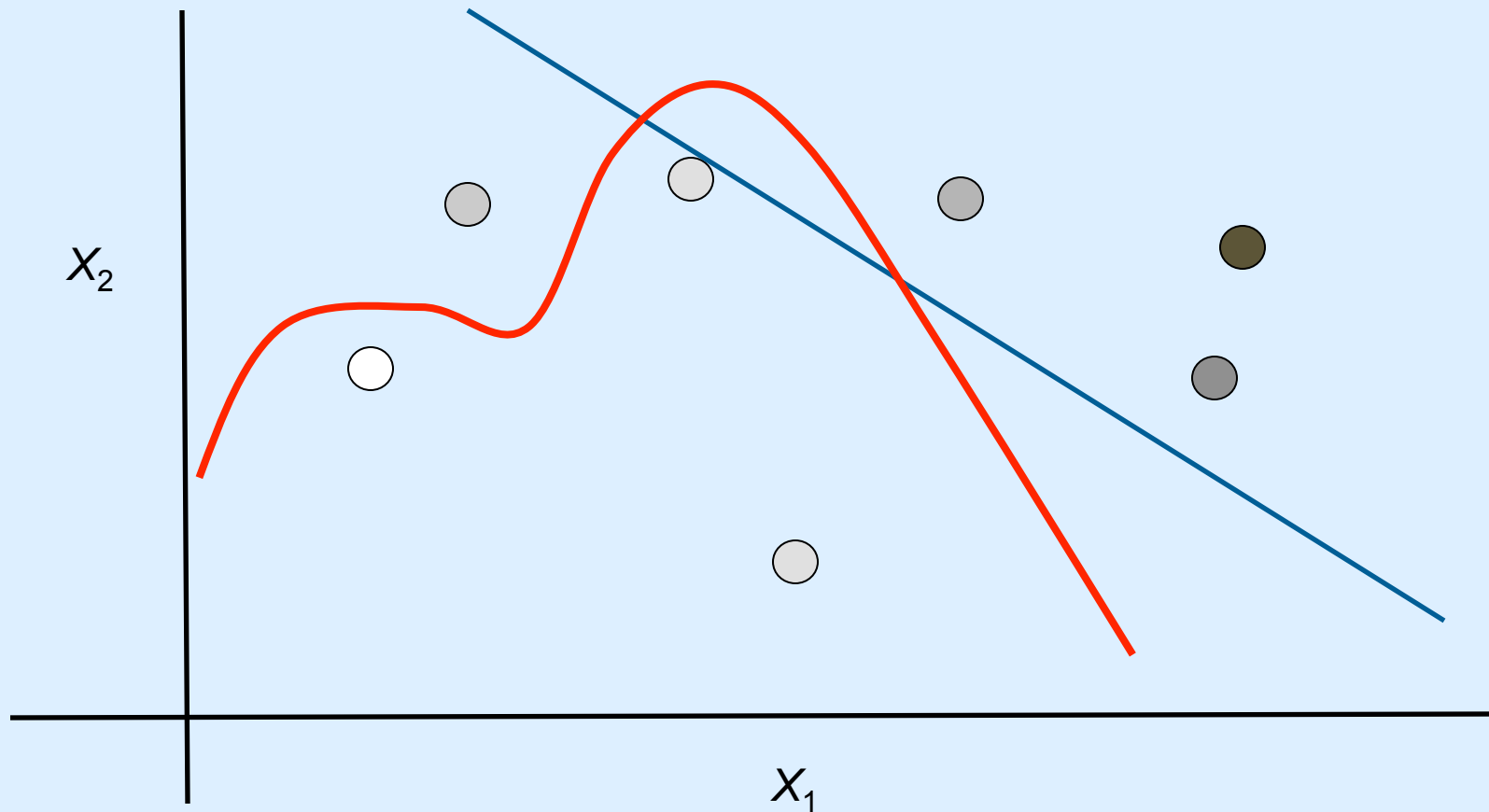
A Classification Problem

Back to Training Set

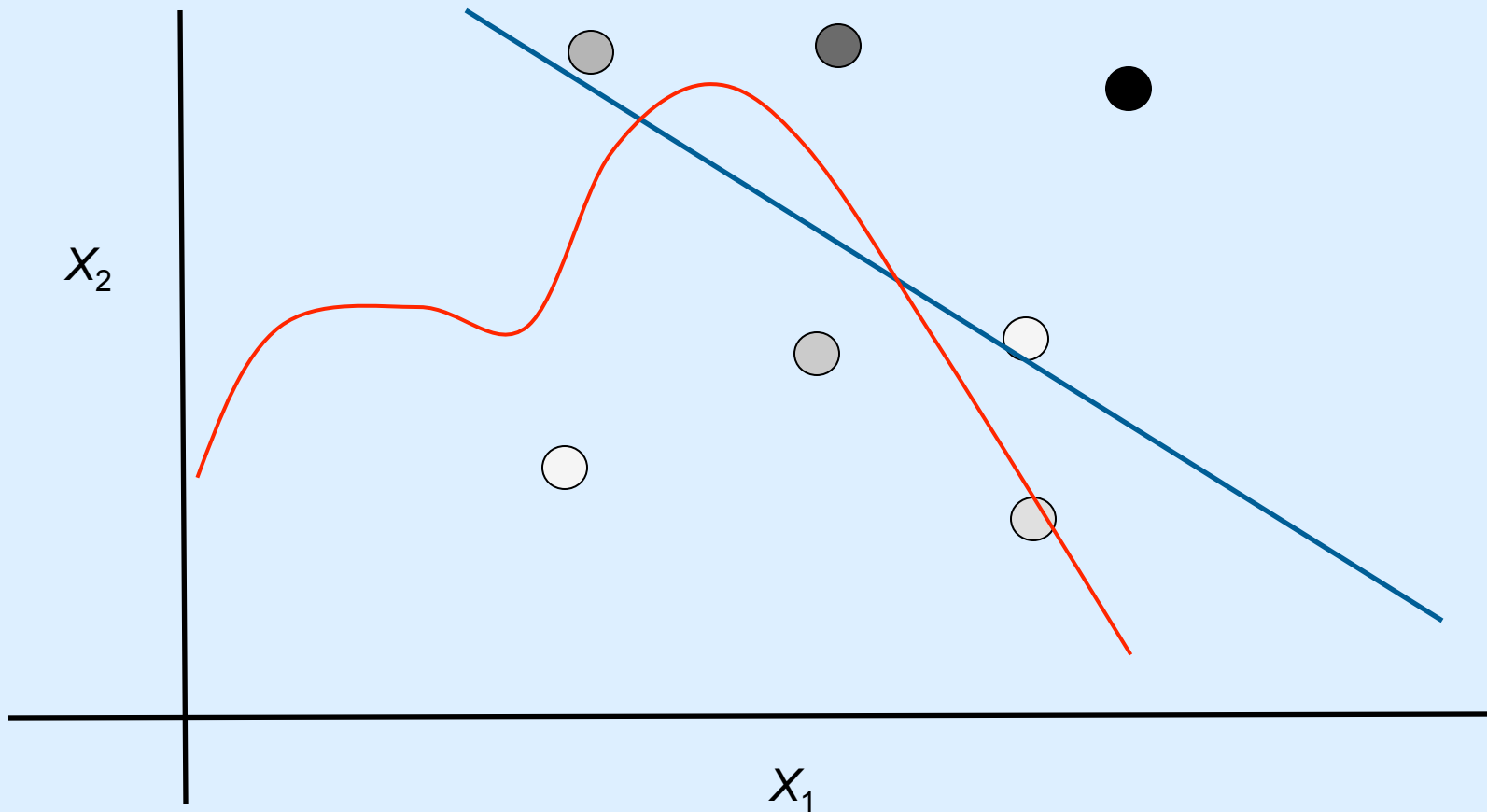




A Classification Problem



The Overtraining Problem



The Overtraining Problem

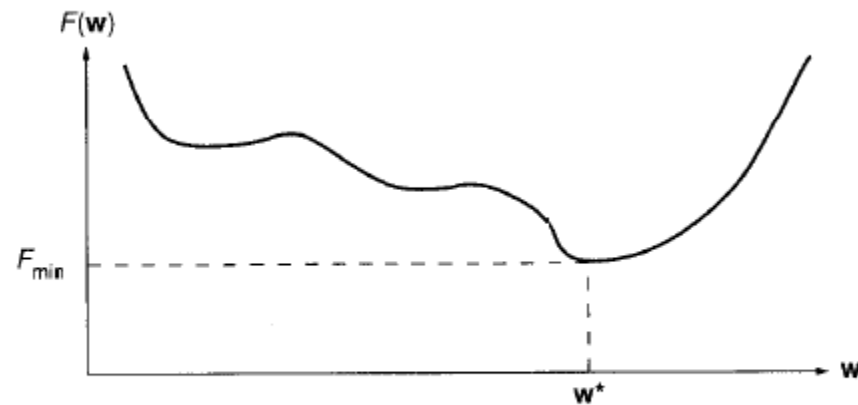


Fig. 5.1. • A typical error surface. A goal of neural network training is to find a network weight vector w^* that minimize the error F .

From *Neurocomputing*
by Hecht-Nielsen

The Overtraining Problem

- Random variations may be part of some underlying process.
- A Regression Line estimates the deterministic part of the process.
- Training attempts to capture this process.
- Training too much may end up including the effects of random variation in the deterministic part of the modeling of a process.

We end up training the network on the randomness instead of the underlying deterministic process!

Training on the errors.

Training Reprise

- During training, we use the error to compute the gradient in steepest descent methods, to guide us towards minimizing the error.
- During testing/evaluation, we use the error to minimize the testing error.
- Must do a lot of experimentation: training, testing, training, testing...
- A lot of computational effort is involved to get it right!

Training Efficiency

- How can we maximize use of our data?
- How do we decide how many times to train and test? How many different partitions to use?
- Efficient and effective training and testing methods must be employed.